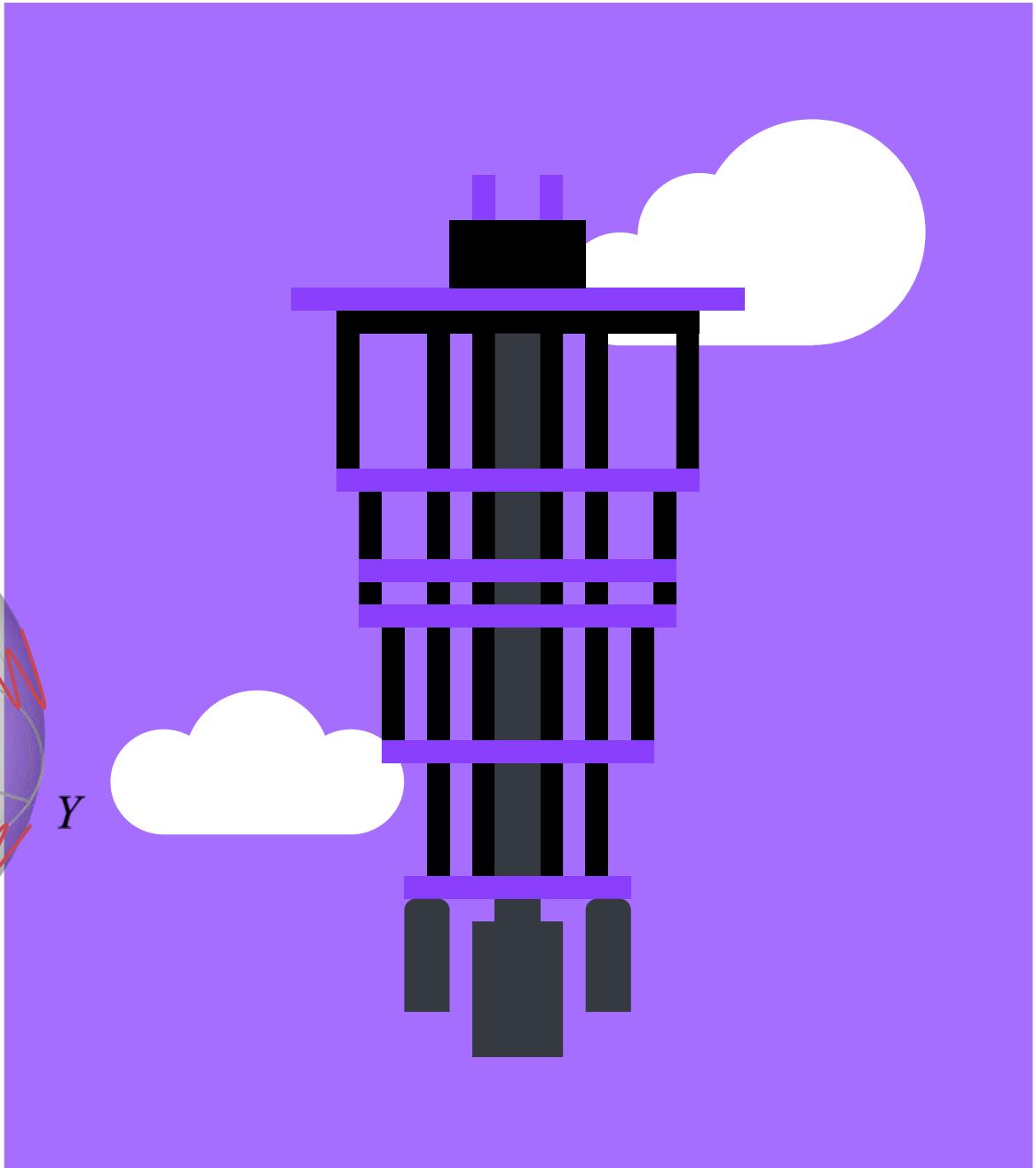
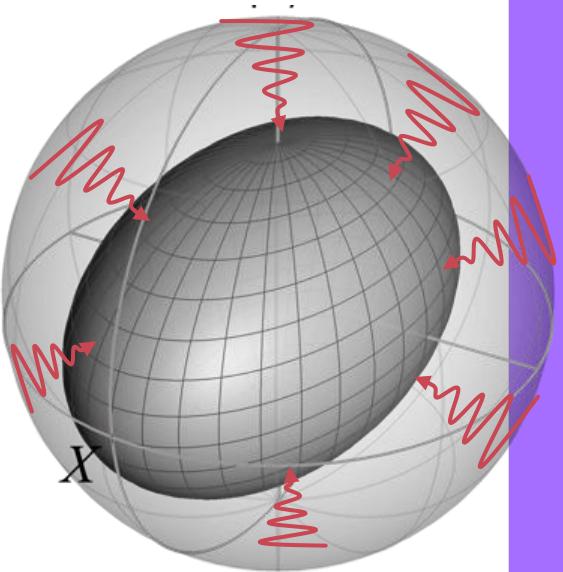


- IBM Quantum Summer Learning Session

Introduction to real quantum computers (and noise)

Zlatko K. Minev
IBM Quantum



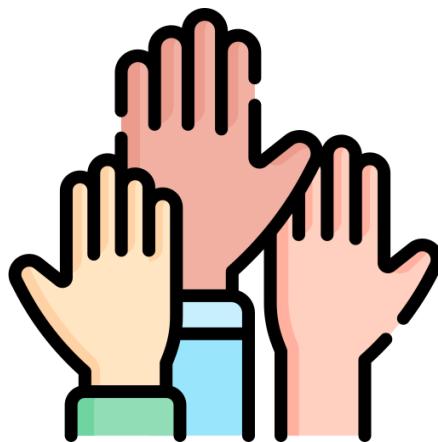
@zlatko_minev



zlatko-minev.com/blog



Have you used
a quantum computer?



Quantum Noise and Error Mitigation

Lecture 1

Big picture

Quantum computers status

Why error mitigation?

Noise in quantum computers

Overview of error mitigation

Mitigation fundamentals

Probabilistic error cancelation (PEC)

Introduction

One qubit example

Next lecture

Learning noise

State-of-art mitigation experiments

Hardware

Outlook



Where?

Slides from lecture

Posted here zlatko-minev.com/education
Tutorials [/blog](https://zlatko-minev.com/blog)

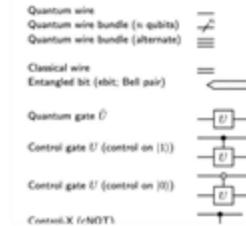
See

IBM Learning
learning.quantum.ibm.com

Weekly seminars
[qiskit YouTube](https://www.youtube.com/qiskit)

7. Digital quantum circuits (pictorial)

7A. Basic elements

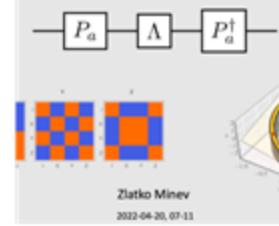


tech-note = quantum circuits, cheat sheet

Cheat sheet: Digital quantum circuits - pictorial 101

Making a qubit cheatsheet,
On this festive Christmas day.

Primer on Pauli Twirling



Zlatko Minev
2022-04-20, 07-11

tutorial = quantum noise

A tutorial on tailoring quantum noise - Twirling 101 (Parts I-IV)

Nutshell introduction to tailoring quantum noise by twirling into stochastic Pauli or

learn and cancel quantum noise cancellation with sparse Pauli-Lindblad models on quantum processors



Zlatko K. Minev
in den Berg, Zlatko K. Minev, Abhinav Kandala, Kristan
arXiv:2201.09668 (2022)

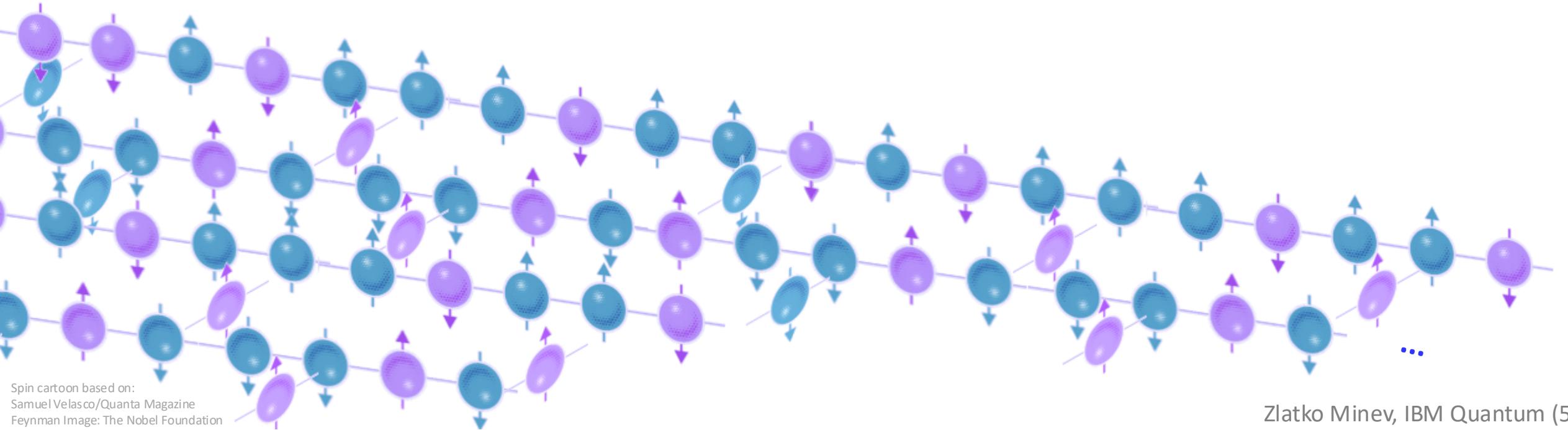
ents: broader IBM Quantum team
@zlatko_minev

talk = pec

Talk: To Learn and Cancel Noise: Probabilistic Error Cancellation with Sparse Pauli-Lindblad Models on Noisy Quantum Processors

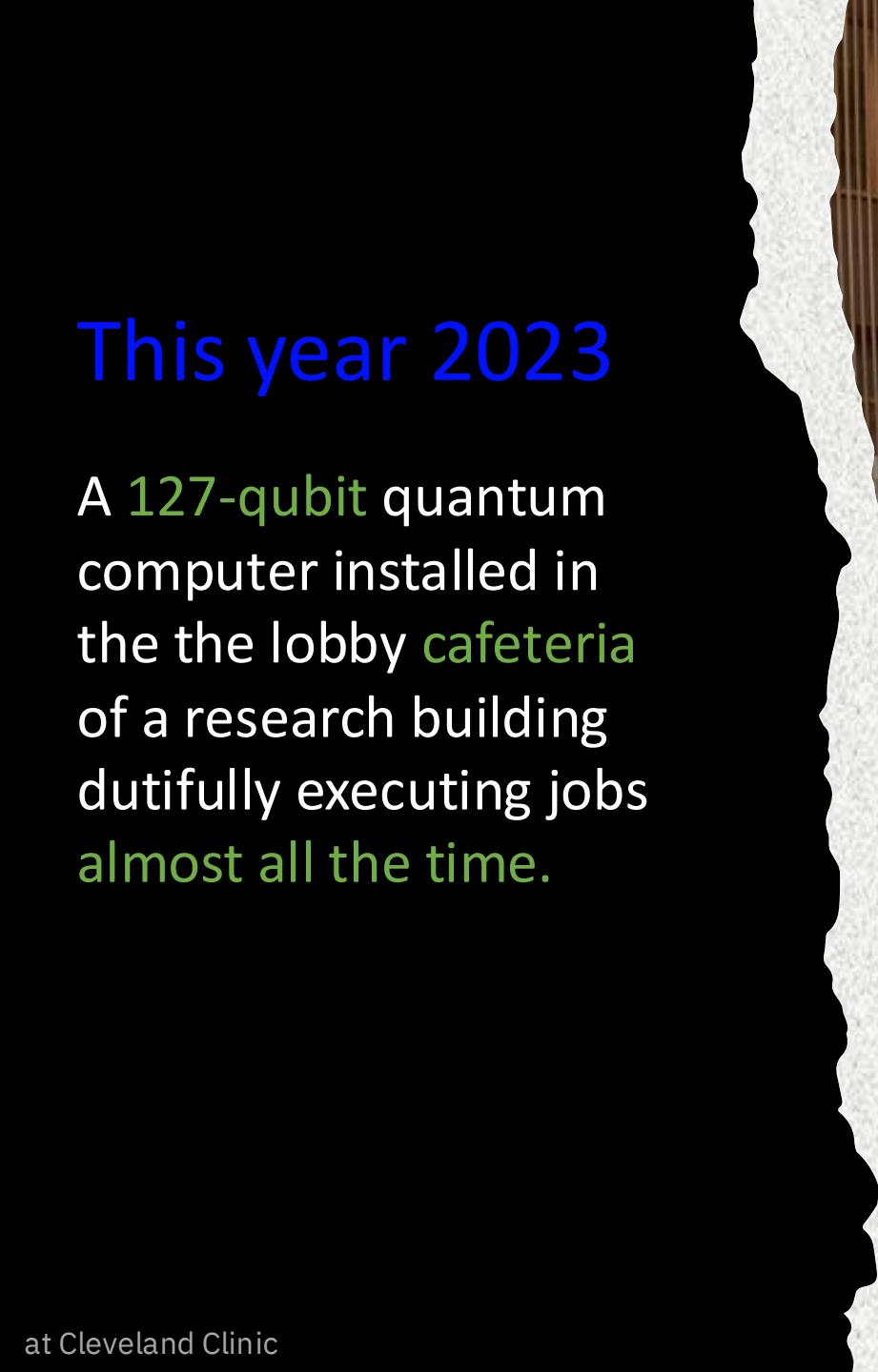


How is it going for quantum computers?



Spin cartoon based on:
Samuel Velasco/Quanta Magazine
Feynman Image: The Nobel Foundation

Zlatko Minev, IBM Quantum (5)



This year 2023

A 127-qubit quantum computer installed in the lobby cafeteria of a research building dutifully executing jobs almost all the time.





Credit: Connie Zhou for IBM



2019

Falcon

27 Qubits

2020

Hummingbird

65 Qubits

2021

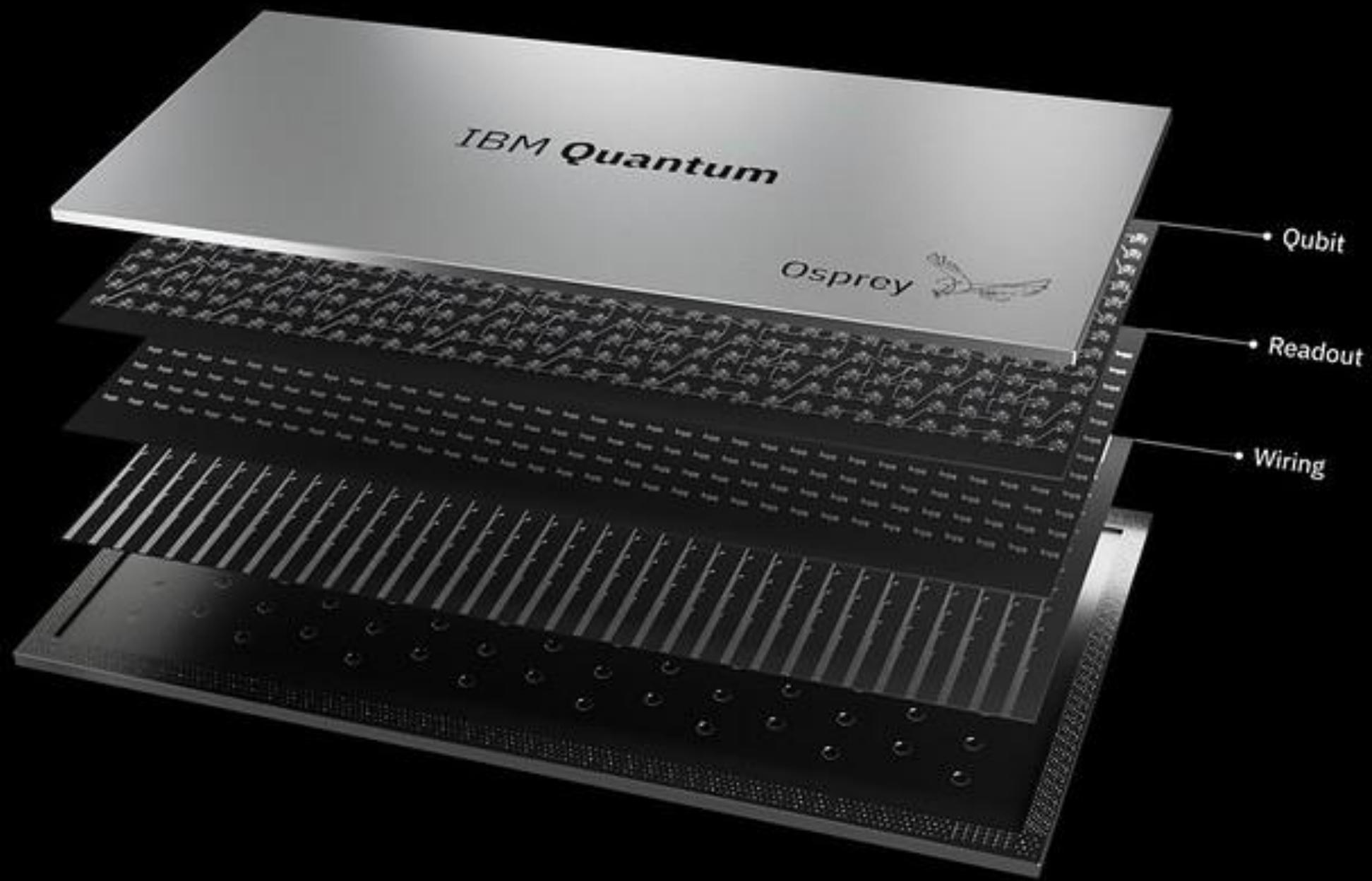
Eagle

127 Qubits

2022

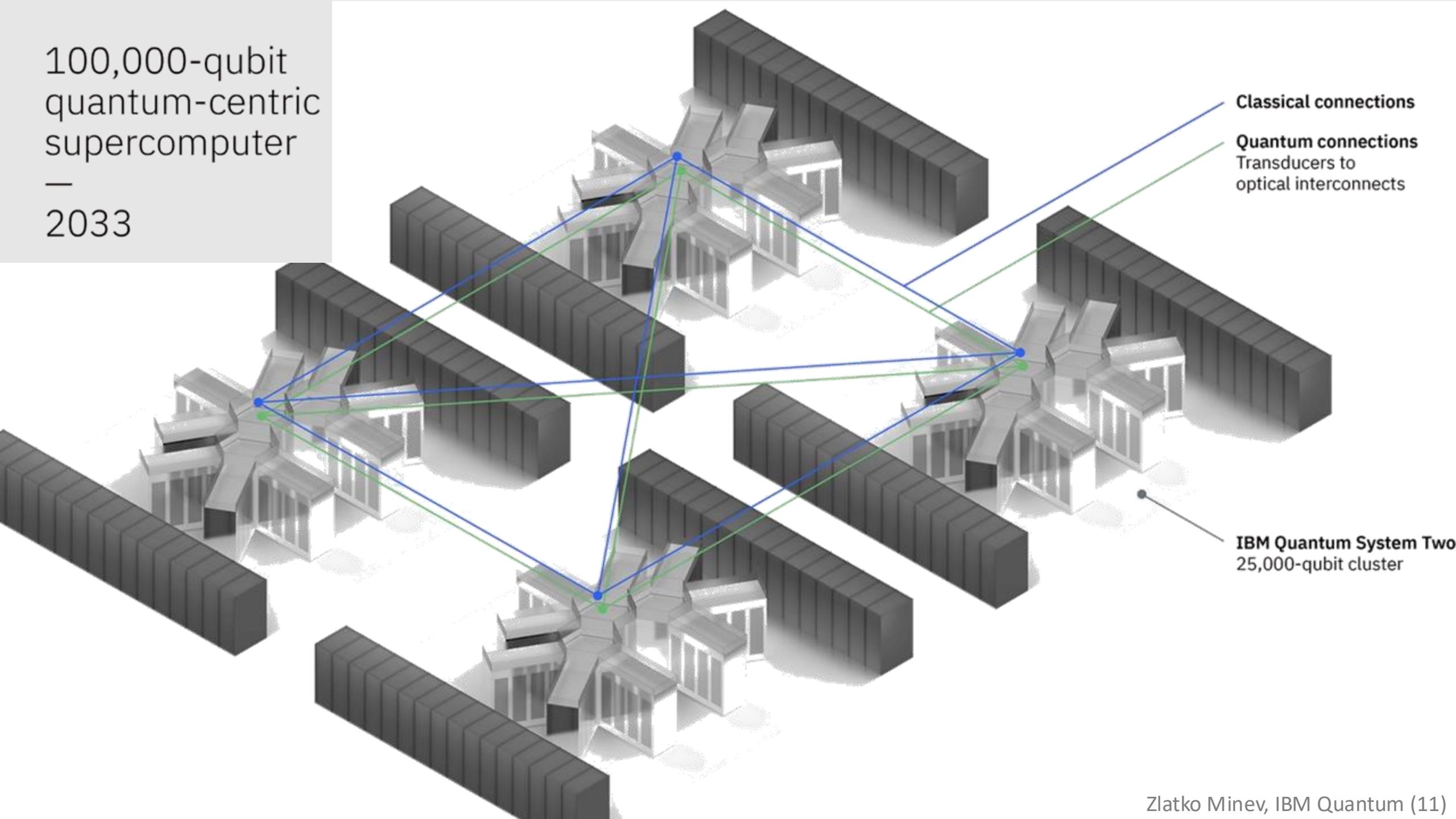
Osprey

433 Qubits





100,000-qubit
quantum-centric
supercomputer
—
2033



Development Roadmap

IBM Quantum

2016–2019 ✓	2020 ✓	2021 ✓	2022 ✓	2023 ✓	2024	2025	2026	2027	2028	2029	2033+	
Run quantum circuits on the IBM Quantum Platform	Release multi-dimensional roadmap publicly with initial aim focused on scaling	Enhancing quantum execution speed by 100x with Qiskit Runtime	Bring dynamic circuits to unlock more computations	Enhancing quantum execution speed by 5x with quantum serverless and Execution modes	Improving quantum circuit quality and speed to allow 5K gates with parametric circuits	Enhancing quantum execution speed and parallelization with partitioning and quantum modularity	Improving quantum circuit quality to allow 7.5K gates	Improving quantum circuit quality to allow 10K gates	Improving quantum circuit quality to allow 15K gates	Improving quantum circuit quality to allow 100M gates	Beyond 2033, quantum-centric supercomputers will include 1000's of logical qubits unlocking the full power of quantum computing	
Data Scientist					Platform	Code assistant	Functions	Mapping Collection	Specific Libraries		General purpose QC libraries	
Researchers					Middleware	Quantum Serverless	Transpiler Service	Resource Management	Circuit Knitting x P	Intelligent Orchestration	Circuit libraries	
Quantum Physicist	IBM Quantum Experience	Qiskit Runtime	QASM3	Dynamic circuits	Execution Modes	Heron (5K)	Flamingo (5K)	Flamingo (7.5K)	Flamingo (10K)	Flamingo (15K)	Starling (100M)	Blue Jay (1B)
	Early Canary 5 qubits Albatross 16 qubits Penguin 20 qubits Prototype 53 qubits	Falcon Benchmarking 27 qubits	Eagle Benchmarking 127 qubits			Error Mitigation 5k gates 133 qubits Classical modular $133 \times 3 = 399$ qubits	Error Mitigation 5k gates 156 qubits Quantum modular $156 \times 7 = 1092$ qubits	Error Mitigation 7.5k gates 156 qubits Quantum modular $156 \times 7 = 1092$ qubits	Error Mitigation 10k gates 156 qubits Quantum modular $156 \times 7 = 1092$ qubits	Error Mitigation 15k gates 156 qubits Quantum modular $156 \times 7 = 1092$ qubits	Error correction 100M gates 200 qubits	Error correction 1B gates 2000 qubits

Innovation Roadmap

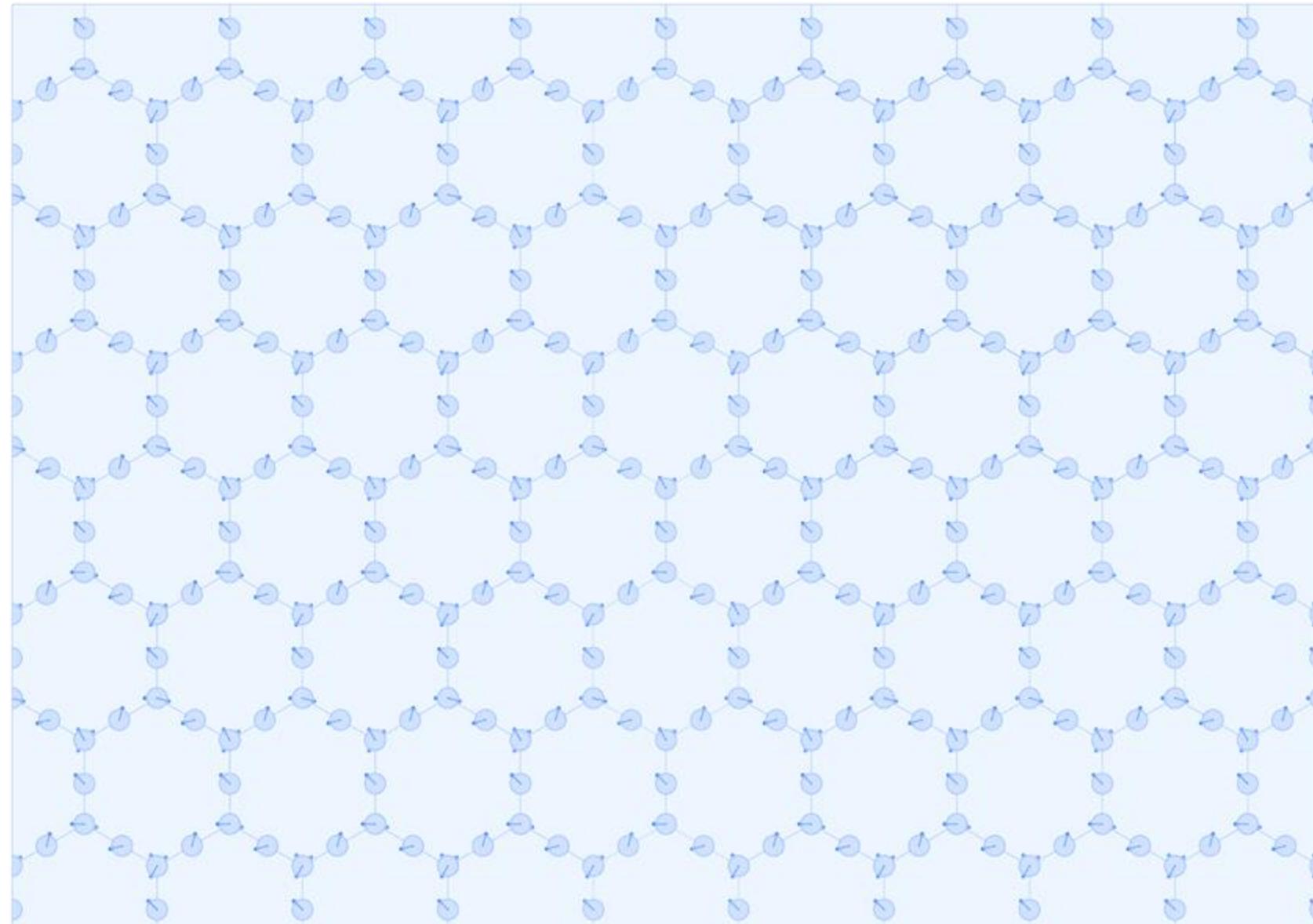
Software Innovation	IBM Quantum Experience ✓	Qiskit ✓	Application modules	Qiskit Runtime ✓	Serverless	AI enhanced quantum	Resource management	Scalable circuit knitting	Error correction decoder		
Hardware Innovation	Early Canary 5 qubits Albatross 16 qubits	Falcon Demonstrate scaling with I/O routing with Bump bonds	Hummingbird Demonstrate scaling with multiplexing readout	Eagle Demonstrate scaling with MLW and TSV	Osprey Enabling scaling with high density signal delivery	Condor Single system scaling and fridge capacity	Flamingo Demonstrate scaling with modular connectors	Kookaburra Demonstrate scaling with nonlocal c-coupler	Cockatoo Demonstrate path to improved quality with logical memory	Starling Demonstrate path to improved quality with logical communication	
 Executed by IBM  On target											

Back to today ...

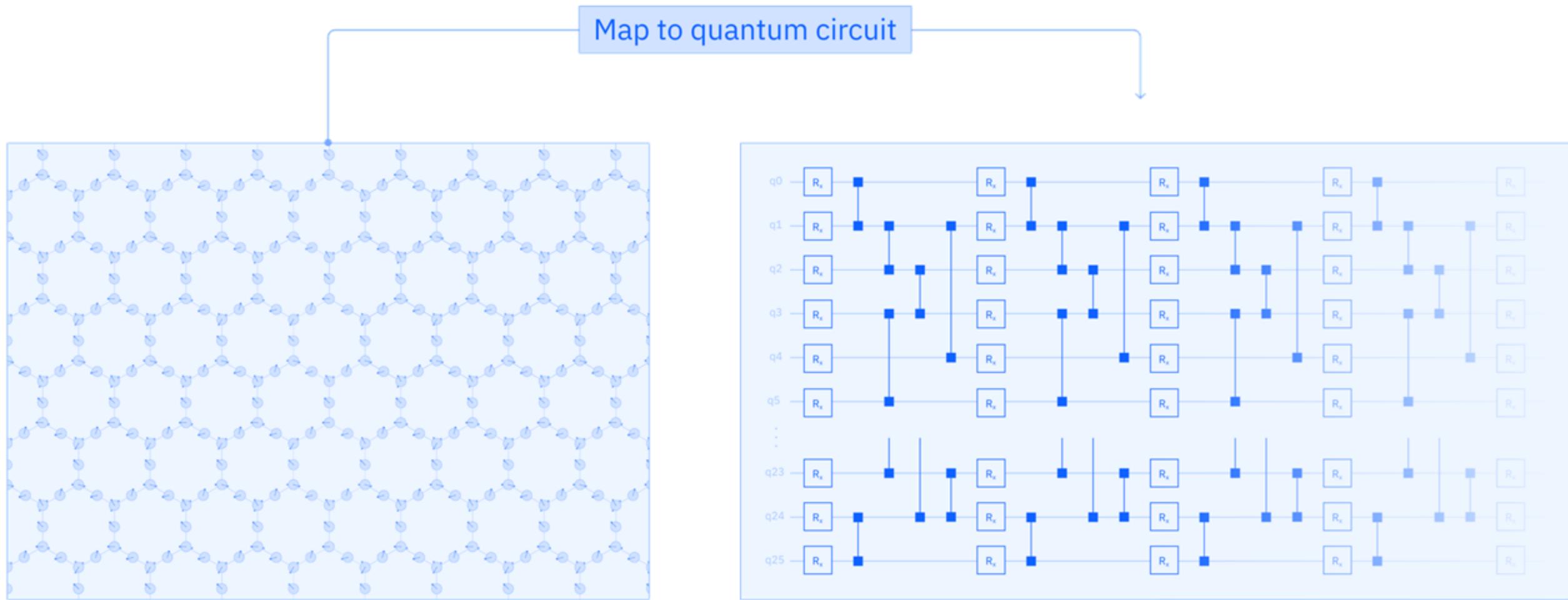
Example: Quantum simulation

Example task:

Simulate the out-of-equilibrium quantum dynamics of a 2D spin chain lattice to find the evolution of the global and local magnetization.

