

3D-CAIPI-BUDA and Joint Hankel Low-Rank Reconstruction Enable Rapid and Distortion-free High-Resolution T2* Mapping and QSM

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Synopsis

Quantitative imaging has been very useful in neuroscientific and clinical applications, including glioma, tumor diagnosis and prognosis, brain maturation, and Alzheimer's disease. EPI is a powerful tool for quantitative imaging owing to its extremely fast acquisition. This work aims to develop a distortion-free, blip-up/down acquisition (BUDA) 3D-EPI with controlled aliasing in parallel imaging (CAIPI) sampling and joint Hankel low-rank image reconstruction for fast and robust multi-contrast high-resolution whole-brain imaging. The developed technique could generate distortion-free high-resolution whole-brain T2* mapping and quantitative susceptibility mapping in 47s at 1.1 × 1.1 × 1 mm³ resolution.

Purpose

Quantitative MRI has gained recent attention owing to its emerging neuroscientific and clinical applications^{1–3}. Echo planar imaging (EPI) is a rapid encoding technique that has played an essential role in functional and diffusion MRI^{4,5}, quantitative imaging^{1,6,7}, and susceptibility mapping⁸. Despite the fast acquisition speed, distortion and voxel pile-ups have remained an open problem^{7,9}, and led to technical developments that aimed to improve the geometric fidelity of EPI^{5,6,10–12}. In this work, we propose to combine 3D blip-up/down acquisition (BUDA)¹³ with CAIPI^{14,15} sampling and joint Hankel low-rank reconstruction to obtain high-resolution, distortion-free, multi-contrast images. The results demonstrate improved image quality by incorporating staggered CAIPI sampling across the multi-shot data to provide complementary information. For *in vivo* T2* mapping, high agreement between the proposed 3D-BUDA and standard multi-echo GRE was observed, as corroborated by Bland-Altman analysis. Further, the ability to perform QSM is demonstrated from the same set of distortion-free multi-echo EPI data.

Method & Experiments

Novel acquisition: The proposed multi-echo 3D-BUDA sequence diagram is presented in Figure 1. Blip-up/down phase encoding is implemented for each echo (yellow and green blips in GPE), respectively. High Rinplane acceleration enabled by multi-shot acquisition allowed for inserting three echoes with adequate echo times for T2* mapping and QSM. CAIPI strategy is employed for improving the conditioning of the image reconstruction^{14,15}. In this work, CAIPI is performed between the blip-up/down shots, as shown in Figure 3.

Novel reconstruction: A joint reconstruction approach is proposed and demonstrated using multi-echo multi-shot 3D-BUDA GRE-EPI data, as shown in Figure 2:

$$\tilde{I} = \arg \min_{t,n} \sum \left\| M_{t,n} F_{t,n} E C I_{t,n} - d_{t,n} \right\|_F^2 + \lambda \| H(I) \|_*$$

Where *t* is the shot count, *n* represents the echo index. *M_{t,n}* and *F_{t,n}* are the sampling mask and Fourier transform operator (*t*th shot, *n*th echo), respectively. *C* represents the coil sensitivity maps; *I* is the to-be-restored images, and *d_{t,n}* stands for the acquired under-sampled k-space data. *E* is the *B*₀ field map generated by TOPUP using FSL on interim blip-up and -down separate reconstructions (<http://fsl.fmrib.ox.ac.uk/fsl>)¹⁶. $\| H(I) \|_*$ denotes the Hankel matrix along both shot and echo dimensions for multi-echo multi-shot data^{17,18}. It enforces local k-space neighborhoods (of size 9×9×9), extended across all echoes/contrasts in the shot dimension, to have structured low-rankness property. A POCS-like algorithm¹⁹ was employed to solve the above equation with a stopping criterion of root mean square error (RMSE) < 1% between consecutive iterations.

