

NOTES

EDITED BY DAVID J. HALLENBECK, DENNIS DETURCK, AND ANITA E. SOLOW

The Problem of the Calissons 可利颂问题

GUY DAVID

École Polytechnique, Centre de Mathématiques, 91128, Palaiseau Cedex, France

CARLOS TOMEI

Departamento de Matemática, PUC/RJ, R. Marquês de São Vicente, 225, Rio de Janeiro, Brasil

A calisson is a French sweet that looks like two equilateral triangles meeting along an edge. Calissons could come in a box shaped like a regular hexagon, and their packing would suggest an interesting combinatorial problem. Suppose a box with side of length n is filled with sweets of sides of length 1. The long diagonal of each calisson in the box is parallel to one of three different lines, as in the picture.

可利颂镶嵌定理

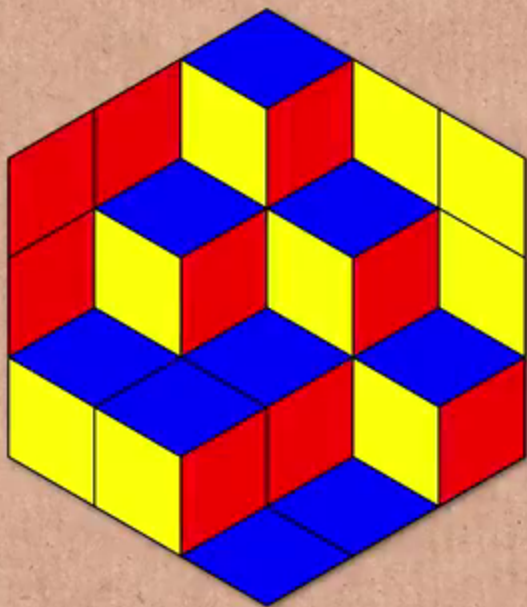




两个边长为1的等边三角形组成

冷科普 bilibili

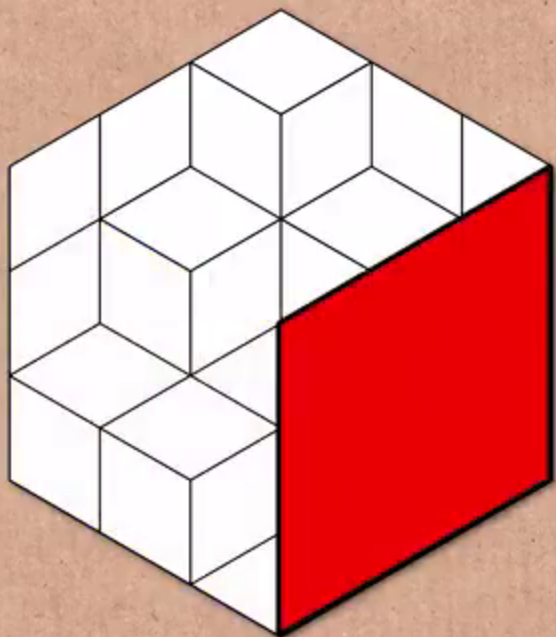




向右倾斜的菱形是红色的

冷科普 bilibili

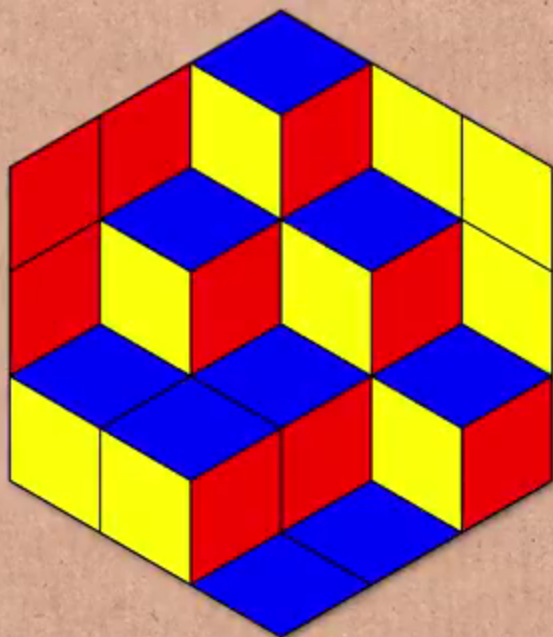




侧视图是一个红色的大正方形

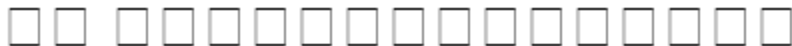
冷科普 bilibili

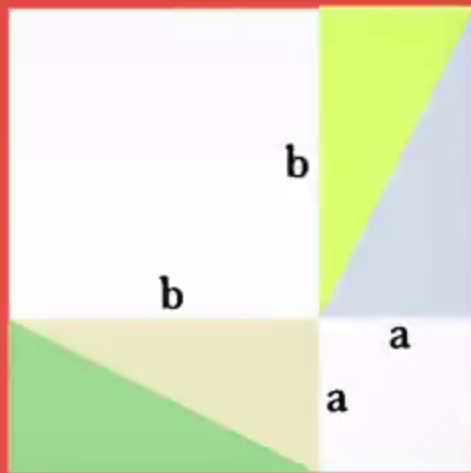




并且 它们都由 n 的平方个小正方形组成

冷科普 bilibili





此时 空出来的位置

冷科普 bilibili



参考资料:

The Problem of the Calissons—Guy David and Carlos Tomei

Problem of calissons—Gábor Damásdi

Proof without words—Wikipedia

视频素材:

Pythagorean theorem water demo—00000000130

How many ways are there to prove the Pythagorean theorem? - Betty Fei—TED-Ed

How It's Made: Calissons—Science Channel

Ma recette de calisson d'Aix—Les secrets de Muriel

背景音乐:

みかん箱 - ひやむぎ、そーめん、時々うどん