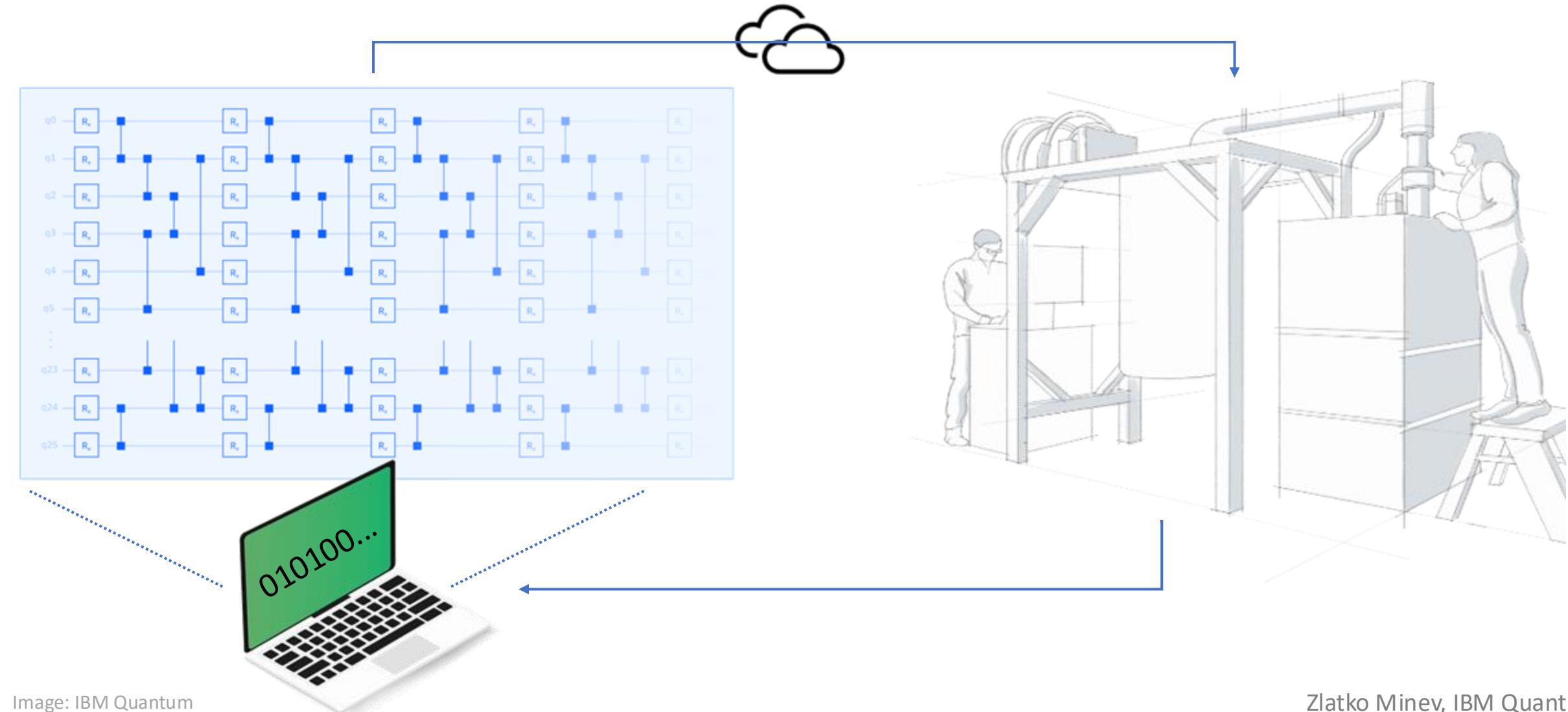


Quantum simulation on a quantum computer



Quantum simulation on a quantum computer

Execute on a real quantum computer device and obtain results as classical data



Biggest challenge?

Please do share

hardware
development

error correction
overheads

scalability

engineering

need CS/EE
talent

decoherence

high error rates

material
quality

Noise (Errors)

Biggest challenge?

loss

heat

stability

algo
development

modularization

importance of N
in NISQ

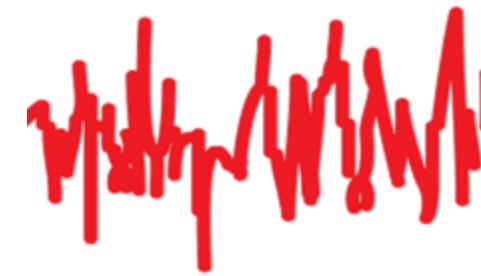
gravity

hype

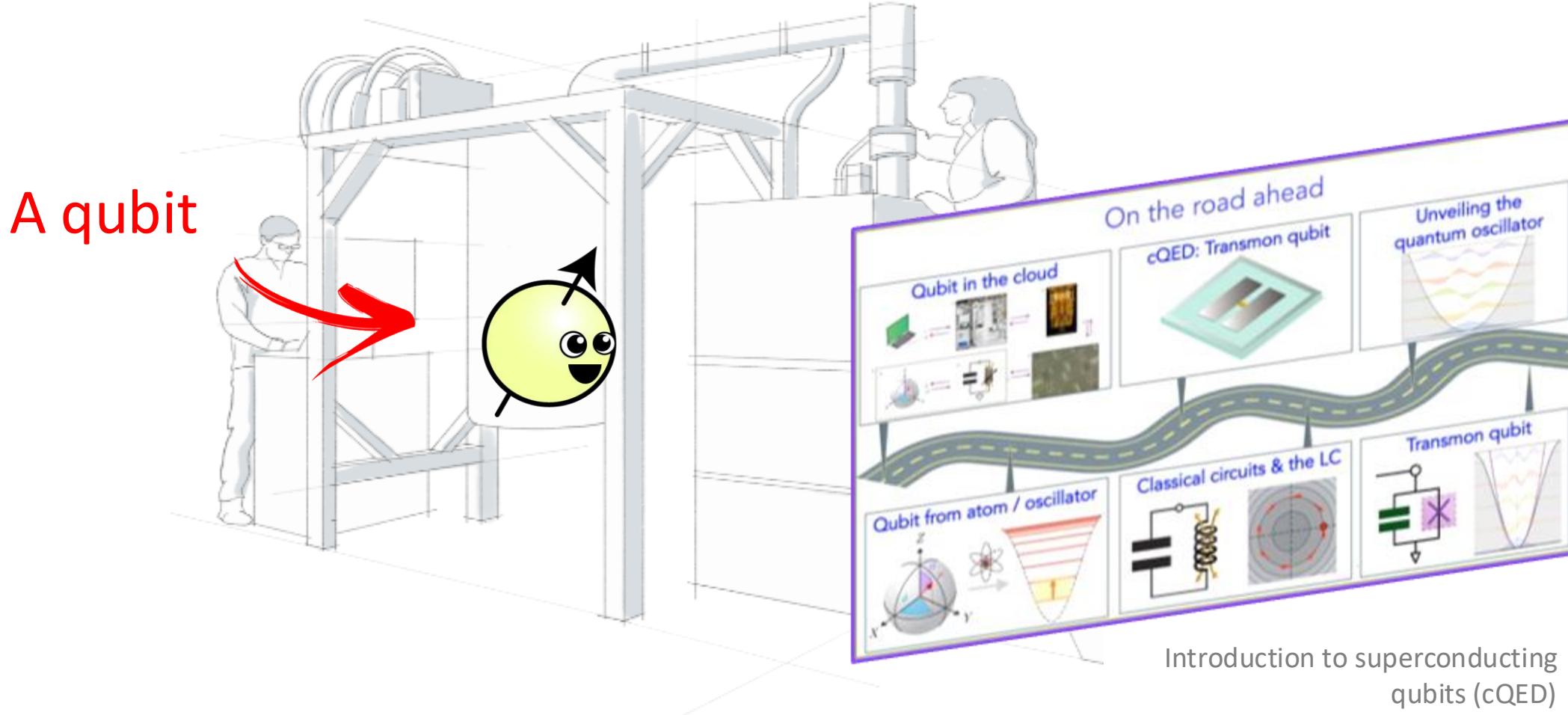
expectations

Biggest challenge

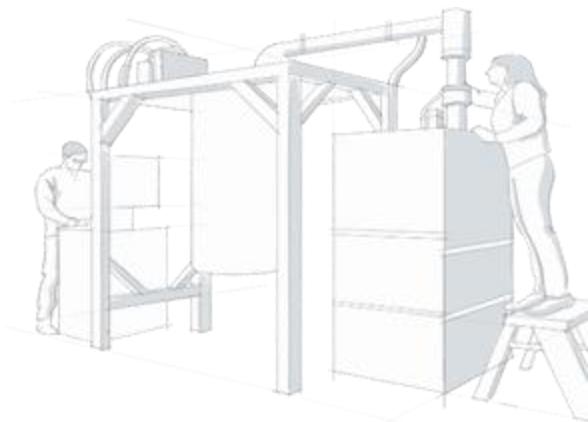
Noise
(Errors)



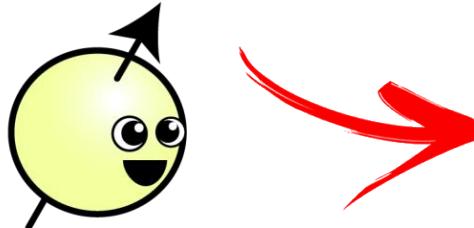
Hello World with a real experiment!



Hello World! building blocks

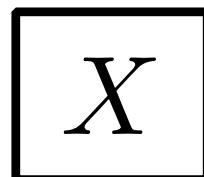


A qubit

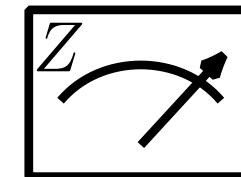
 $|1\rangle$ $|0\rangle$

Computational
basis states

Operations: qubit gate



Measurements: qubit observable



refresher:

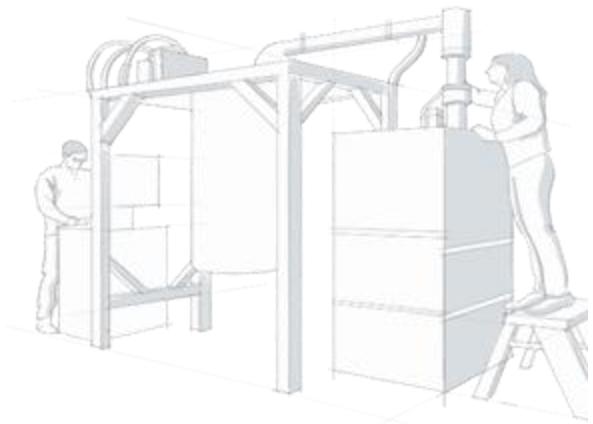
$$X |0\rangle = |1\rangle$$

$$X |1\rangle = |0\rangle$$

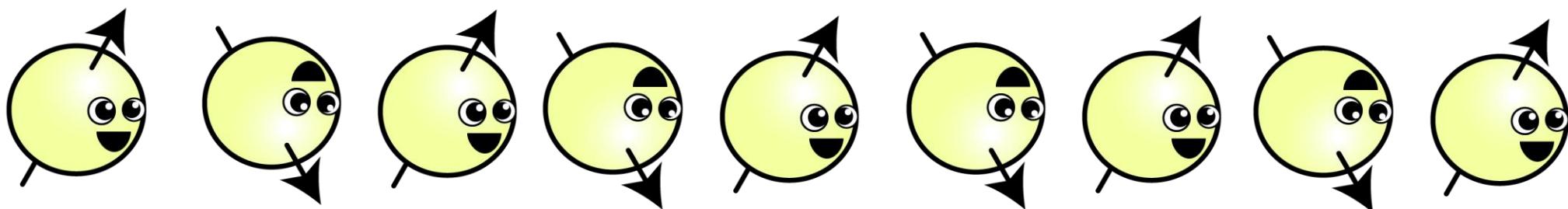
$$Z |0\rangle = +1 |0\rangle$$

$$Z |1\rangle = -1 |1\rangle$$

Hello World! Even-odd algo: qubit flipper



Task: Classify or report if a classical positive integer d is even or odd.



flip spin d times, measure polarization

refresher:

$$X |0\rangle = |1\rangle$$

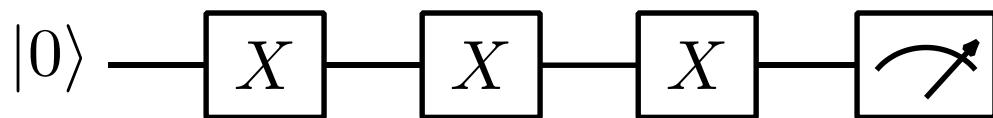
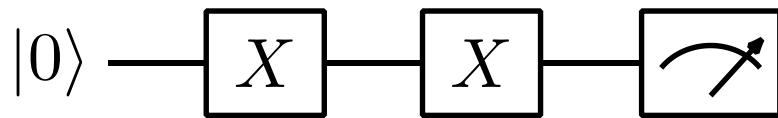
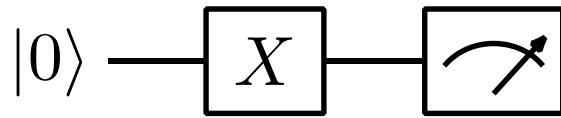
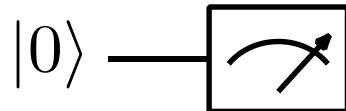
$$X |1\rangle = |0\rangle$$

$$Z |0\rangle = +1 |0\rangle$$

$$Z |1\rangle = -1 |1\rangle$$

Hello World! qubit flipper quantum circuits

depth



:

refresher:

$$X |0\rangle = |1\rangle$$

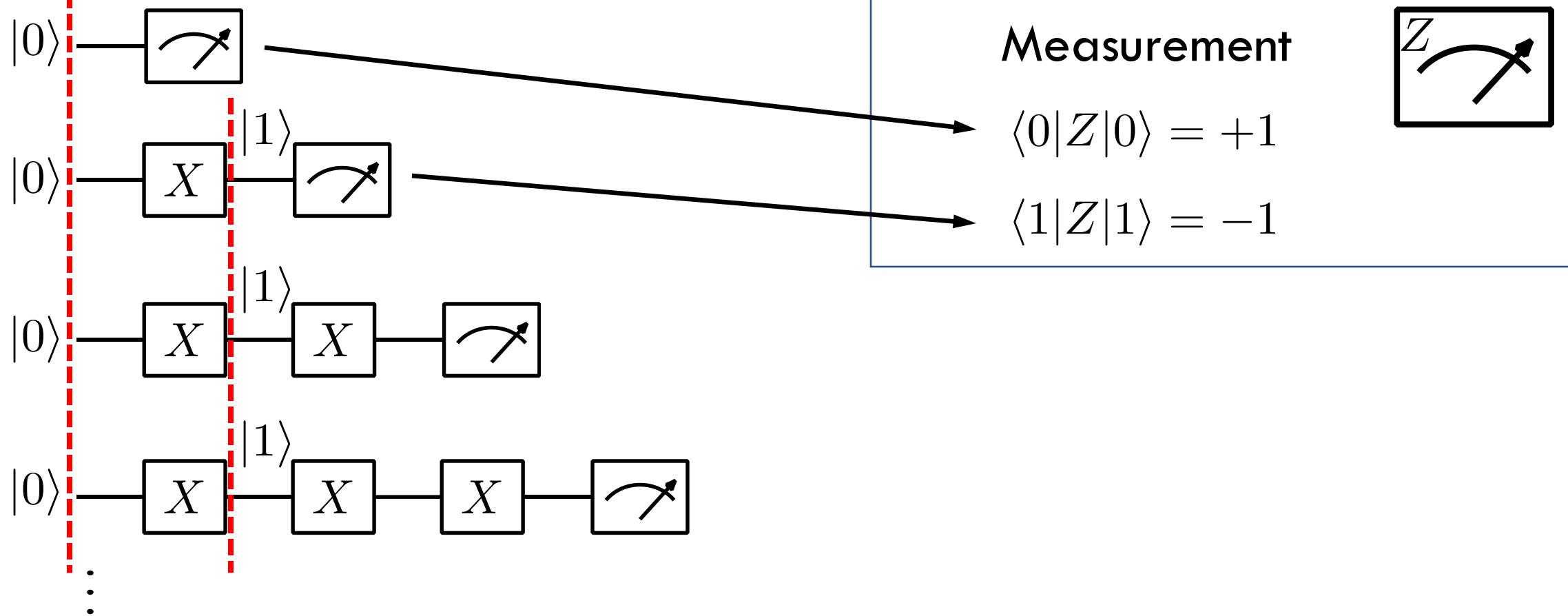
$$X |1\rangle = |0\rangle$$

$$Z |0\rangle = +1 |0\rangle$$

$$Z |1\rangle = -1 |1\rangle$$

Hello World! “debugger” step through

depth



refresher:

$$X |0\rangle = |1\rangle$$

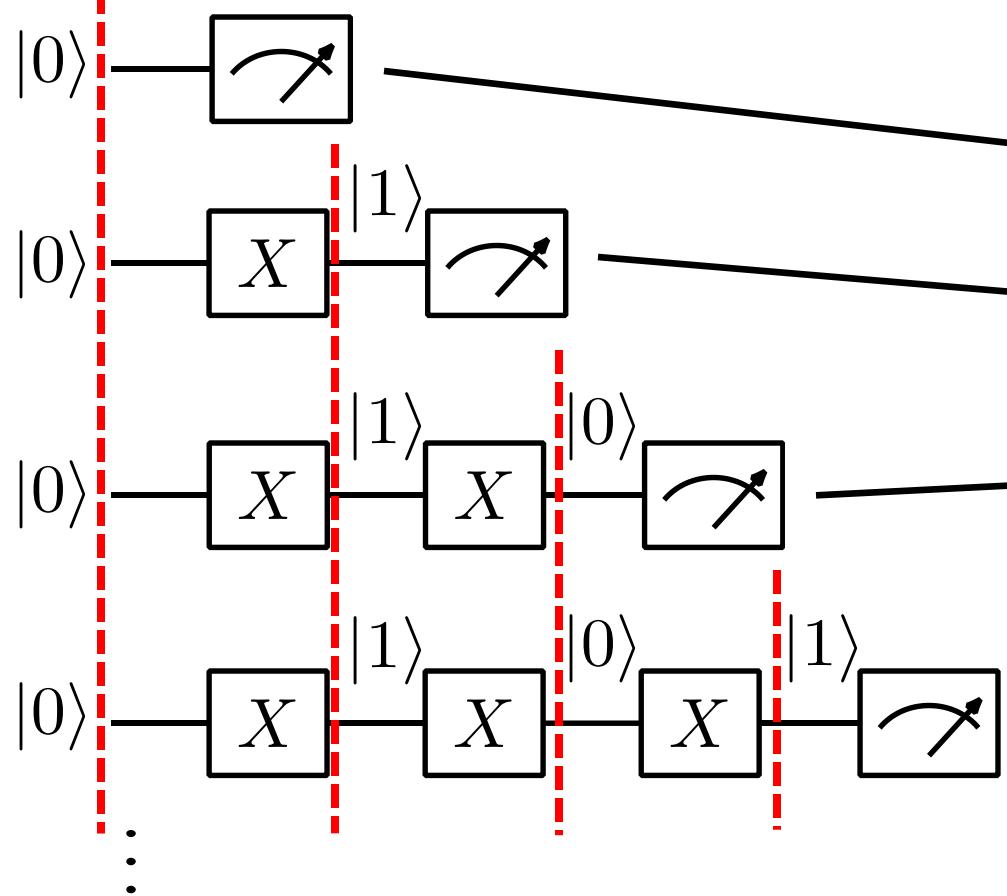
$$X |1\rangle = |0\rangle$$

$$Z |0\rangle = +1 |0\rangle$$

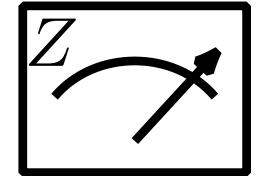
$$Z |1\rangle = -1 |1\rangle$$

Hello World! “debugger” step through

depth



Measurement



$$\langle 0|Z|0\rangle = +1$$

$$\langle 1|Z|1\rangle = -1$$

$$\langle 0|Z|0\rangle = +1$$

$$\langle Z \rangle = (-1)^d$$

where d is the circuit depth

refresher:

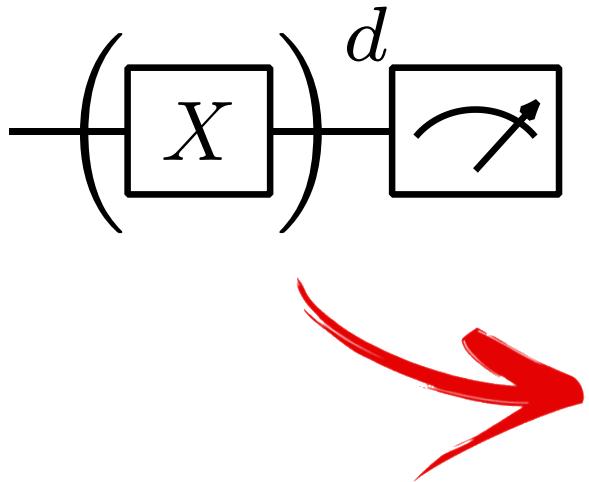
$$X |0\rangle = |1\rangle$$

$$X |1\rangle = |0\rangle$$

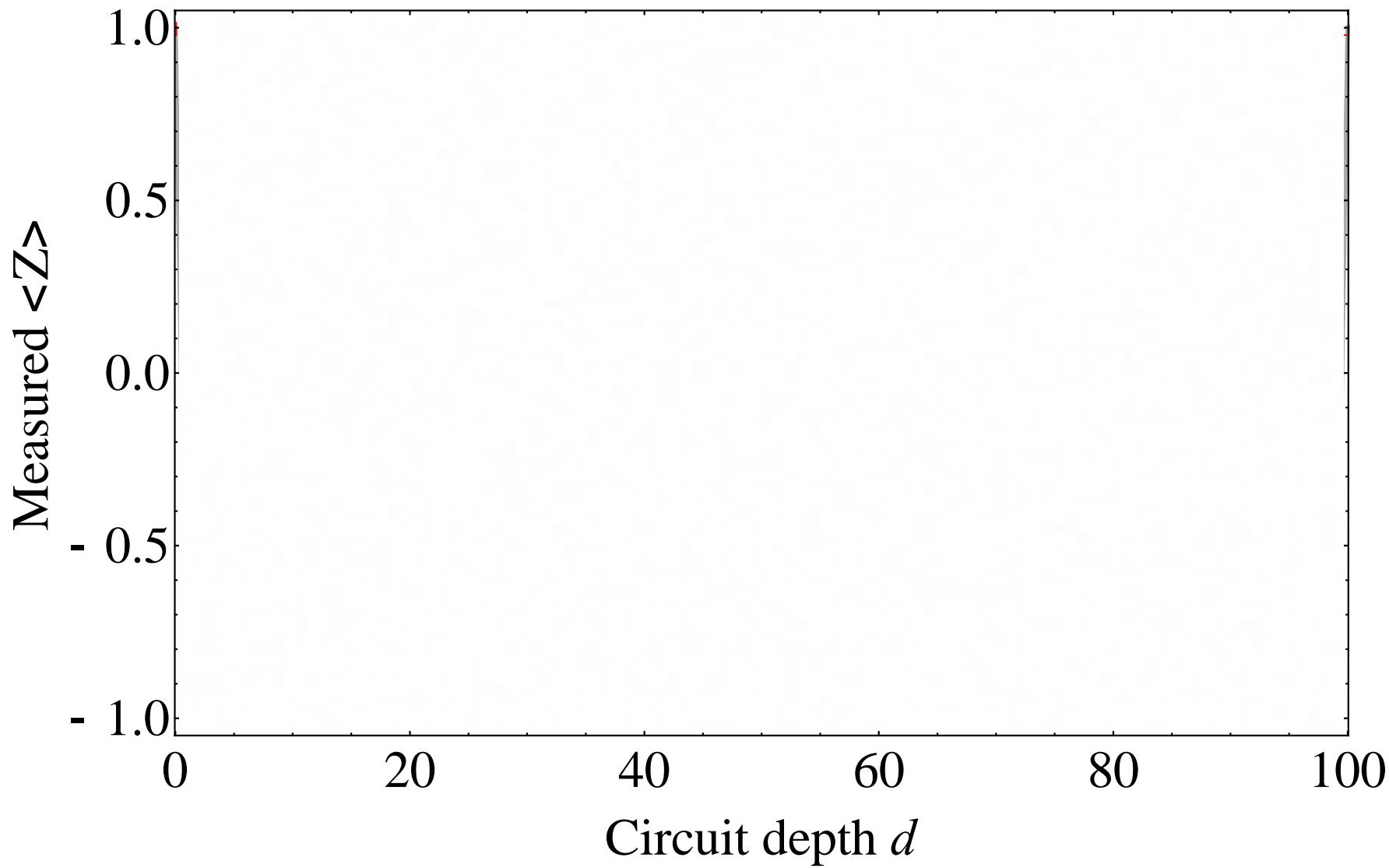
$$Z |0\rangle = +1 |0\rangle$$

$$Z |1\rangle = -1 |1\rangle$$

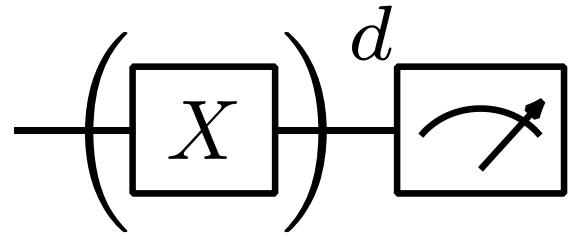
Hello World! Ideal expectation results



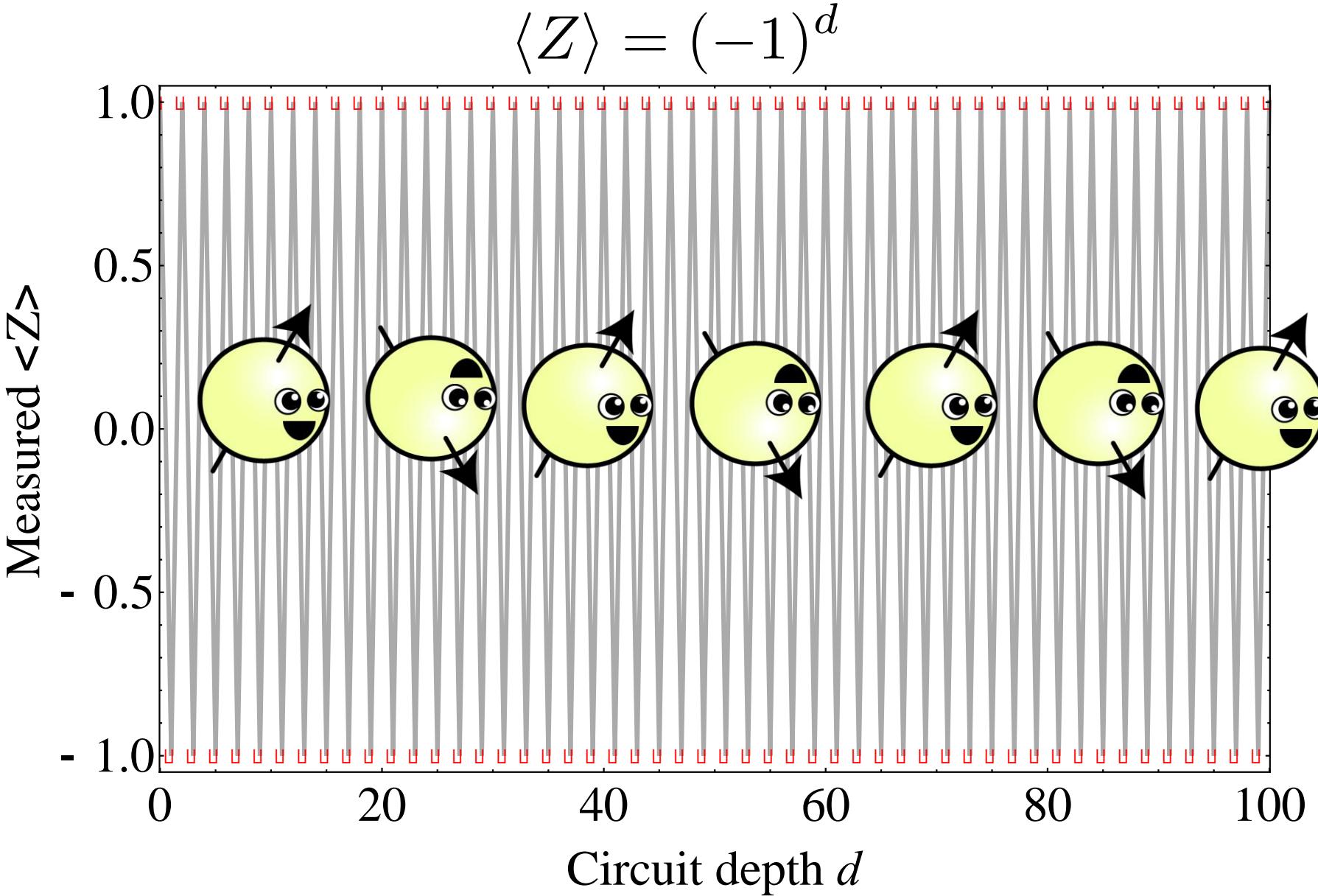
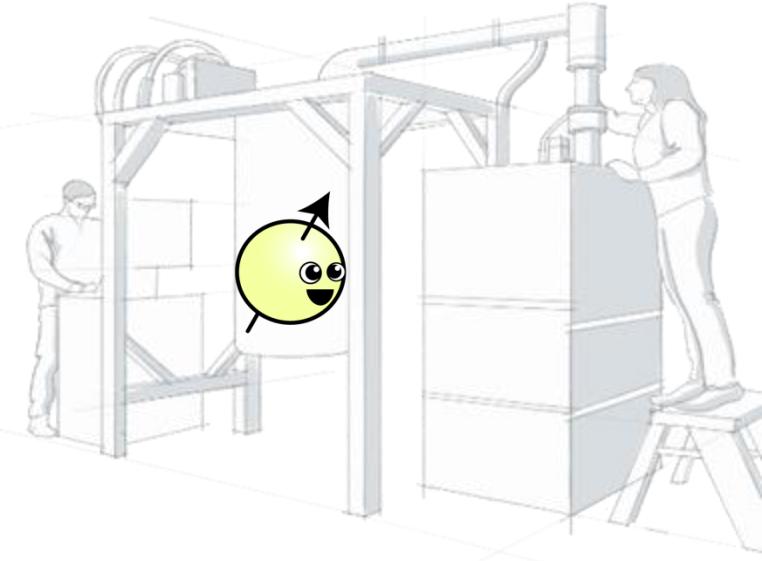
$$\langle Z \rangle = (-1)^d$$



