

Machine learning for practical quantum error mitigation

Haoran Liao, Derek Wang, Iskandar Situdikov, Ciro Salcedo, Alireza Seif, **Zlatko Minev (IBM*)**

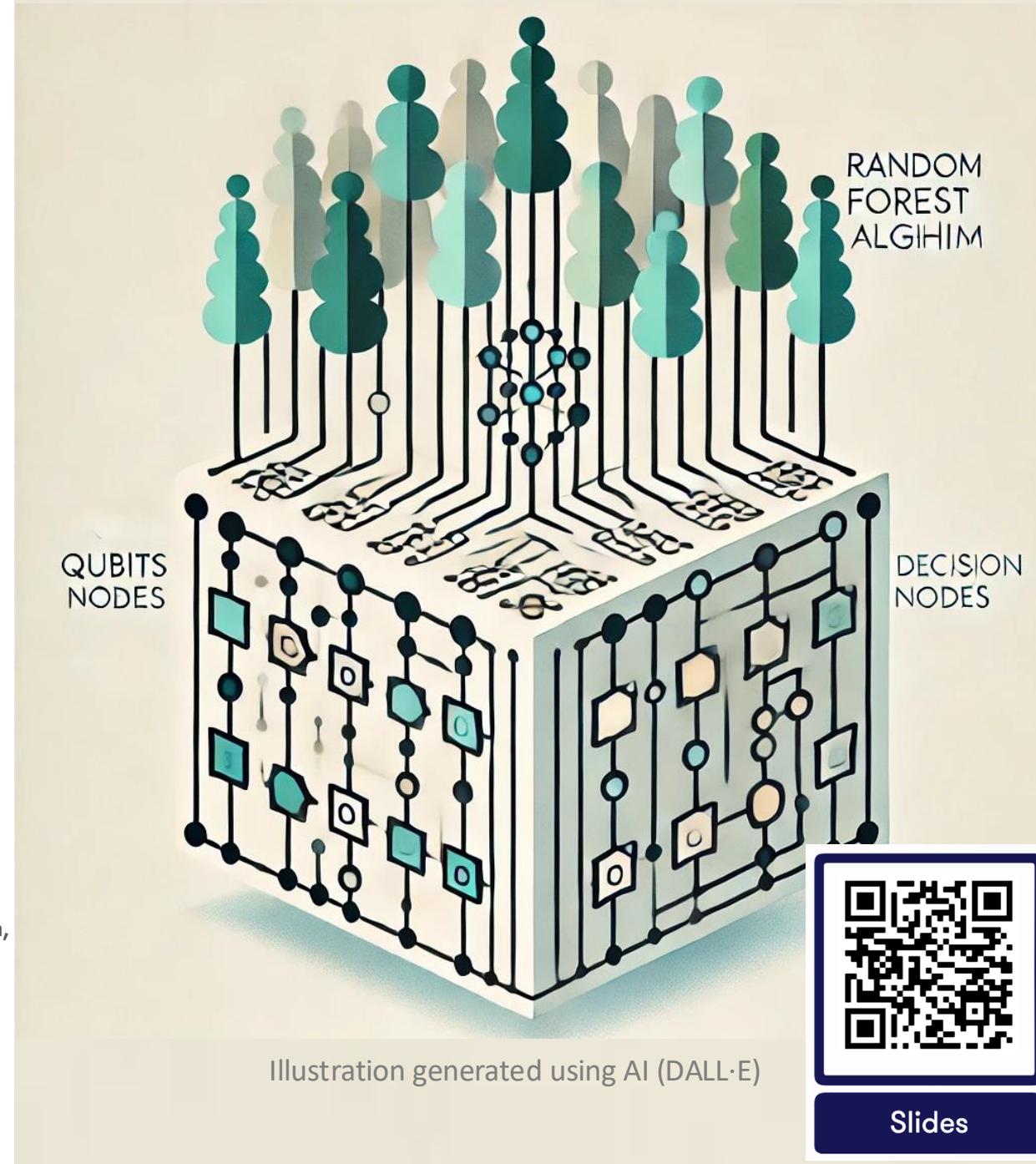
Nature Machine Intelligence v. 6, p. 1478 (2024)

Acknowledgements: Brian Quanz, Patrick Rall, Oles Shtanko, Roland De Putter, Kunal Sharma, Barbara Jones, Sona Najafi, Thaddeus Pelligrini, Grace Harper, Vinay Tripathi, Antonio Mezzacapo, Christa Zoufal, Travis Scholten, Bryce Fuller, Swarnadeep Majumder, Sarah Sheldon, Youngseok Kim, Pedro Rivero, Will Bradbury, Nate Gruver, Minh Tran, Kristan Temme, and the broader IBM Quantum team



Slides?

zlatko-minev.com/blog @zlatko_minev



Why?

Biggest challenge?

Please do share

Noise (Errors)

Biggest challenge?

engineering

need CS/EE
talent

hardware
development

error correction
overheads

scalability

decoherence

high error rates

loss

stability

heat

algo
development

importance of N
in NISQ

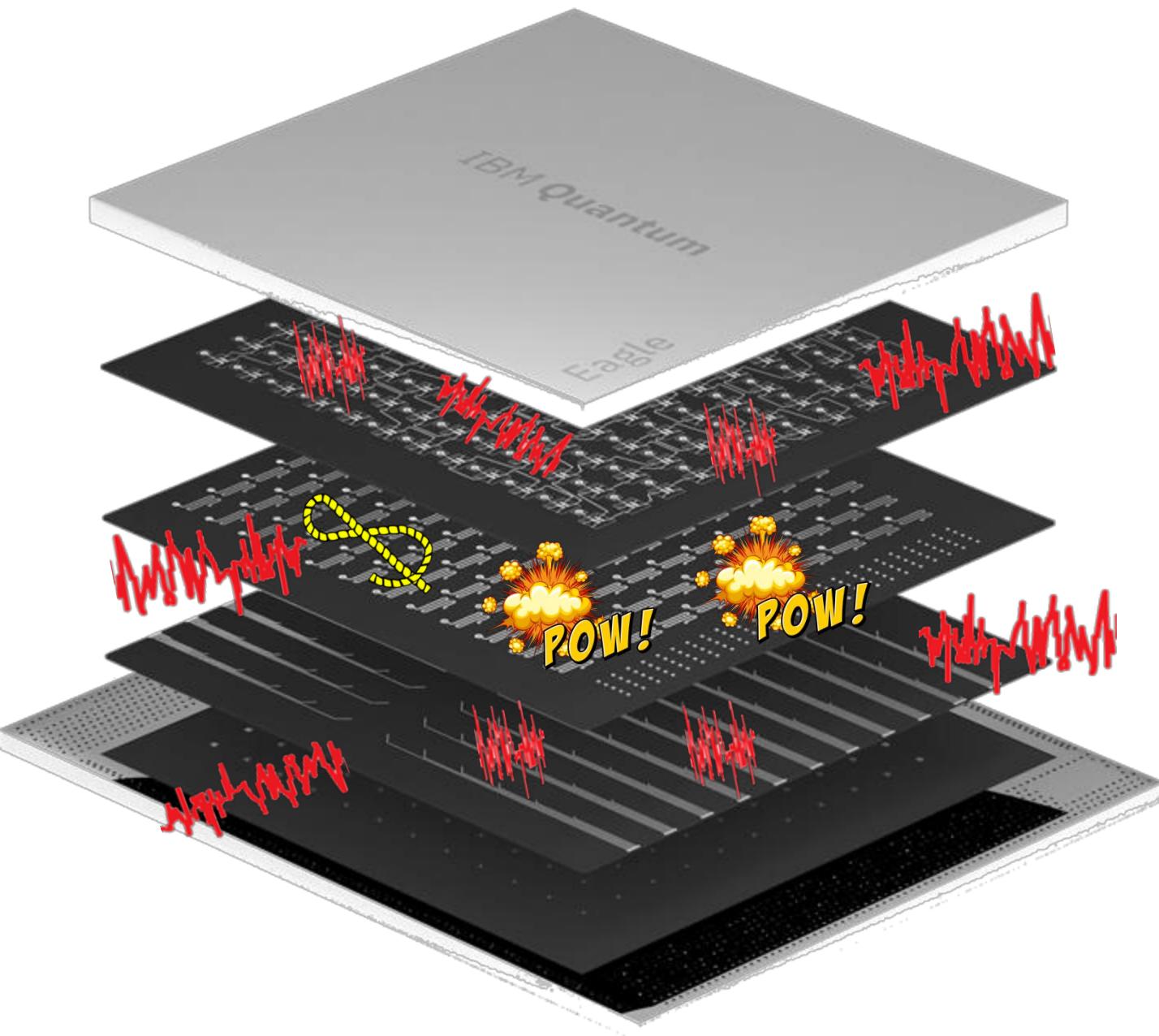
material
quality

modularization

hype

gravity

expectations



Noise (Errors)



How to deal with errors due to noise?

Monitor

Error occurs

Error detect



Quantum error correction

Shor, PRA (1995), ...

Monitor

Error anticipated

Tell signal detected



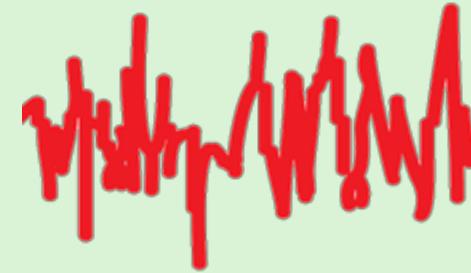
Catch and reverse

Minev, Nature (2019), ...

No monitor

Error occurs

Error undetected

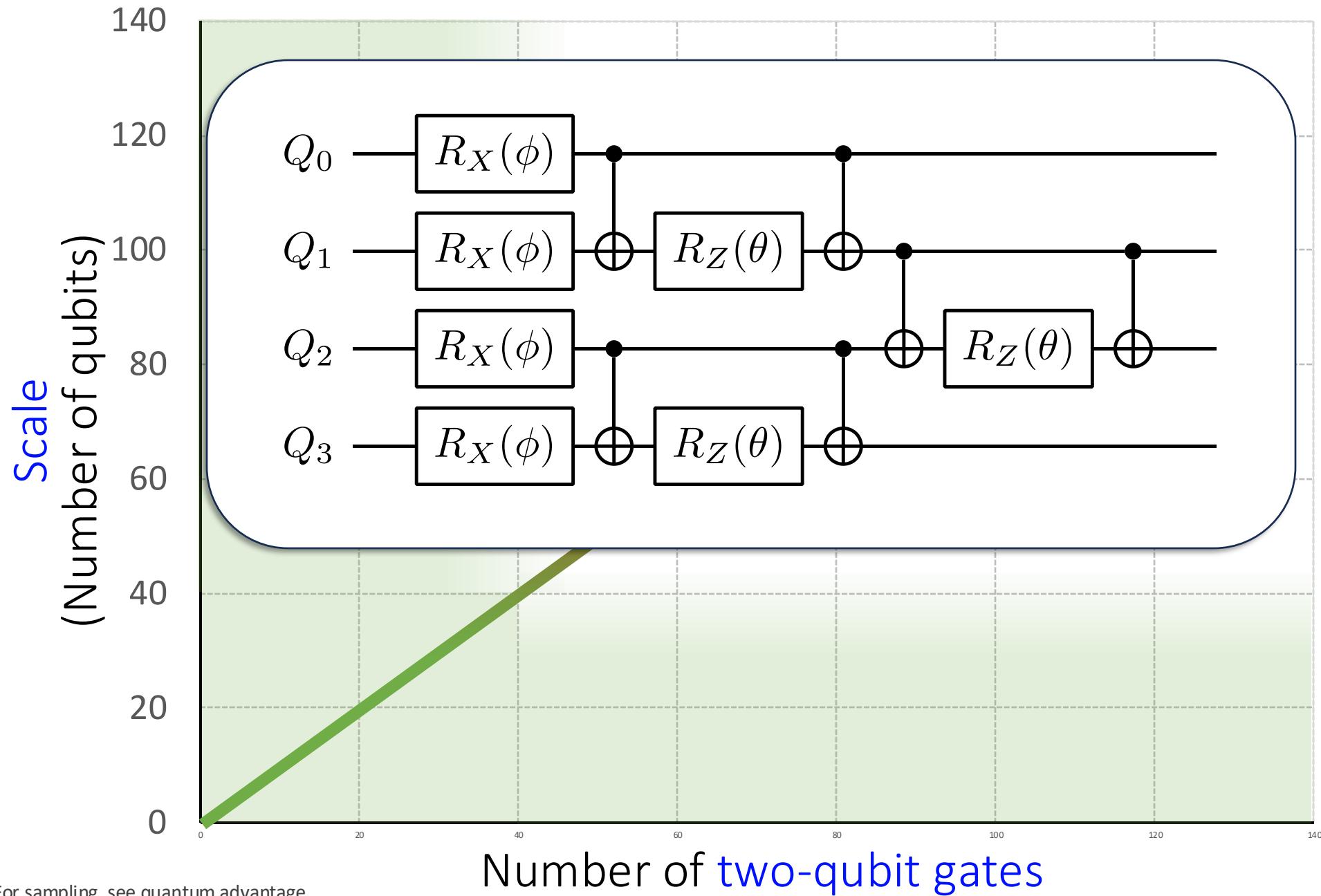


Error mitigation

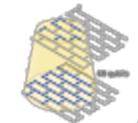
RMP 95, 045005 (2023)
... subject of today

