

4. 2]

4. 2 A.

1. ~~1~~ 1) $4 \pm \sqrt{2}$ 2) $\pm a/b (a^2 + b^2)$

$$7^4 = \frac{1}{5} \quad a^4 = a \quad a^2(a^2 + b^2) \quad a^2 b^2 (a^2 + b^2)^2$$

$$1 - q^4 = 5 - 5q^2 \quad \# \quad q^4 - 5q^2 + 4 = 0 \quad (q^2 - 4)(q^2 + 1)$$

$$q = \pm 2 \quad q = \pm i$$

2. 1) $a_5 = 8, c_8 = 1, q = \frac{1}{2}, c_{11} = \frac{1}{256} \cdot 128$

2) $a_5 = 2, q = -1, z_{15} = a_5 q^{n-5} = 2$

3) $a_4 = 12, a_8 = 6 \Rightarrow q = \sqrt[4]{\frac{1}{2}} \Rightarrow c_{12} = 3$

3. 1) $\frac{z_{2n}}{z_{2n-1}} = q$ 是, $1/n$ 为 q

2) $\frac{a_{n+1} + a_{n-1}}{a_n + a_{n-1}} \neq q$ 不是

4. $\frac{a_n b_n}{a_{n+1} b_{n+1}} = q_1 \cdot q_2$ 是, $1/n$ 为 q_1, q_2

5. $\begin{cases} a^2 + \frac{1}{2} b^2 = c^2 \\ c^2 = 2b \end{cases} \Rightarrow \begin{cases} a^2 - \frac{1}{2} c^2 = 0 \\ 4a^2 - a^2 - 4c^2 = 0 \end{cases} \quad a^2 c = \frac{1 + \sqrt{5}}{8}$

6. $105 \cdot q^4 = 260 \quad \# \quad 1 - q = 15.1\%$

7. 1) $S_5 = 605$ 2) $S_8 = \frac{255}{16}$ 3) $S_n = \frac{-1865}{1024}$ 4) $a_i = 24$

8. $\frac{a_1(1-q^4)}{1-q} = \frac{a_1(1-q^2)}{1-q} \cdot S \quad a_n = -2 \cdot (-1)^n \quad \text{or} \quad z_n = -\frac{1}{4} (-1)^n$

9. 1) $S_{\infty} = \frac{1}{1-q} \{a_n\} \text{ GP} \quad c_{100} = 100 \cdot (\frac{1}{2})^{100-1} \quad S_{100} \approx 200 \text{ m}$

2) 不可解, 其最大为 200 米.