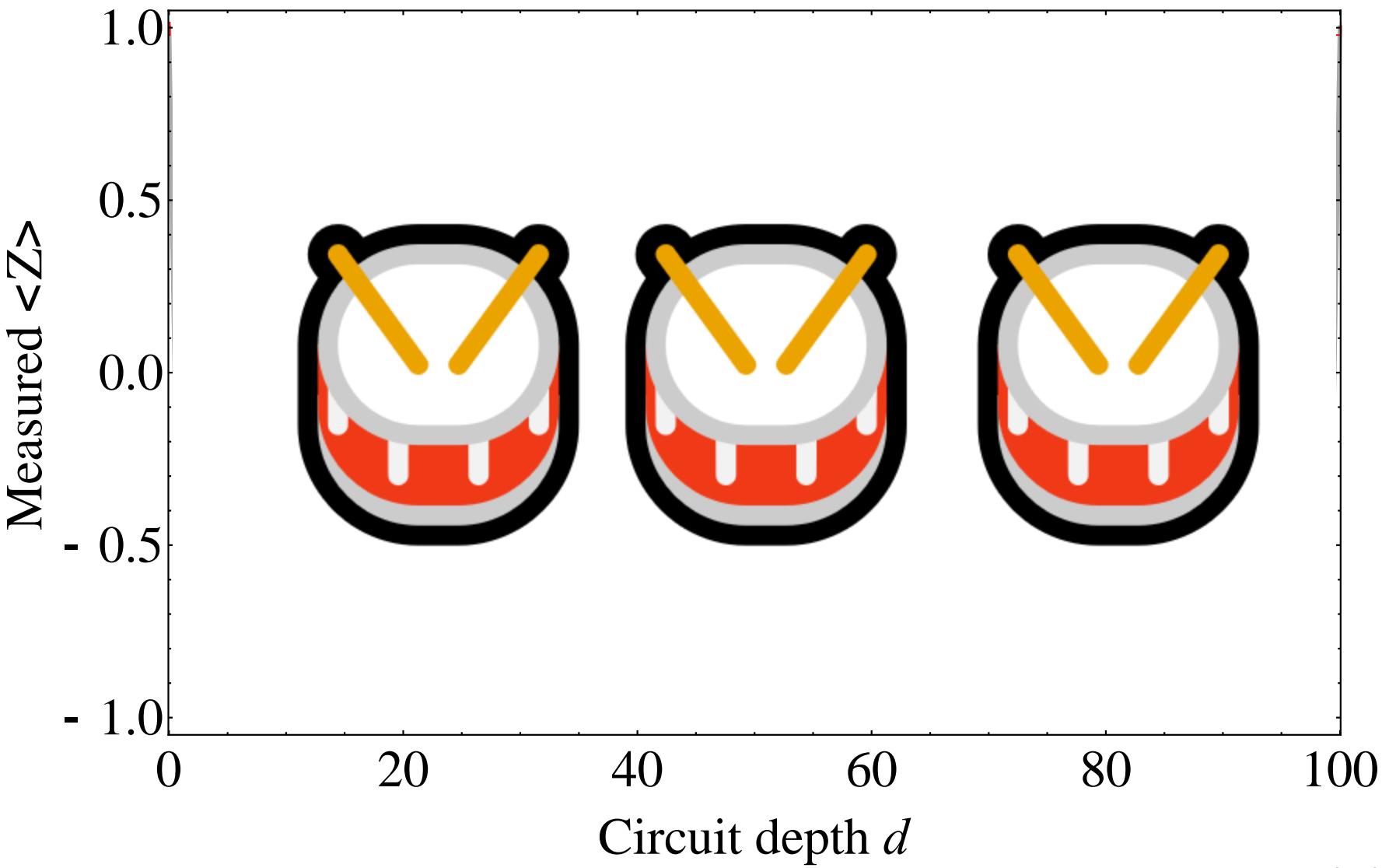
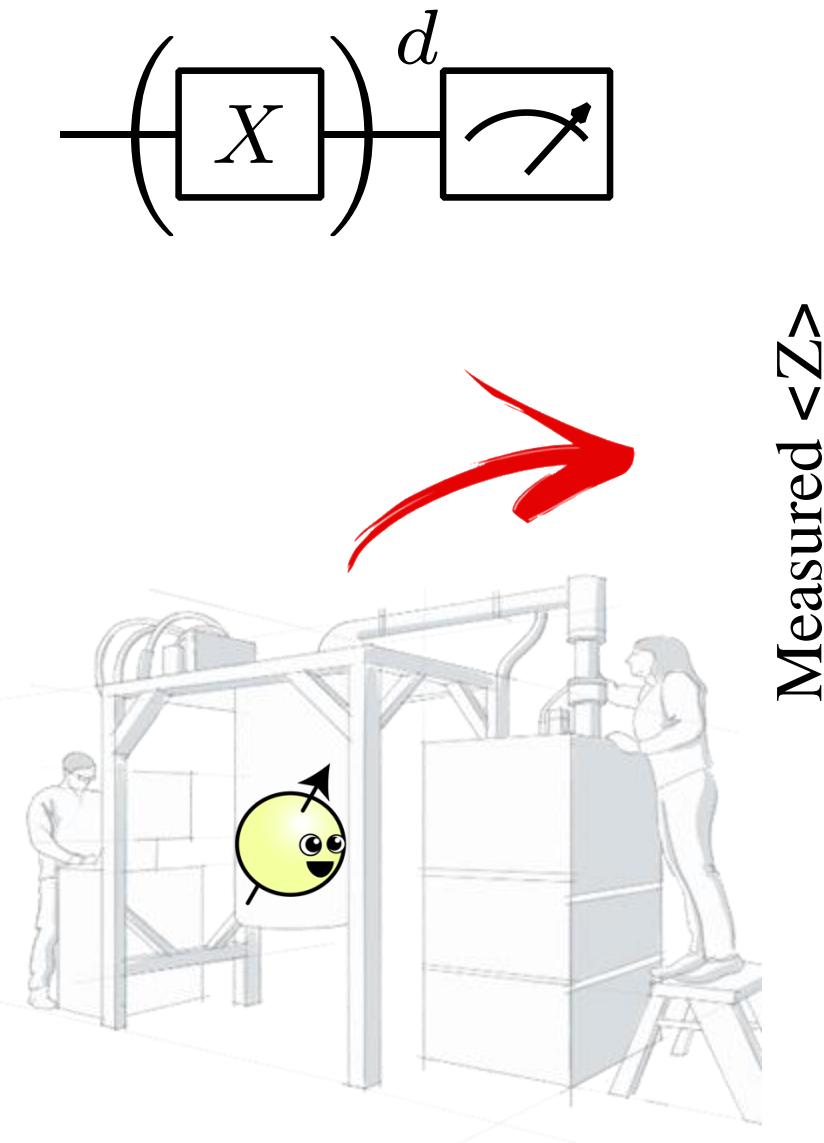
Hello World! Ideal expectation results



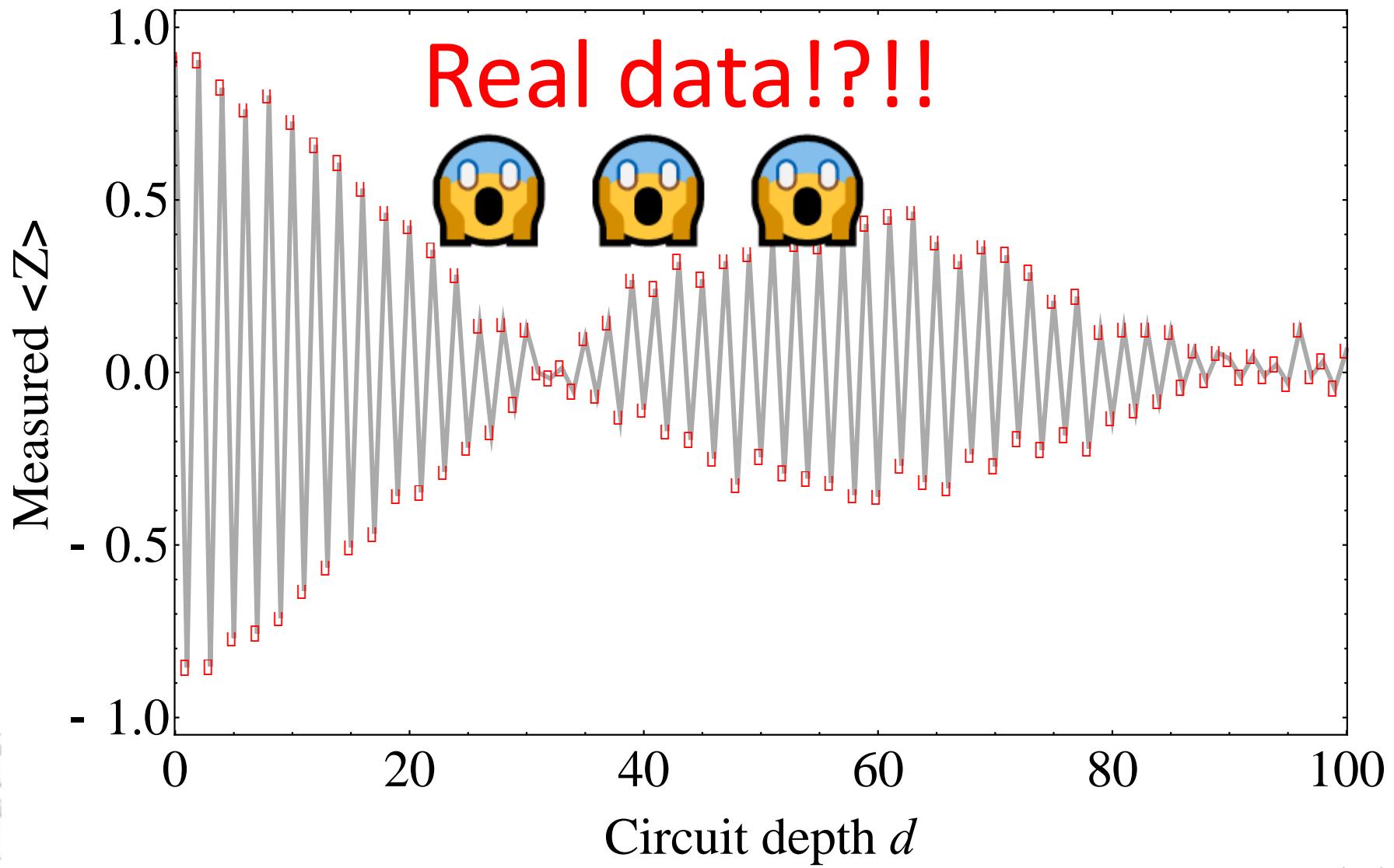
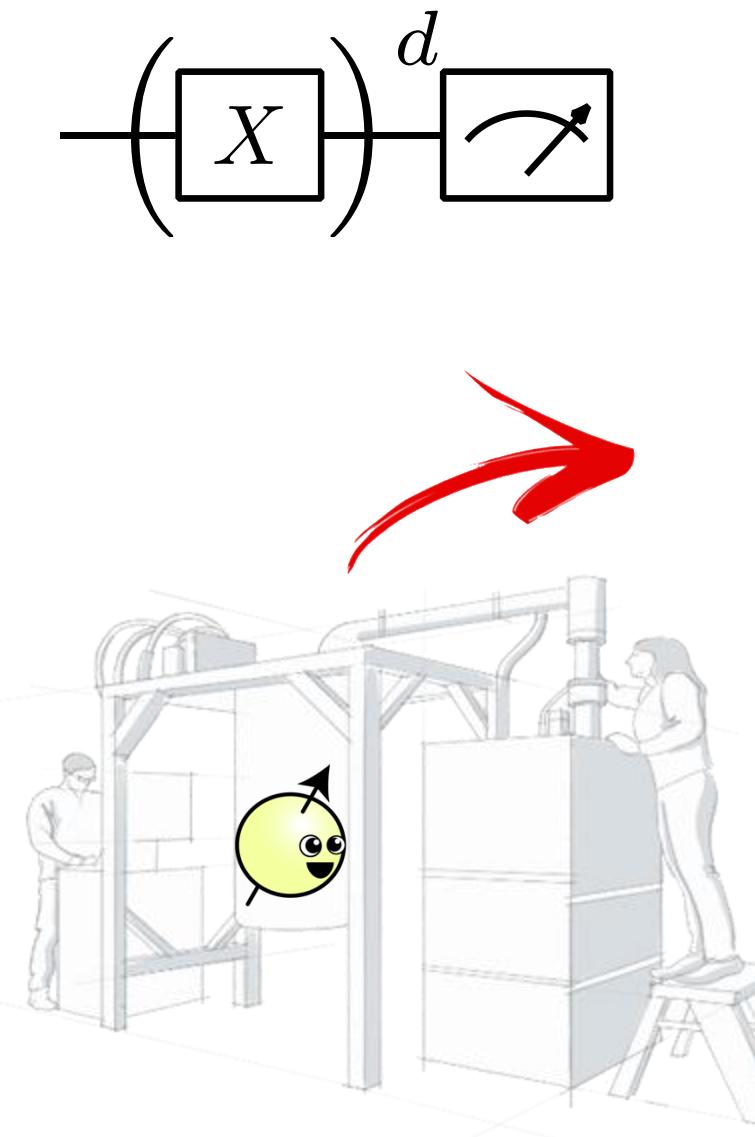
Let's run on a real device!



Hello World! Running



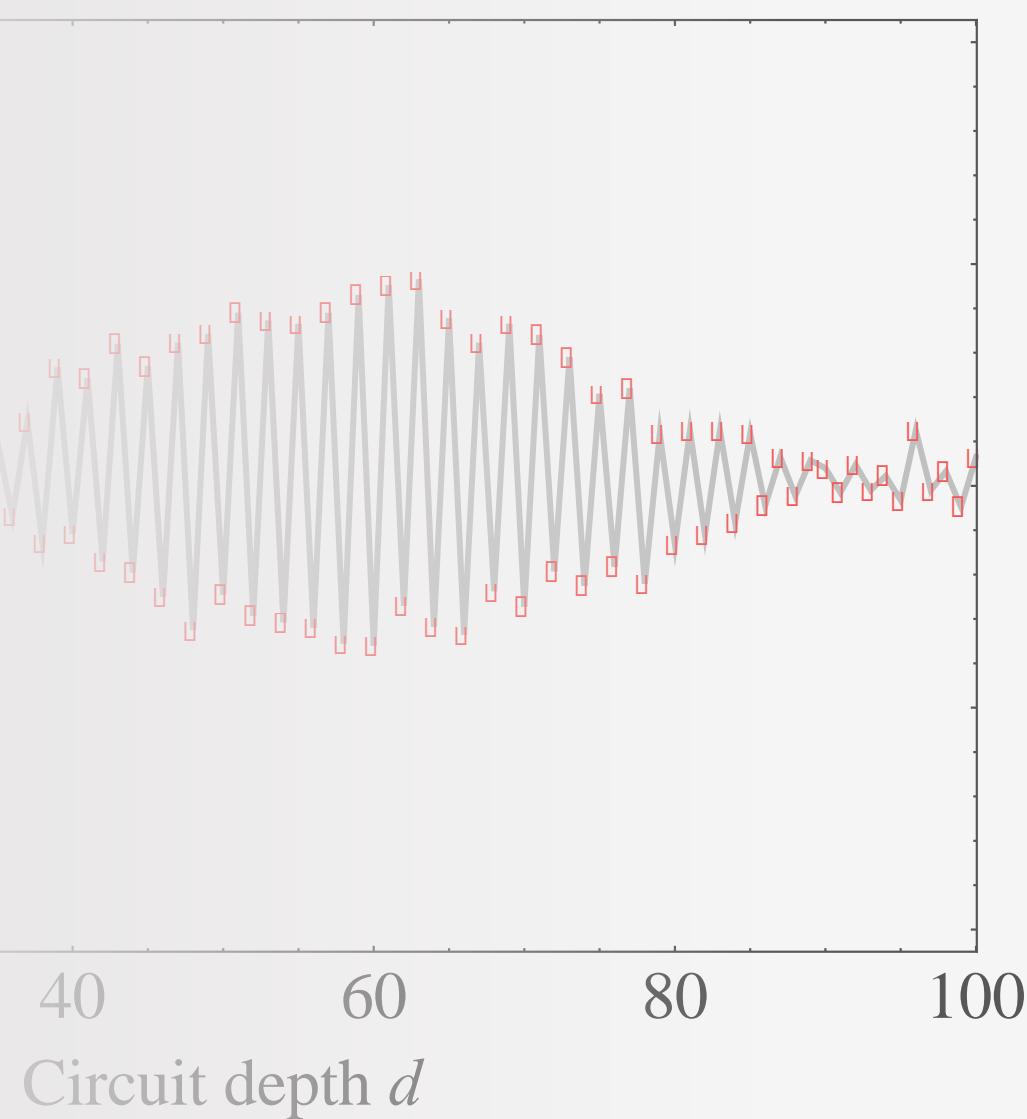
Hello World! Real expectation results

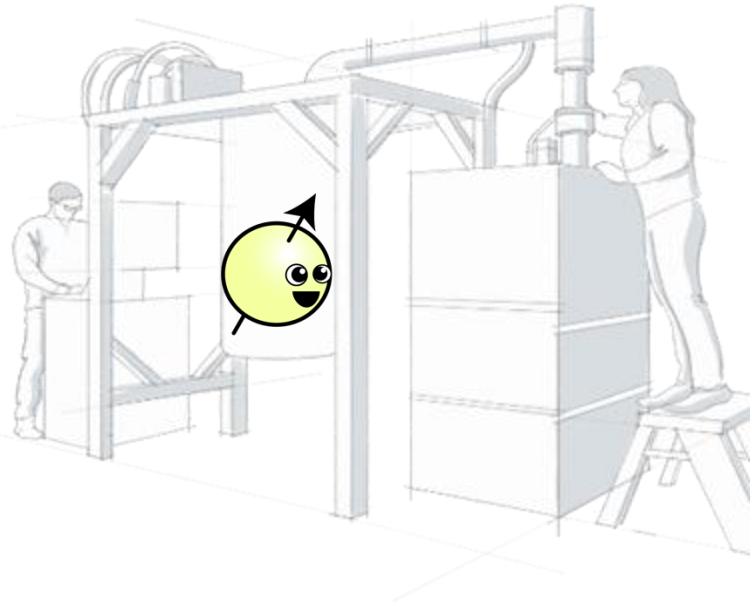


Real & noisy quantum processors: Why study noise?



*"Well, your quantum computer is broken in
every way possible simultaneously."*

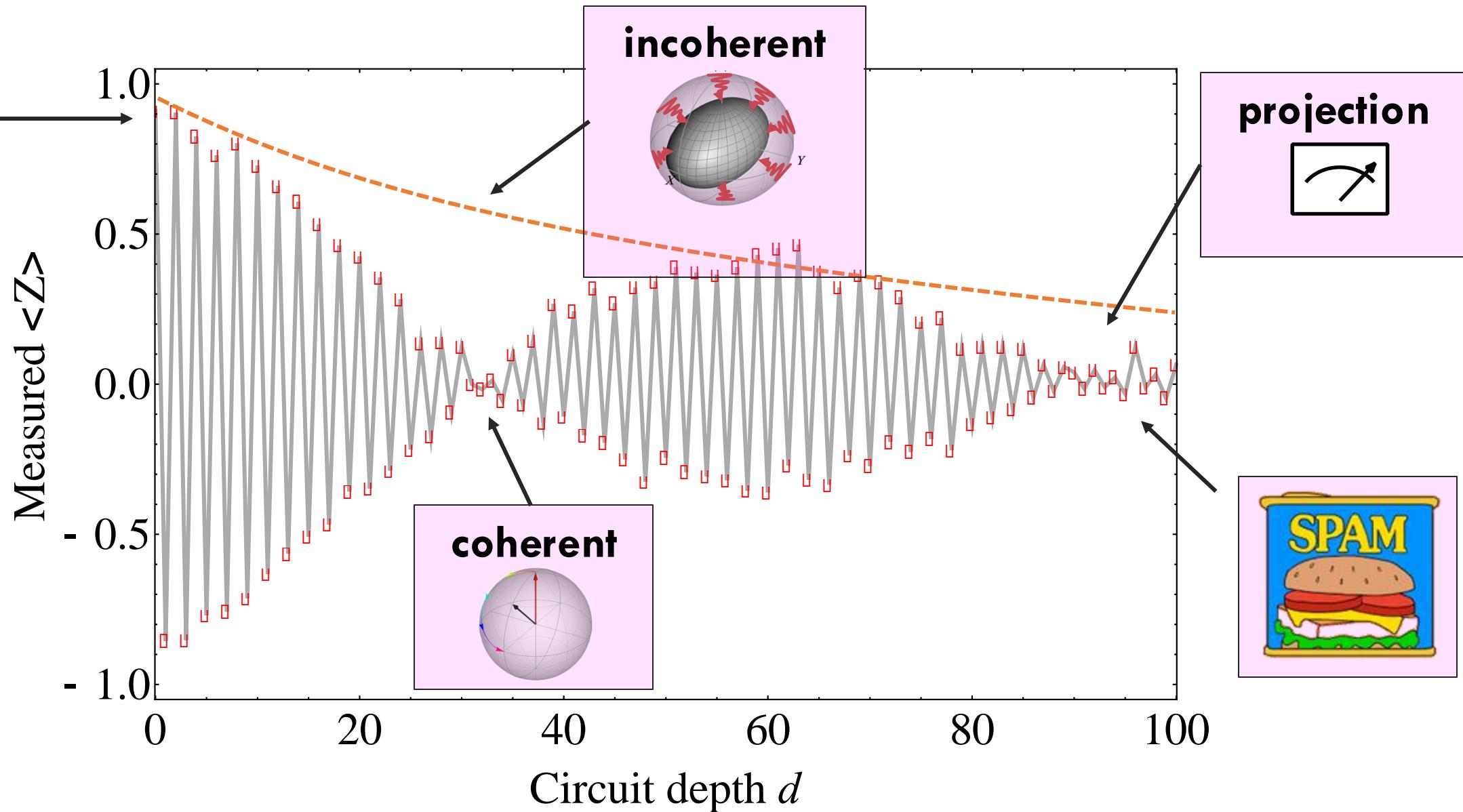




“Quantum phenomena
do *not* occur in a Hilbert space,
they occur in a laboratory.”

Asher Peres

Elements of noise



How to deal with errors due to noise?

Monitor

Error occurs

Error detect



Quantum error correction

Shor, PRA (1995), ...

Monitor

Error anticipated

Tell signal detected



Catch and reverse

Minev, Nature (2019), ...

No monitor

Error occurs

Error undetected

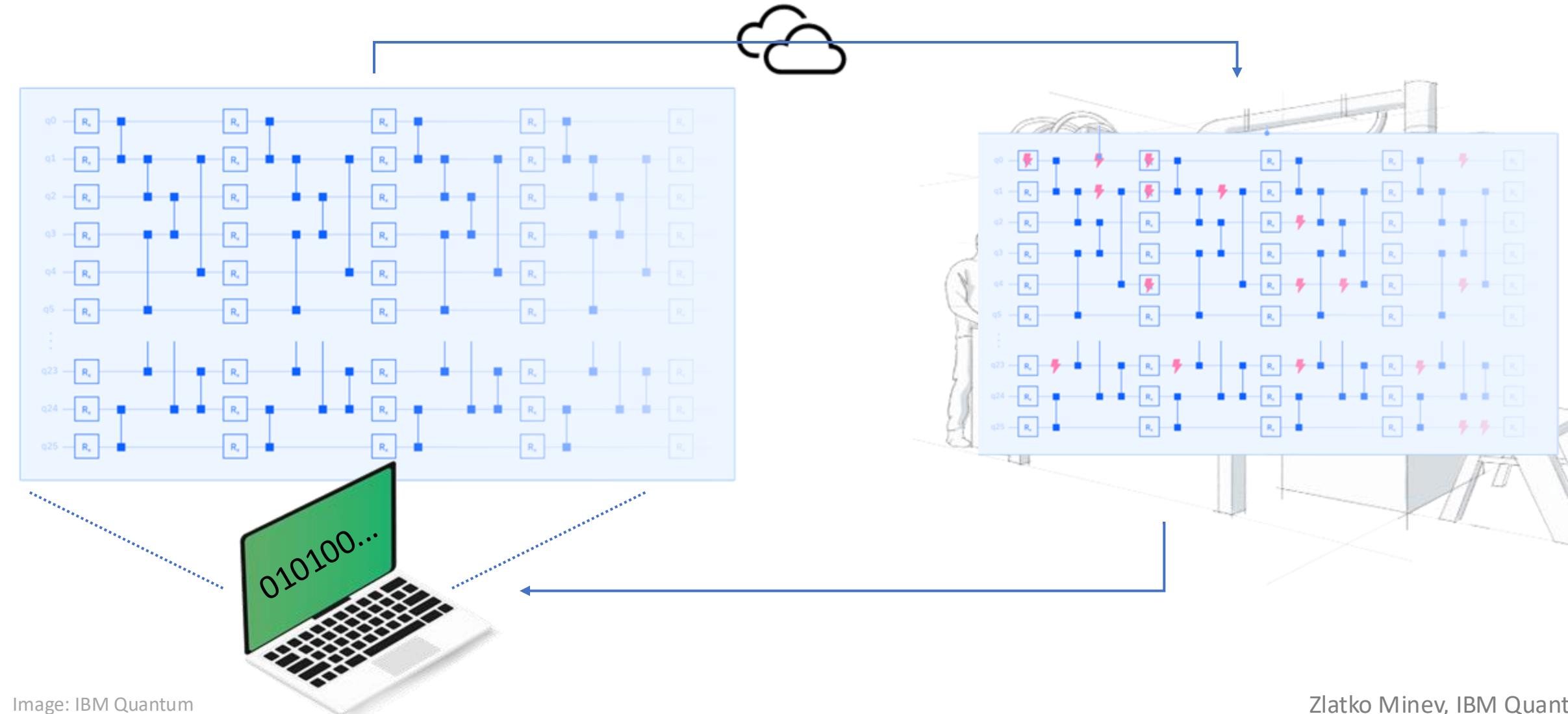


Error mitigation

... subject of today

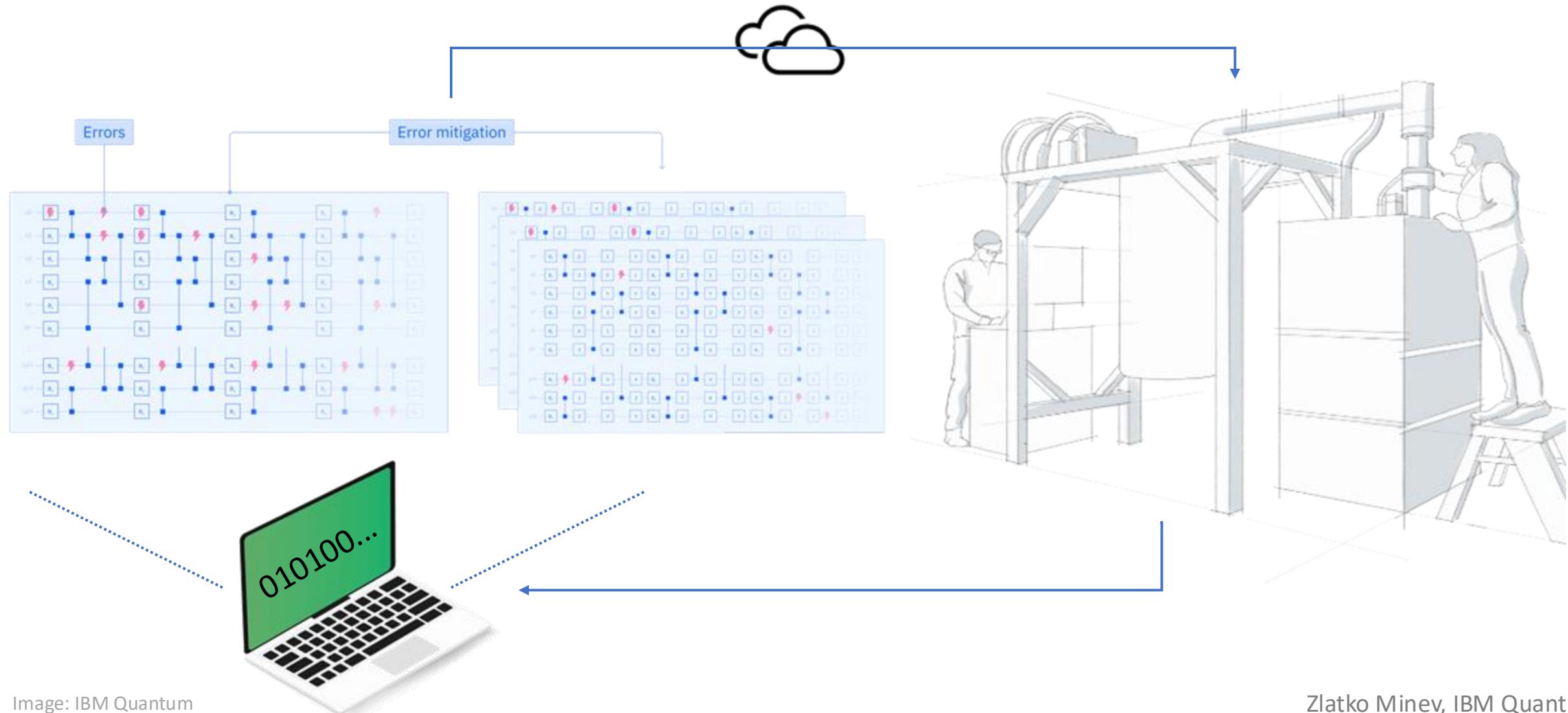
Quantum simulation on a noisy quantum computer