Landscape of quantum circuits

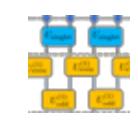
and the use of quantum error mitigation



Some early utility-scale experiments



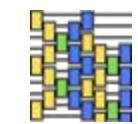
[0] Kim, Eddins, ..., Temme, Kandala.
Nature 618, 500–505 (2023)



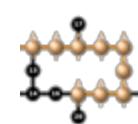
[1] Yu, Zhao, Wei.
arXiv: 2207.09994 (2022)



[2] Shtanko, Wang, Zhang, Harle,
Seif, Movassagh, Minev.
arXiv: 2307.07552 (2023)



[3] Farrell, Illa, Ciavarella, Savage.
arXiv: 2308.04481 (2023)



[4] Bäumer, Tripathi, Seif,
Minev.
arXiv: 2308.13065 (2023)

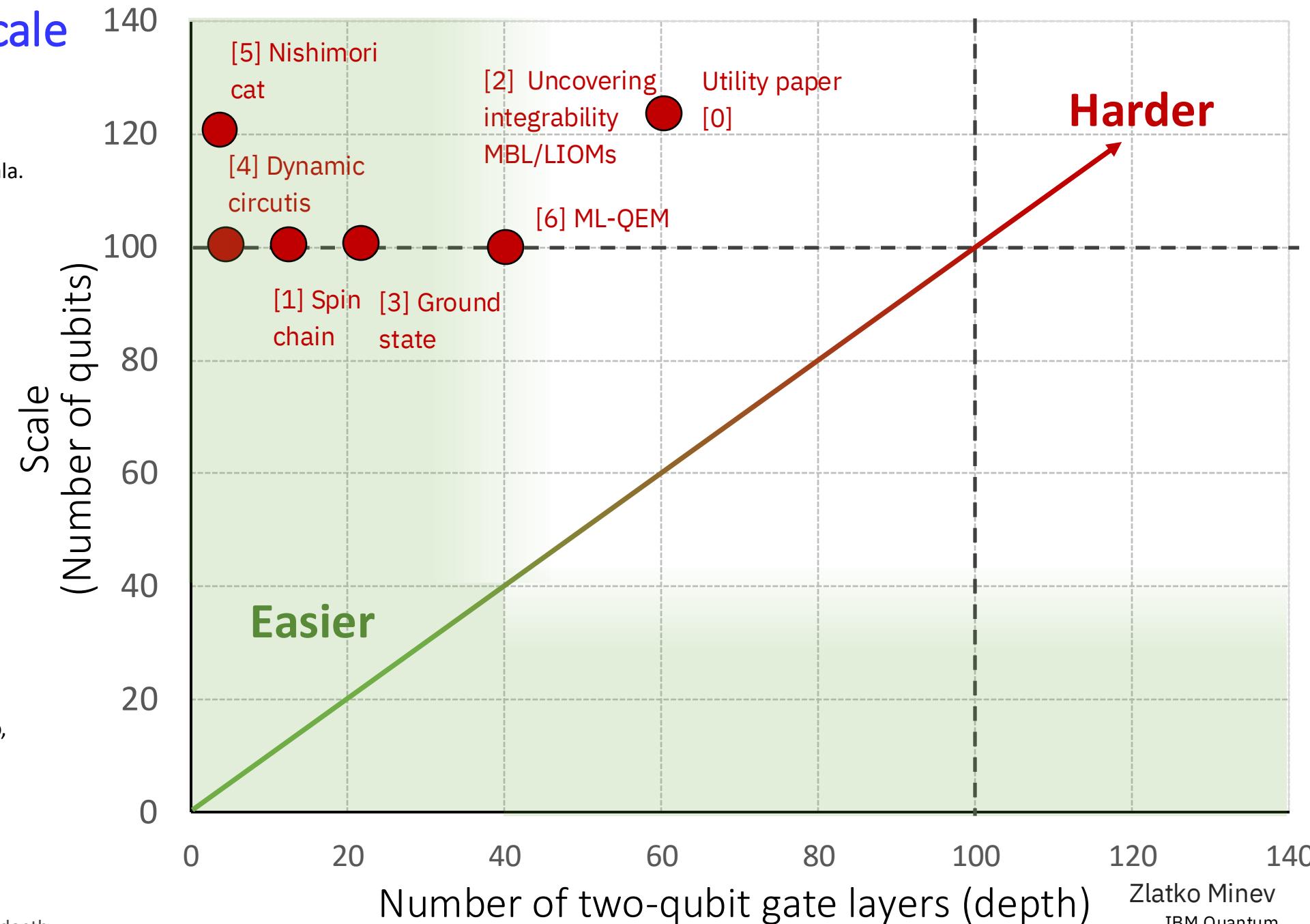


[5] Chen, Zhu, Verresen, Seif,
Bäumer, ... Trebst, Kandala.
arXiv: 2309.02863 (2023)



[6] Liao, Wang, Situdikov, Salcedo,
Seif, Minev.
arXiv: 2308.13065 (2023)

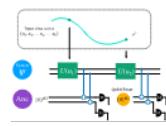
... see next slide



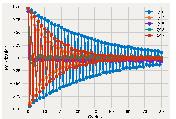
Utility-scale demos: More recent examples



Evidence for the utility of quantum computing before fault tolerance
Nature, 618, 500 (2023)
127 qubits / 2880 CX gates

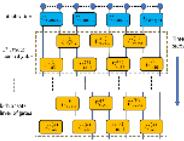


simulation



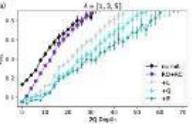
Characterizing quantum processors using discrete time crystals
arXiv:2301.07625
80 qubits / 7900 CX gates

simulation



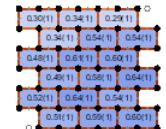
Simulating large-size quantum spin chains on cloud-based superconducting quantum computers
Phys. Rev. Research 5, 013183 (2023)
102 qubits / 3186 CX gates

simulation



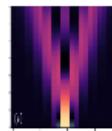
Best practices for quantum error mitigation with digital zero-noise extrapolation
arXiv:2307.05203
104 qubits / 3605 ECR gates

tools



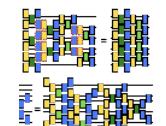
Quantum reservoir computing with repeated Measurements on superconducting devices
arXiv:2310.06706
120 qubits / 49470 ECR gates + meas.

QML



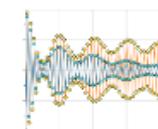
Quantum Simulations of Hadron Dynamics in the Schwinger Model using 112 Qubits
arXiv:2401.08044
112 qubits / 13,858 CZ gates

simulation



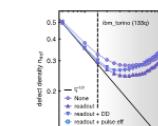
Realizing the Nishimori transition across the error threshold for constant-depth quantum circuits
arXiv:2309.02863
125 qubits / 429 gates + meas.

simulation



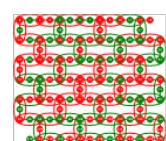
Unveiling clean two-dimensional discrete time quasicrystals on a digital quantum computer
arXiv:2403.16718
133 qubits / 15,000 CZ gates

simulation



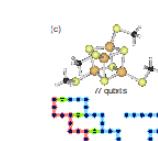
Benchmarking digital quantum simulations and optimization above hundreds of qubits using quantum critical dynamics
arXiv:2404.08053
133 qubits / 1440 CX gates

simulation



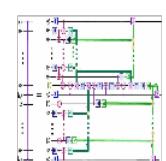
Scalable Circuits for Preparing Ground States on Digital Quantum Computers: The Schwinger Model Vacuum on 100 Qubits
PRX Quantum 5, 020315 (2024)
100 qubits / 788 CX gates

simulation



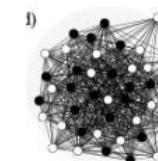
Chemistry Beyond Exact Solutions on a Quantum-Centric Supercomputer
arXiv:2405.05068
77 qubits / 3590 CZ gates

simulation



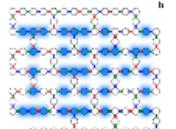
Scaling Whole-Chip QAOA for Higher-Order Ising Spin Glass Models on Heavy-Hex Graphs
arXiv:2312.00997
127 qubits / 420 CX gates

optimization



Towards a universal QAOA protocol: Evidence of quantum advantage in solving combinatorial optimization problems
arXiv:2405.09169
109 qubits / 21,200 ECR gates

optimization

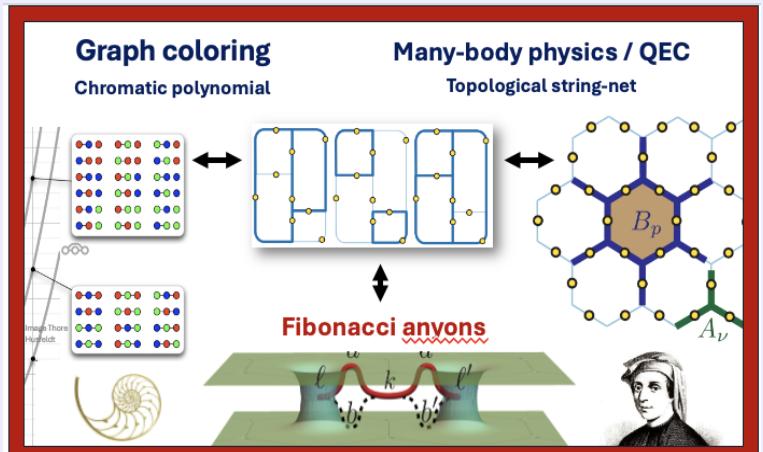


Uncovering Local Integrability in Quantum Many-Body Dynamics
arXiv:2307.07552
124 qubits / 2641 CX gates

simulation

Some related utility-scale & advantage experiments

Towards classically-hard hard problems and universal topological quantum computation through Fibonacci string-net condensate



