

# Subset Node Anomaly Tracking over Large Dynamic Graphs

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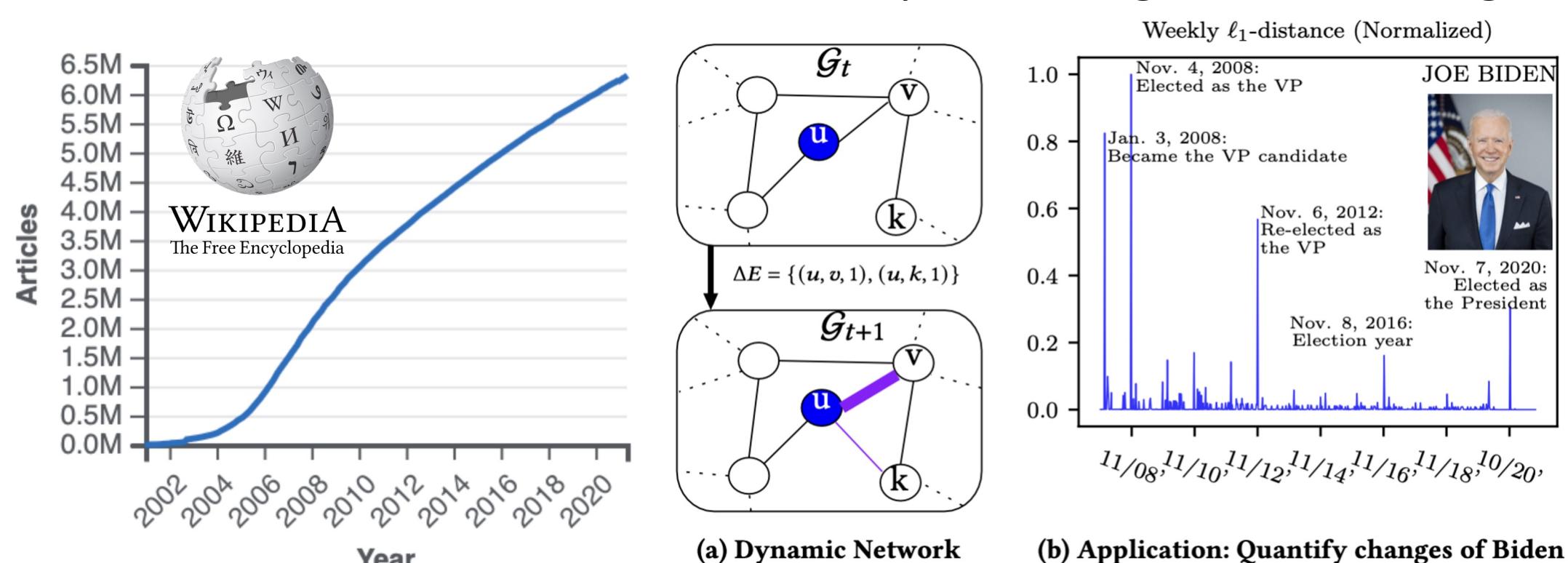
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## Introduction:

- Tracking a targeted subset of nodes in an evolving large graph is important for many real-world applications.
  - ❖ Node-level anomaly: Identify when specific nodes significantly changed their context.
  - ❖ Graph-level anomaly: Uncover when global changes occurred in the overall graph structure.
- These tasks become challenging as the graph size and time horizon scale up.
  - ❖ It's expensive to re-train whole node embeddings across time.
  - ❖ It's difficult to detect node anomaly in mis-aligned embeddings.



- We propose a unified framework **DynAnom** for subset node anomaly tracking over large dynamic graphs:
  - ❖ Efficient Personalized PageRank (PPR)-based node embeddings for a subset of nodes over dynamic graphs.
  - ❖ Flexible framework to localize both node/graph anomalies with customizable anomaly score functions for various applications.
  - ❖ Compared to others, **DynAnom** is 2x better and 2.3x faster.

## Key Contributions

- > We proposed an efficient anomaly tracking framework, **DynAnom**, that supports node/graph-level anomaly tracking over dynamic graph.
- > We generalized dynamic forward push algorithm for calculating PPR, making it suitable for weighted-graph anomaly tracking.
- > Released Resources @ <https://github.com/zjlxgz/DynAnom>.
  - We derived a real-world graph, PERSON, for personal life changes detection.
  - We released our python codebase for reproducibility.