Execute on a real quantum computer device and obtain results as classical data

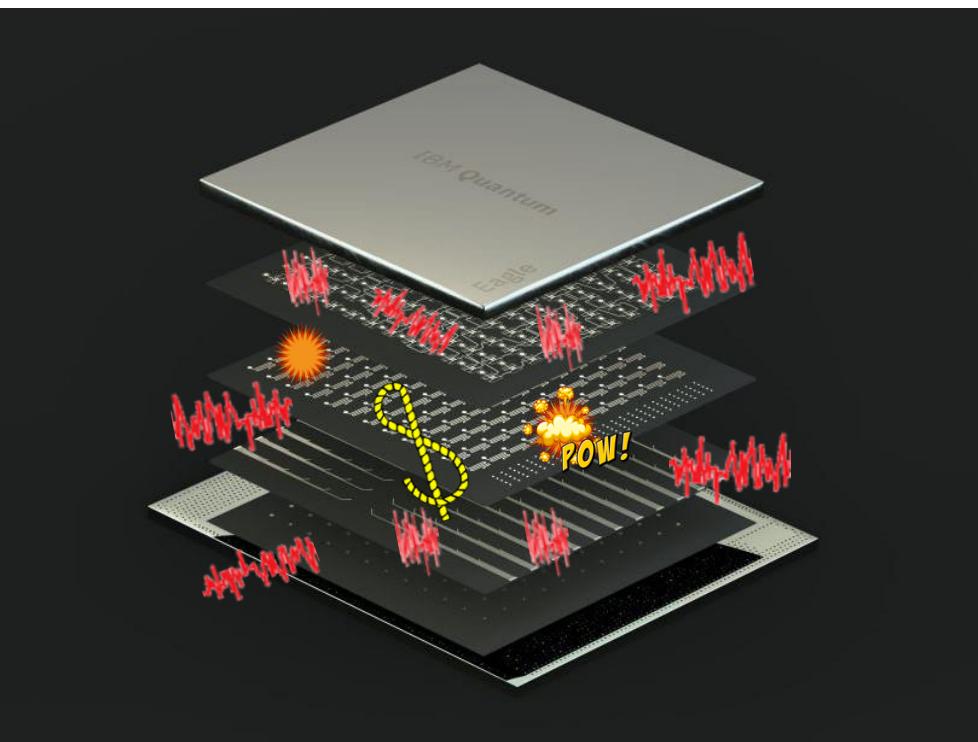


Quantum error mitigation overview

Execute on a real quantum computer device and obtain results as classical data



Error mitigation and error correction



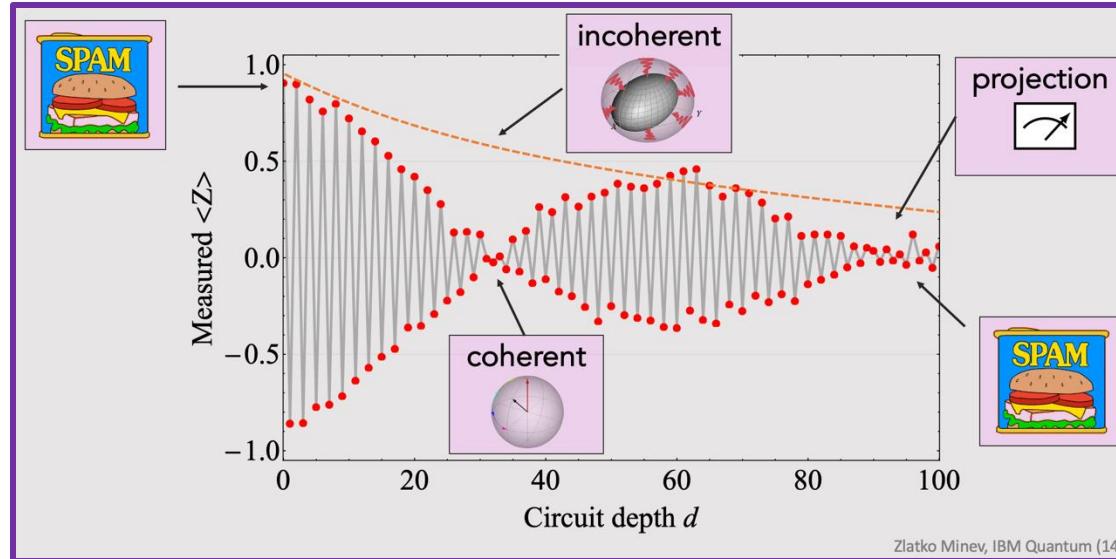
Error mitigation: working with what you have

- **benefit** suppress errors on classical results (expectation values)
- **q-cost** no extra qubits or hardware resources needed
- **c-cost** trades classical resources (post-processing) for lower error
- **limitation** bad asymptotic scaling: high number of samples & circuits

Error correction: protecting quantum information

- **benefit** suppress & correct errors to arbitrarily small level
- **q-cost** very large qubit and hardware overhead
- **c-cost** decoding and encoding can be classically costly
- **challenge** requires fault-tolerant operations and readout

Error mitigation landscape



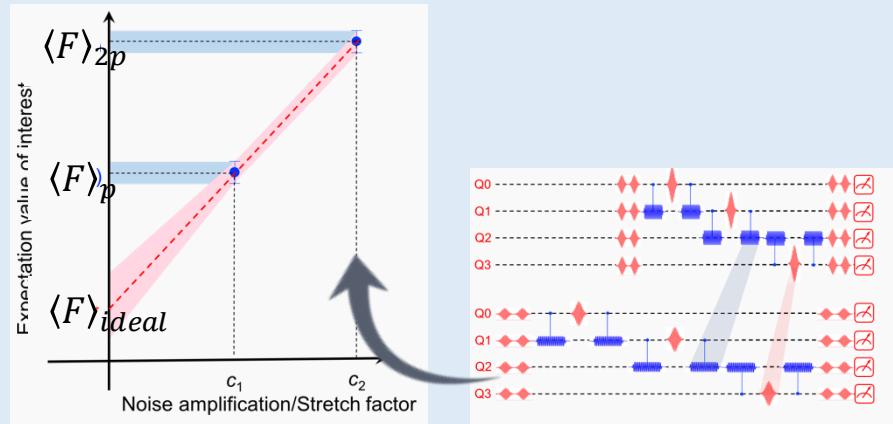
more speed

more information, accuracy



Error mitigation landscape

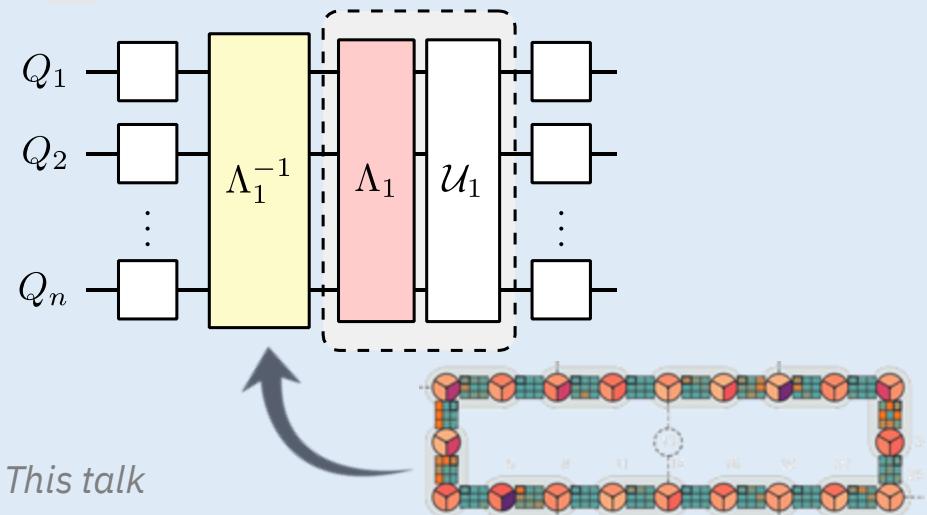
Zero-noise extrapolation (ZNE)



Nature 567, 491 (2019)

...

Probabilistic error cancellation (PEC)



This talk

more speed



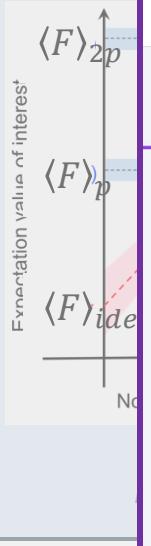
more information, accuracy



Zlatko Minev, IBM Quantum (38)

Error mitigation landscape

Zero-noise extrapolation (ZNE)



The graph illustrates the effect of noise on the expectation value of interest. The y-axis is labeled "Expectation value of interest" and the x-axis is labeled "Noise". Three curves are shown: $\langle F \rangle_{2p}$ (top), $\langle F \rangle_p$ (middle), and $\langle F \rangle_{ideal}$ (bottom). All curves show a decreasing trend as noise increases, with the ideal curve being the most stable.

Qiskit IBM Qiskit

English

Search Qiskit Runtime IBM

Get started

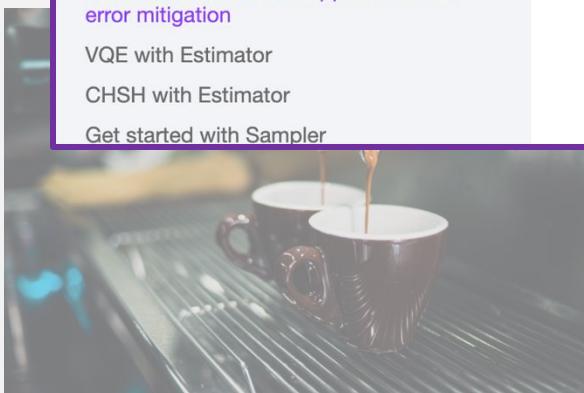
Overview

Getting Started

backend.run vs. Qiskit Runtime

Introduction to primitives

more speed



Probabilistic error cancelation (PEC)

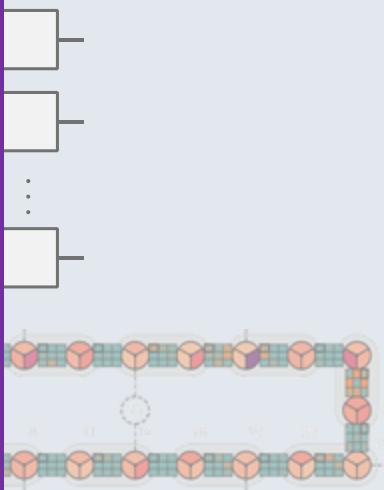
Qiskit Runtime IBM Client documentation > Error suppression and error mitigation with Qiskit Runtime

Overview Learn Community

• NOTE

This page was generated from [docs/tutorials/Error-Suppression-and-Error-Mitigation.ipynb](#).

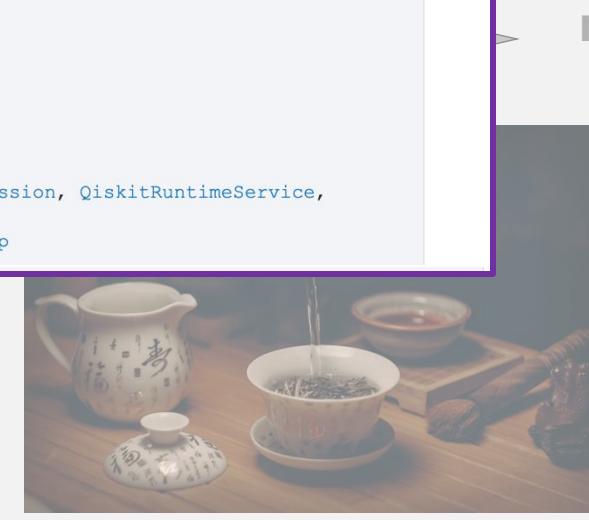
Error suppression and error mitigation with Qiskit Runtime



A quantum circuit diagram showing a sequence of operations on multiple qubits. The circuit includes various gates like H, CNOT, and rotation gates, with specific parameters indicated by numbers and symbols.

```
[1]: import datetime
import numpy as np
import matplotlib as mpl
import matplotlib.pyplot as plt
plt.rcParams.update({"text.usetex": True})
plt.rcParams["figure.figsize"] = (6,4)
mpl.rcParams["figure.dpi"] = 200

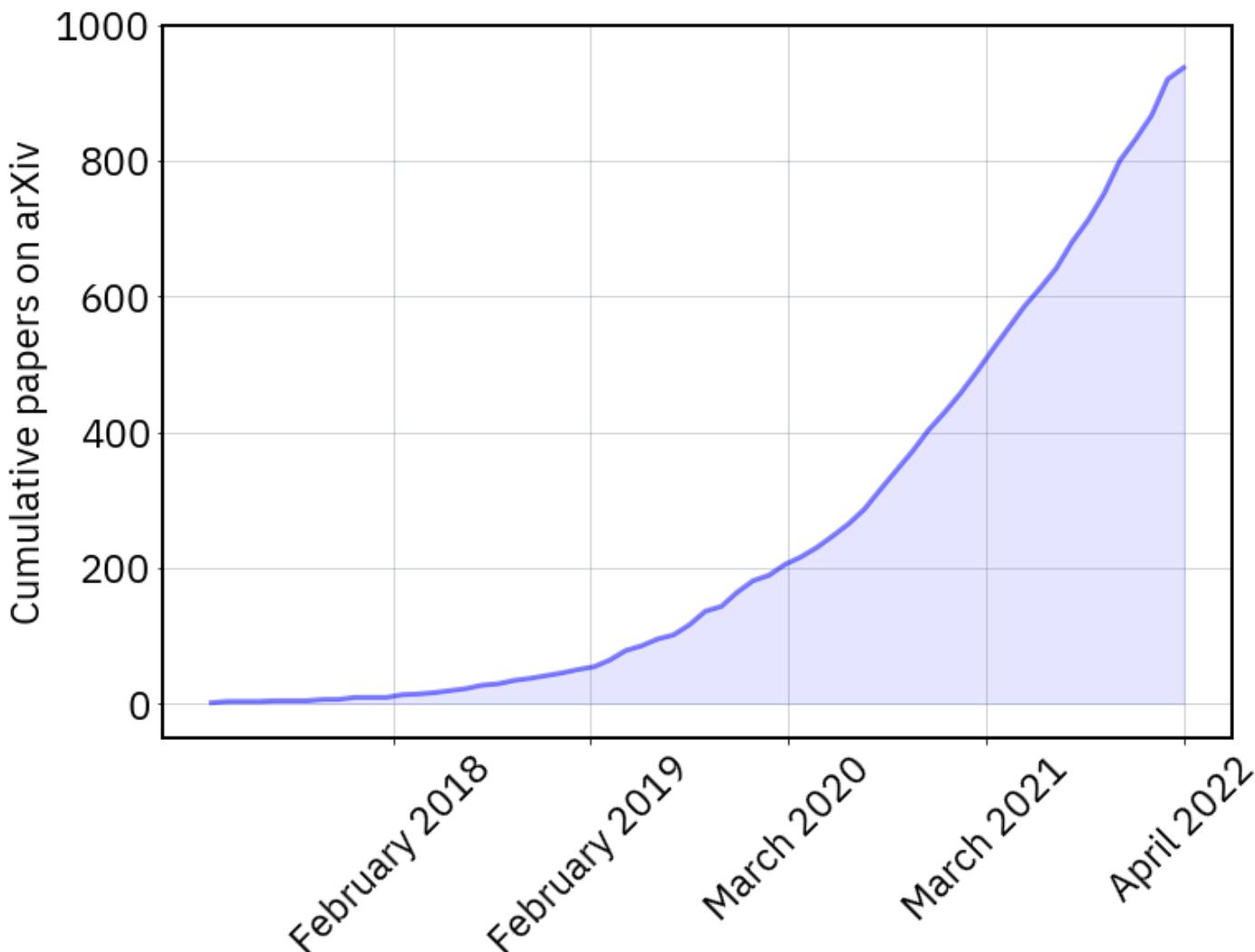
from qiskit_ibm_runtime import Estimator, Session, QiskitRuntimeService,
Options
from qiskit.quantum_info import SparsePauliOp
```



more information, accuracy

Adoption of error mitigation

Papers involving error mitigation over time



Examples

ARTICLE
<https://doi.org/10.1038/s41467-020-14376-z> OPEN

Error-mitigated quantum gates exceeding physical fidelities in a trapped-ion system

Shuaining Zhang¹, Yao Lu¹, Kuan Zhang^{1,2}, Wentao Chen¹, Ying Li^{3*}, Jing-Ning Zhang^{1,4*} & Kiwhan Kim^{1*}

Article | Published: 08 May 2023

Probabilistic error cancellation with sparse Pauli-Lindblad models on noisy quantum processors

Ewout van den Berg, Zlatko K. Minev, Abhinav Kandala & Kristan Temme

Nature Physics (2023) | Cite this article

npj quantum information

ARTICLE OPEN

Fundamental limits of quantum error mitigation

Ryuji Takagi¹, Suguru Endo², Shintaro Minagawa³ and Mile Gu^{1,4}

PHYSICAL REVIEW LETTERS 127, 200505 (2021)

Error Mitigation for Universal Gates on Encoded Qubits

Christophe Piveteau
IBM Quantum, IBM Research—Zurich, 8803 Rüschlikon, Switzerland

Model-free readout-error mitigation for quantum expectation values

Ewout van den Berg, Zlatko K. Minev, and Kristan Temme
Phys. Rev. A **105**, 032620 – Published 30 March 2022

Matrix product channel: Variation to mitigate noise and reduce errors

Sergey Filippov,* Boris Sokolov, Ma Borrelli, Daniel Cavalcanti, Sabrina Algoritmia Ltd, Kanavakat

Quantum Error Mitigation

Zhenyu Cai,^{1,2,*} Ryan Babbush,³ McClean,³ and Thomas E. O'Brien¹

¹Department of Materials, University of California, Berkeley, Berkeley, CA 94720, USA

²Quantum Motion, 9 Sterling Way, San Francisco, CA 94103, USA

³Google Quantum AI, Venice, California 90253, USA

⁴NTT Computer and Data Sciences, Kyoto, Japan

⁵Graduate School of China Academy of Chinese Medical Sciences, Beijing, China

(Dated: July 3, 2023)

Single-shot error mitigation

Ewout van den Berg, Sergey B. Bravyi, and Dmitri Maslov
IBM Quantum, IBM Research—Zurich, 8803 Rüschlikon, Switzerland

Is science with noisy devices of
broad interest today?



Some of these ideas covered
in other lectures at the
school

Zlatko Mihaljević

2)

Deep dive:
Probabilistic error cancellation (PEC)
To learn and cancel quantum noise



Got Slides?



Ewout van den Berg, Zlatko K. Minev, Abhinav Kandala, Kristan Temme
Nature Physics (2023)

Cancel quantum noise



High-level message

Learn

accurate, efficient, scalable



Cancel

noise with noise,
practical



Cost

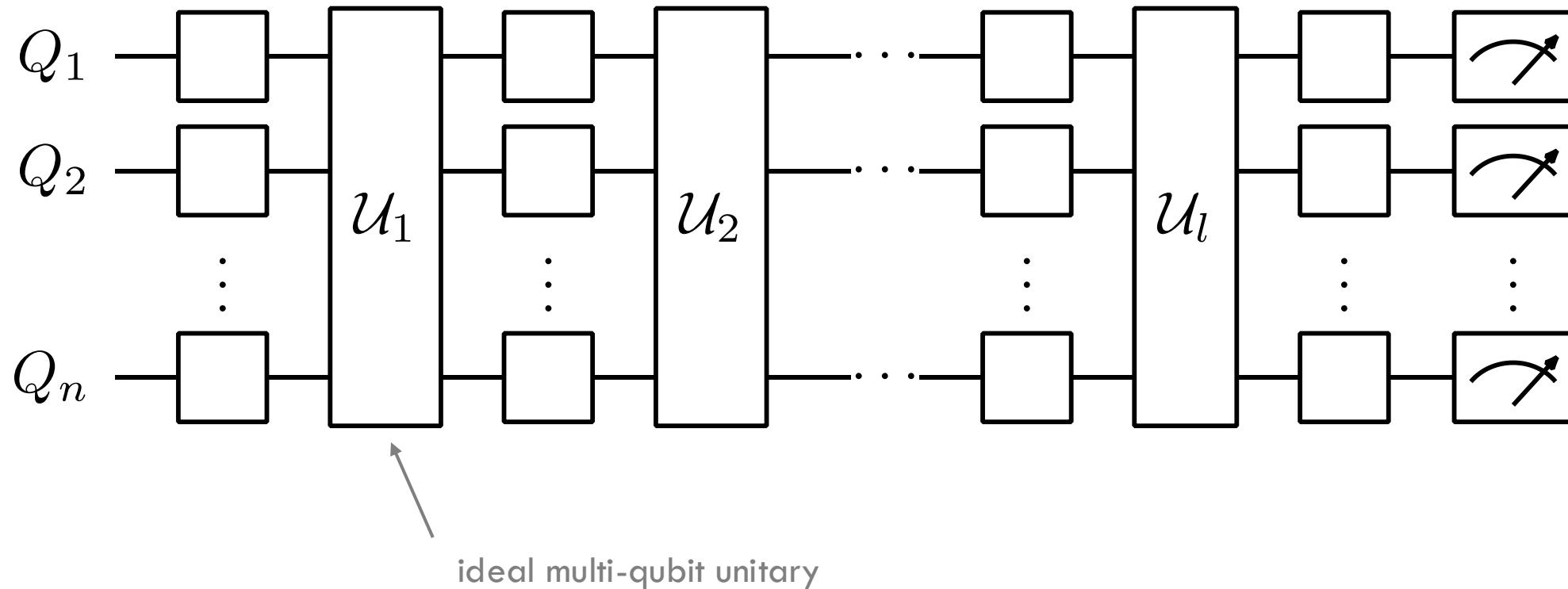
more noise more cost





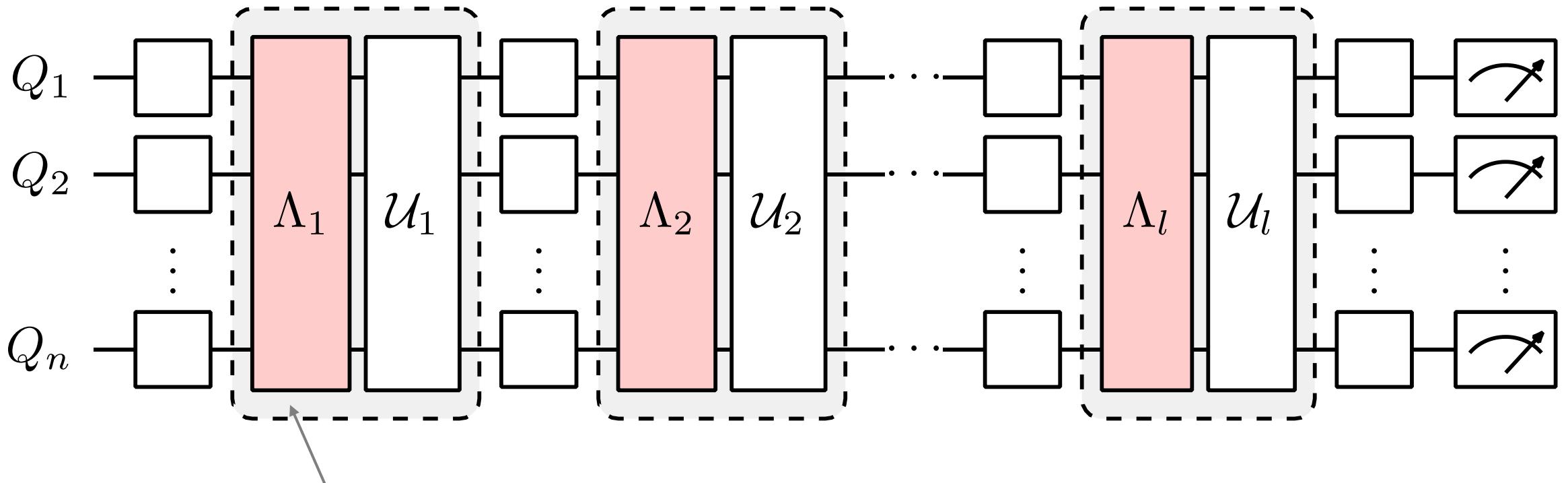
Idea

Ideal (noise-free) quantum circuit



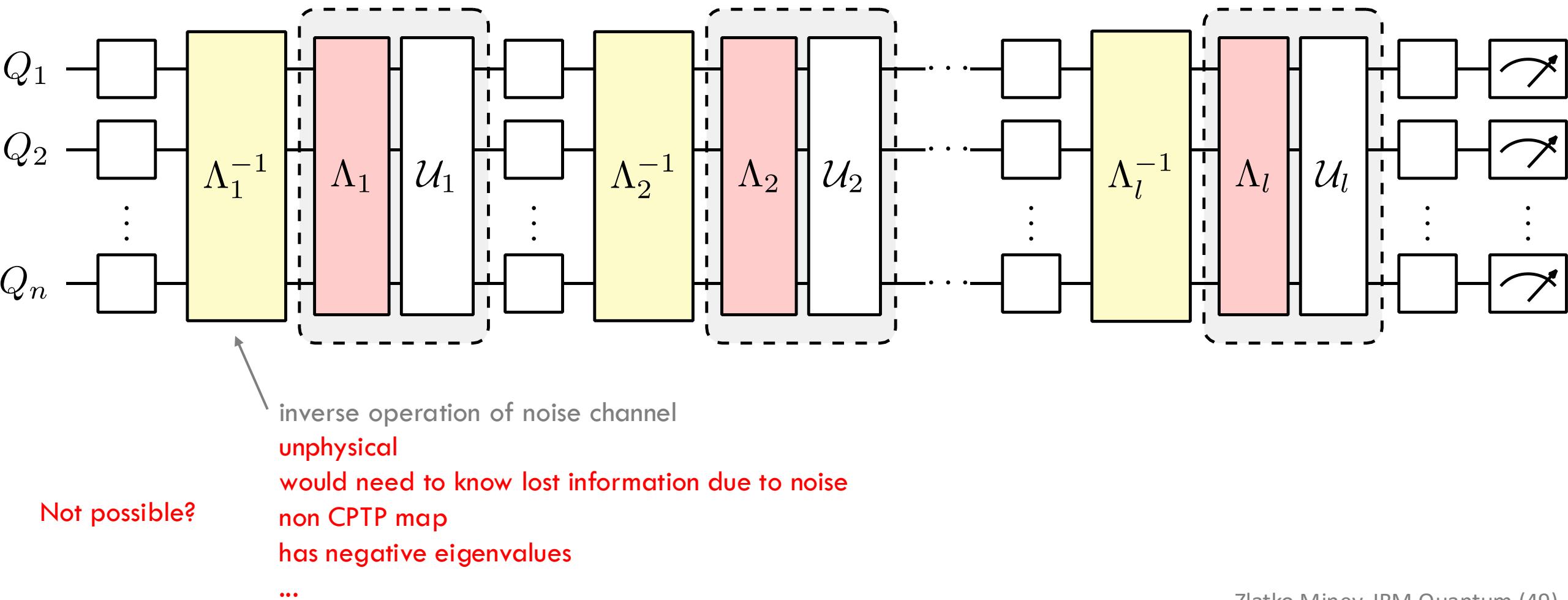
A circuit can be decomposed into a layer construction
Example: Trotterization of Ising model simulation

Real (noisy) quantum circuit

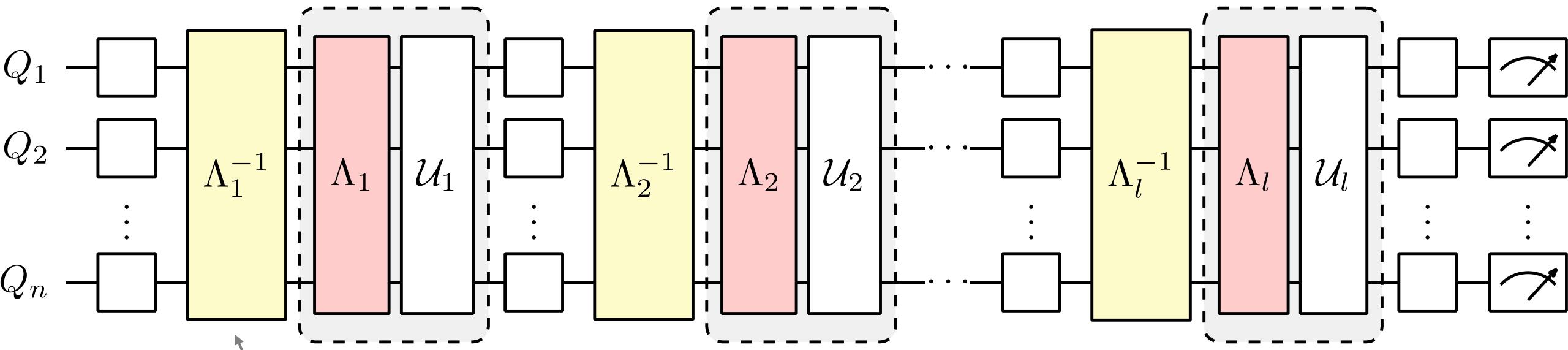


completely positive and trace preserving (CPTP)
representable by a $4^n \times 4^n$ matrix

Why not invert noise?