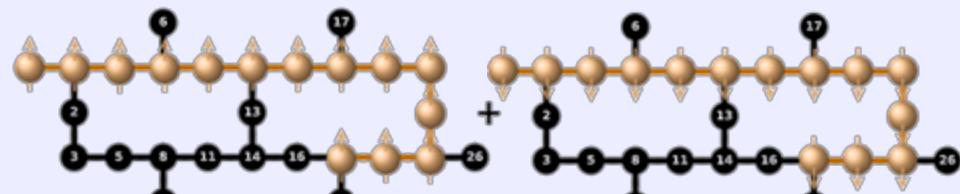
string-net
condensate

arXiv:2406.12820

Z. Minev, K. Najafi,
S. Majumder, J. Wang,
A. Stern, Eun-Ah Kim,
C.-M. Jian, G. Zhu



Efficient Long-Range Entanglement using Dynamic Circuits

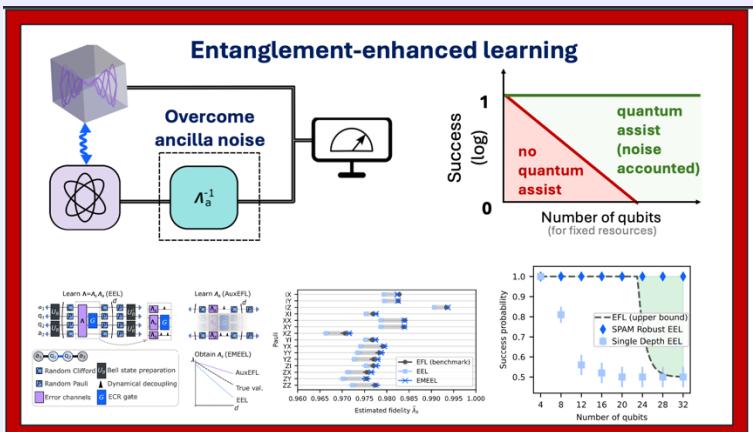


Gate teleportation over 100+ qubits

PRX Quantum 5, 030339

Bäumer, Tripathi, Wang, Rall, Chen, Majumder, Seif, Minev

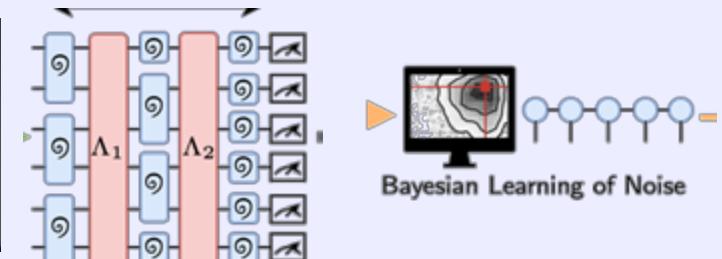
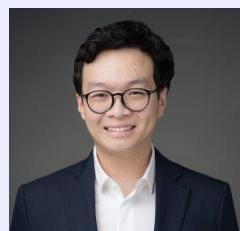
Noise-Robust Quantum Learning Advantage at Scale



arXiv:2408.03376

A. Seif, S. Chen, S. Majumder,
H. Liao, D. Wang,
M. Malekakhlagh, A. Javadi-
Abhari, L. Jiang, Z. Minev

Demonstration of Robust and Efficient Quantum Property Learning with Shallow Shadows



arXiv:2402.17911 (2024)

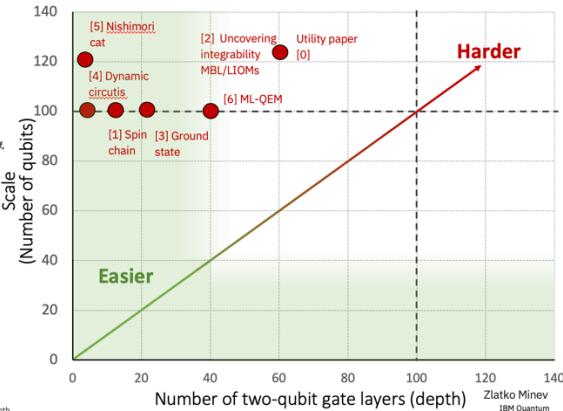
Hu, Gu, Majumder, Ren, Zhang, Wang, Minev, You, Seif, Yelin

These utility-scale results enabled by quantum error mitigation

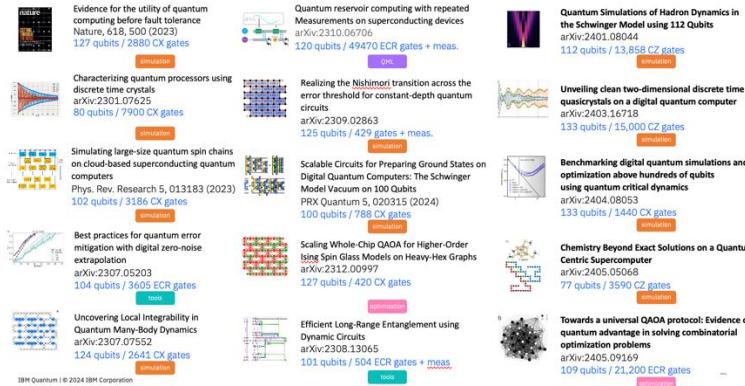
Some early utility-scale experiments



On superconducting qubit platforms
Signal stops or decays more than 50% beyond this depth

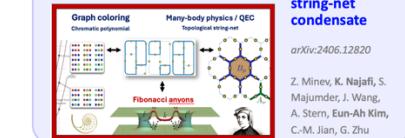


Utility-scale demos: More recent examples

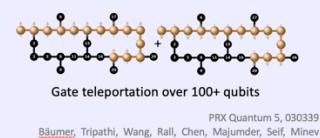


Related utility-scale and quantum advantage work

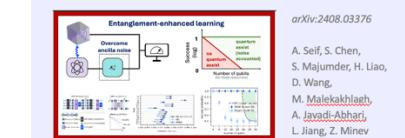
Towards classically-hard hard problems and universal topological quantum computation through Fibonacci string-net condensate



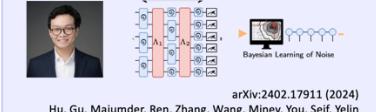
Efficient Long-Range Entanglement using Dynamic Circuits



Noise-Robust Quantum Learning Advantage at Scale



Demonstration of Robust and Efficient Quantum Property Learning with Shallow Shadows

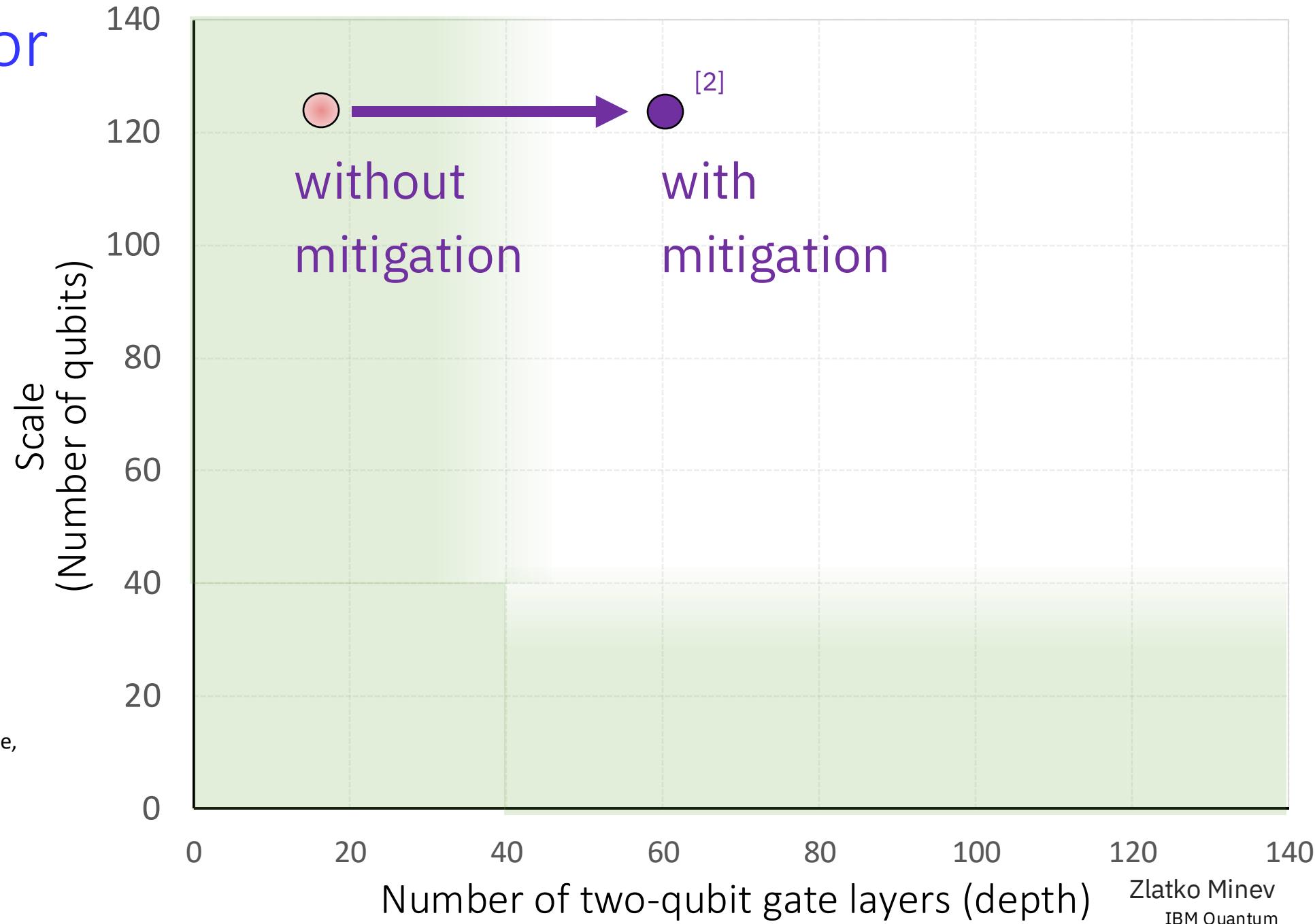


Quantum Error Mitigation

Quantum error mitigation: example

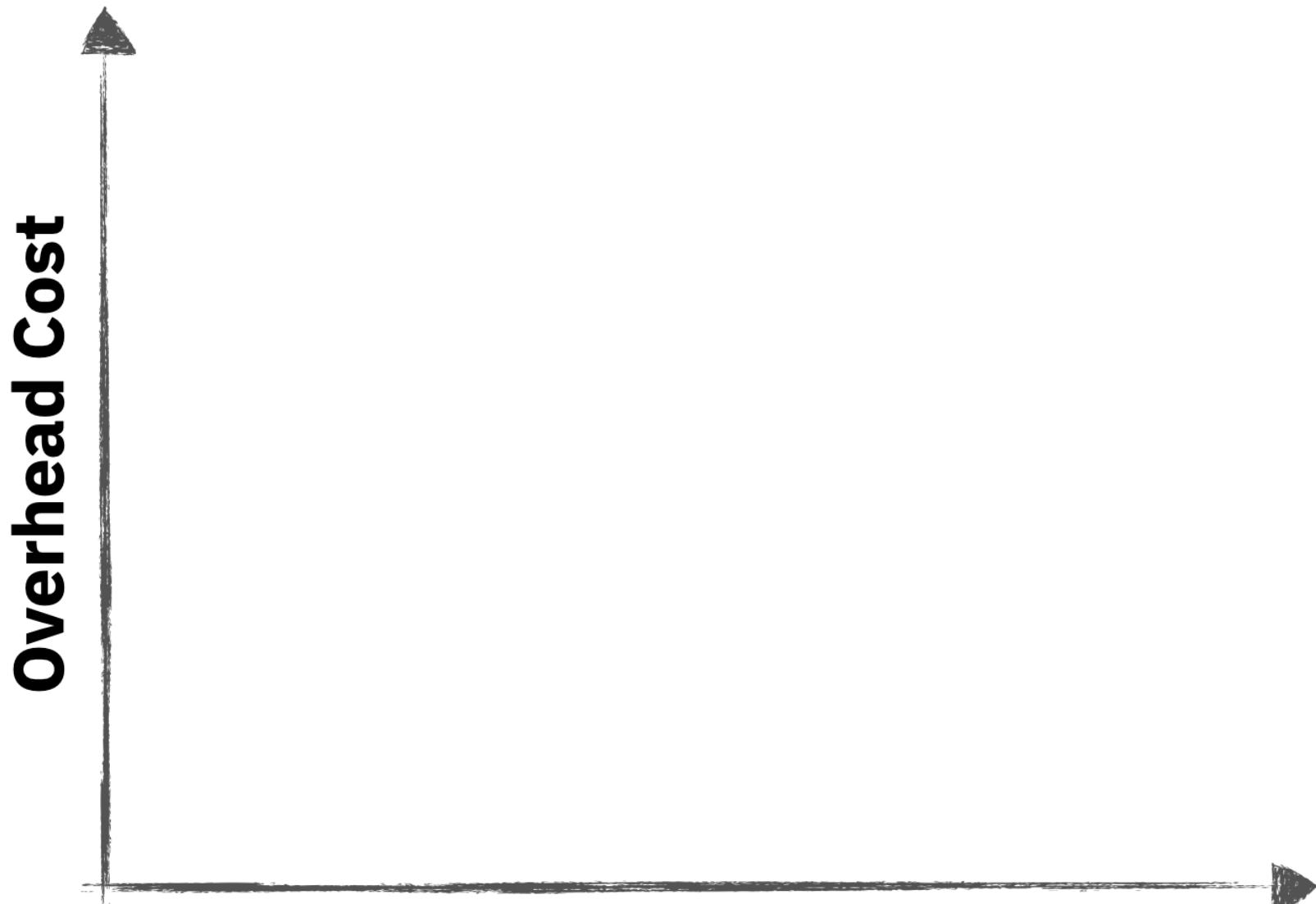


[2] Shtanko, Wang, Zhang, Harle,
Seif, Movassagh, Minev.
arXiv: 2307.07552 (2023)