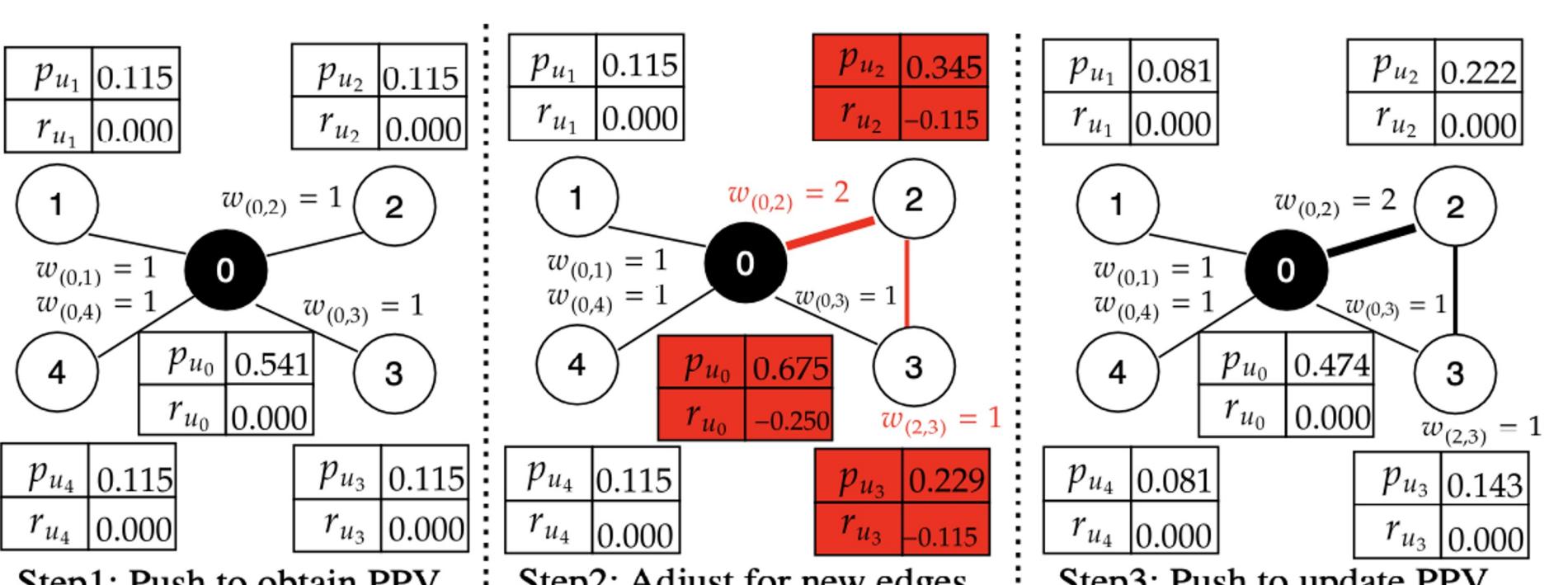
## Related Work

- Many graph-level anomaly detection cannot identify individual node changes but only uncover the global changes. Edge-level methods cannot identify node evolution when there is no direct edge event associated with the node.
- Many node embedding-based methods must calculate all embeddings even only for subset tracking. The embedding space is not well-aligned across time, making the algorithm only detects anomalies (outliers) in each static snapshot.

Method	Feature	Anomaly		Edge Event Types			Algorithm		
		Node level	Graph level	Edge Stream	Add/ Delete	Weight Adjust	V  Ind.	Align Repr.	Flex. Score
SedanSpot									
AnomRank									
NetWalk									
DynPPE									
<b>DynAnom</b>									

## Proposed Algorithm: **DynAnom**

- Step 1: Maintain PPR-Vector (PPV) for the target subset**
  - ❖ Incremental Local Push over dynamic weighted graphs
  - ❖ Complexity is linear to #edge changes, not #nodes.
- Step 2: Obtain PPR-based node embeddings in constant time**
  - ❖ Hash or Random Projection for Dimension Reduction
- Step 3: Detect node/graph anomaly for the target subset**
  - ❖ Node anomaly: Compare embedding change ( $\ell_1$ -distance).
  - ❖ Graph anomaly: Aggregate node anomaly of high-degree nodes (max, median, mean).



## Experiments

- Node-level anomaly: Comparing to the best baseline our method **DynAnom** is effective (2x better) and scalable (2.3x faster) with the simplest anomaly score function.

Methods	Accuracy	Wall-time (s)	DARPA	PERSON
AnomRank	0.2790	905.98	# Nodes	25.5K
AnomRank (W)	0.2652	905.98	# Edge events	4.5M
NetWalk	OOM	OOM	# Snapshots	1.4K
DynPPE	0.1701	84.25		
<b>DynAnom</b>	0.5425	379.33		

- Graph-level anomaly tracking: **DynAnom** is useful and flexible:
  - ❖ The simplest heuristic anomaly design outperforms others.
  - ❖ Easily adapt to most ML system for more sophisticated detection systems.