Probabilistic error cancellation

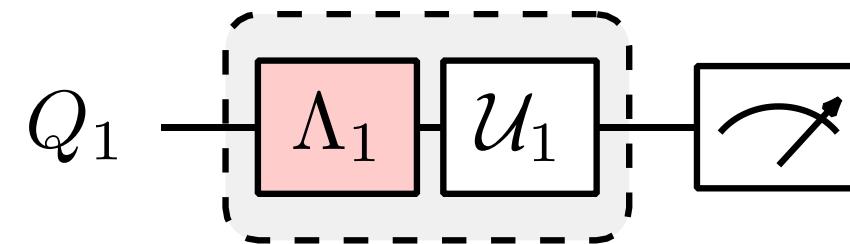
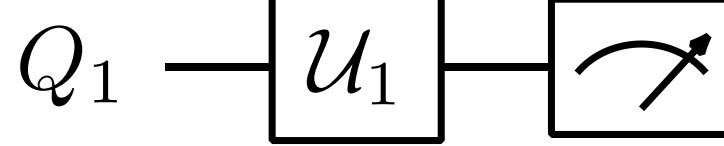


inverse operation of noise channel
implement on average

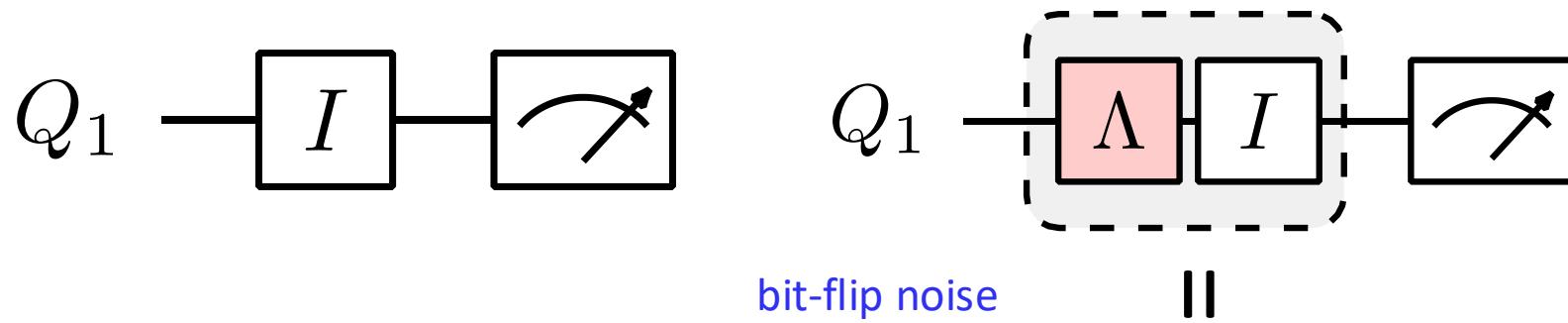
K. Temme, S. Bravyi, and J. M. Gambetta
PRL 119, 180509 (2017)

See also S. Endo, S. Benjamin, and Y. Li
Phys. Rev. X 8, 031027 (2018)

Toy model



Toy model: noise unraveling into quantum trajectories

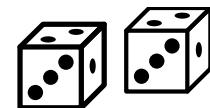


bit-flip noise

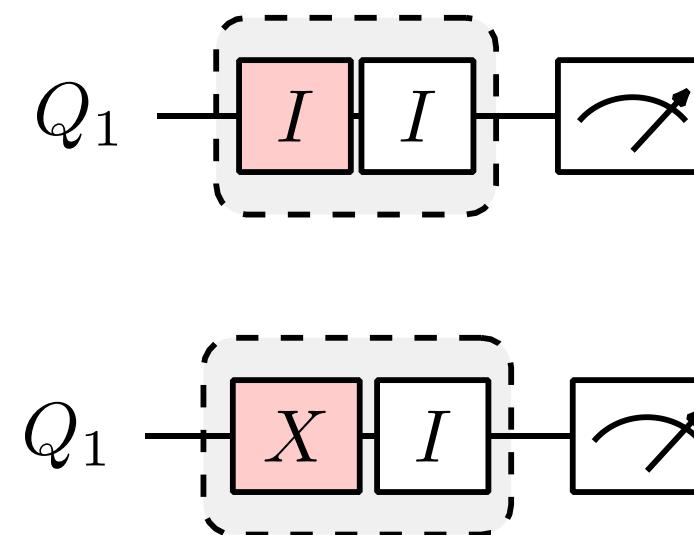
II

unraveling
(quantum trajectories)

probability $1-p$

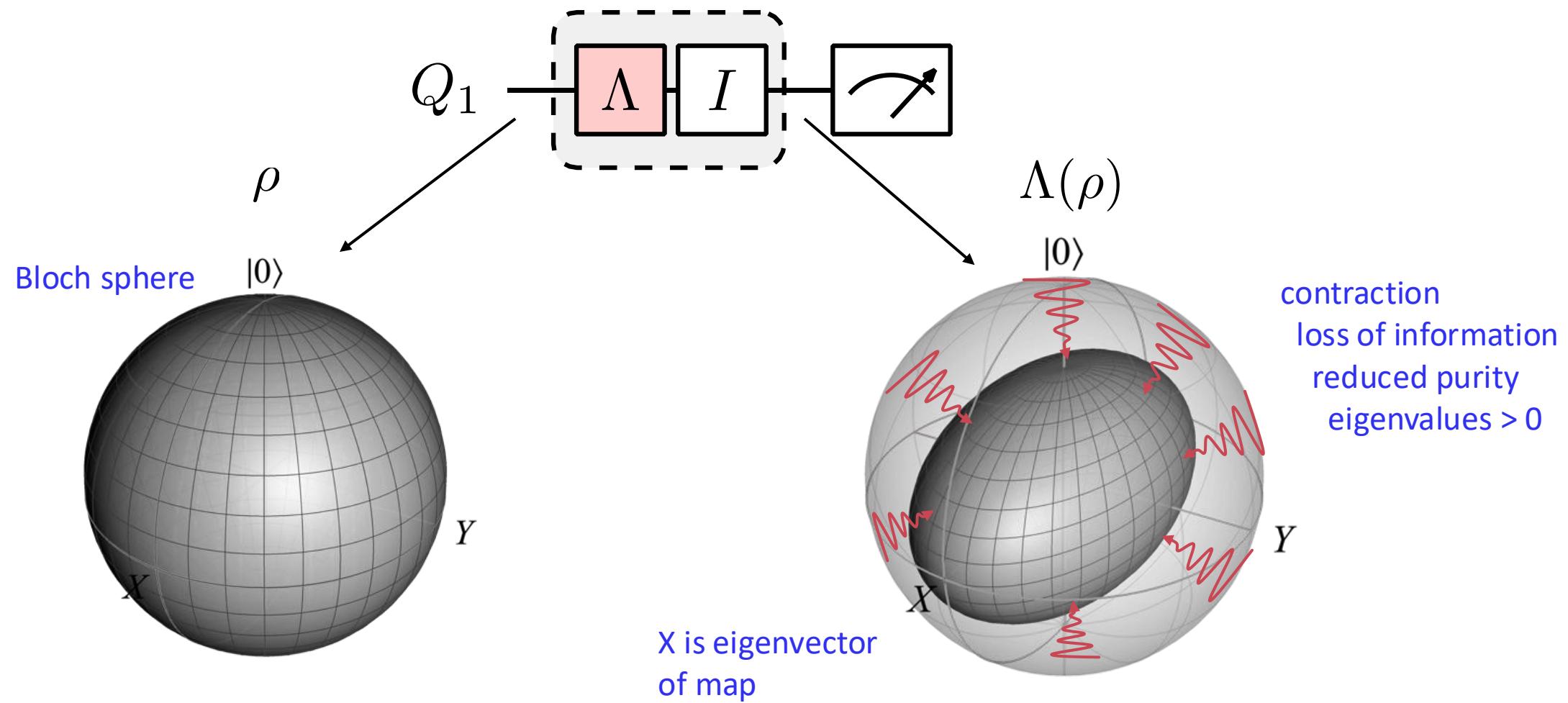


probability p

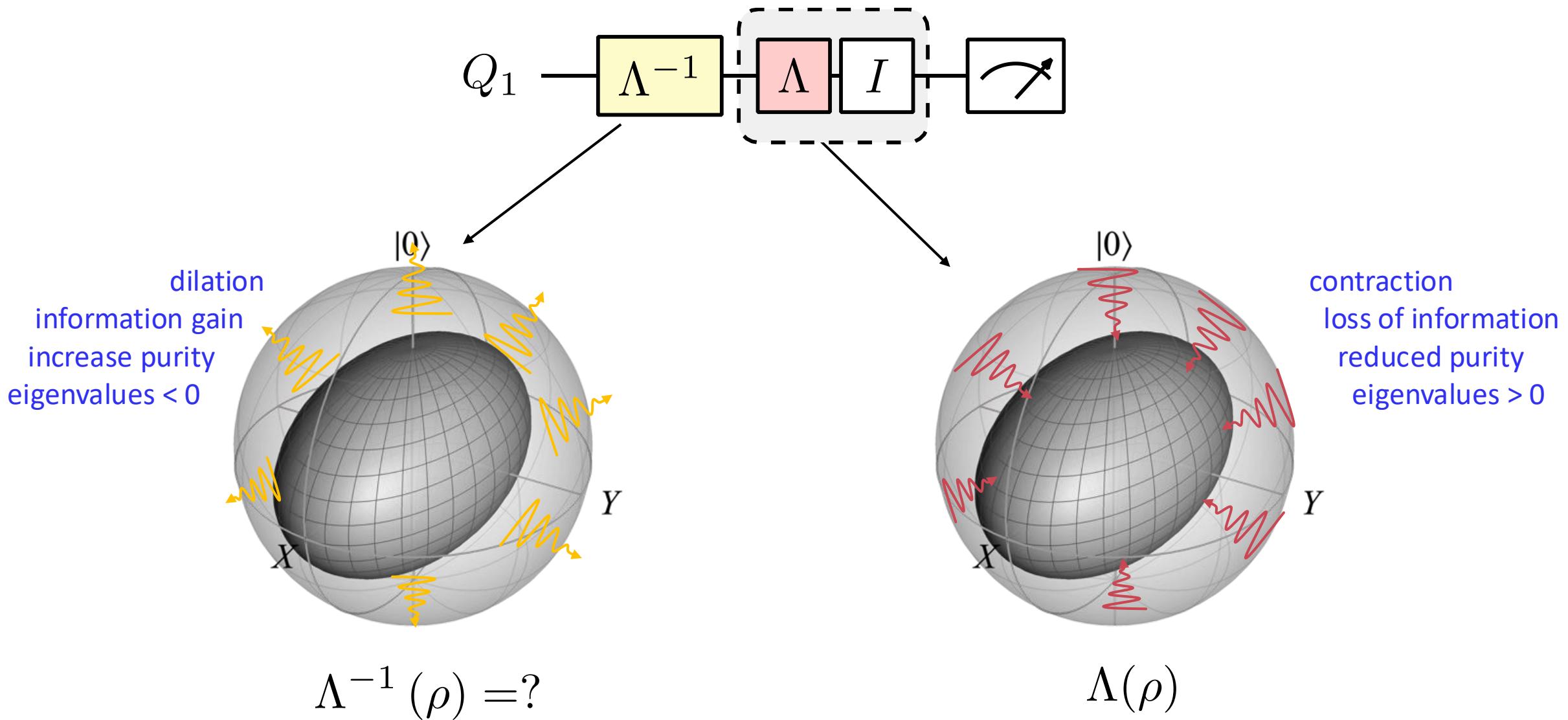


$$\Lambda(\rho) = (1 - p)I\rho I + pX\rho X$$

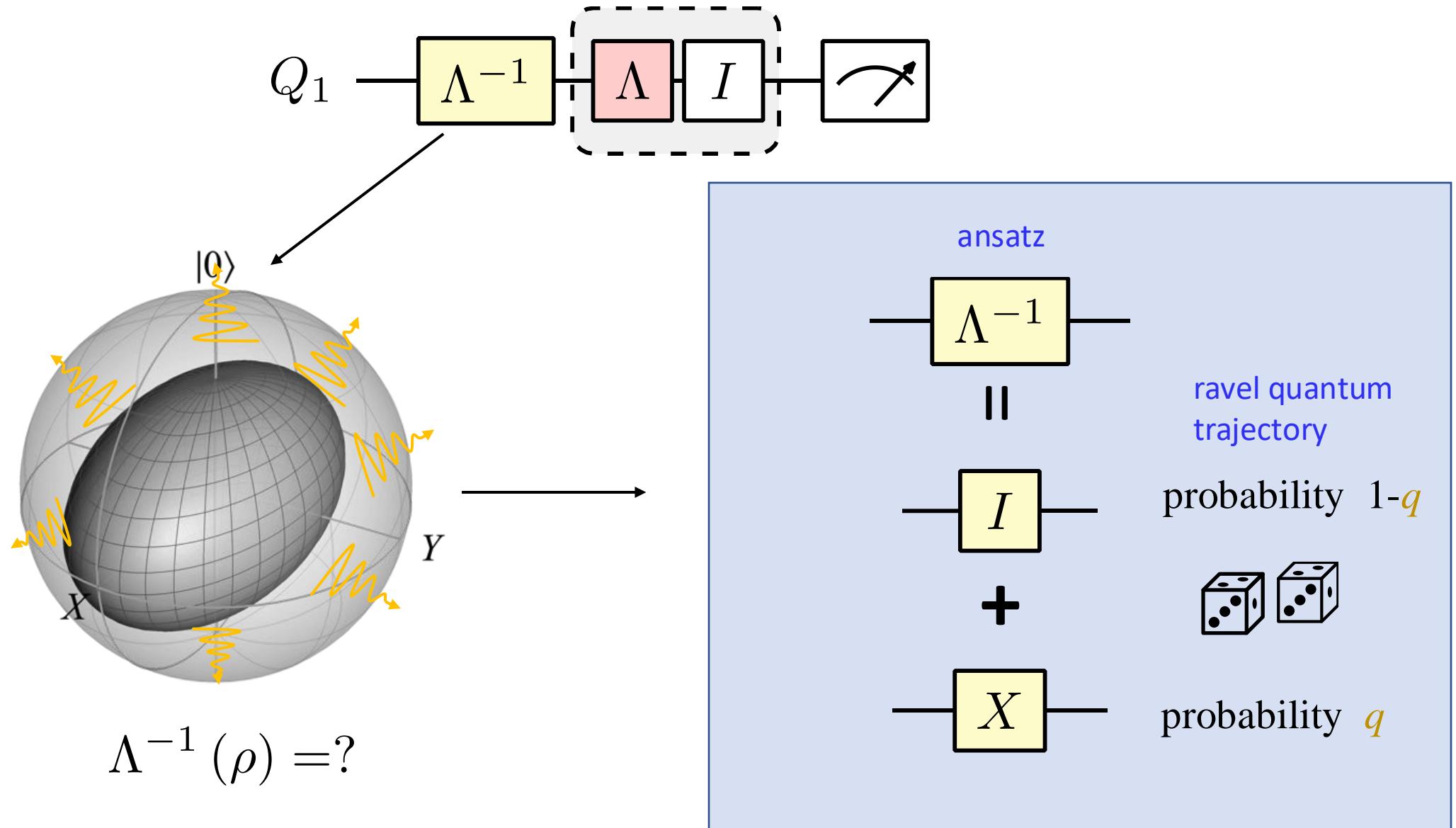
Toy model: noise unraveling into quantum trajectories



Inverse of noise map is not physical

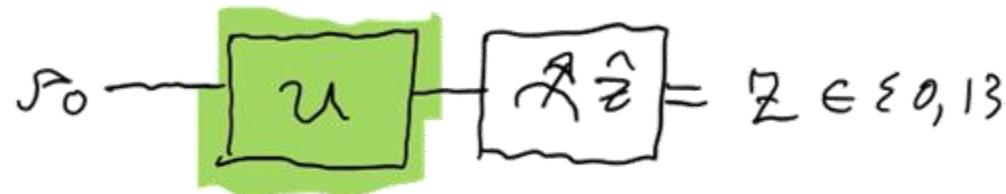


Inverse of noise map is not physical



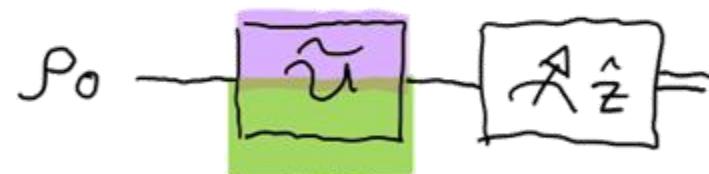
Blackboard derivation

Setup

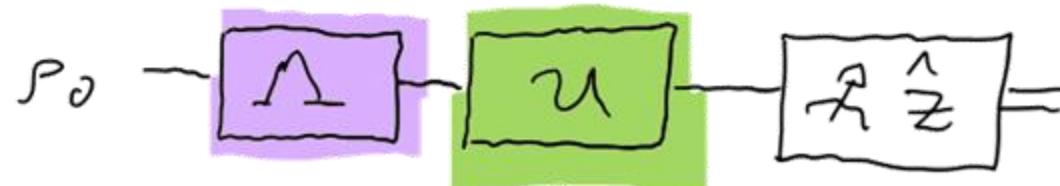


Details on notation:

Quantum register alphabet $S = \{0, 1\}$
Hilbert space $\mathcal{H} = \mathbb{C}^S$
Initial state $\rho_0 \in D(\mathcal{H}) \subset L(\mathcal{H})$
Ideal unitary $U \in U(\mathcal{H}) \subset L(\mathcal{H})$
Ideal u-channel $U(f) = U \rho_0 U^\dagger$
 $U \in C(\mathcal{H}) \subset L(L(\mathcal{H}))$



Noisy gate / circuit $\tilde{U} \in L(L(\mathcal{H}))$



Decompose noisy gate $\tilde{U} = U A$

Blackboard derivation

Simple Example

Keeping it simple and illustrative, let's do a simple case

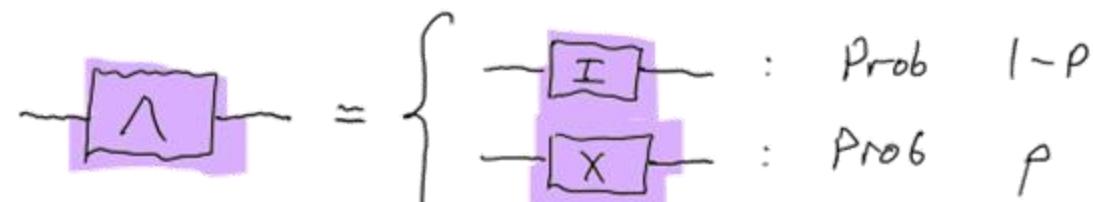
$$\text{Let } U = I$$
$$U = I \cdot I$$

For the noise, let's play with the simplest bit-flip channel

$$N(p) = \underbrace{(1-p)}_{\text{prob of no error}} F_p I + \underbrace{p X_p X}_{\text{prob of a bit flip error}}$$

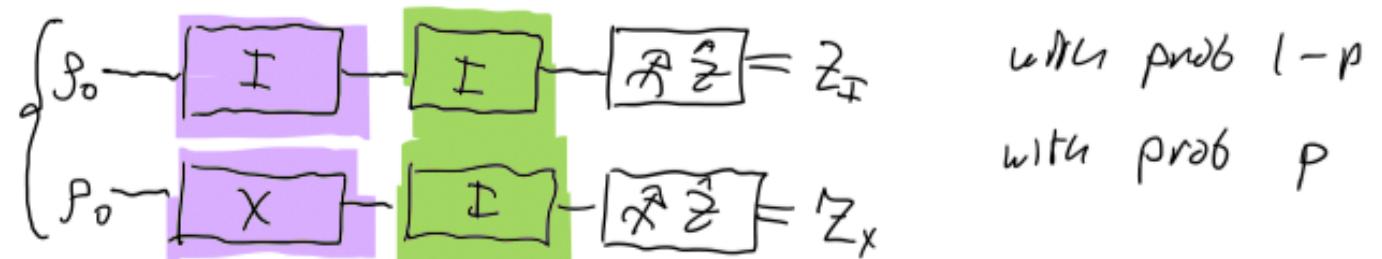
$$\left(N_p = (1-p) Z_p + p X_p \quad \begin{array}{l} \text{Equivalent superoperator} \\ \text{channel representation} \end{array} \right)$$
$$X_F = X_F X$$
$$X_P = I_P I = P$$

Equivalent trajectory unraveling



Blackboard derivation

Our circuit then is equivalent to either



Simple Example

Keeping it simple and illustrative, let's do a simple case

$$\begin{aligned} U &= I \\ U &= I \cdot I \end{aligned}$$

For the noise, let's play with the simplest bit-flip channel

$$N(p) = (1-p)E_p I + pX_p X$$

prob of no error prob of a bit flip error

$$\left(\begin{array}{l} N_p = (1-p)Z_p + pX_p \\ \text{Equivalent superoperator} \\ \text{channel representation} \\ X_p = X_p X \\ X_p = I \cdot I = p \end{array} \right)$$

Equivalent trajectory unravelling

$$\boxed{\Delta} = \left\{ \begin{array}{ll} \boxed{I} : & \text{Prob } 1-p \\ \boxed{X} : & \text{Prob } p \end{array} \right.$$

The ideal expectation value is

$$Z_{\text{ideal}} = \langle \hat{Z} \rangle = \text{Tr}(Z \rho_0) = \text{Tr}(Z \rho_p) = \rho_Z$$

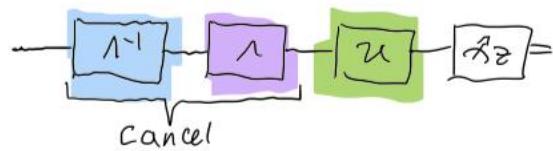
When the channel introduces an error however,

$$\begin{aligned} \text{IE}[Z_X] &= \text{Tr}(Z X \rho_p X) \approx \text{Tr}(X Z X \rho_p) \\ &= \text{Tr}(-Z \rho_p) \\ &= -\rho_Z \end{aligned}$$

Blackboard derivation

Noise Inverse

To undo the noise, we'd like to introduce the inverse noise

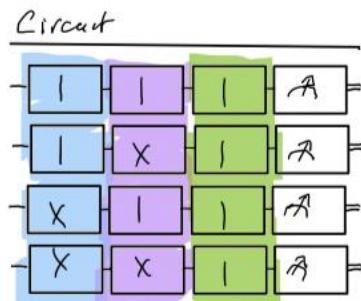


$$A^\dagger A = A A^\dagger = I$$

Taking the ansatz $A^\dagger(p) = (1-r)I \cdot I + r(X \cdot X)$

we see 4 cases of unravelling

inverse	noise	no error	prob
I	I	✓	$(1-r)(1-p)$
I	X	X	$(1-r)p$
X	I	X	$r(1-p)$
X	X	✓	$r p$



ideally, we want to interfere trajectories so that the no-error ones will coherently add to unity probably, and the ones with an error will cancel.

$$\begin{aligned} \therefore \textcircled{A} \quad (1-r)(1-p) + r \cdot p &= 1 & \textcircled{B} \quad (1-r)p + r(1-p) &= 0 \\ 1 - r - p + 2rp &= 1 & p + r - 2rp &= 0 \\ r + p - 2rp &= 0 & \text{same condition} \\ \Rightarrow r(1-2p) &= -p \end{aligned}$$

$$r = \frac{-p}{1-2p}$$

Recall p is a probability $0 \leq p \leq 1$,

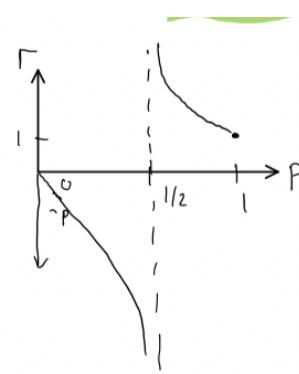
$$p=0 \Rightarrow r=0$$

$$p=1 \Rightarrow r=1$$

$$p=1/2 \Rightarrow r=\infty$$

$$p \ll 1 \Rightarrow r \approx -p$$

no noise, no need to do anything
deterministic bit-flip requires deterministic
bit flip usually for $d=1$
singular value, since at $p=1/2$, we fully
scramble the state



Blackboard derivation

Note that we could equivalently have used the algebraic condition and solved for r

$$\begin{aligned} \Lambda(\Lambda^{-1}(p)) &= \mathcal{I}(p) = p && \text{Solve for } r \\ &= \Lambda((1-r)p + rX_{\neq}X) \\ &= ((1-p)(1-r)p + pr) \cancel{X_{\neq}X} + (1-p)rX_{\neq}X + (1-r)pX_{\neq}X \\ &\quad \underbrace{\hspace{10em}}_{\text{no error}} \quad \underbrace{\hspace{10em}}_{\text{error}} \\ &= [(1-p)(1-r) + pr]p + [(1-p)r + (1-r)p]X_{\neq}X \end{aligned}$$

Same conditions as above \Rightarrow solution $r = \frac{-p}{1-2p}$

Blackboard derivation

How to implement? Quasi-Probability

$$\begin{aligned}\Lambda^{-1} &= (1-r)I_P I + r X_P X \\ &= \left[\frac{|1-r|}{|1-r| + |r|} sgn(1-r) I_P I + \frac{|r|}{|1-r| + |r|} sgn(r) X_P X \right] (|1-r| + |r|) \\ &= \gamma \left[S_I P_I I_P I + S_X P_X X_P X \right]\end{aligned}$$

with

$$\gamma = |1-r| + |r|$$

$$P_I = \frac{|1-r|}{\gamma} \quad S_I = sgn(1-r)$$

$$P_X = \frac{|r|}{\gamma} \quad S_X = sgn(r)$$

valid prob distribution

$$0 \leq P_I, P_X \leq 1 \quad \text{and} \quad |P_I| + |P_X| = 1$$

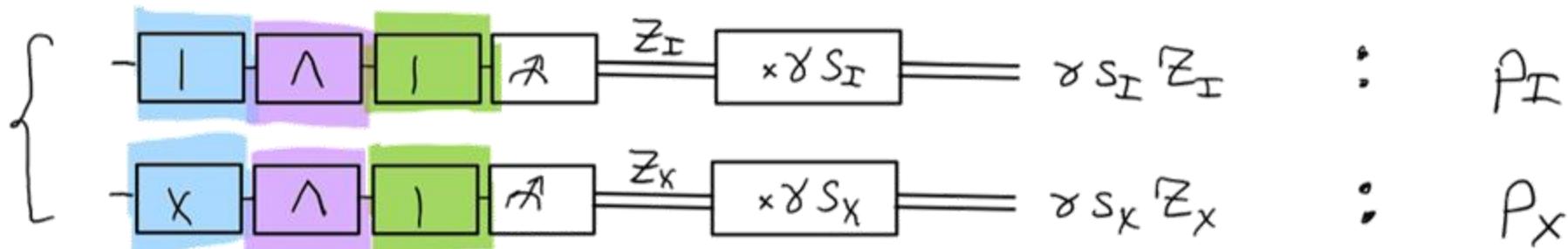
Blackboard

How to sample?

$$\begin{aligned}\langle Z \rangle &= \text{Tr}(Z \tilde{\mathcal{I}} \Lambda^{-1} P_0) \\ &= \text{Tr}(Z \tilde{\mathcal{I}} [\gamma s_I P_I + \gamma s_X P_X X_{P_0}]) \\ &= \gamma s_I P_I \text{Tr}(Z \tilde{\mathcal{I}} P_0) + \gamma s_X P_X \text{Tr}(Z \tilde{\mathcal{I}} X_{P_0}) \\ &= \gamma [s_I P_I \underbrace{\langle Z \rangle}_\text{quantum} + s_X P_X \underbrace{\langle Z \rangle}_\text{circuit eval using ancilla}]\end{aligned}$$

Equivalent interpretation:

Sample prob



Blackboard

Estimator

$$E_{\text{mit}_g} = \gamma s_I Z_I + \gamma s_X Z_X$$

$$\mathbb{E}[E_{\text{mit}_g}] = \langle \hat{Z} \rangle_{\text{ideal}}$$

$$\mathbb{V}[E_{\text{mit}_g}] = \mathbb{V}[\gamma s_I Z_I] + \mathbb{V}[\gamma s_X Z_X]$$

$$= \gamma^2 \mathbb{V}[Z_I] + \gamma^2 \mathbb{V}[Z_X]$$

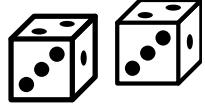
$$= \gamma^2 (2 \sigma_{\text{ideal}}^2)$$

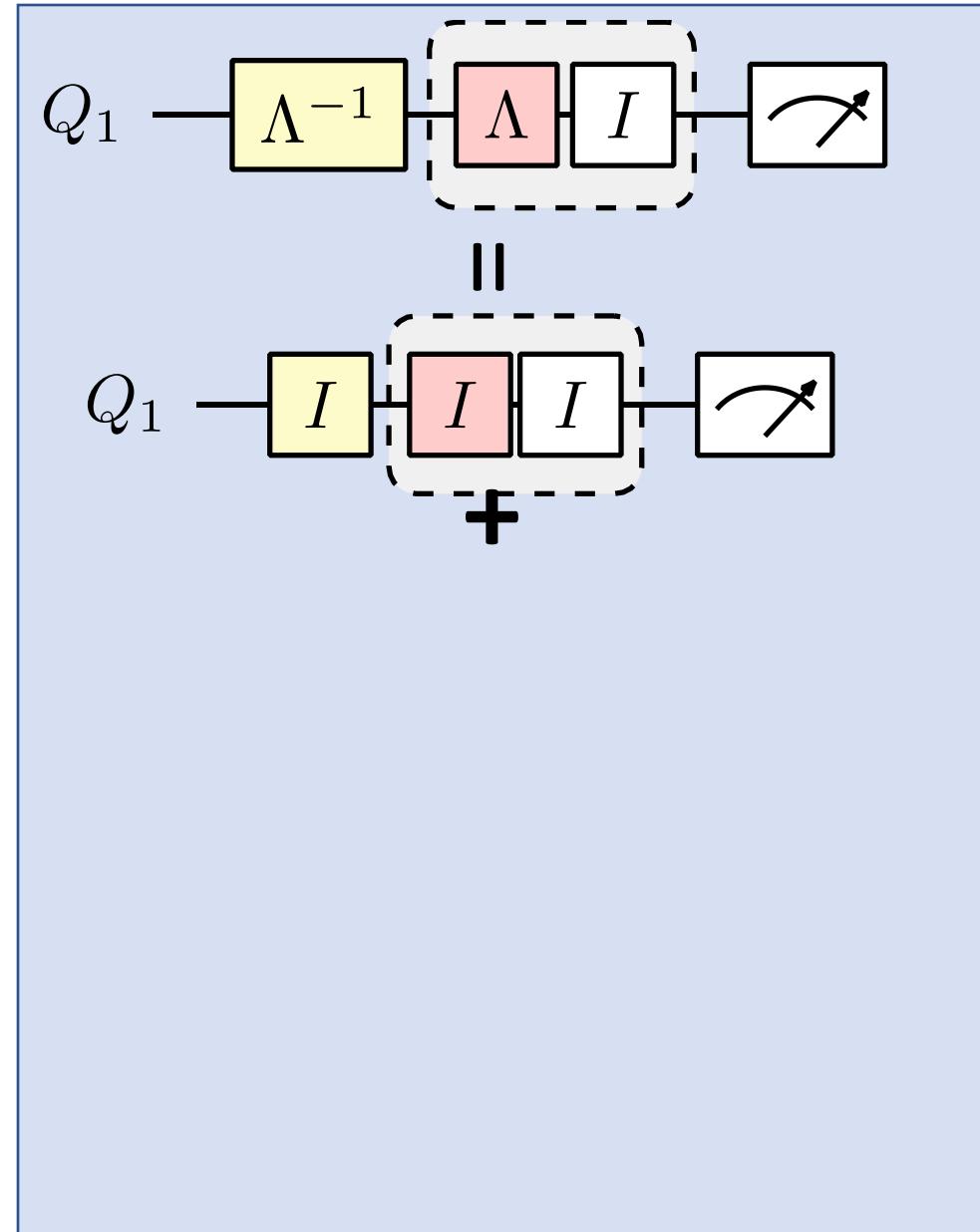
$$\sigma_{\text{ideal}}^2 = \mathbb{V}[Z_I] = 4q(1-q)$$

$$q = 1 - 2 \beta_Z = \left\langle \frac{1-\hat{Z}}{2} \right\rangle$$

Since the X just flip $Z \rightarrow -Z$ of P , it follows
that the variance is the same, since symmetric