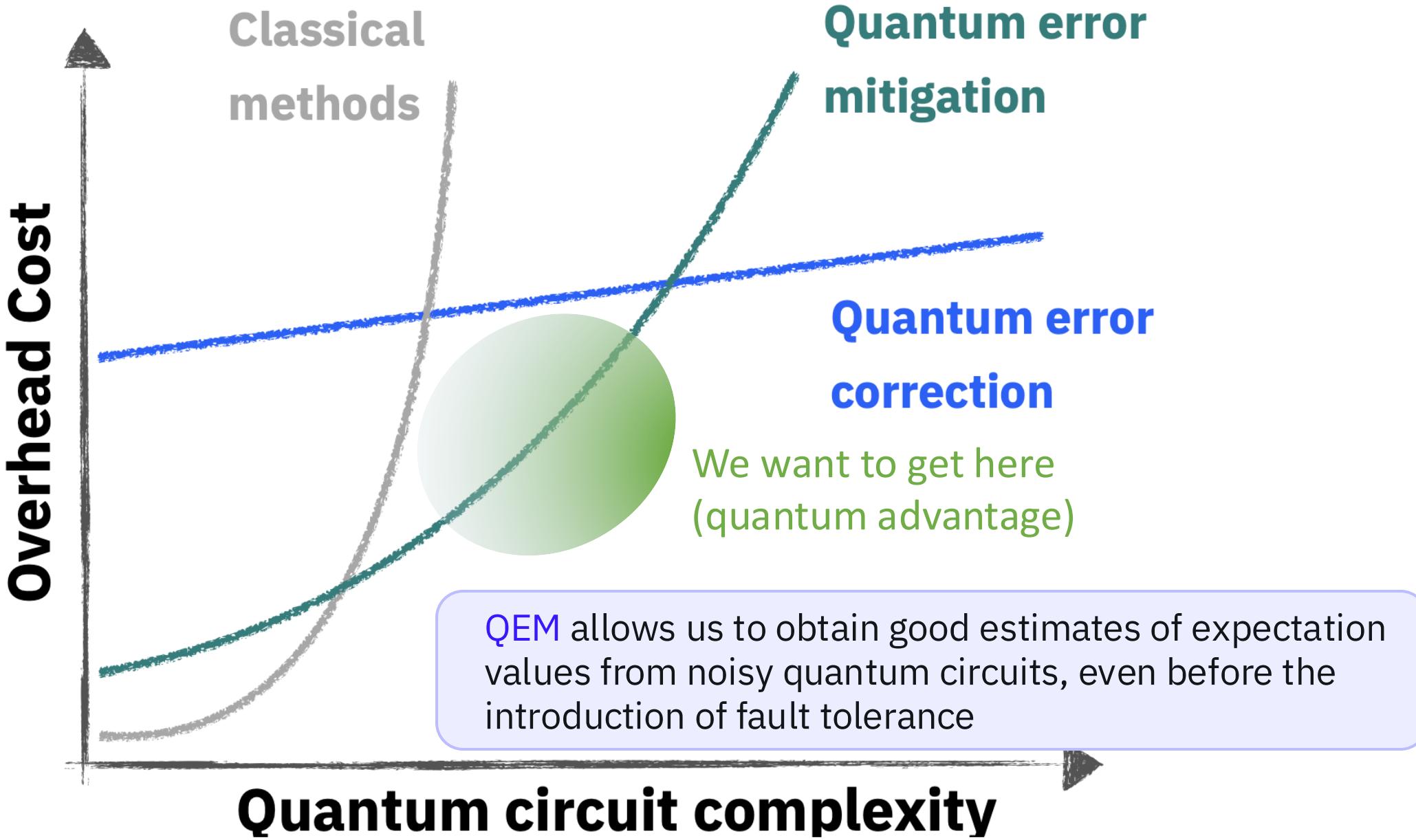


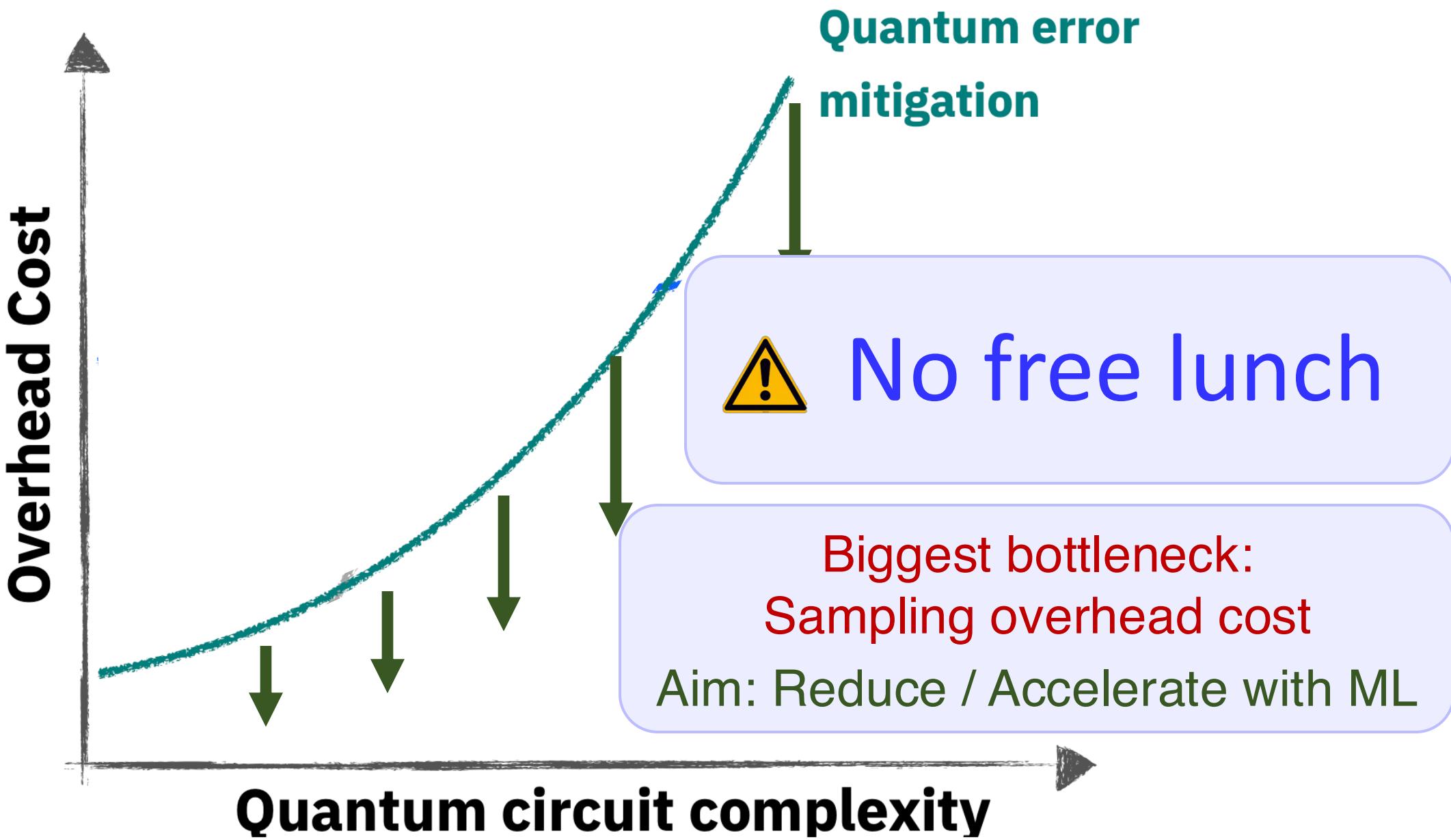
Number of two-qubit gate layers (depth)

Zlatko Minev
IBM Quantum

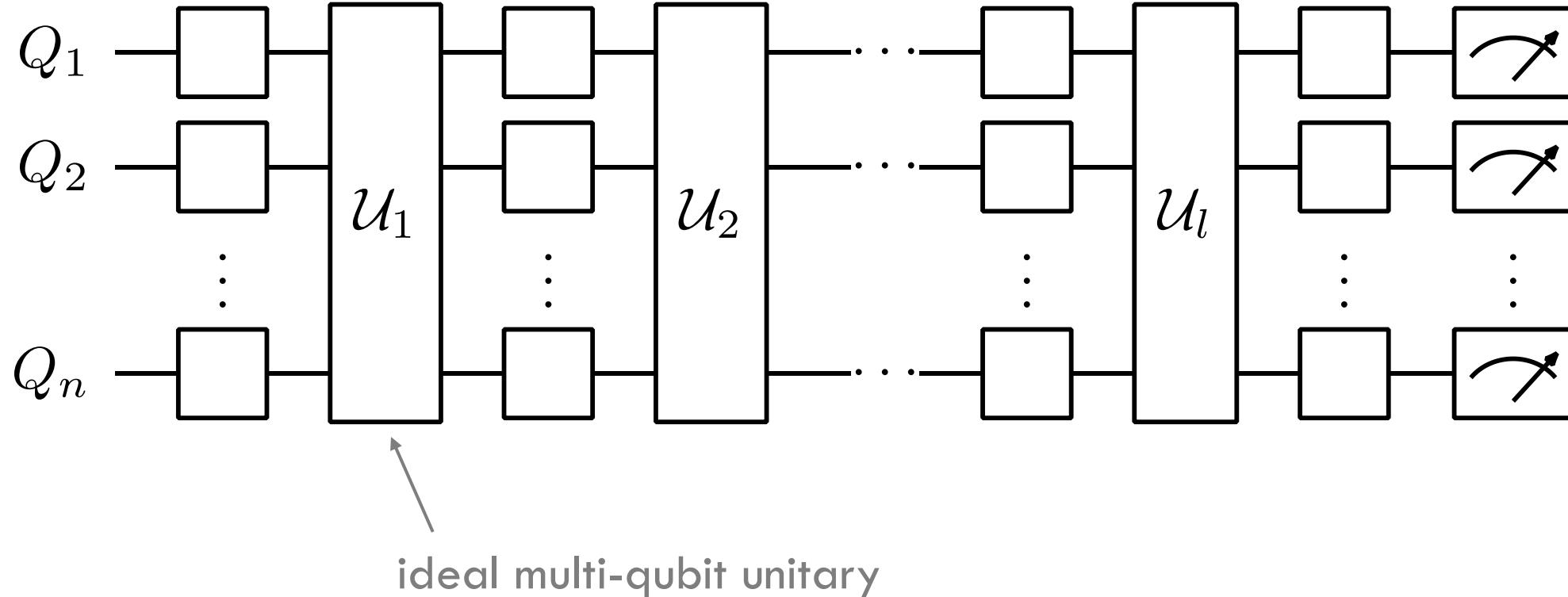


Quantum advantage: Quantum computation that delivers a significant, practical benefit beyond either brute force or approximate classical computing methods, calculating solutions in a way that is cheaper, faster or more accurate than all known classical alternatives.”
ibm.com/quantum/blog/gammabar-for-quantum-advantage





