

4. 题 2.5

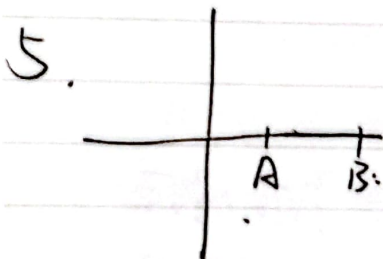
3. 将 $P(2,1)$ 代入, $4+k^2-6-k-4=0 \Rightarrow k=3$ 或 -2 .

4. 设 $P(x,y), A(x_1, y_1), B(x_2, y_2)$

$$\begin{cases} x_1+x_2=2x \\ y_1+y_2=2y \end{cases}$$

$$\sqrt{(x_1-x_2)^2+(y_1-y_2)^2}=4$$

$$\therefore x^2+y^2=4$$



设 $C(x,y)$

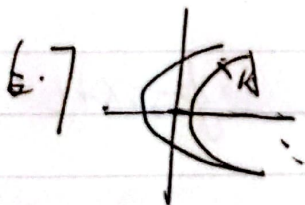
$$\therefore CA = \frac{1}{2} CB$$

$$\therefore \sqrt{(x-2)^2+y^2} = \frac{1}{2} \sqrt{(x-1)^2+y^2}$$

$$4(x-2)^2+4y^2=(x-1)^2+y^2$$

$$3x^2+16-64+3y^2=0$$

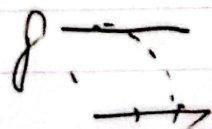
$$\underline{x^2+y^2=16}$$



设 $P(x_1, y_1), B(x_2, y_2), A(3,1)$

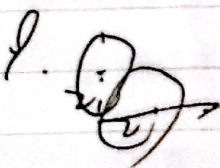
$$\begin{cases} x_1-3=2x_2 \\ y_1-1=2y_2 \end{cases} \Rightarrow \begin{cases} x_2 = \frac{x_1-3}{2} \\ y_2 = \frac{y_1-1}{2} \end{cases}$$

$$\Rightarrow x_2^2+y_2^2=x_2+1 \Rightarrow \frac{(y_1-1)^2}{4} = \frac{x_1-3}{2}+1$$



$$\frac{2}{\sin(\alpha-\beta)} = \frac{f}{\sin(\alpha+\beta)} = \frac{2}{\sin 2\alpha}$$

$$\underline{f=0}$$



$$\underline{r_1 r_2 = 2\sqrt{2}}$$

NO.

Date

$$zy = t - x$$

$$B \quad \begin{cases} x^2 + (x-t)^2 = 4 \\ x^2 + x^2 - 2tx + t^2 = 4 \end{cases} \quad \begin{cases} 4t^2 - 4t^2 = 0 \\ -4t^2 + 3t = 0 \end{cases} \quad \begin{cases} 4t^2 - 4t^2 = 0 \\ -4t^2 + 3t = 0 \end{cases} \quad \begin{cases} 4t^2 - 4t^2 = 0 \\ -4t^2 + 3t = 0 \end{cases}$$

$$2. \quad \begin{cases} C_1 = (x-1)^2 + (y+1)^2 = 1 \\ C_2 = (x+2)^2 + y^2 = 5 \end{cases}$$

$$\therefore C_1(1, -1) \quad C_2(-2, 0)$$

$$\therefore d = \sqrt{1 + \frac{1}{5}} = \frac{3}{\sqrt{5}} \quad \therefore \frac{1}{d} = \frac{\sqrt{5}}{3}$$

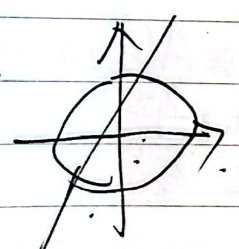
$$\begin{cases} 3x^2 + 4y^2 = 12 \\ 4x^2 + 3y^2 = 12 \end{cases} \quad \therefore \begin{cases} x = \sqrt{\frac{12}{7}} \\ y = \sqrt{\frac{12}{7}} \end{cases} \quad \begin{cases} x = -\sqrt{\frac{12}{7}} \\ y = \sqrt{\frac{12}{7}} \end{cases} \quad \begin{cases} x = -\sqrt{\frac{12}{7}} \\ y = -\sqrt{\frac{12}{7}} \end{cases} \quad \begin{cases} x = \sqrt{\frac{12}{7}} \\ y = -\sqrt{\frac{12}{7}} \end{cases}$$

$$\therefore \text{共 4 个}$$

$$4. \quad \begin{cases} x^2 + 4y^2 = 4 \\ x + 2y - t = 0 \end{cases} \quad \therefore d_{\max} = \frac{|-2+t|}{\sqrt{5}} = \frac{2}{\sqrt{5}} \sqrt{16} + \frac{2}{\sqrt{5}} \sqrt{5}$$

$$\Rightarrow t = 0$$

$$\therefore t = \pm \sqrt{8}$$

6. 

$$\therefore \frac{x_1 + x_2}{2} + m = \frac{y_1 + y_2}{2}$$

$$\therefore m = \frac{12}{13}t + \frac{44}{13}t = \frac{56}{13}t$$

$$m \in (-\frac{1}{2}\sqrt{2}, \frac{1}{2}\sqrt{2})$$

$$\begin{cases} 3x^2 + 4y^2 = 16 \\ 4y^2 + 4t = x \end{cases}$$

$$\Rightarrow 52y^2 - 16ty + 48t^2 - 16 = 0$$

$$\begin{cases} x_1 + x_2 = -\frac{44}{13}t \\ y_1 + y_2 = -\frac{b}{a} = -\frac{-16t}{52} = \frac{4t}{13} \end{cases}$$

670

$$(96t^2 - 4 \cdot 52(48t^2 - 16)) > 0$$