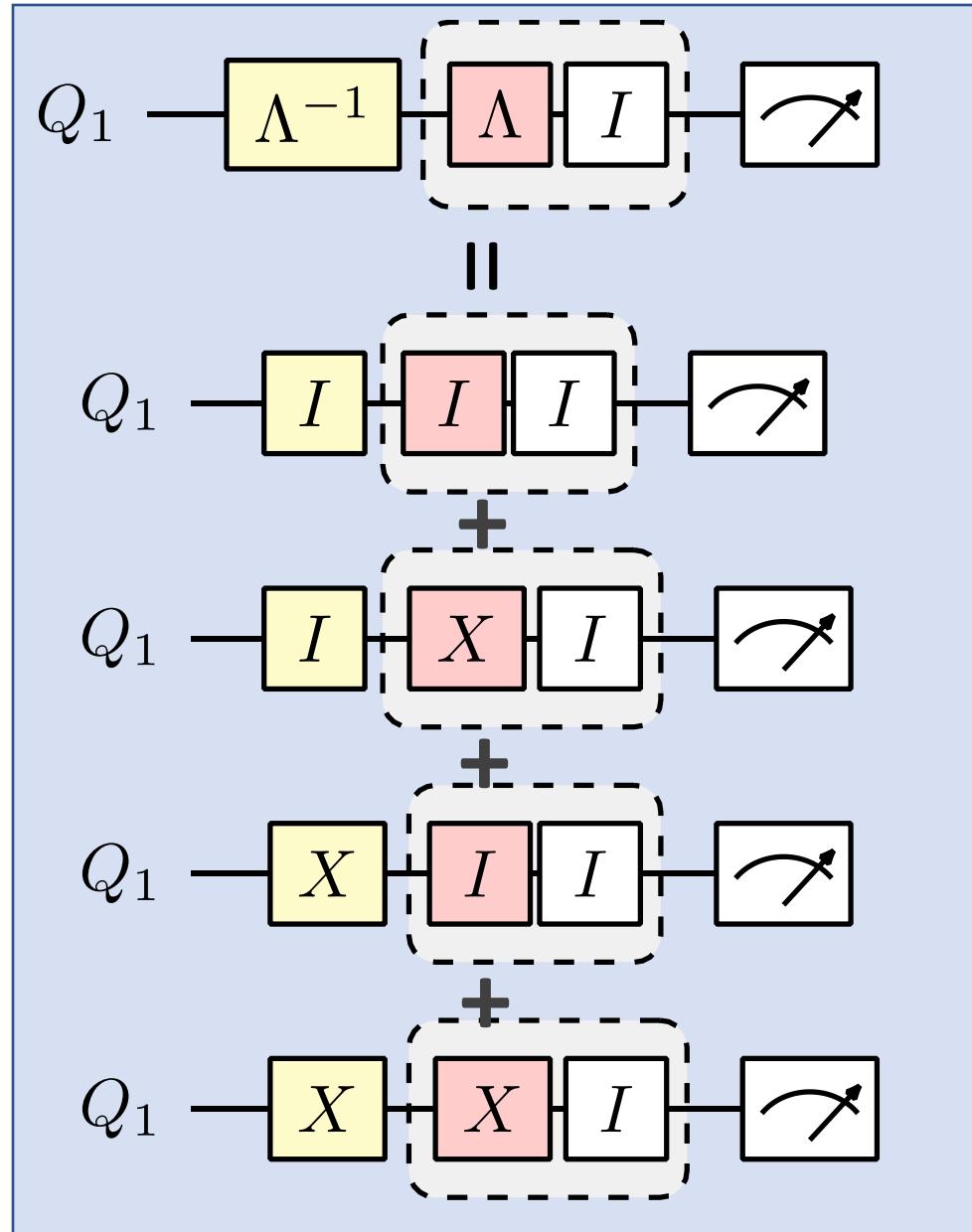
Raveling quantum trajectories to undo noise

No error probability
 $(1-q)(1-p)$




Raveling quantum trajectories to undo noise

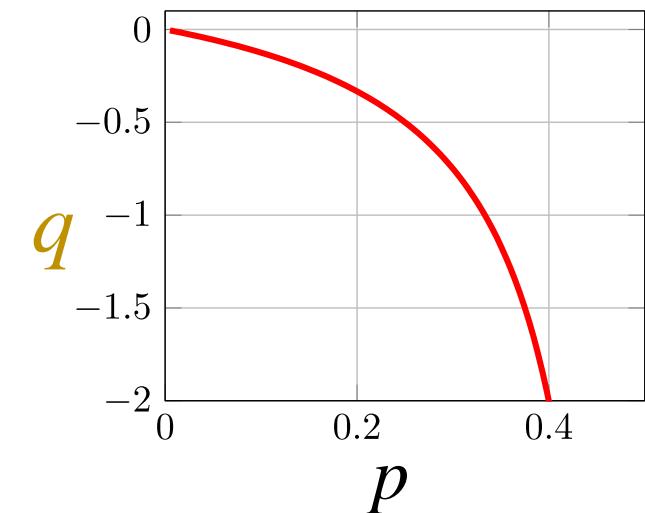
No error	probability $(1-q)(1-p)$	
ERROR!	$(1-q)p$	
ERROR!	$q(1-p)$	
Error CANCELED!	qp	



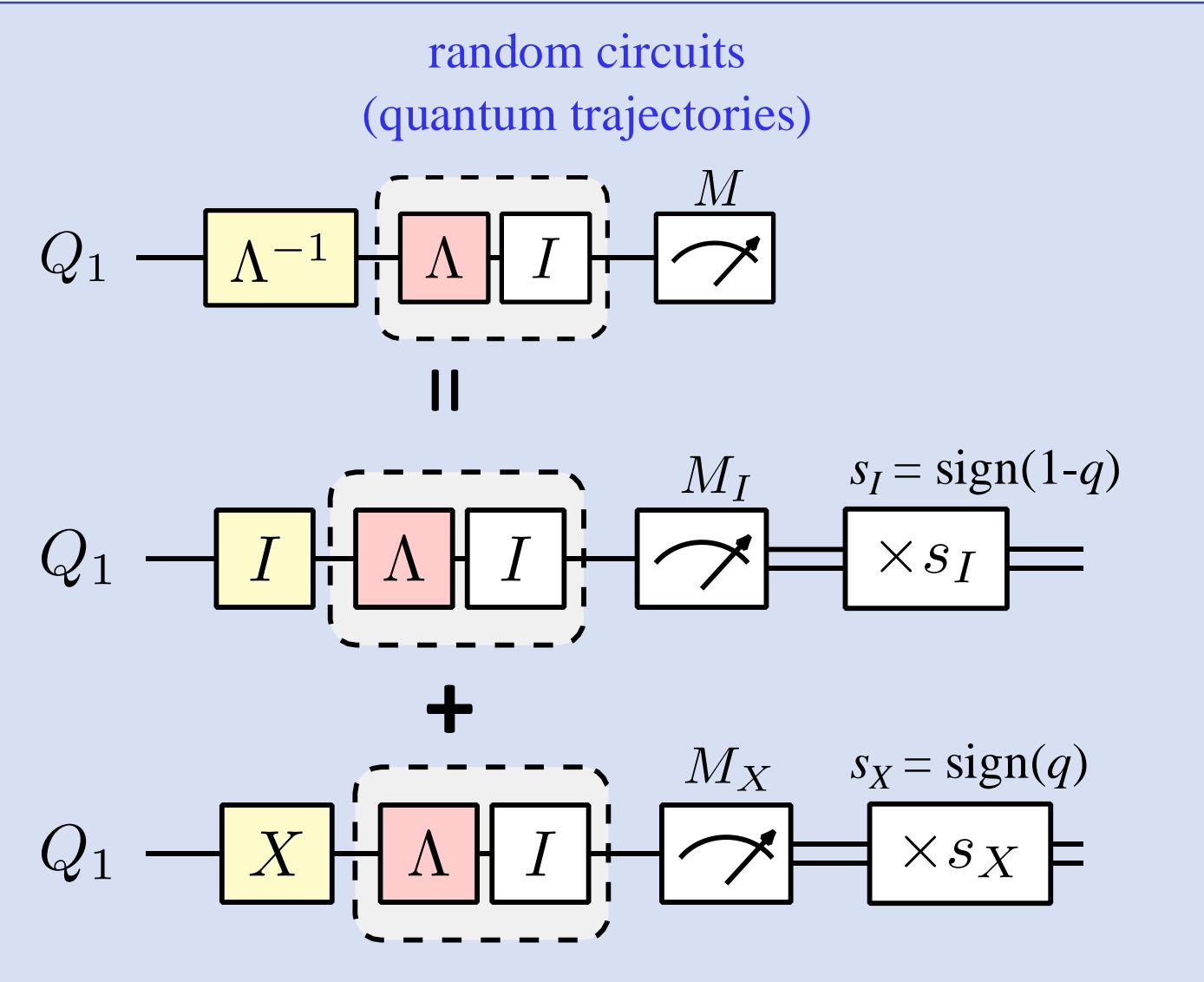
Solution to noise free!

$$q = \frac{-p}{1 - 2p}$$

Sign & scale:
quasi-probability

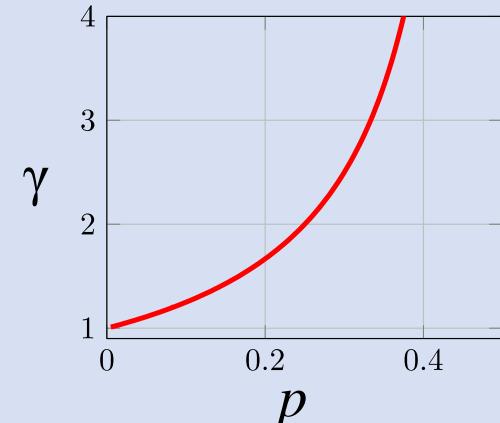


How to implement?



sampling overhead

$$\gamma = |1-q| + |q|$$



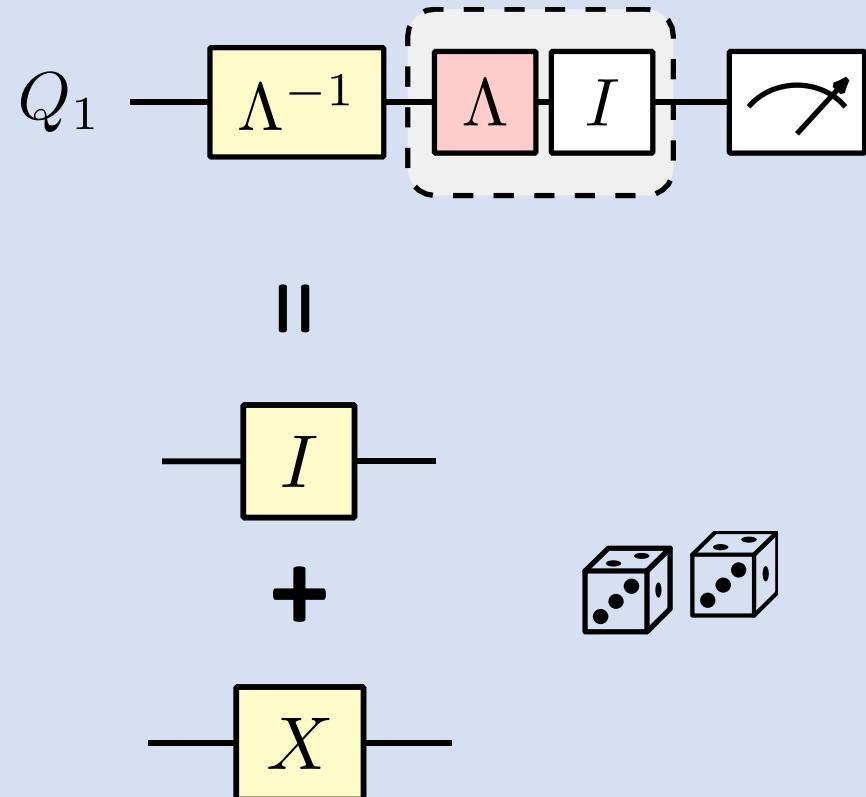
mitigated expectation

$$\langle M \rangle = \gamma(s_I P_I M_I + s_X P_X M_X)$$

Gain: Bias-free estimate!

Cost: Variance

Cancelling noise with noise



Cancelling noise with noise: Drunkard's classical random walk analogy



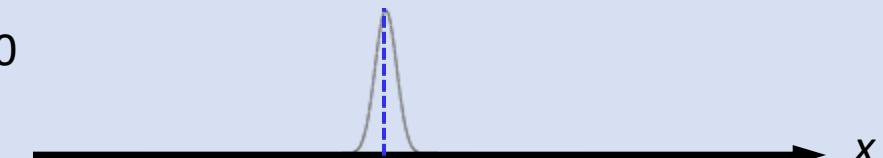
$$P(1 \text{ step left}) = \frac{1}{2} - p$$

$$P(1 \text{ step right}) = \frac{1}{2} + p$$

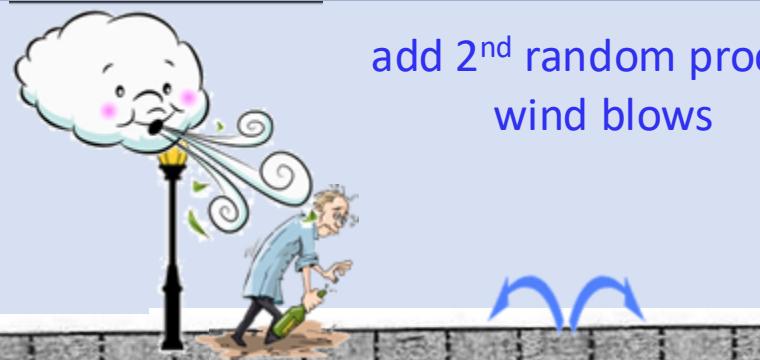
Random step

Distribution of random walk

$t = 0$



$t > 0$



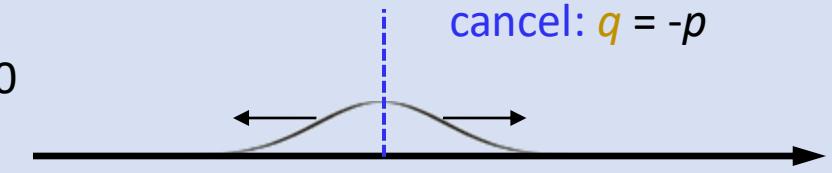
add 2nd random process
wind blows

$$P(1 \text{ step left}) = \frac{1}{2} + q$$

$$P(1 \text{ step right}) = \frac{1}{2} - q$$

Distribution of random walk with wind

$t > 0$



Gain: Bias-free estimate!
Cost: Variance

Quantum Noise and Error Mitigation

Lecture 1

Big picture

Quantum computers status

Why error mitigation?

Noise in quantum computers

Overview of error mitigation

Mitigation fundamentals

Probabilistic error cancelation (PEC)

Introduction

One qubit example

Next lecture

Learning noise

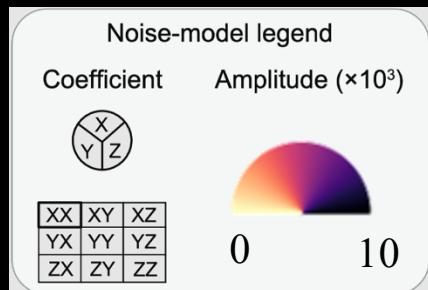
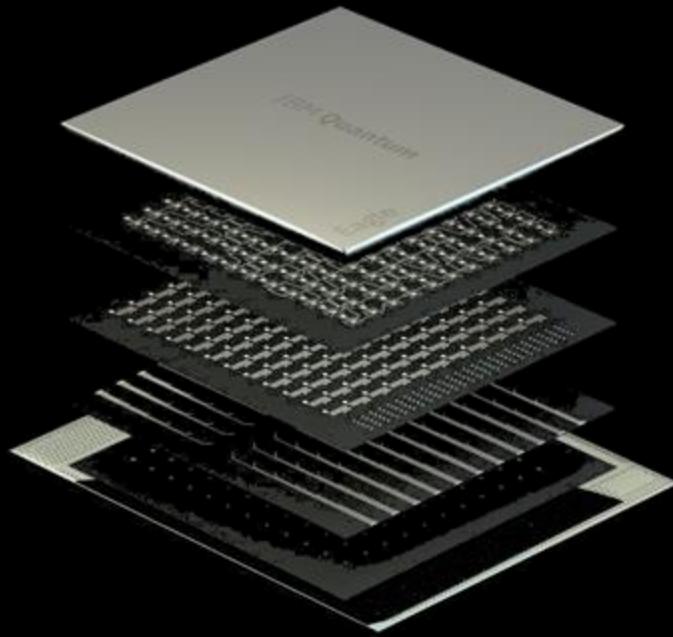
State-of-art mitigation experiments

Hardware

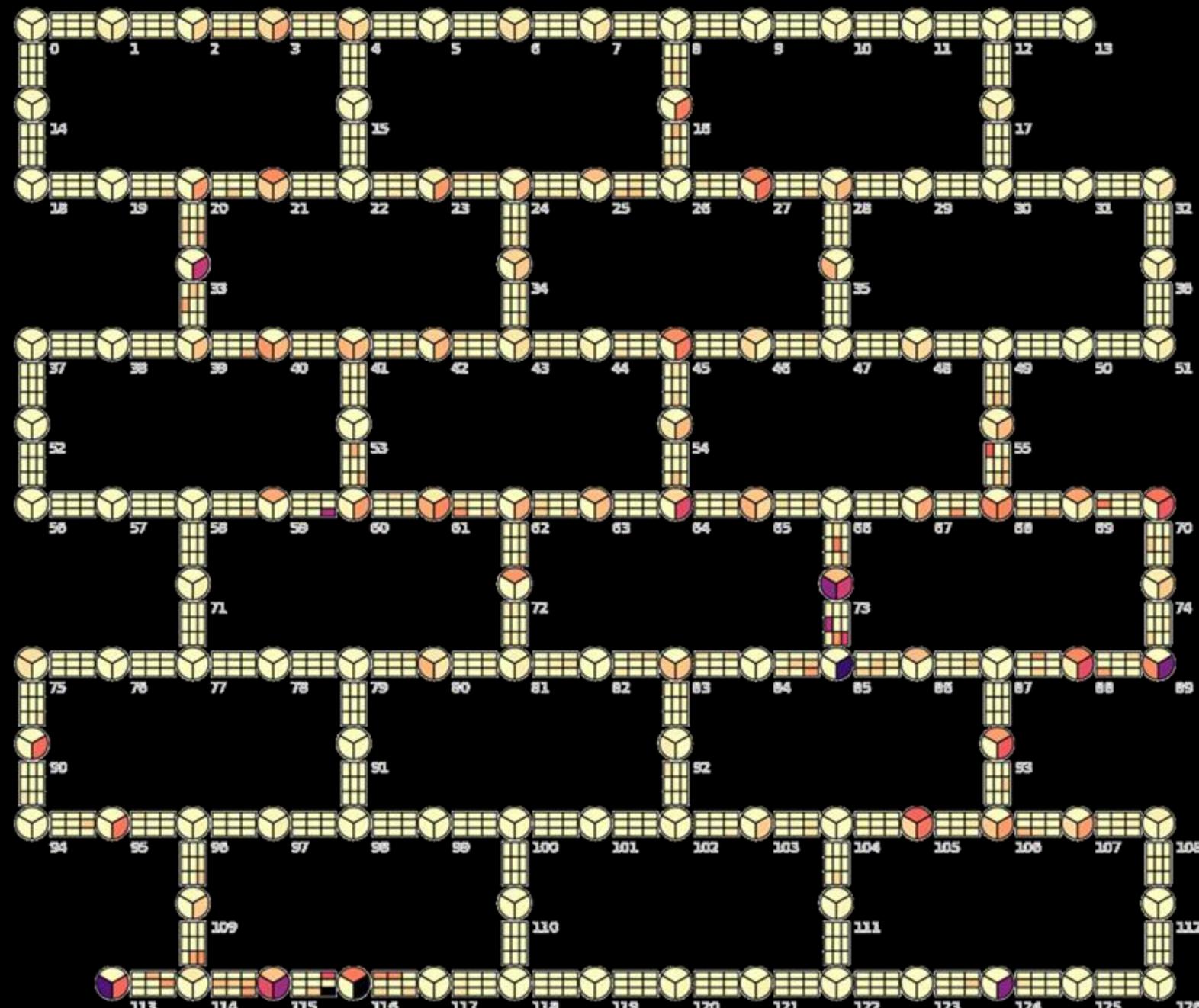
Outlook



Noise tomogram for 127Q Trotter layer



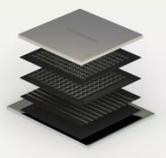
Same number of
learning circuits
as for 4Q



Zlatko Minev, IBM Quantum

Scaling and error budget

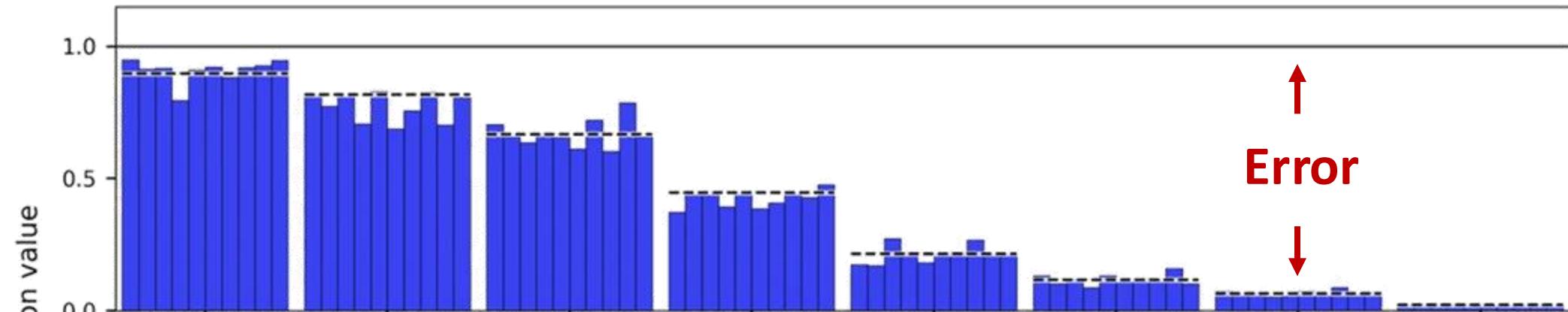




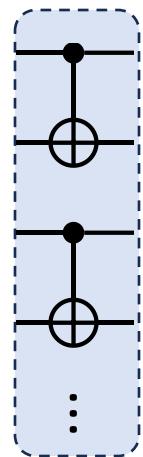
PEC on 50 qubit observables

Z stabilizers of increasing weight

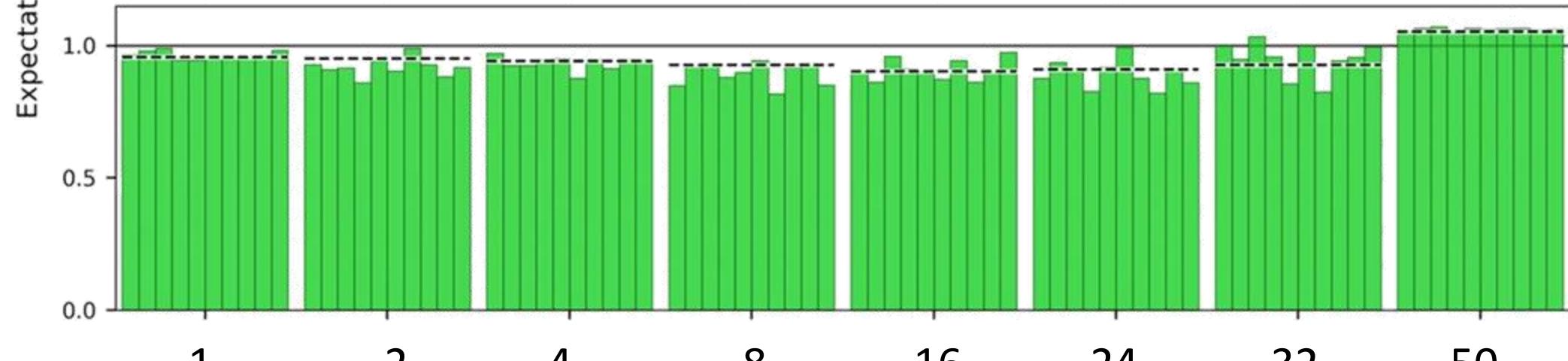
Without PEC



With PEC



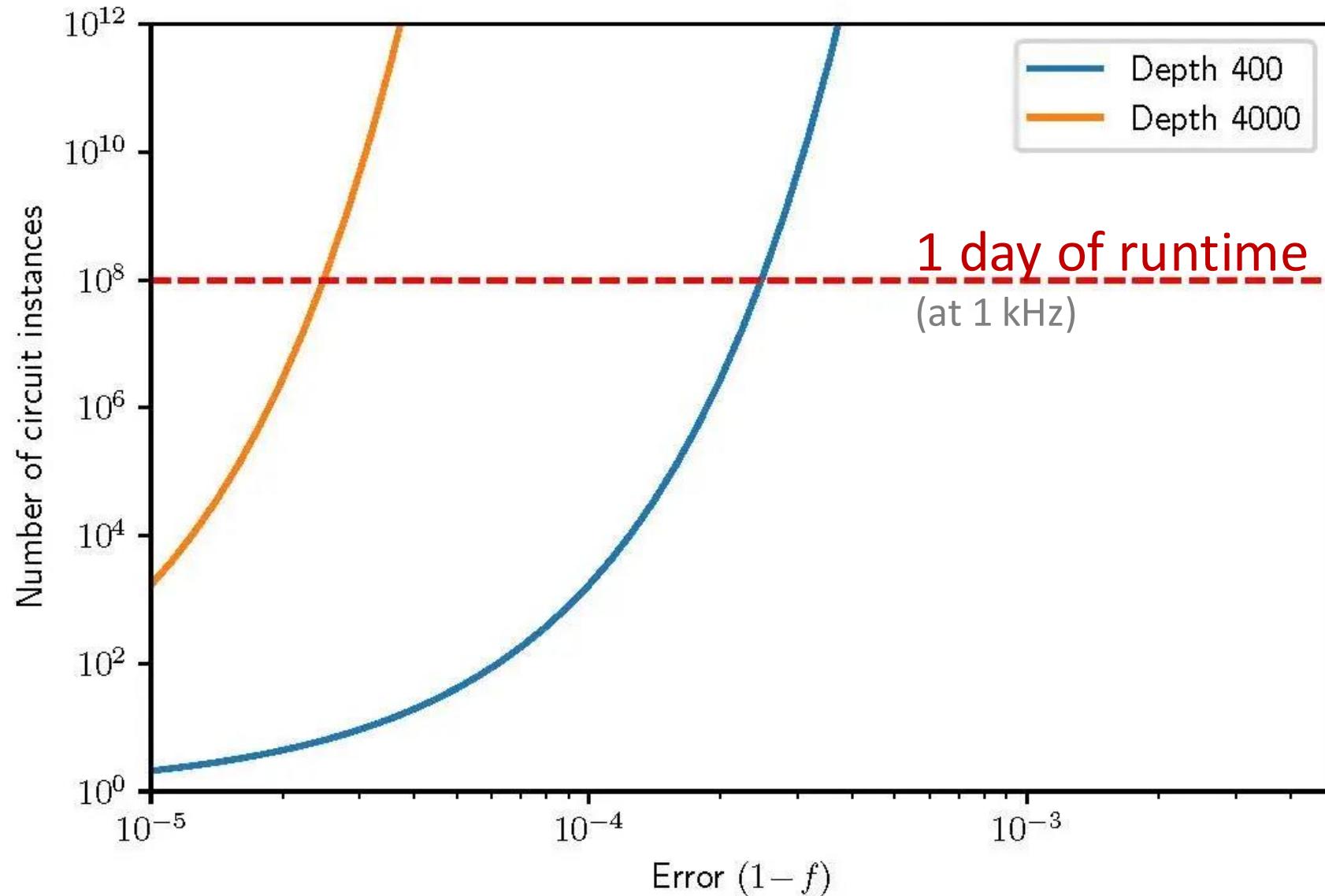
50Q
2 layers of
cNOT gates



Weight of mitigated observable

Path to 100+ qubits?

Estimating
PEC overhead
for Trotter
circuits
comprising
100 qubits



See also on speed: A. Wack, et al., Quality, speed, and scale: three key attributes to measure the performance of near-term quantum computers (2021).