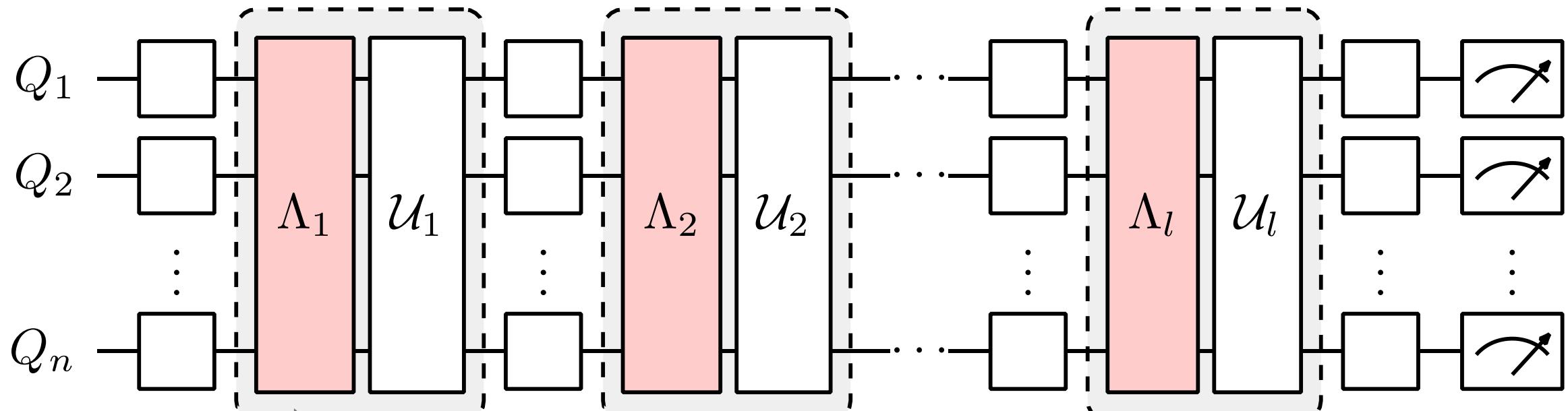
Ideal (noise-free) quantum circuit



A circuit can be decomposed into a layer construction

Example: Trotterization of Ising model simulation

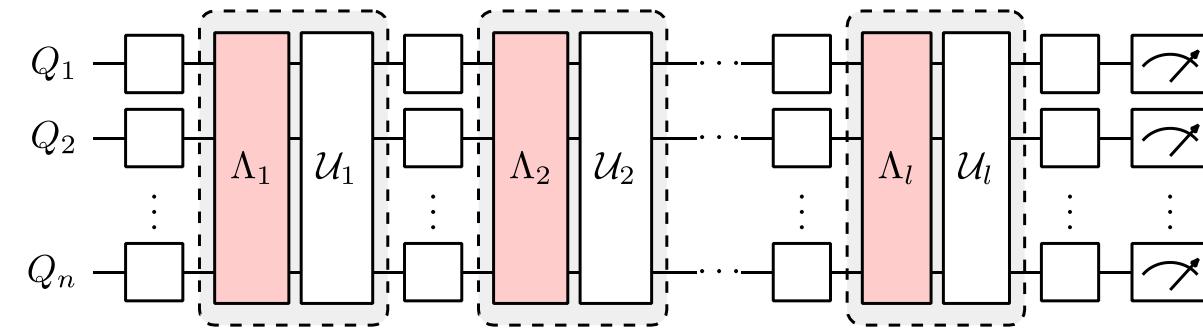
Real (noisy) quantum circuit



multi-qubit noise channel
inseparable from gate

completely positive and trace preserving (CPTP)
representable by a $4^n \times 4^n$ matrix

Error mitigation: Wish list



1. Mitigate *all* observables of interest

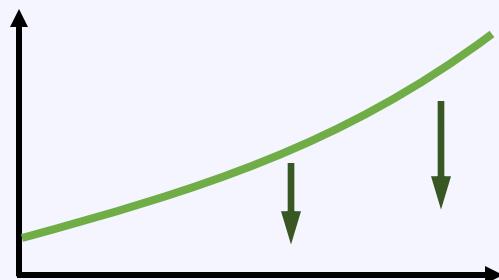
$$\{\langle \hat{O}_1 \rangle, \langle \hat{O}_2 \rangle, \dots\}$$

$\langle \hat{O}_i \rangle_{\text{ideal}}$ $\langle \hat{O}_i \rangle_{\text{mitigated}}$ $\langle \hat{O}_i \rangle_{\text{noisy}}$



2. Precision with high probability

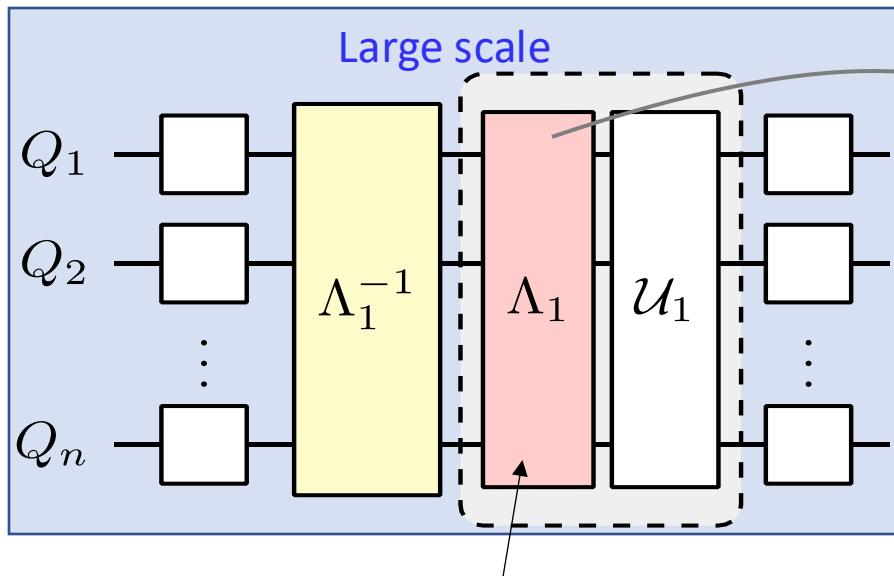
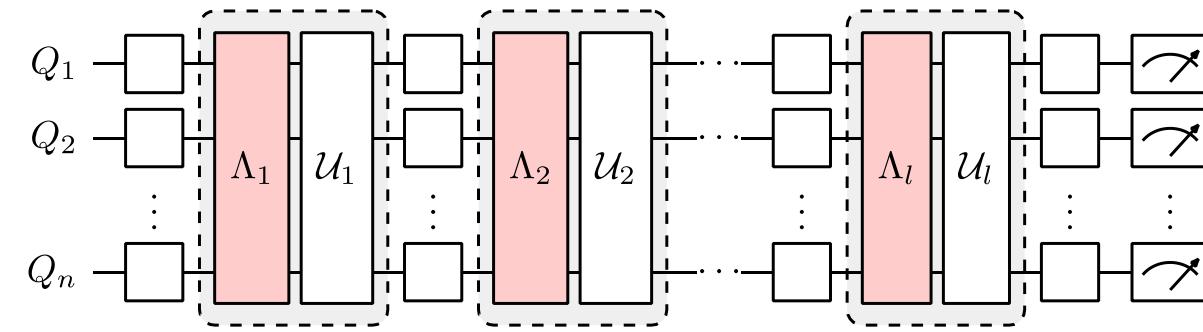
$$\Pr \left[\left| \langle \hat{O}_i \rangle_{\text{ideal}} - \langle \hat{O}_i \rangle_{\text{mitigated}} \right| \geq \epsilon \right] = \delta$$



3. Minimize mitigation sampling overhead

$$\min N_{\text{mitigation}} / N_{\text{ideal}}$$

Error mitigation: Challenges



noise in full device

- cross-talk (quantum and classical), ...
- correlated errors, context-dependence, ...
- leakage, time instability, ...

1. Beyond classical circuits

Paradoxical: How can classical ML learn handle these?

2. Quantum noise is exponentially complex

Quantum noise is exponentially complex and even simple noise mixed by complex unitary yields complex noise.

A. exp params

B. noise param values

C. additive error sampling cost ($>10^2 - 10^{10}$)

10^{60} params for 50Q

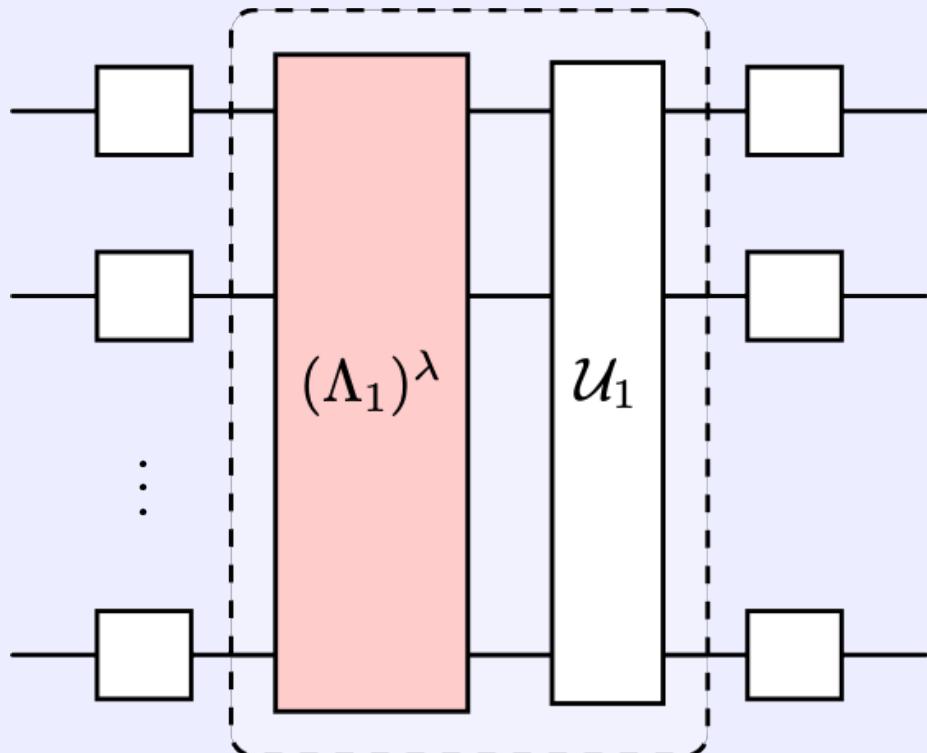
$10^{-2} - 10^{-5}$

3. Runtime cost

Number of circuits, construction and execution speed of circuits, platform speed, monetary expense, ...

Two state-of-the-art physics-based QEM methods

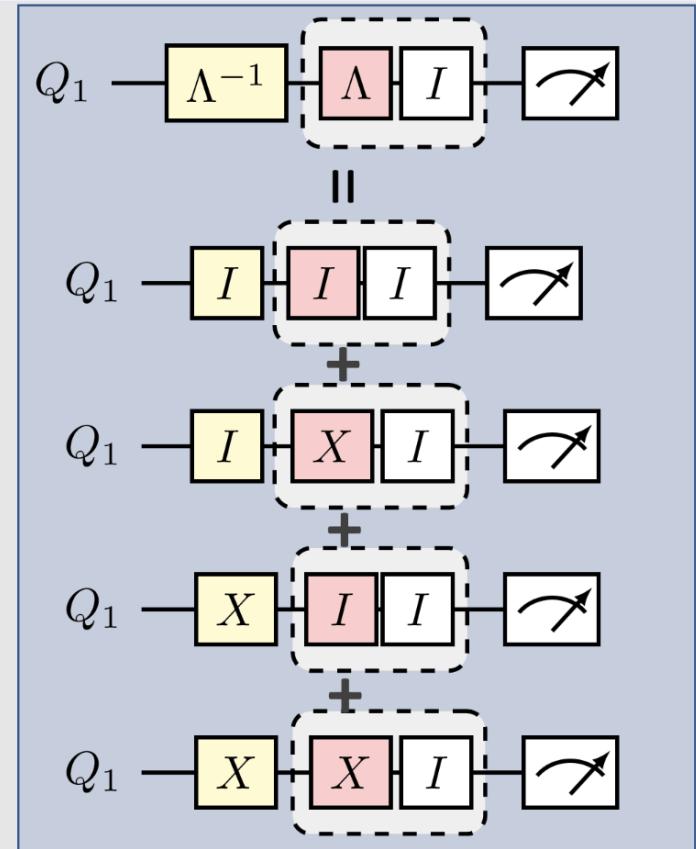
Zero-noise extrapolation (ZNE)



K. Temme, S. Bravyi, and J. M. Gambetta. PRL (2017)
Li and Benjamin PRX (2017)
Note: PEA = ZNE + PEC combination

Probabilistic error cancellation (PEC)

No error	probability $(1-q)(1-p)$
ERROR!	$(1-q)p$
ERROR!	$q(1-p)$
Error CANCELED!	qp