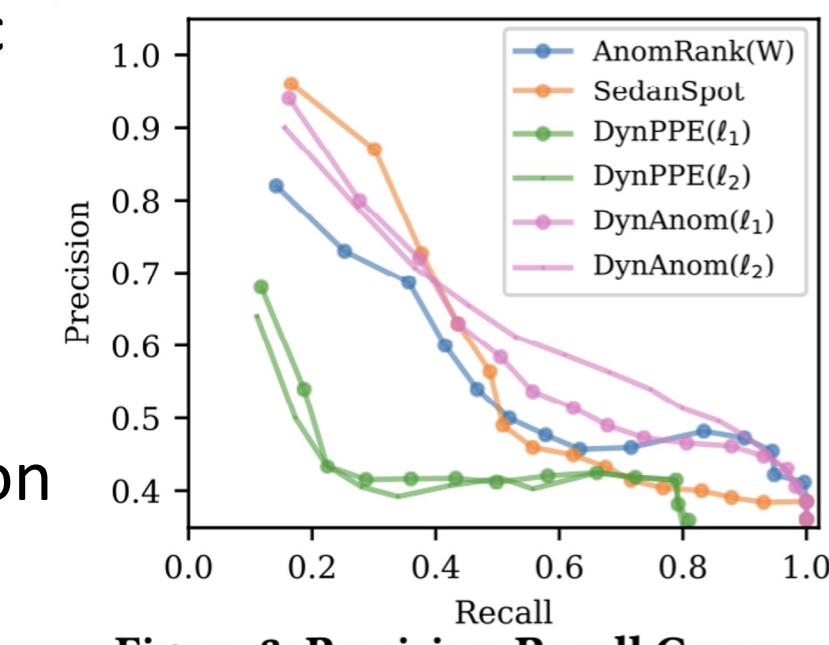
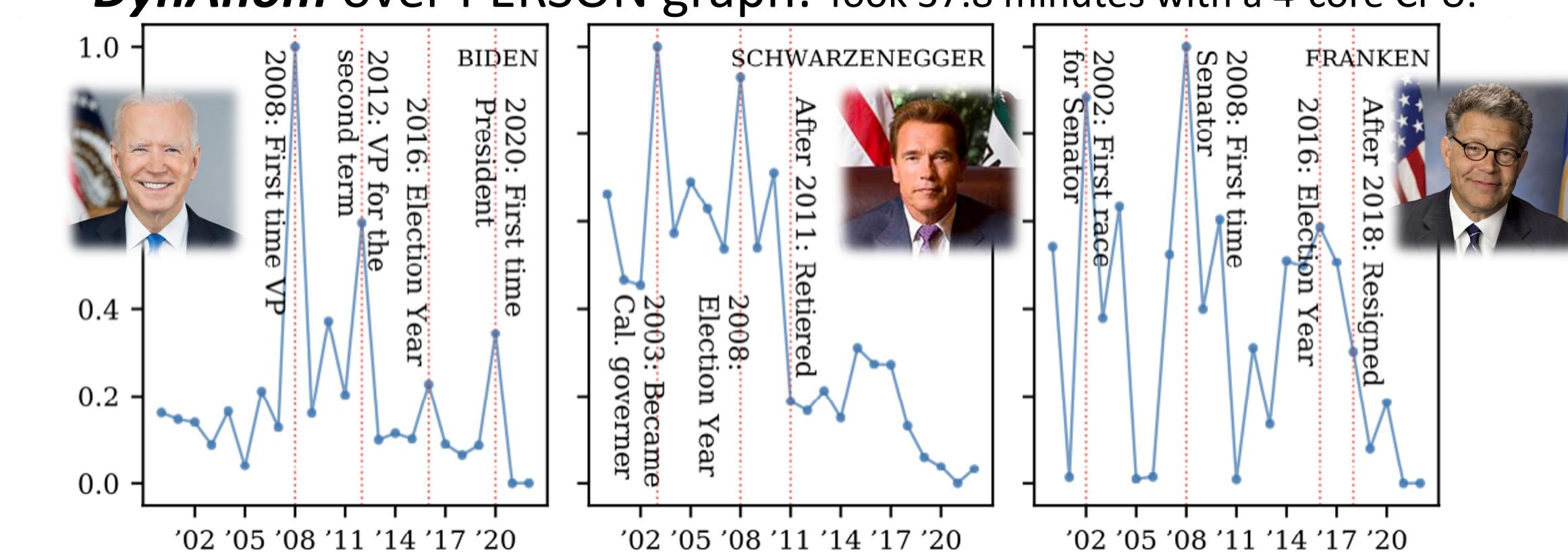


Table 6: The precision of top-250 anomalies	
Algorithms	Precision
NetWalk	OOM
AnomRankW	0.5400
SedanSpot	0.5640
DynPPE(t <sub>1</sub> )	0.4160
DynPPE(t <sub>2</sub> )	0.3920
DynAnom(t <sub>1</sub> )	0.5840
<b>DynAnom(t<sub>2</sub>)</b>	<b>0.6120</b>

- Tracking Real-world personal life changes over 22 years with **DynAnom** over PERSON graph: Took 37.8 minutes with a 4-core CPU.



## Conclusions

- We propose a unified framework **DynAnom** for subset node anomaly tracking over large dynamic graphs.
- **DynAnom** can be easily applied to different graph anomaly detection tasks with a flexible score function.
- Experiments demonstrate its effectiveness and efficiency.