Path to quantum computing

Noise-free estimators can be obtained from noisy quantum computers TODAY, at a runtime cost that is exponential in number of qubits n and circuit depth d

$$\text{Runtime} = \beta d (\bar{\gamma})^{n^d} \text{ seconds}$$

d is the depth of the quantum circuit

β is a measure of the time per circuit layer operation (CLOPS) (increase by pushing **speed**)

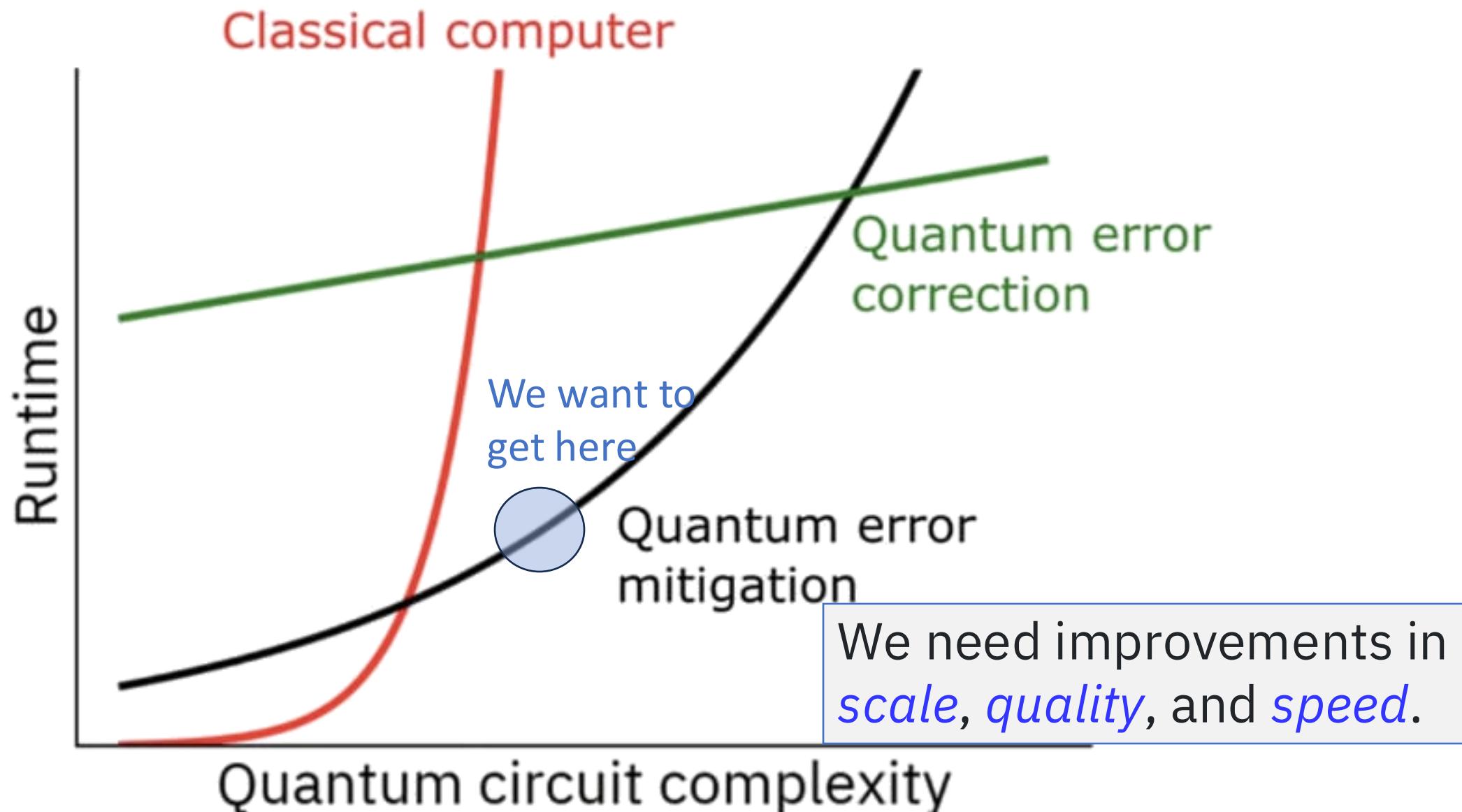
$\bar{\gamma}$ is a measure of the collective quantum noise (increasing **quality** brings it closer to 1)

n is the number of operational qubits (increase by pushing **scale**)

You can further reduce runtime using light cones and other strategies.

	Improvements	$\bar{\gamma}$
Hummingbird r2 (Brooklyn, 65Q)		1.038
Hummingbird r3 (Ithaca, 65Q)	2-3x coherence improvements over r2	1.024
Falcon r10 (Prague, 32Q)	State-of-the-art two-qubit gates, reduced crosstalk	1.012

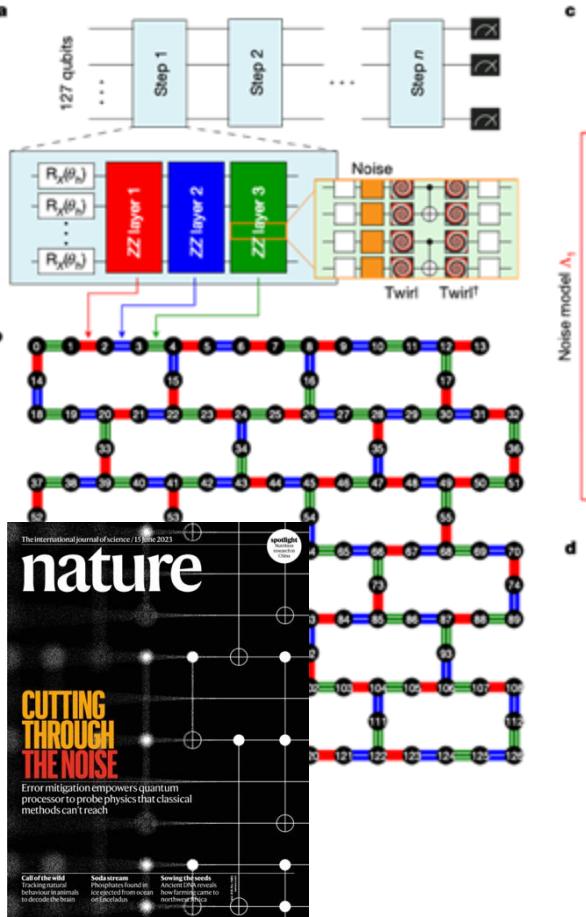
Path to utility of quantum computers before error correction



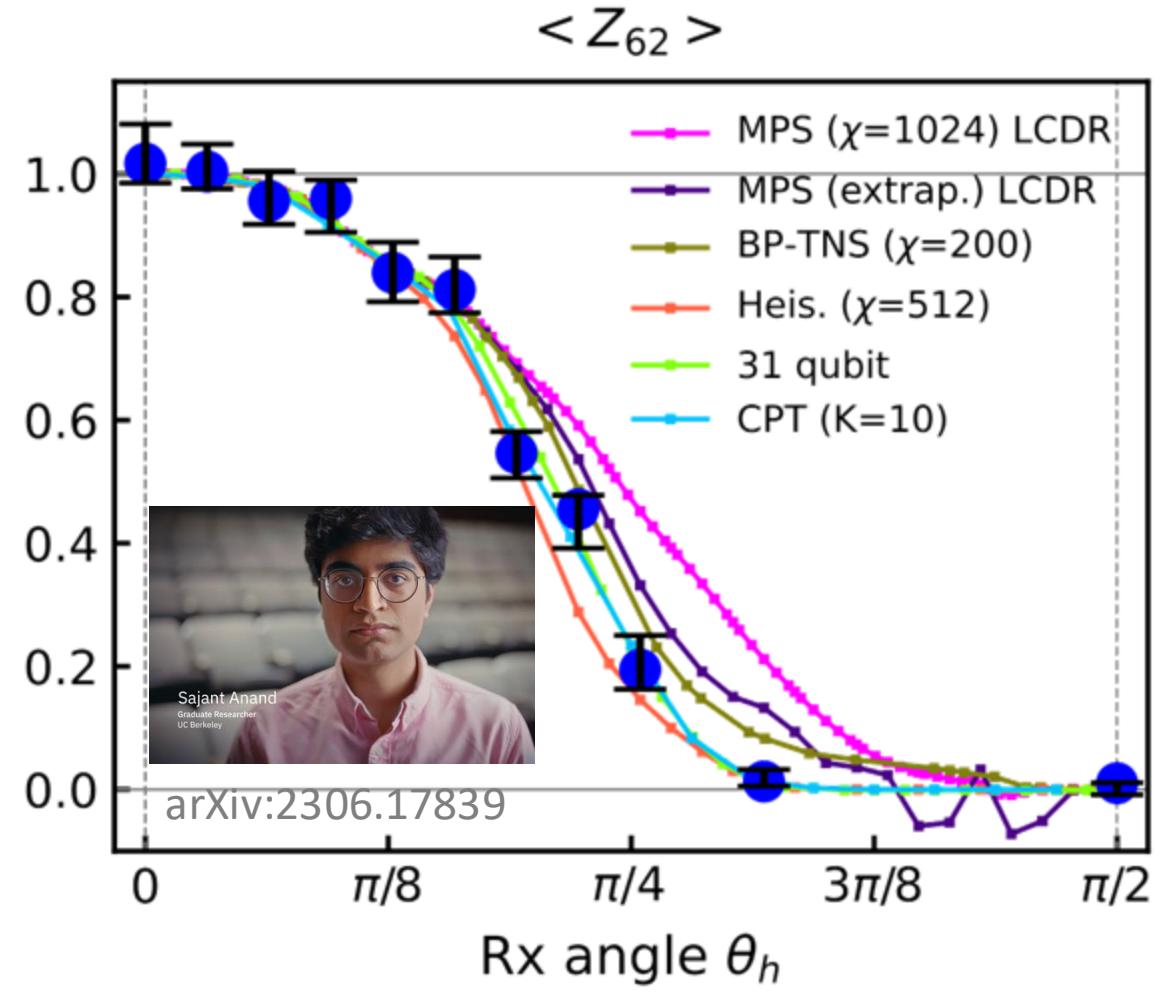
PEC + ZNE for 127 qubits

Article

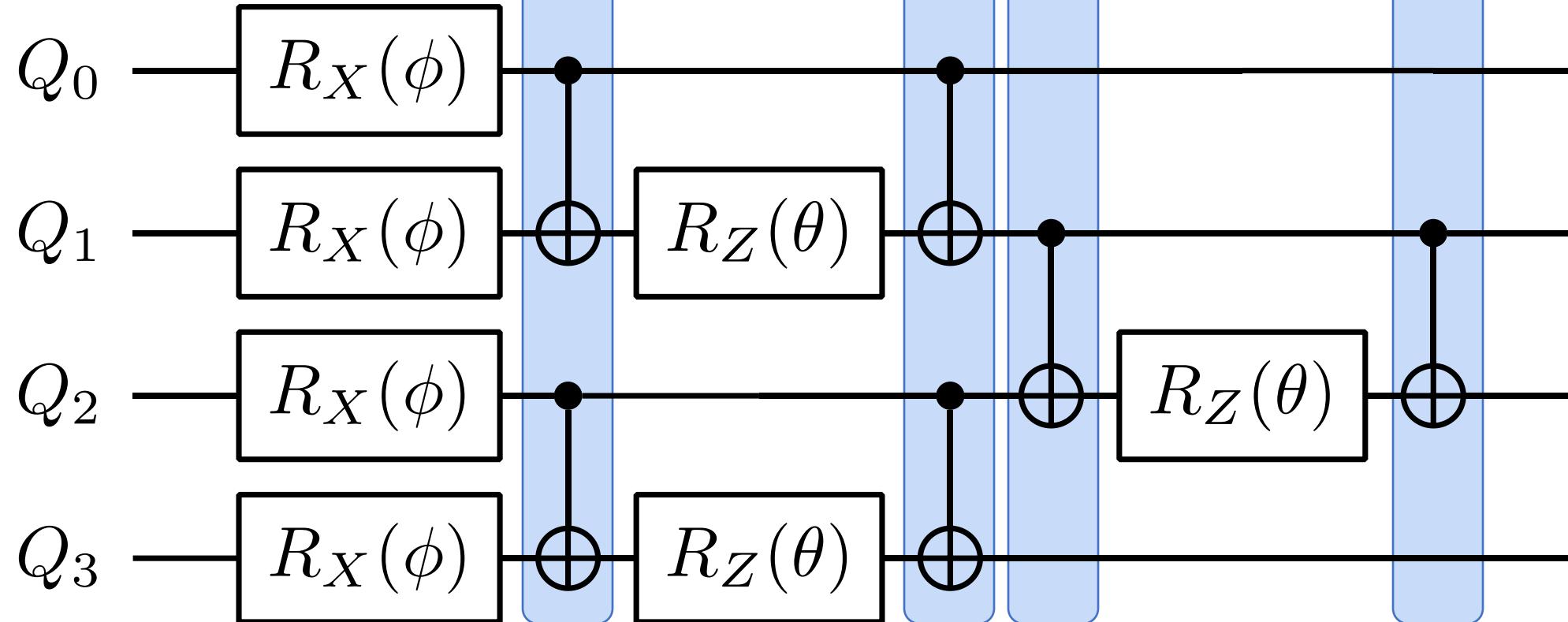
Evidence for the utility of quantum computing before fault tolerance



Youngseok Kim^{1,6}✉, Andrew Eddins^{2,6}✉, Sajant Anand³, Ken Xuan Wei¹, Ewout van den Berg¹, Sami Rosenblatt¹, Hasan Nayfeh¹, Yantao Wu^{3,4}, Michael Zaletel^{3,5}, Kristan Temme¹ & Abhinav Kandala¹✉

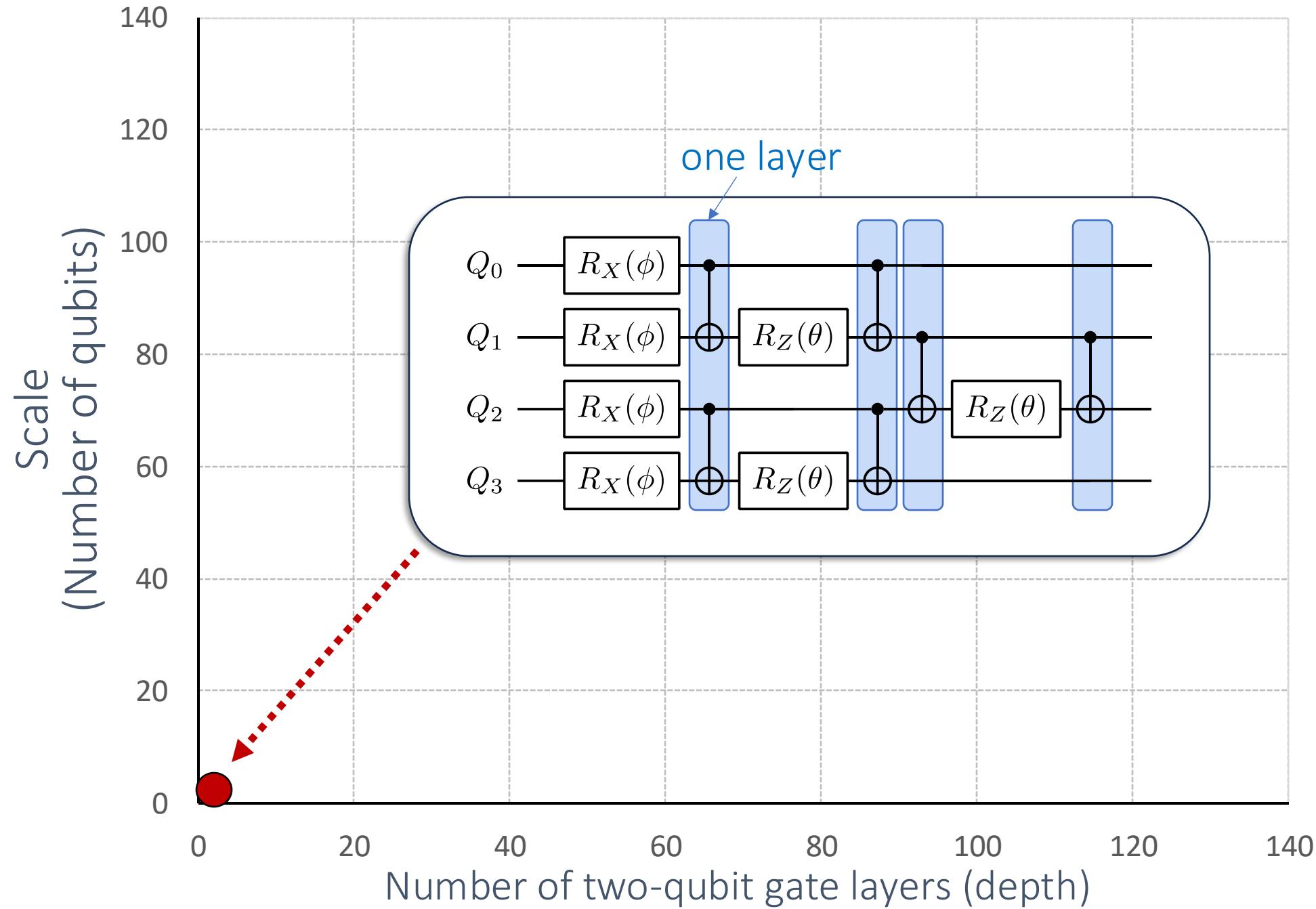


one gate layer

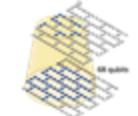


4 qubits x 4 gate layers

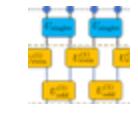
Circuit width × depth



Some early utility-scale experiments



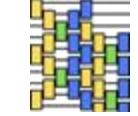
[0] Kim, Eddins, ..., Temme, Kandala.
Nature 618, 500–505 (2023)



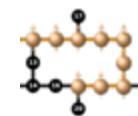
[1] Yu, Zhao, Wei.
arXiv: 2207.09994 (2022)



[2] Shtanko, Wang, Zhang, Harle, Seif,
Movassagh, Minev.
arXiv: 2307.07552 (2023)



[3] Farrell, Illa, Ciavarella, Savage.
arXiv: 2308.04481 (2023)



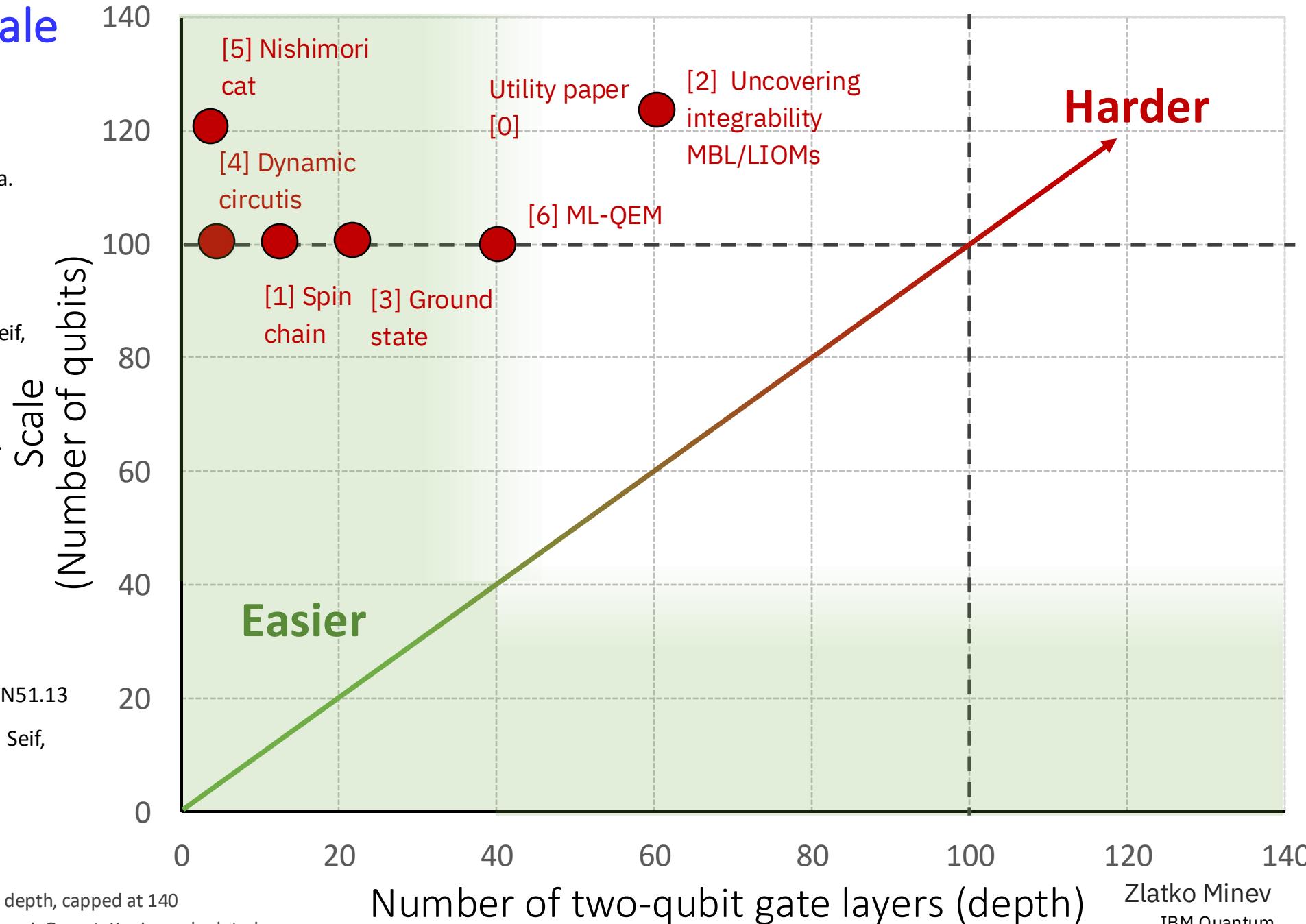
[4] Bäumer, Tripathi, Seif,
Minev. APS Y45.4
arXiv: 2308.13065 (2023)



[5] Chen, Zhu, Verresen, Seif,
Baümer, ... Trebst, Kandala.
arXiv: 2309.02863 (2023) APS N51.13



[6] Liao, Wang, Sitdikov, Salcedo, Seif,
Minev.
arXiv: 2308.13065 (2023)

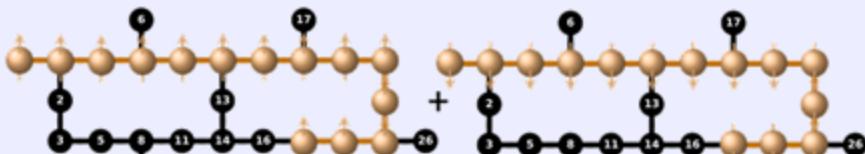


* signal stops or decays more than 50% beyond this depth, capped at 140

* note: quantum advantage with shallow circuits, Bravyi, Gosset, Konig, and related

Check out related utility-scale work

Efficient Long-Range Entanglement using Dynamic Circuits (invited)

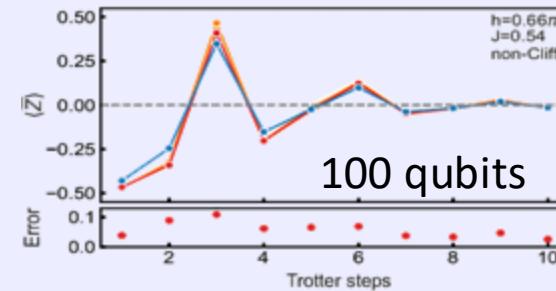


Gate teleportation over 100+ qubits

arXiv:2308.13065 (2023)

Bäumer, Tripathi, Wang, Rall, Chen, Majumder, Seif, Minev

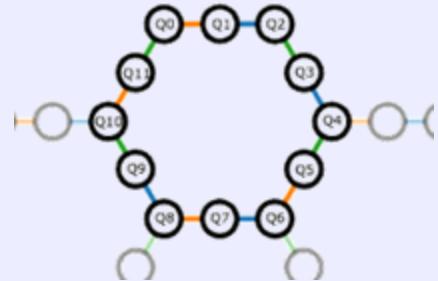
Machine Learning for Practical Quantum Error Mitigation (ML-QEM)



arXiv:2308.13065 (2023)

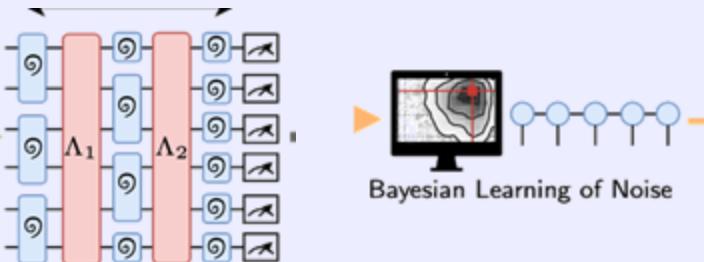
Liao, Wang, Situdikov, Salcedo, Seif, Minev

Learning about Quantum Noise at Scale



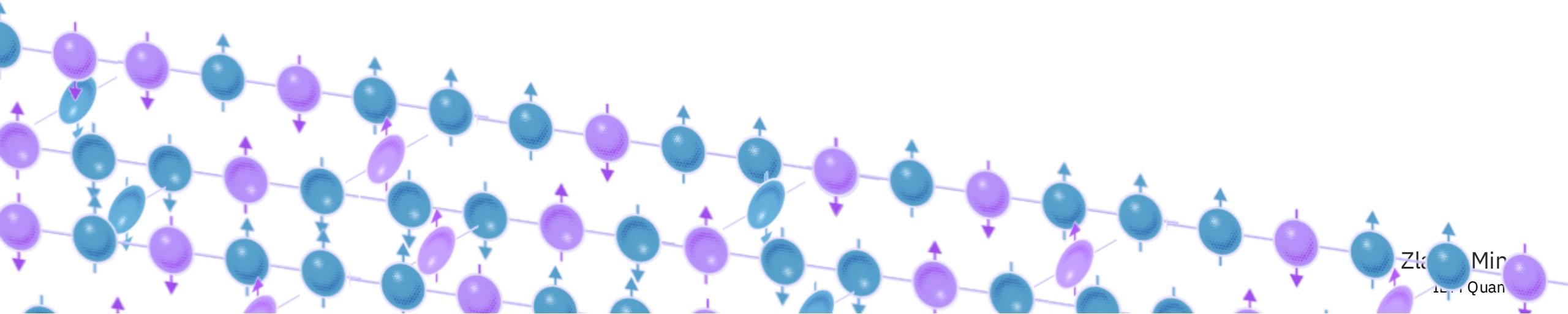
Seif, Liao, Majumder, Chen, Wang, Bäumer, Malekakhlagh, Javadi-Abhari, Jiang, Minev
arXiv:2408.03376 (2024)

Demonstration of Robust and Efficient Quantum Property Learning with Shallow Shadows



arXiv:2402.17911 (2024)
Hu, Gu, Majumder, Ren, Zhang, Wang, Minev, You, Seif, Yelin

Preview



Can quantum computers be useful for
many-body physics in the next 3-5 years?

Uncovering the dynamics of many-body systems

Many-body quantum systems and their dynamics

- fundamental and technological
- but generically difficult to simulate and understand

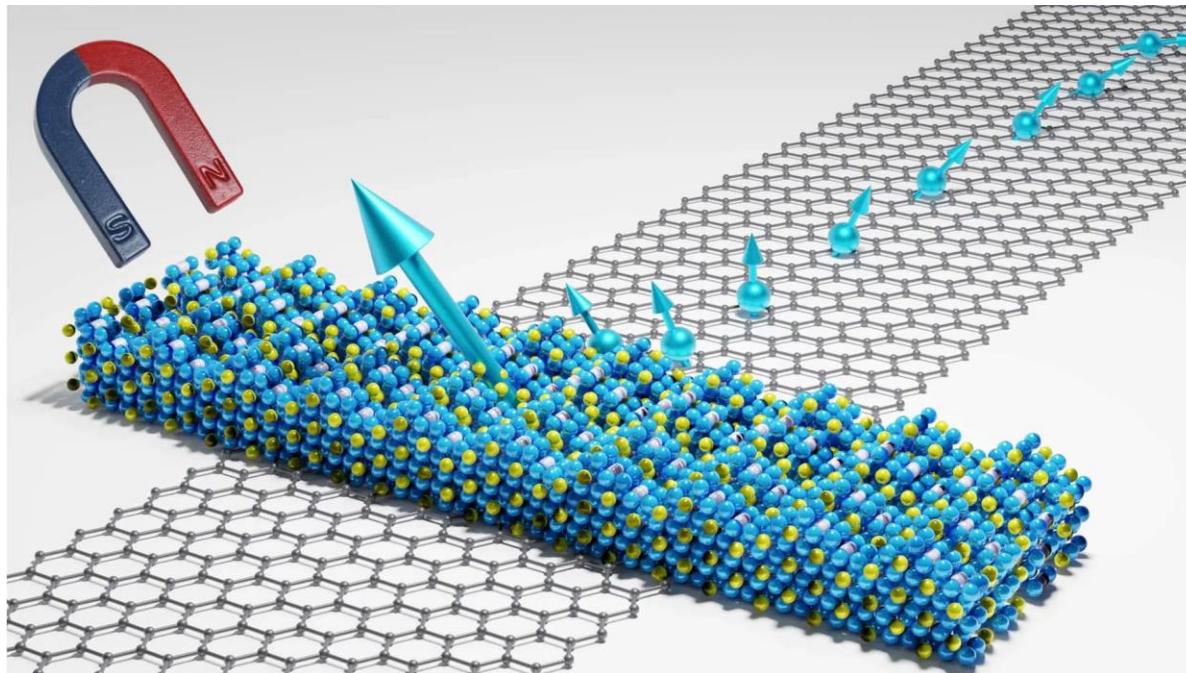


Image: Chalmers

Symmetries, conservation laws, and integrability

- can unravel intricacies of these complex systems
- but generically difficult to discover

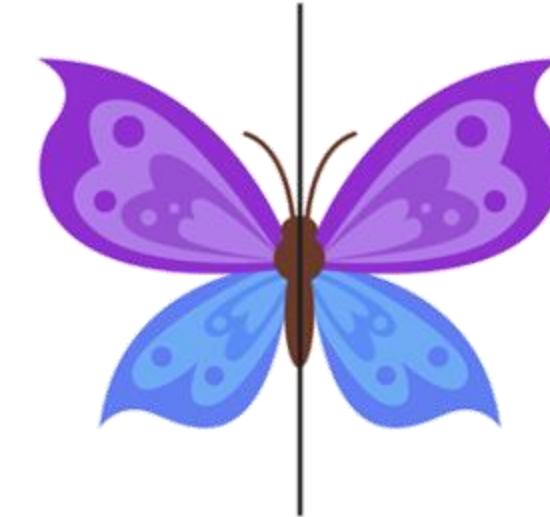
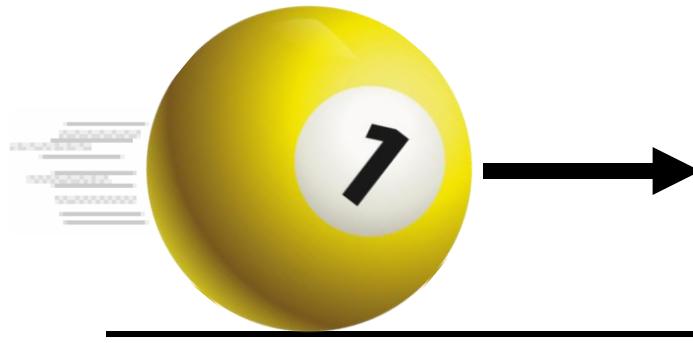