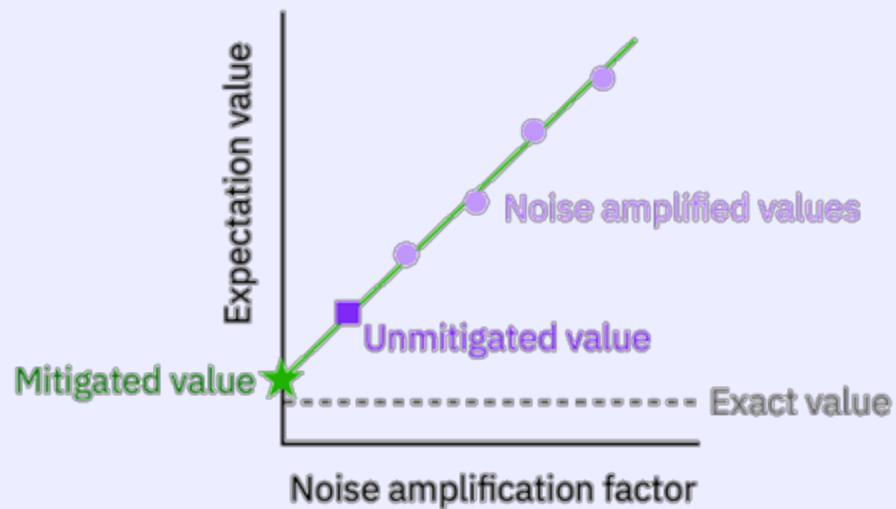
K. Temme, S. Bravyi, and J. M. Gambetta. PRL (2017)
E. Berg, Z. K. Minev, A. Kandala, and K. Temme. Nat. Phys. (2023)
Graphic: PEC tutorial zlatko-minev.com/blog/pec-talk

Physics-Based Methods

Zero-noise extrapolation (ZNE)

Pros: Relatively low overhead, no training, more straightforward to implement

Cons: Expectation values not bias-free in general

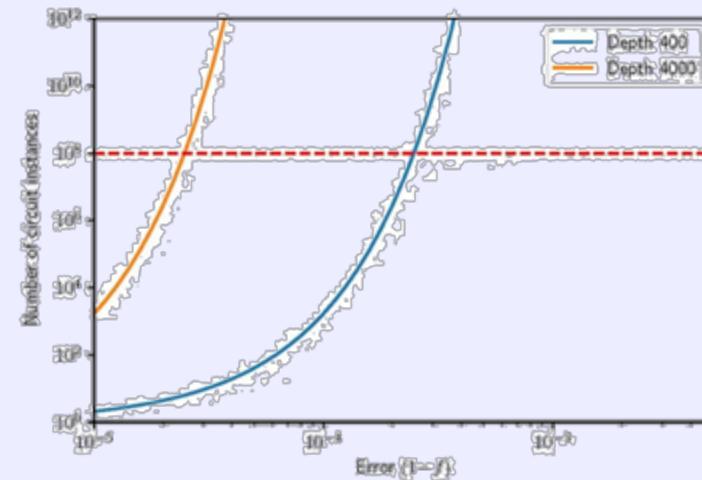


K. Temme, S. Bravyi, and J. M. Gambetta. Phys. Rev. Lett. 119, 180509 (2017)
Li and Benjamin PRX (2017)

Probabilistic error cancellation (PEC)

Pros: Unbiased expectation values

Cons: Fast and exponentially growing sampling overhead with noise. Restricted to layered circuits.



K. Temme, S. Bravyi, and J. M. Gambetta. Phys. Rev. Lett. 119, 180509 (2017)
E. Berg, Z. K. Minev, A. Kandala, and K. Temme. Nat. Phys. (2023)
Graphic: PEC tutorial zlatko-minev.com/blog/pec-talk

ML-QEM

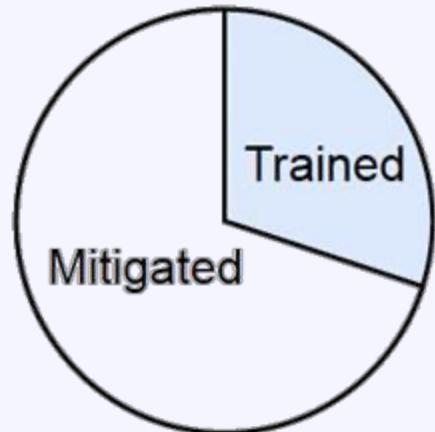
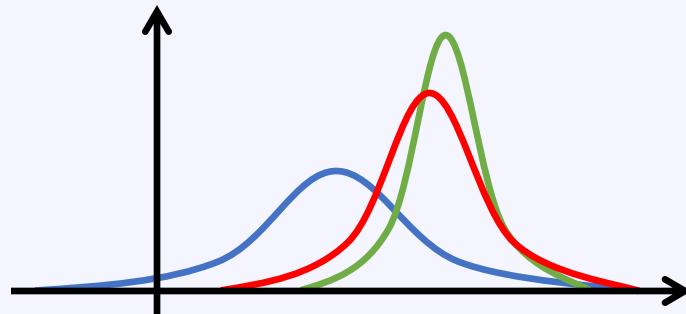
Machine-learning quantum error mitigation

Machine learning accelerates error mitigation

ML-QEM reduces the cost of quantum error mitigation without sacrificing accuracy.

Pros: Arguably lowest runtime overhead, applies to multiple and generic expectation value, accelerates essentially any existing physics-based method ...

Cons: Could have biased expectation values, requires circuit-class specific training



Practical utility metrics

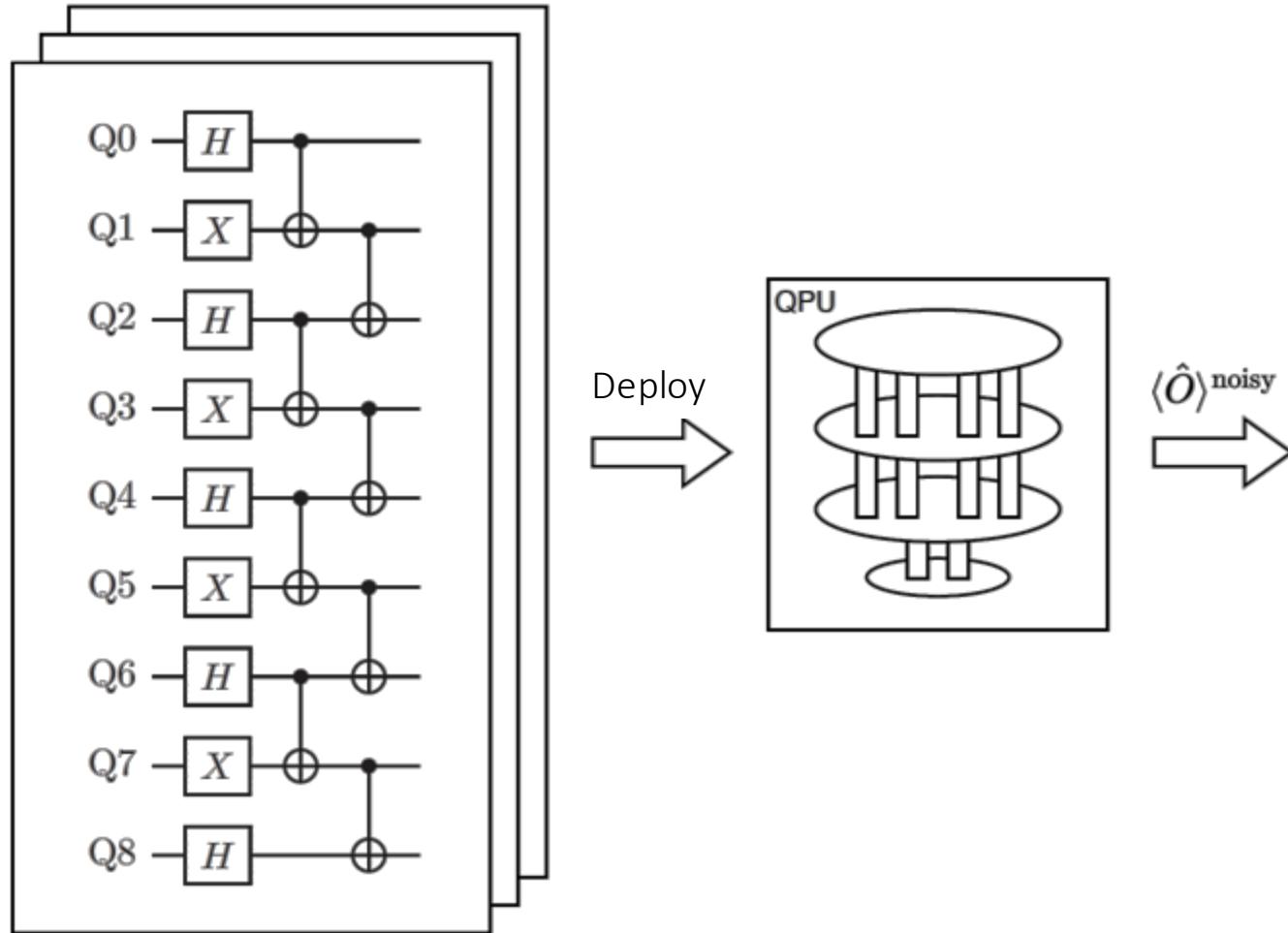
- Performance / precision
- Cost / efficiency
- Scalability
- Applicability

Disclaimer: No DeepSeek, ChatGPT, or Transformer moment here.

First proof of concept with very simple ideas.

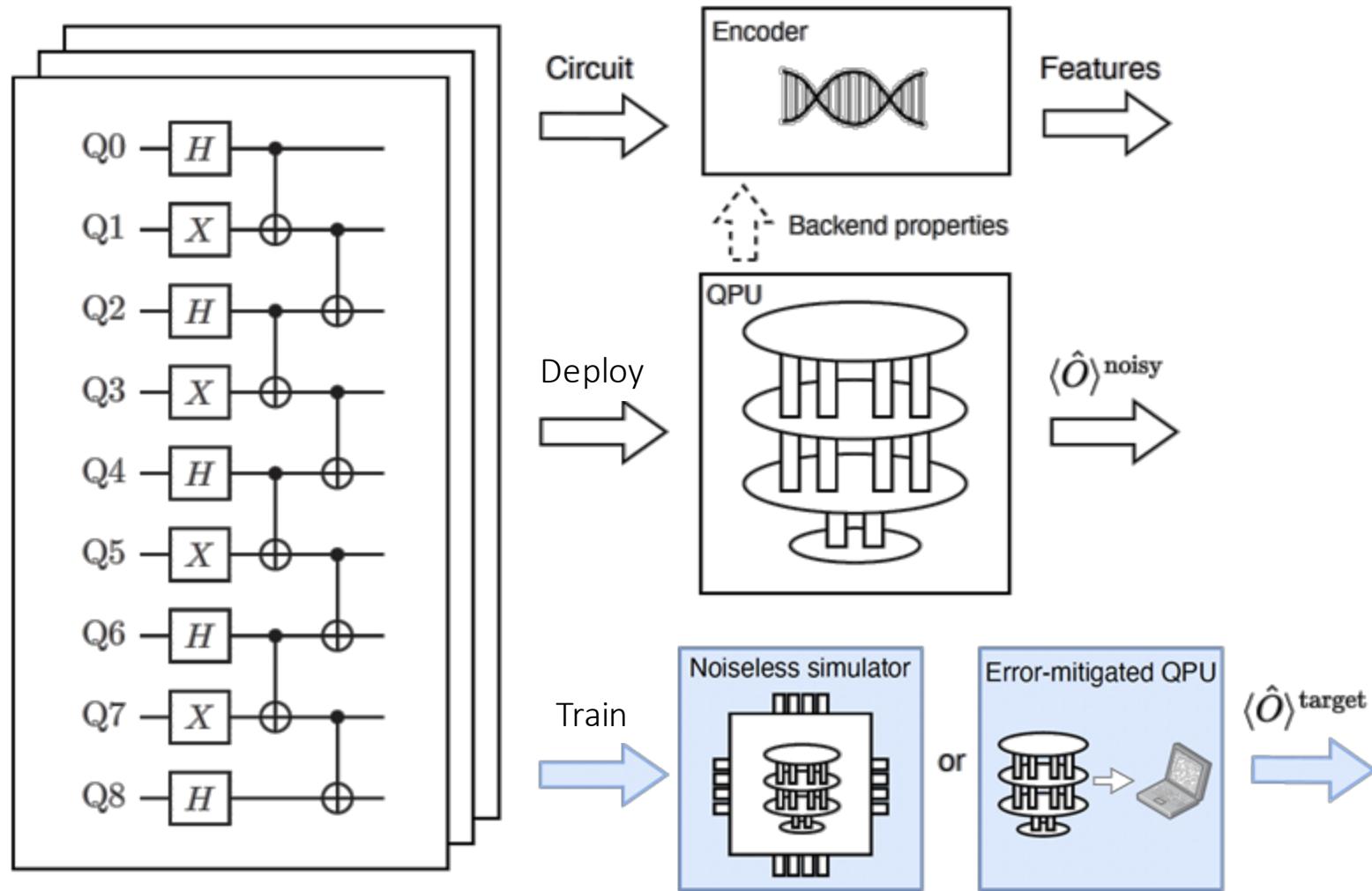
Not be confused with the step of “learning device noise” in quasi-probability-based QEM approaches, e.g., PEC or probabilistic error amplification (PEA)**.

