## Homework 3 zl9901

1)

- a) A -> B A can determine B
  - C -> A C can determine A
  - C -> B C can determine B
  - $AC \rightarrow B$  Since it is entailed by  $C \rightarrow B$ , we should drop this
  - BC -> A Since it is entailed by C -> A, we should also drop this
- b) According to the relation above, the only candidate key should be C.

2)

- a) Since {Car#, Salesman#} is the candidate key,
  - according to Car# -> Date\_sold, this is a partial dependency, this relation is in 1st normal form.
- b) For the relationship: Date\_sold -> Discount\_amt
  - Both the determinant and dependent are non-key attribute, it is a transitive dependency, we should split it into two tables.
  - R1(<u>Date\_Sold</u>, Discount\_amt) and R2(Car#, Date\_sold, Salesman#, Commission%)
  - $R1 \cap R2 = \{Date\_sold\} \rightarrow R1$ , there are no losses.
  - For table R1, candidate key is {Date\_sold}, this table is in BCNF already.
  - For table R2, the relationship: Car# -> Date\_sold, it is a partial dependency, we should split it into two tables.
  - R21(Car#, Date\_sold) and R22(Car#, Salesman#, Commission%)
  - $R21 \cap R22 = \{Car\#\} \rightarrow R3$ , there are no losses.
  - For table R21, candidate key is {Car#}, this table is in BCNF already.
  - For table R22, the relationship: Salesman# -> Commission%, it is a partial dependency, we should split it into two tables.
  - R221(Salesman#, Commission%) and R222(Car#, Salesman#)
  - $R221 \cap R222 = \{Salesman\#\} \rightarrow R221$ , there are no losses.
  - For table R221, candidate key is {Salesman#}, this table is in BCNF already...
  - For table R222, candidate key is {Car#, Salesman#}, this table is in BCNF already.
  - So the final result should be:
  - R1(<u>Date\_Sold</u>, Discount\_amt)R21(<u>Car#</u>, Date\_sold)R221(<u>Salesman#</u>, Commission%) R222(<u>Car#</u>, <u>Salesman#</u>)

3)

- a) The candidate key of R should be {A, B, D}
- b) For the relation: AB -> C, it is a partial dependency, so it is not in 2NF.
- c) For the relationship: AB -> C, it is a partial dependency, we should split it into two tables.

R1(A, B, C, I) and R2(A, B, D, E, F, G, H, J)

 $R1 \cap R2 = \{A, B\} \rightarrow R1$ , there are no losses.

For table R1, the candidate key is  $\{A, B\}$ , the relation: A -> I is a partial dependency, we should split it into two tables.

 $R11(\underline{A}, I)$  and  $R12(\underline{A}, \underline{B}, C)$ 

 $R11 \cap R12 = \{A\} \rightarrow R11$ , there are no losses.

For table R11, the candidate key is {A}, this table is in BCNF already.

For table R12, the candidate key is {A, B}, this table is in BCNF already.

For table R2, the candidate key is  $\{A, B, D\}$ , the relation: BD -> EF is a partial dependency, we should split it into two tables.

R21(<u>B</u>, <u>D</u>, E, F) and R22(A, B, D, G, H, J)

 $R21 \cap R22 = \{B, D\} \rightarrow R21$ , there are no losses.

For table R21, the candidate key is {**B**, **D**}, this table is in BCNF already.

For table R22, the candidate key is {A, B, D}, the relation: AD -> GH is a partial dependency, we should split it into two tables.

R221(<u>A</u>, <u>D</u>, G, H, J) and R222(<u>A</u>, <u>B</u>, <u>D</u>)

 $R221 \cap R222 = \{A, D\} \rightarrow R221$ , there are no losses.

For table R221, the candidate key is  $\{A, D\}$ , the relation H -> J is a transitive dependency, we should split it into two tables.

R2211(H, J) and R2212(A, D, G, H)

 $R2211 \cap R2212 = \{H\} \rightarrow R2211$ , there are no losses.

For table R2211, the candidate key is {H}, this table is in BCNF already.

For table R2212, the candidate key is {A, D}, this table is in BCNF already.

For table R222, the candidate key is {A, B, D}, this table is in BCNF already.

So the final result should be:

R11(<u>A</u>, I) R12(<u>A</u>, <u>B</u>, C) R21(<u>B</u>, <u>D</u>, E, F) R2211(<u>H</u>, J) R2212(<u>A</u>, <u>D</u>, G, H) R222(<u>A</u>, <u>B</u>, <u>D</u>)

- a) The candidate key of R should be {Book title, Author name}
  - For the relation: Book\_title -> Publisher, Book\_type, it is a partial dependency, so it is in 1<sup>st</sup> normal form
- b) For the relationship: Book\_title -> Publisher, Book\_type, it is a partial dependency, we should split it into two tables.

R1(Book title, Publisher, Book type, List price) and

R2(Book title, Author name, Author affil)

 $R1 \cap R2 = \{Book \ title\} \rightarrow R1$ , there are no losses.

For table R1, the candidate key is {**Book\_title**}, the relation: Book\_type -> List\_price is a transitive dependency, we should split it into two tables.

R11(<u>Book type</u>, List price) and R12(<u>Book title</u>, Publisher, Book type)

 $R11 \cap R12 = \{Book \ type\} \rightarrow R11$ , there are no losses.

For table R11, the candidate key is {Book\_type}, this table is in BCNF already.

For table R12, the candidate key is {**Book\_title**}, this table is in BCNF already.

For table R2, the candidate key is {**Book\_title, Author\_name**}, the relation:

Author name -> Author affil is a partial dependency, we should split it into two tables.

R21(Author name, Author affil) and R22(Book title, Author name)

 $R21 \cap R22 = \{Author\_name\} \rightarrow R21$ , there are no losses.

For table R21, the candidate key is {Author name}, this table is in BCNF already.

For table R22, the candidate key is {Book title, Author name}, it is in BCNF already:

So the final result should be:

R11(Book type, List price)

R12(Book title, Publisher, Book type)

R21(Author name, Author affil)

R22(Book title, Author name)