Image: SuperSimple

Zlatko Minev
IBM Quantum

Classical Physics: Integrals of Motion

Before



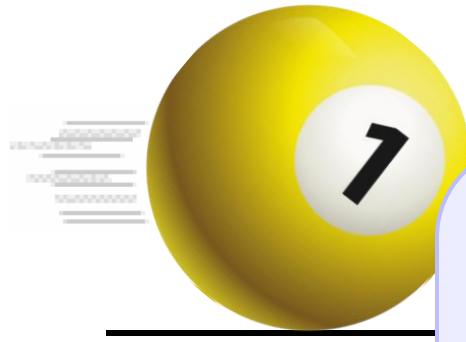
After



Integrals of motion:
Total Linear Momentum
Total Kinetic Energy

Classical Physics: Integrals of Motion

Before



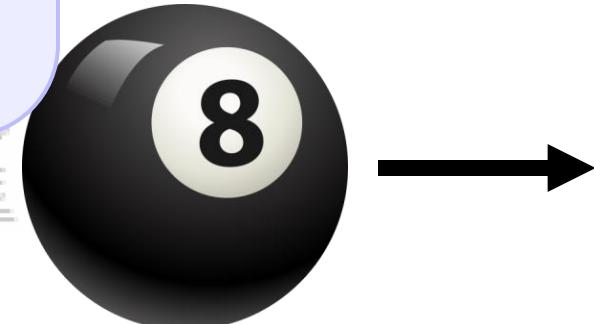
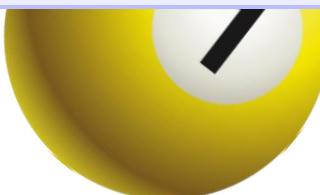
If you can find enough
Integrals of Motion (IOM),

Integrals of

Total Linear Momentum

Total Kinetic Energy

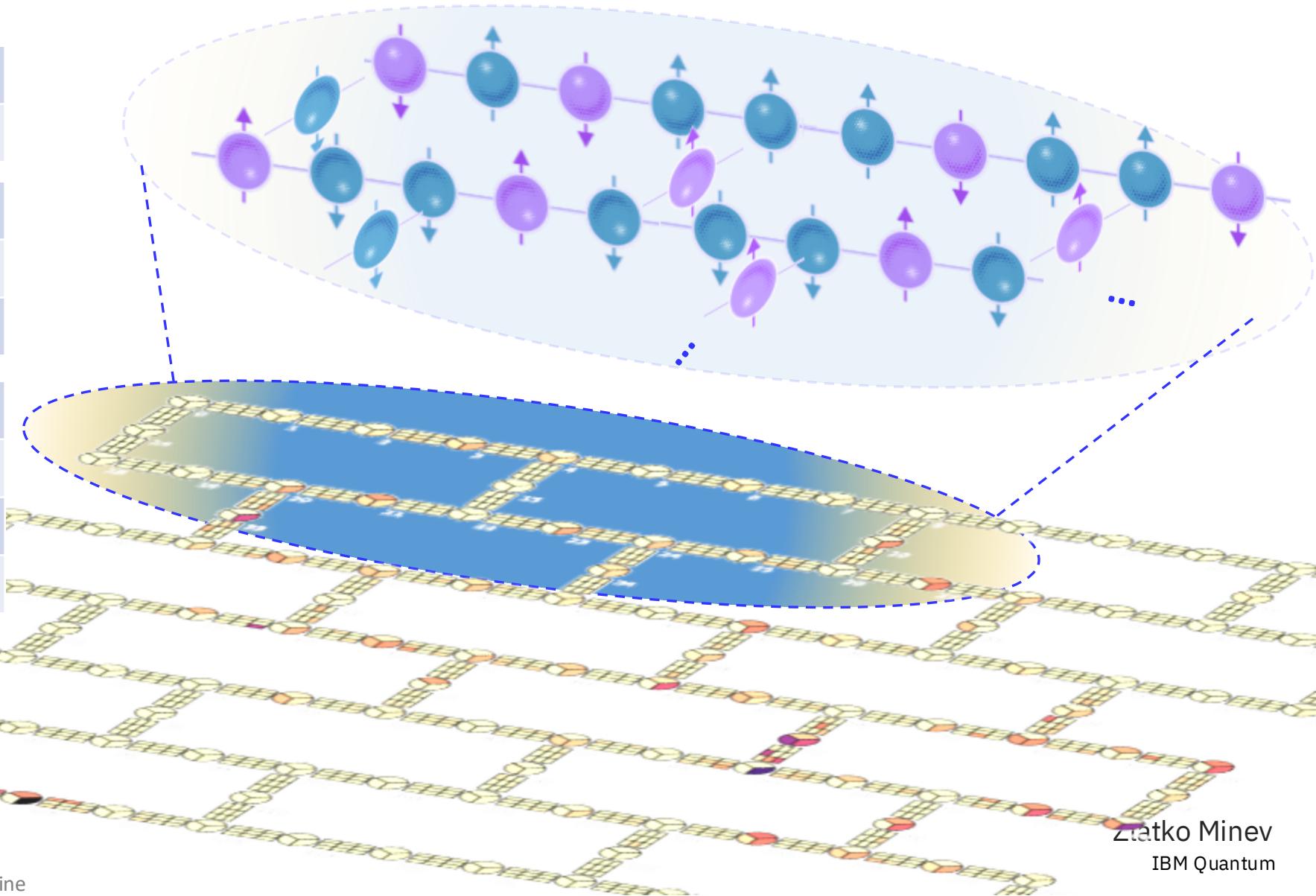
After



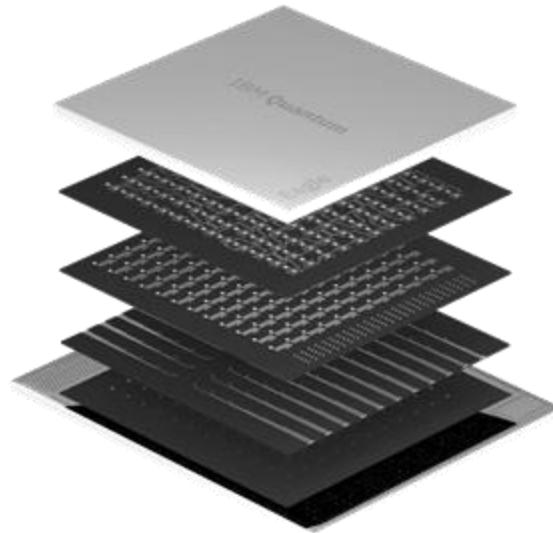
QSim on 100Q+: 2D interacting many-body Floquet system

Experimental setting

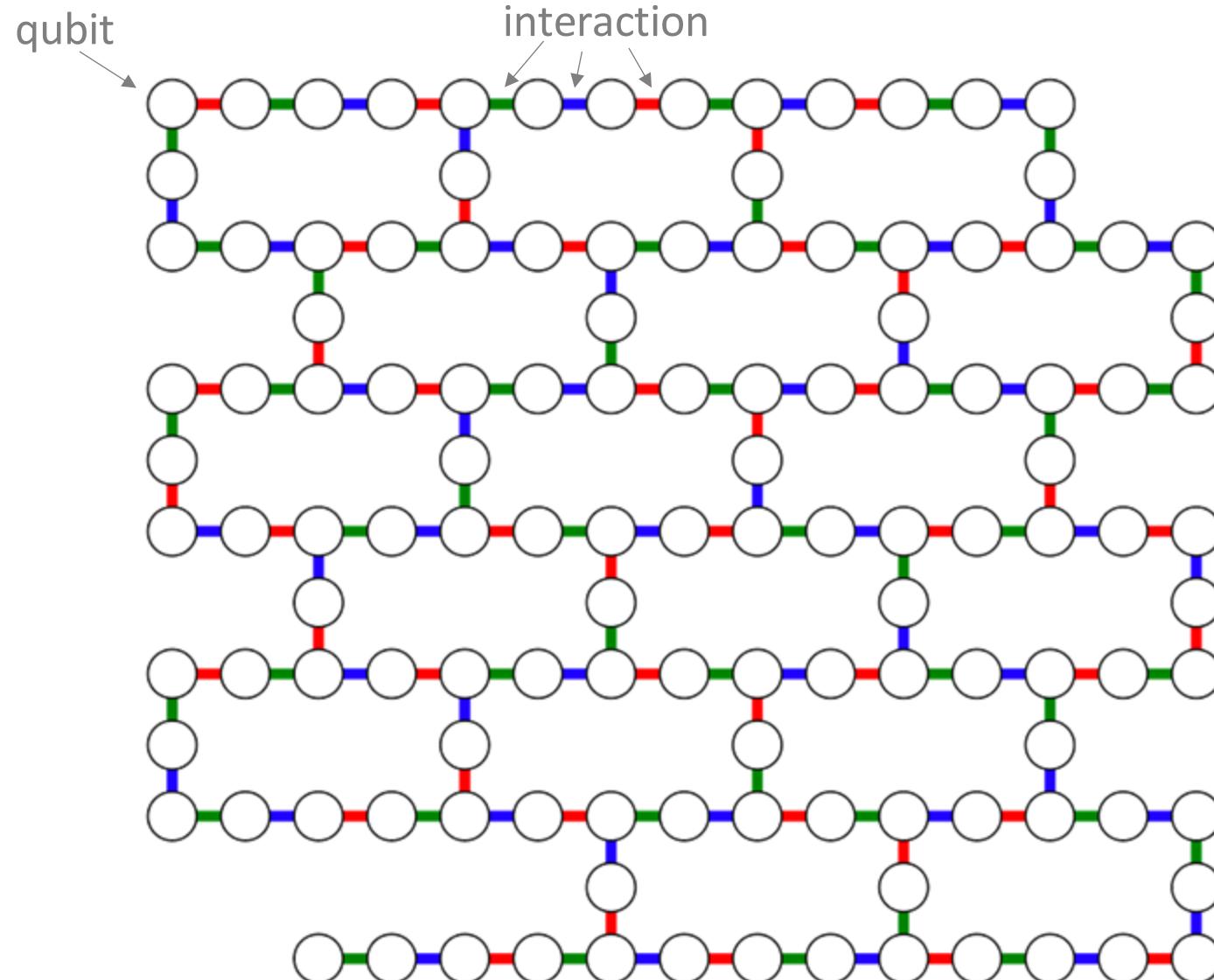
Number of qubits	124Q
Connectivity	2D h-hex
Depth in 2Q layers	60
Floquet steps	20
Total num. of cX gates	2,641
Circuits (entire paper)	3.5×10^5
Shots (entire paper)	5.3×10^8
QPU runtime	80 hours
Environment	Cloud



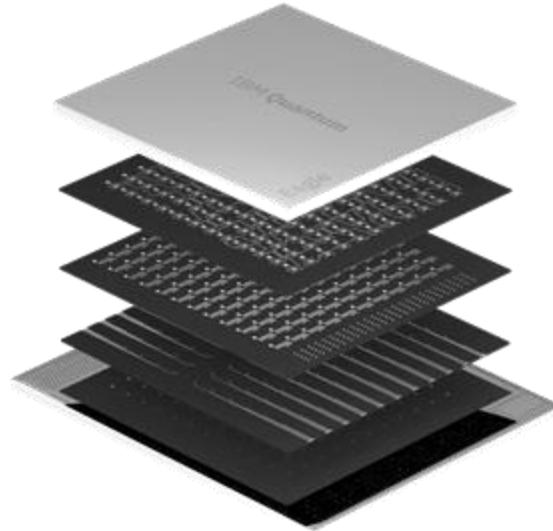
Interaction map and device layers



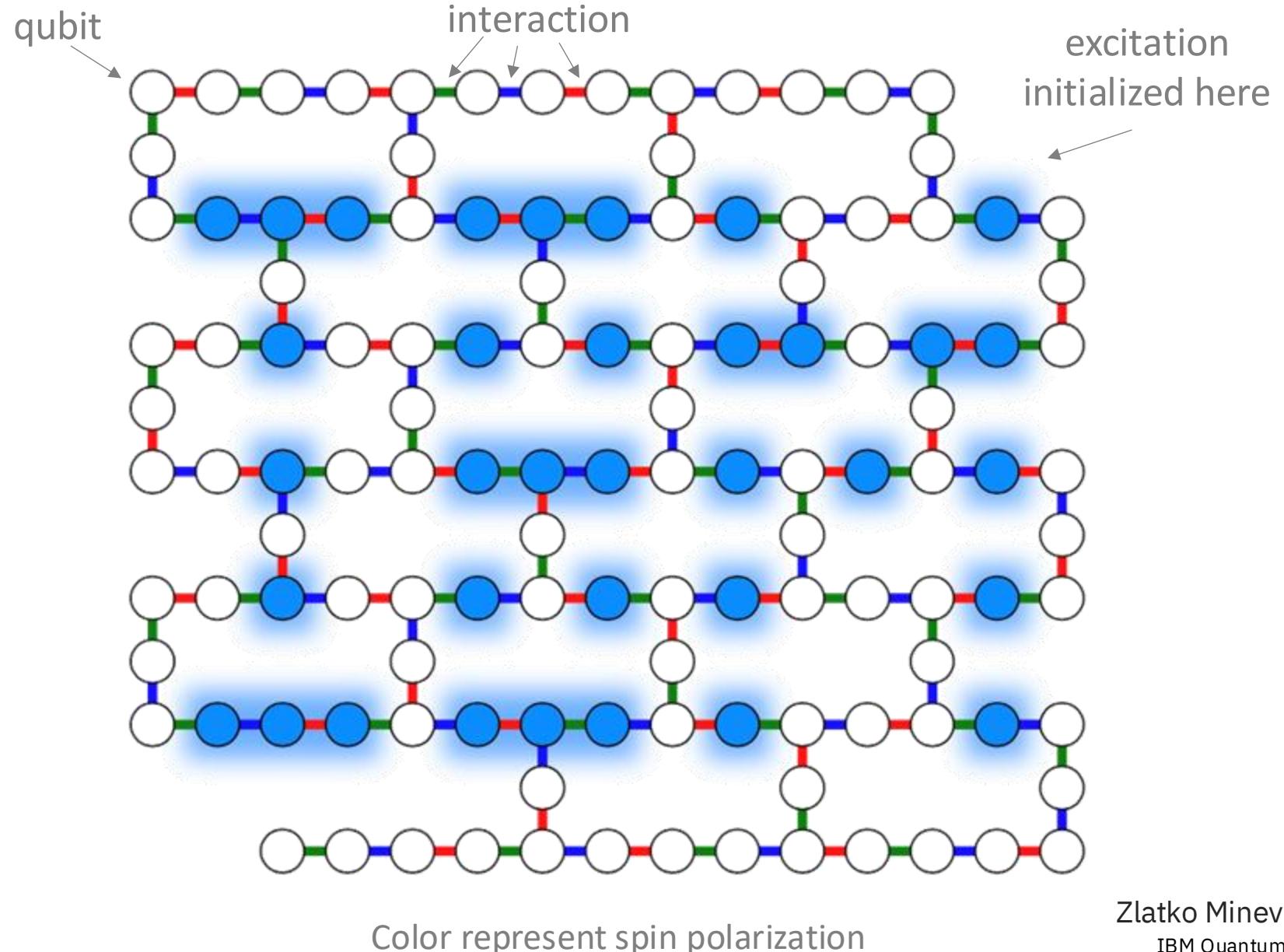
Number of qubits	124Q
Connectivity	2D h-hex
Depth in cX gates	60
Floquet steps	20
Total number of cXs	2,641



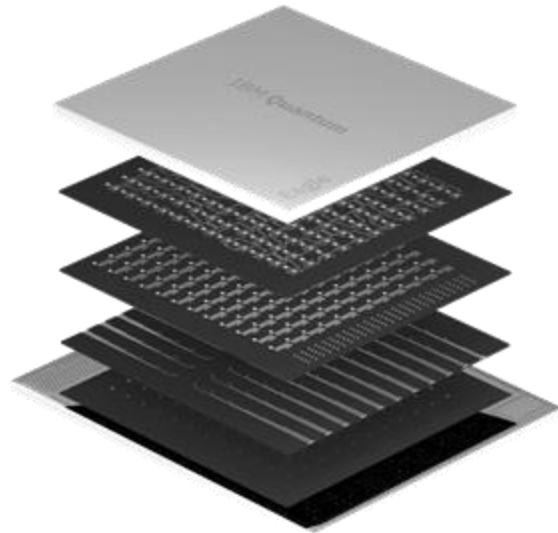
Initialize lattice in fun states



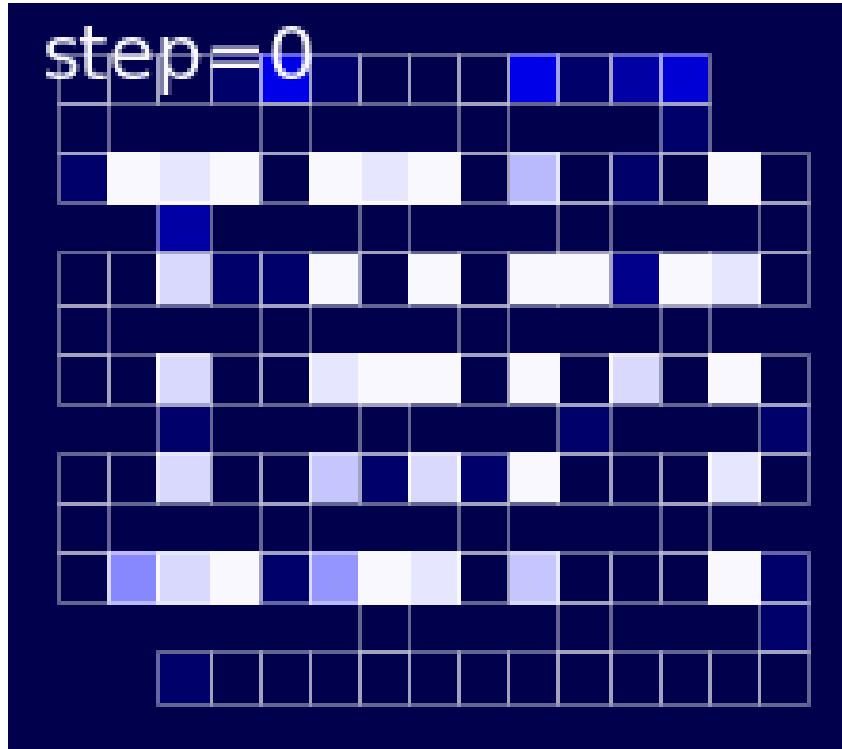
Number of qubits	124Q
Connectivity	2D h-hex
Depth in cX gates	60
Floquet steps	20
Total number of cXs	2,641



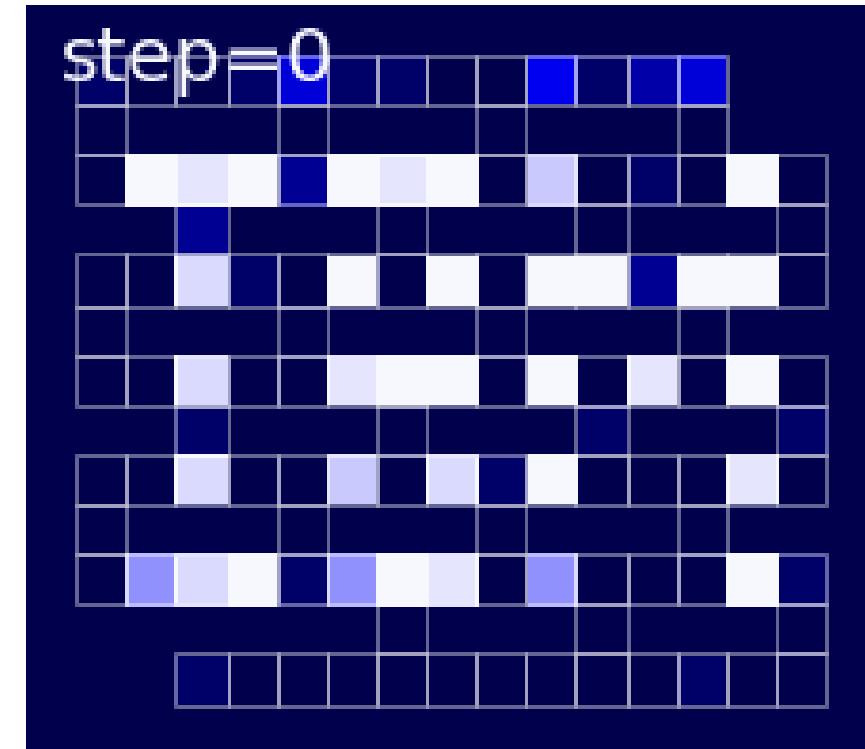
Quantum dynamics in different regimes



Number of qubits	124Q
Connectivity	2D h-hex
Depth in cX gates	60
Floquet steps	20
Total number of cXs	2,641



Thermalizing regime



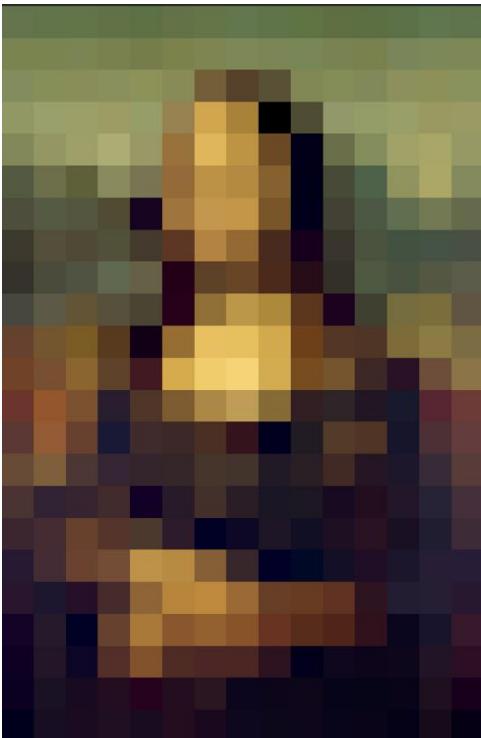
Prethermal regime

Color represent spin polarization

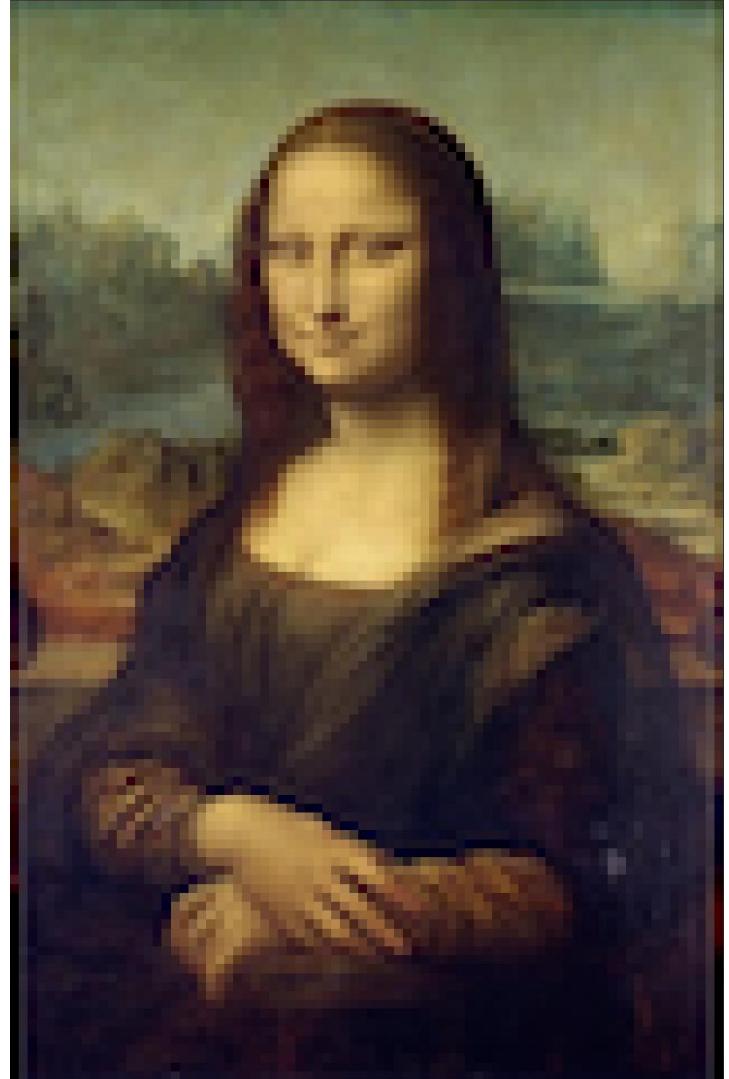
A more detailed portrait



Spin
imbalance

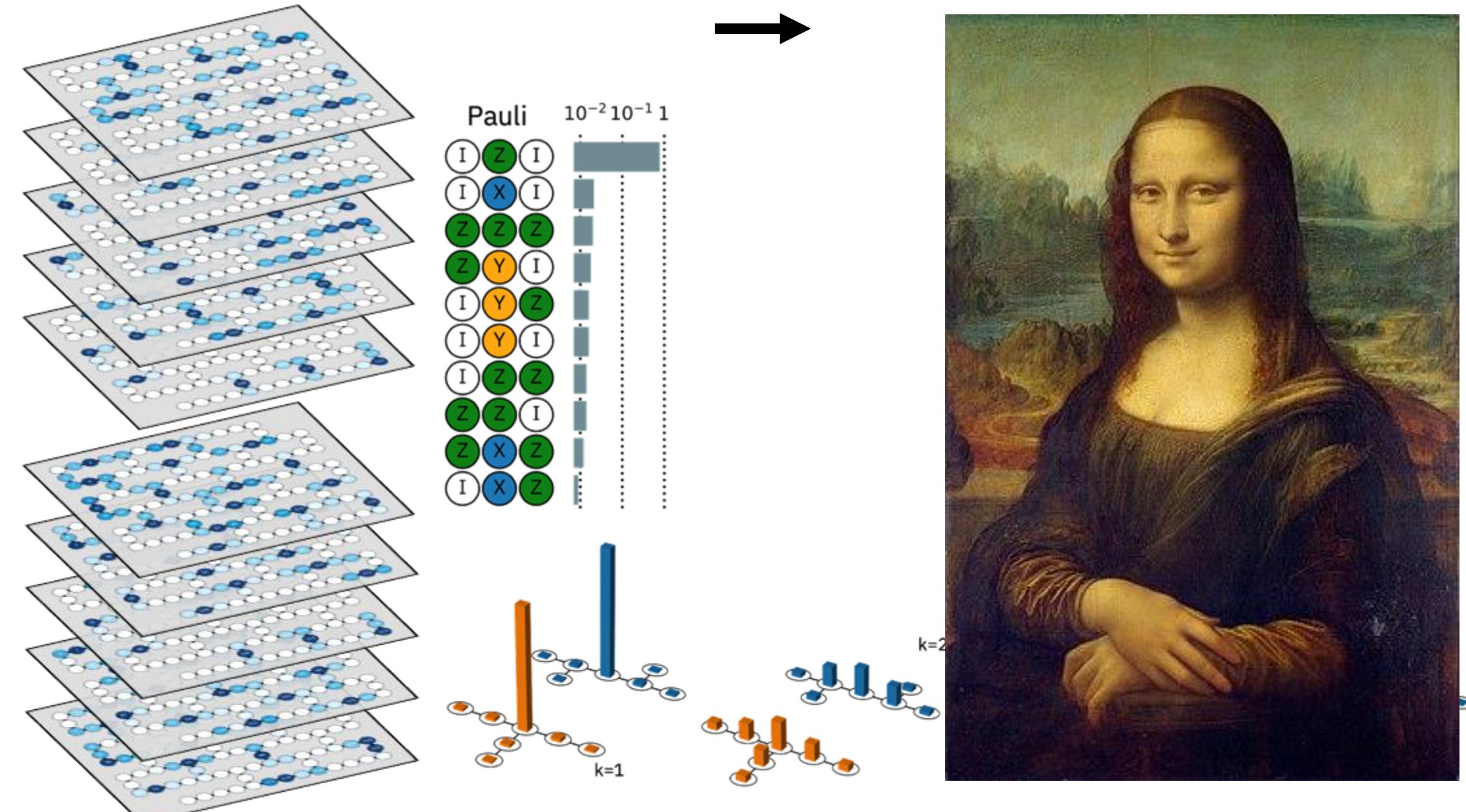


One-particle density
matrix (OPDM)



Local integrals of motion
(LIOMs)

Operational LIOM description on observation timescales



The important thing is not to stop questioning. Curiosity has its own reason for existence.

One cannot help but be in awe when they contemplate the mysteries of eternity, of life, of the marvelous structure of reality.

It is enough if one tries merely to comprehend a little of this mystery each day.

Albert Einstein

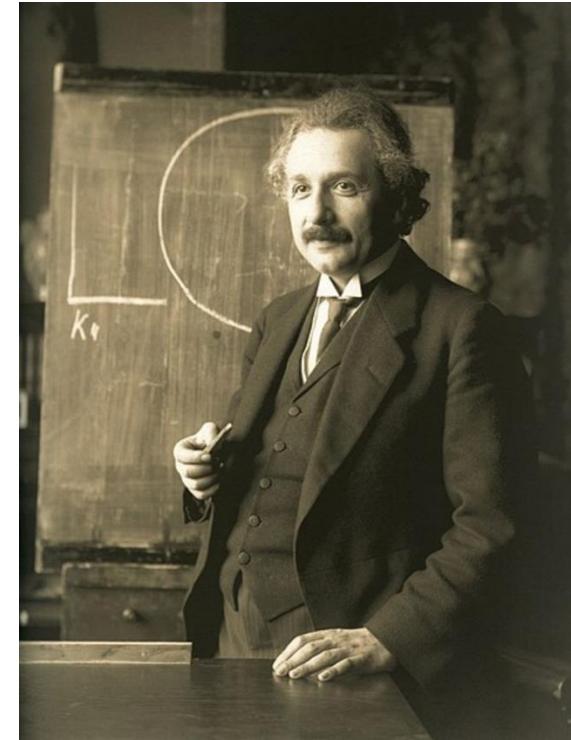


Photo: F. Schmutzler



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IBM Quantum

Quantum Working Groups

From utility to advantage

IBM Quantum working groups bring together the best scientists in our field to accelerate our path to achieving Quantum Advantage by 2025, across domain areas:

Optimization

Quantum Optimization:
Potential, Challenges, and the
Path Forward

arXiv:2312.02279



Materials & HPC

Quantum-centric
Supercomputing for Materials
Science: A Perspective on
Challenges and Future
Directions

arXiv:2312.09733



High-Energy Physics

Quantum Computing for High-
Energy Physics: State of the Art
and Challenges. Summary of
the QC4HEP Working Group

arXiv:2307.03236



Healthcare & Life Sciences

Towards quantum-enabled
cell-centric therapeutics.

arXiv:2307.05734



Sustainability

Collaborative projects in the
fields of Materials and
Energy leveraging quantum
computers.

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