Data acquisition: *In vivo* multi-echo, multi-shot 3D-BUDA experiments were performed on a 3T scanner (Magnetom Tim Trio; Siemens Healthineers) with a 32-ch head coil. Imaging parameters include: Rinplane=8, TR=86ms, TE={18, 43.17, 68.34}ms, FA 19° (Ernst angle), FOV 220×220×128 mm³, spatial resolution=1.1×1.1×1 mm³. T2* maps were obtained using Bloch dictionary matching²⁰. The dictionary comprised signal evolution curves of T2* values were set as [1:1:100, 101:2:200, 201:3:300] ms. QSM was estimated using a nonlinear dipole inversion (NDI)^{21,22}:

$$\tilde{\chi} = \arg \min_{\chi} \left\| W \left(e^{iF^{-1} D F \chi} e^{i\phi} \right) \right\|_2^2$$

where **W** is magnitude weighting, *D* and *F* are the dipole kernel and 3D-DFT operator. *φ* is the tissue phase, *χ* is the to-be-calculated susceptibility map. All computations were implemented in MATLAB; code/data will be found on Github(<https://github.com/zjucz168/zjucz168/blob/main/3D-BUDA>) upon publication of this work.

Data Analysis

“Fully sampled” multi-shot multi-echo BUDA data were used as a reference, where all 8 shots were acquired at Rinplane=8 acceleration per shot. Bland-Altman analysis²³ was used to assess the accuracy of T2* maps generated by proposed reconstructions. Several ROIs were manually selected for this analysis (Figure 4). For QSM, tissue phase was estimated using Laplacian unwrapping²⁴ and V-SHARP^{25,26} background removal.

Results & Discussion

Figure 3 shows results from multi-echo multi-shot 3D-BUDA acquisition at Rinplane=8. Two time-matched acceleration strategies are considered: Sampling 8-shots at R_z=2-fold partition acceleration and 4-shots with full sampling in partition direction (R_z=1). Both joint multi-echo and separate reconstructions for each echo are performed. When echoes are separately reconstructed, Rinplane×R_z=8×2 case using 8-shots has higher reconstruction accuracy (3.90% RMSE) than Rinplane×R_z=8×1 with 4-shots (6.14%), due to higher image quality produced by more evenly distributed ky-kz sampling pattern in k-space coverage. Having acquired 8-shots also permitted better B₀ estimation using interim 4-shot blip-up and 4-shot blip-down reconstructions in *topup*, which were “effectively” Rinplane×R_z=2×2-fold accelerated and could be readily reconstructed using SENSE. Joint reconstruction with CAIPI sampling across echoes/shots further improved these results, where 8-shot Rinplane×R_z=8×2 yielded 2.25%, and 4-shot Rinplane×R_z=8×1 had 5.98% RMSE. As such, the proposed joint multi-echo reconstruction provided >2.5-fold improvement over separate reconstructions.

For T2* mapping, Figure 4 indicates the Bland-Altman analysis comparing 3D-joint-CAIPI-BUDA reconstruction and reference standard multi-echo 3D-GRE data (TA: ~35 minutes). Bland-Altman plots show the mean and difference for the ROIs of T2* values; all values are within the limits of agreement, although some minor biases exist. Figure 5 displays QSM results from 3D-joint-CAIPI-BUDA (Rinplane×R_z=8×2, TA: 47s, 8-shot). Shot-to-shot and echo-to-echo phase variations caused by physiologic variations were effectively removed in the proposed joint-Buda scheme. The conditioning of dipole inversion can be further improved using multi-orientation sampling²⁷, which is facilitated by the proposed efficient acquisition strategy.

Conclusion

The proposed 3D-joint-CAIPI-BUDA combines staggered CAIPI-sampling across multiple shots, multi-echo acquisition with inverted polarity and joint Hankel structured low-rank reconstruction to boost SNR and eliminate distortion simultaneously. This enables accurate, distortion-free whole-brain T2* mapping and QSM at the resolution of 1.1×1.1×1 mm³ in 47s.

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Figures

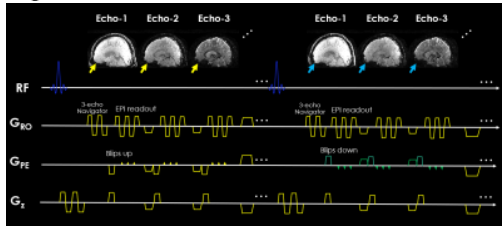


FIG.1. 3D-BUDA multi-shot multi-echo sequence schematic. 3D slab-selective EPI data were acquired using a complementary blip-up /down acquisitions multi-shot EPI with frequency-selective fat suppression. Blip up/down were implemented for each echo (see yellow and green blips in phase encoding gradient), respectively. Subsequently, followed by a rewinder gradient before the next echo.