Normal execution of quantum circuit

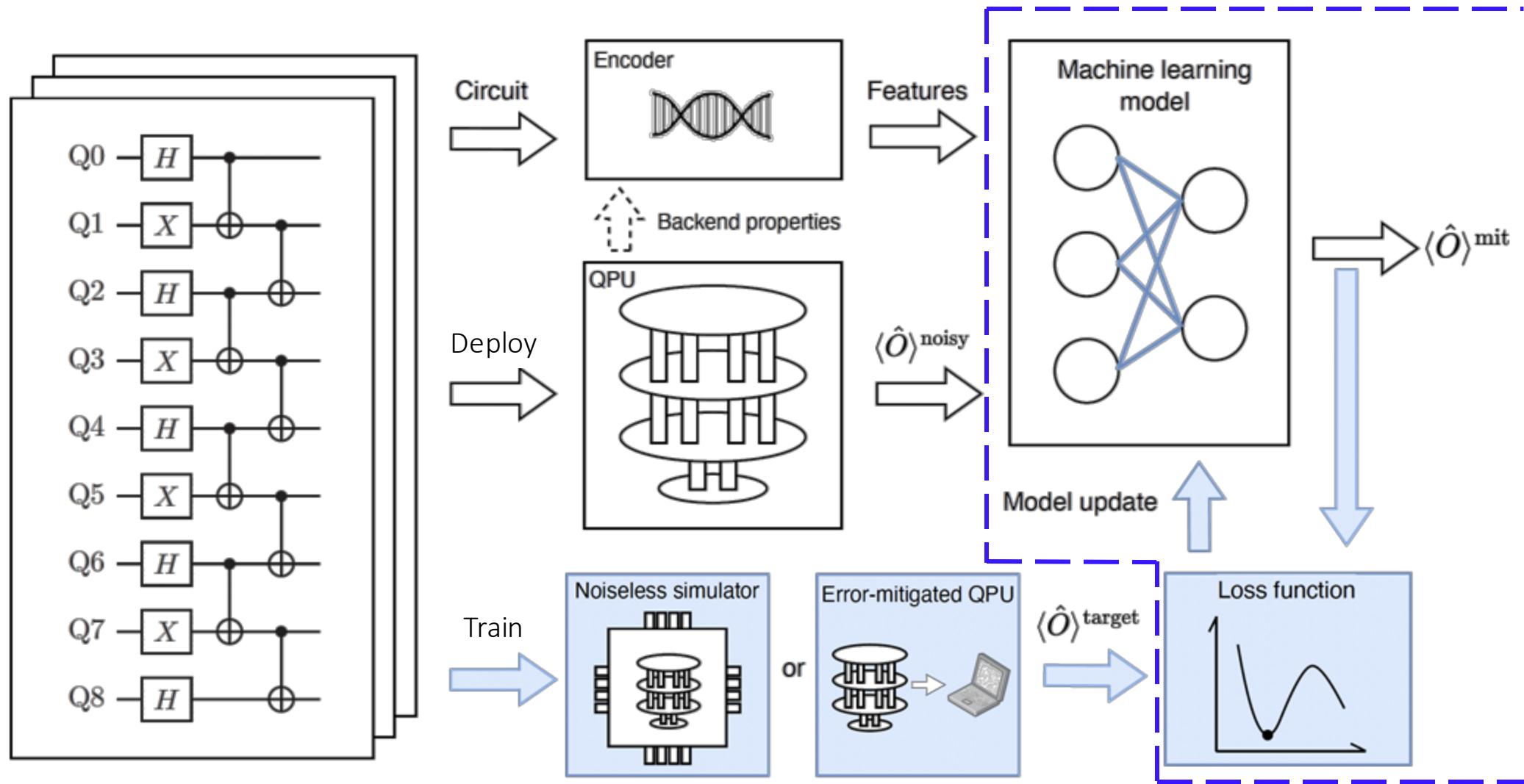


Workflow of ML-QEM

1. Generate training data

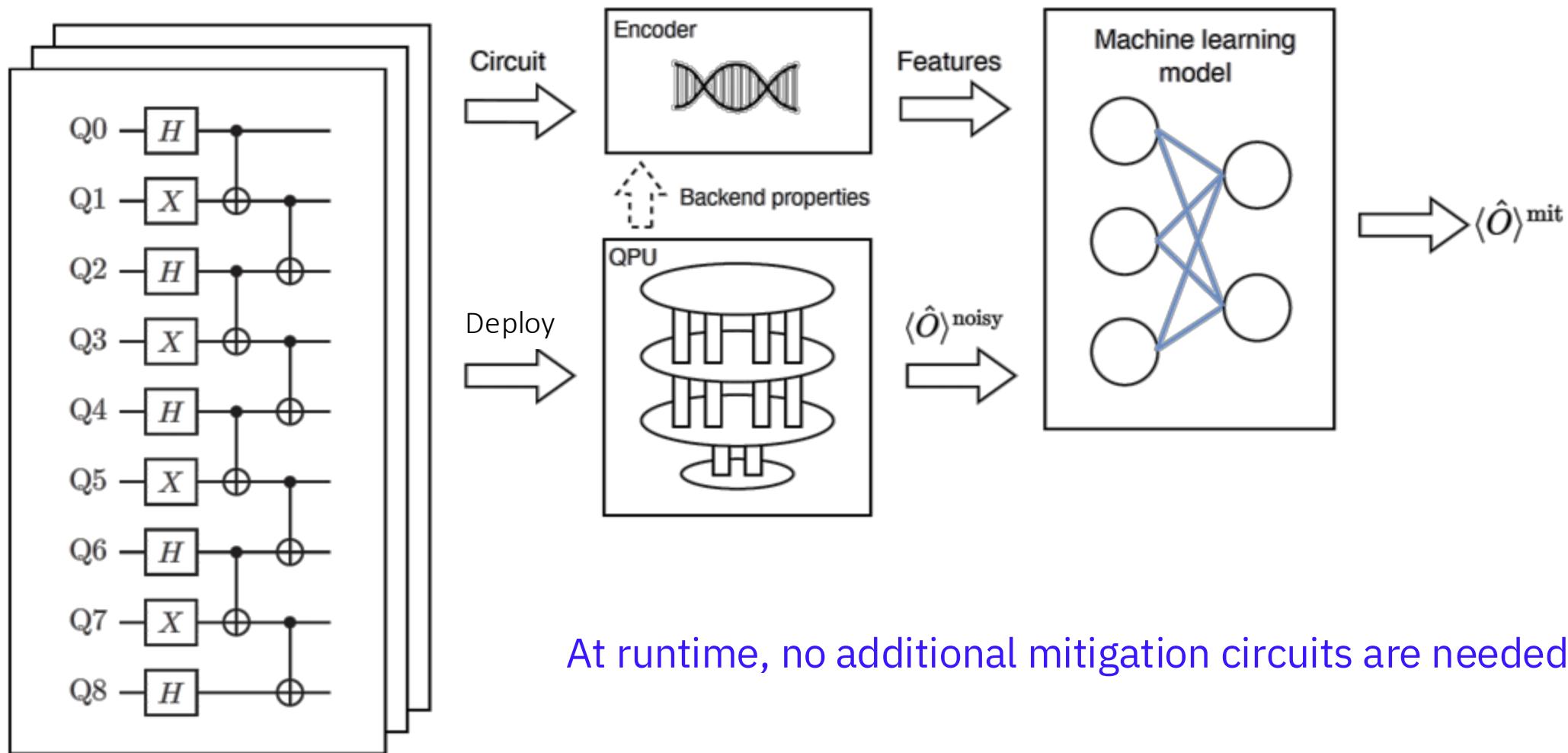


Workflow of ML-QEM: Train



Workflow of ML-QEM: Deploy

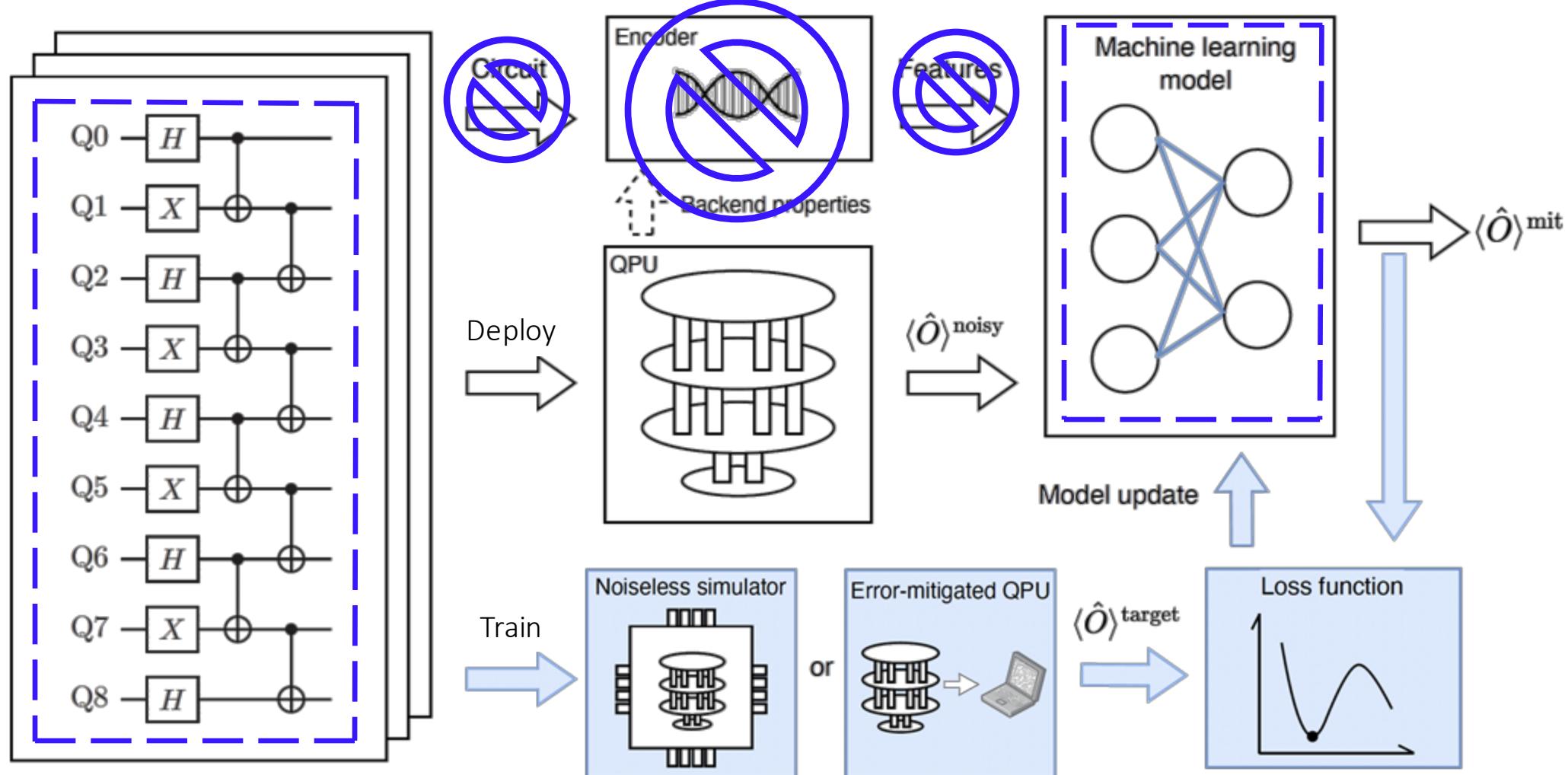
3. Mitigate noisy expectation values at runtime