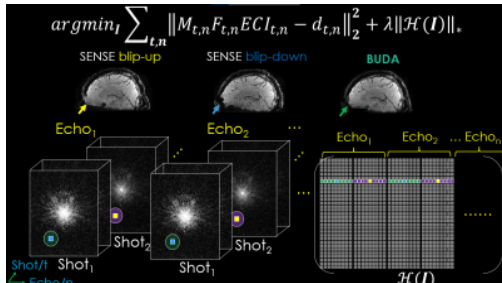


FIG.2. The proposed 3D-joint-BUDA image reconstruction framework for multi-shot multi-echo GRE-EPI data. For joint image reconstruction, the new Hankel matrix is constructed using the neighborhood along both echo and shot dimensions of the GRE-EPI dataset.

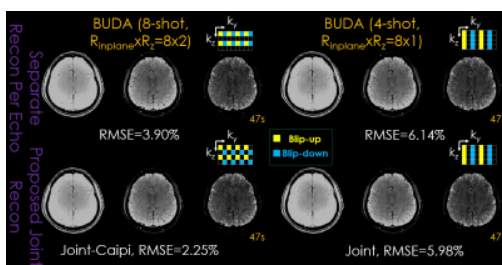


FIG.3. Comparison of different approaches with different sampling patterns (upper right corner of each subpart) on image quality for 3D-BUDA dataset with the same sampling amount (TA: 47s). First column: conventional 8-shot without and with CAIPIRINHA sampling. Second column: conventional 4-shot $R_z = 1$ without and with joint structured low-rank reconstruction. Three columns in each part are the three echoes of 3D-BUDA imaging, respectively.

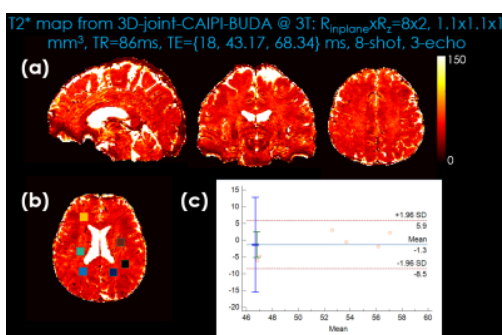


FIG.4. Comparison of the Bland-Altman plots displaying the mean and difference of T2* mapping generated by 3D-joint-CAIPI-BUDA image reconstruction and standard multi-echo GRE. (a) T2* mapping generated by 3D-joint-CAIPI-BUDA (8-shot, $R_{\text{inplane}} \times R_z = 8 \times 2$). (b) Selected regions of interest. (c) 3D-joint-CAIPI-BUDA ($R_{\text{inplane}} = 8$, $R_z = 2$, 8-shot) vs. standard multi-echo GRE (mean: GRE-51.58 vs. 3D-joint-CAIPI-BUDA-52.88).

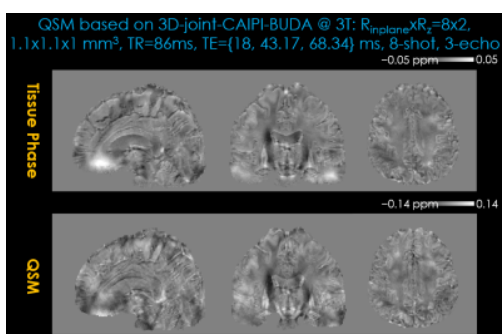


FIG.5. Tissue phase (first row) and quantitative susceptibility mapping (second row) results estimated using 3D-joint-CAIPI-BUDA image reconstruction (Reduction factor: $R_{\text{inplane}} = 8$, $R_z = 2$, TA=47s). The local tissue phase was obtained by Laplacian unwrapping and V-SHARP filtering (10 mm largest kernel size).