Relation to Clifford data regression (CDR)

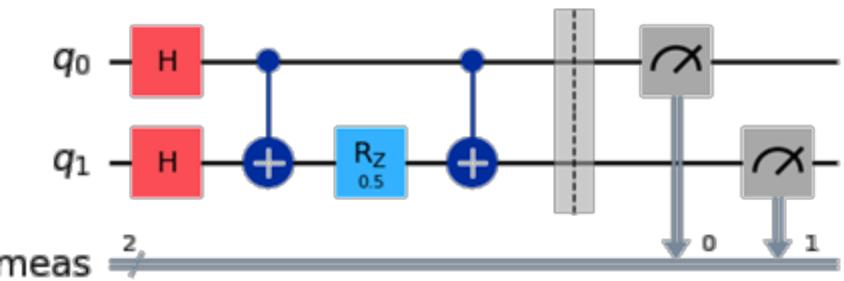
Clifford data regression (CDR)* generates near-Clifford circuits constructed for only a single-expectation value for training

CDR uses only linear regression for mitigation

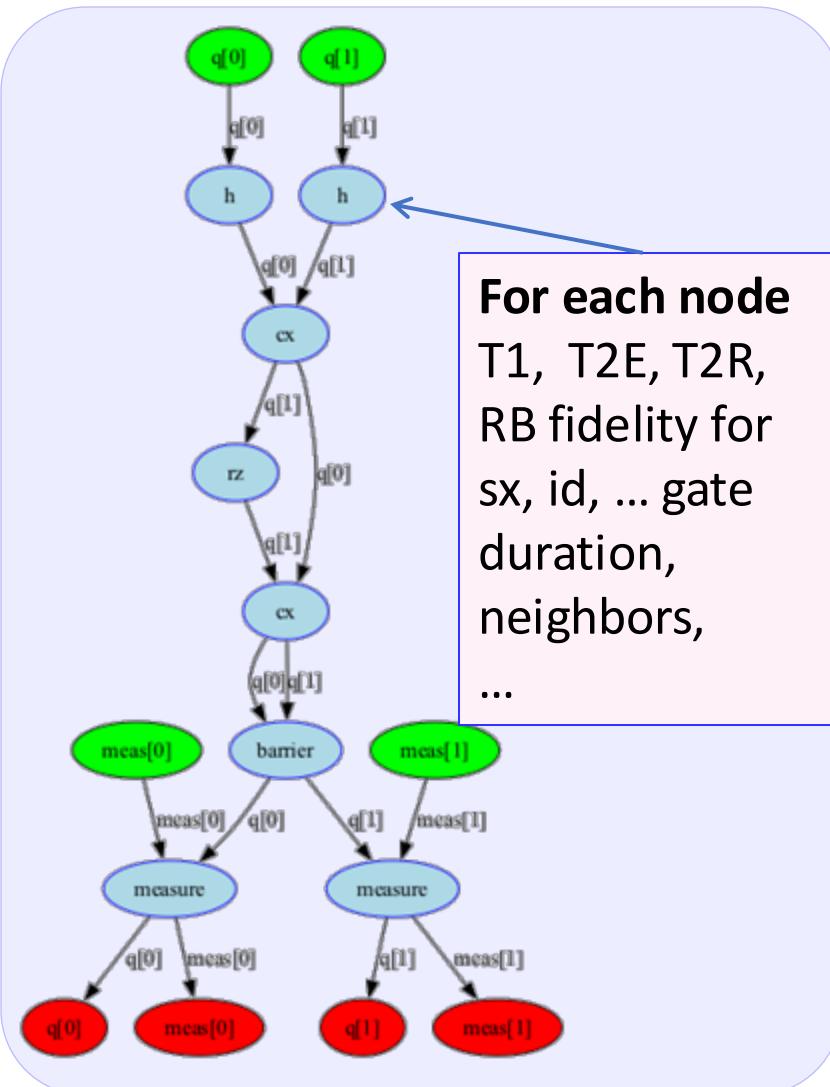


Encodings

Quantum circuit



Quantum circuit as a
directed acyclic graph (DAG)



Feature vector

Circuit properties

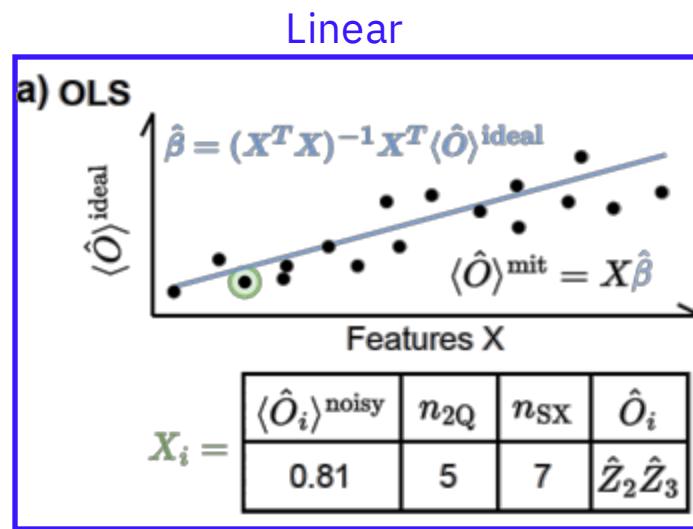
number of qubits
number of cx gates
number of sx gates
number of id gates
number of rx gates
histogram of rotation angles
measurement basis
...

Device properties

T1 times
T2 times
readout error for each qubit
...

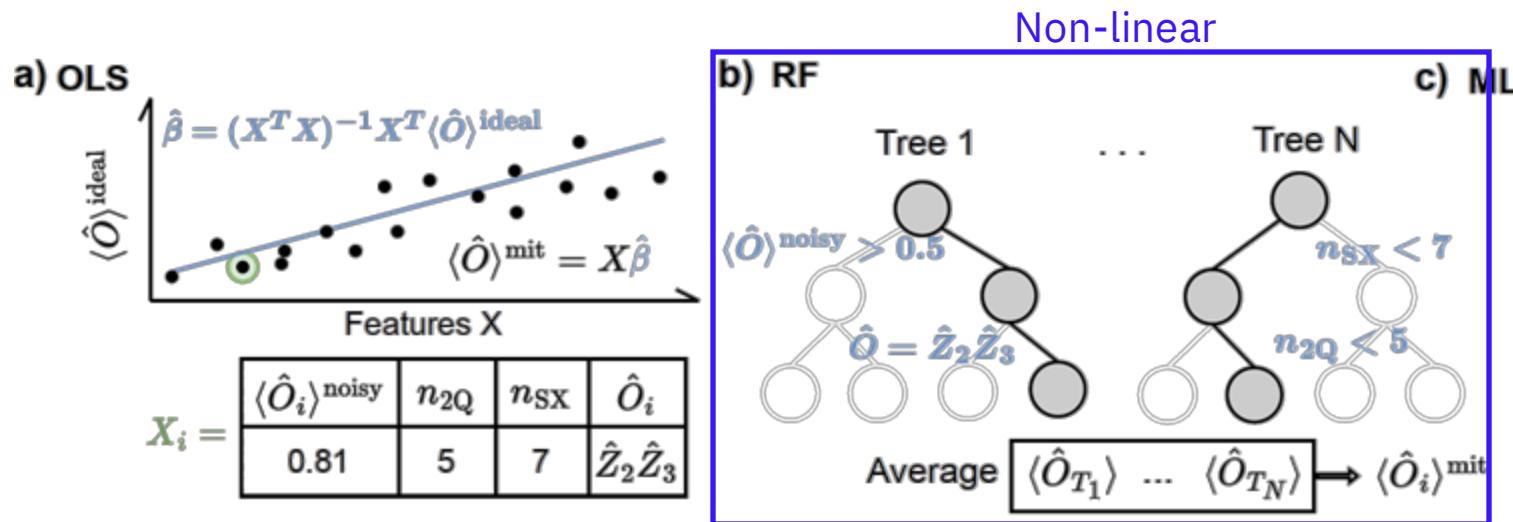
Benchmark performance of variety of ML models

a) Ordinary least square (OLS)



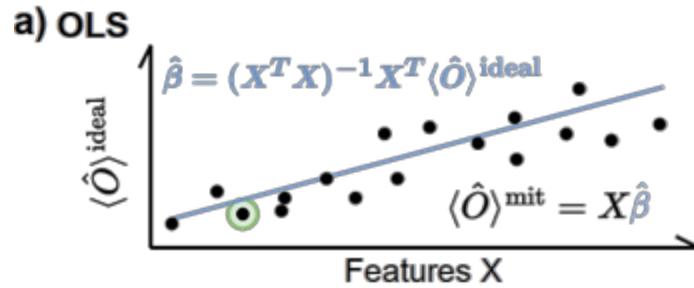
Benchmark performance of variety of ML models

- a) Ordinary least square (OLS)
- b) Random forest regression (RF)
[new]

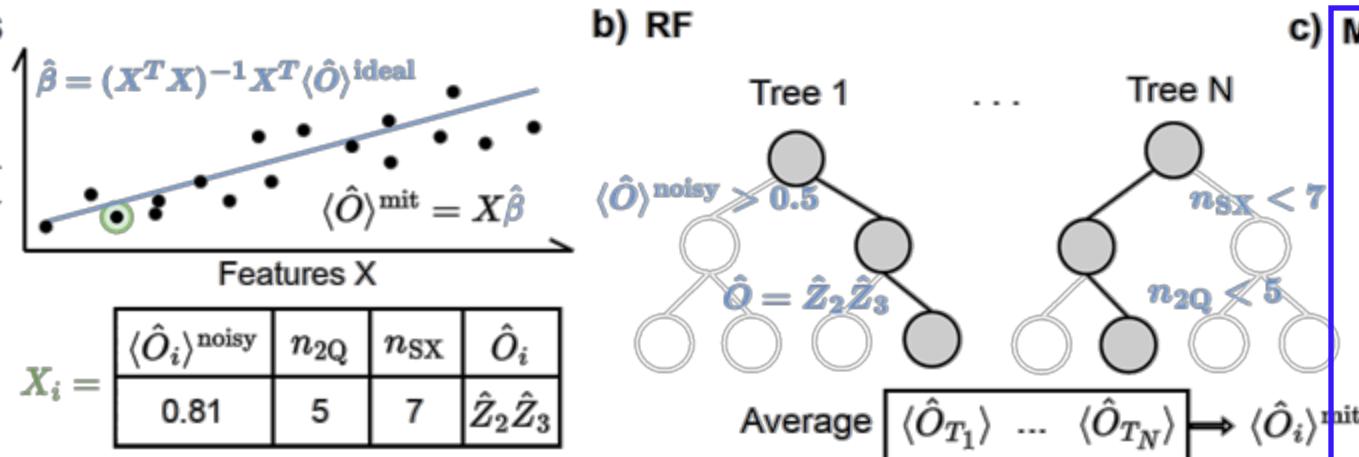


Benchmark performance of variety of ML models

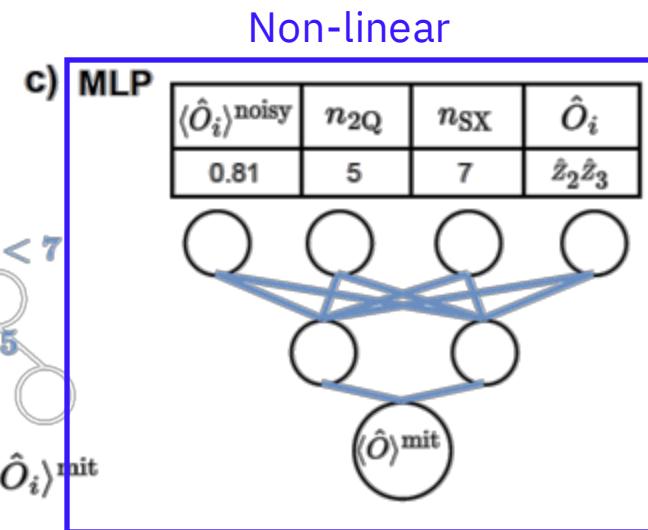
a) Ordinary least square (OLS)



b) Random forest regression (RF)

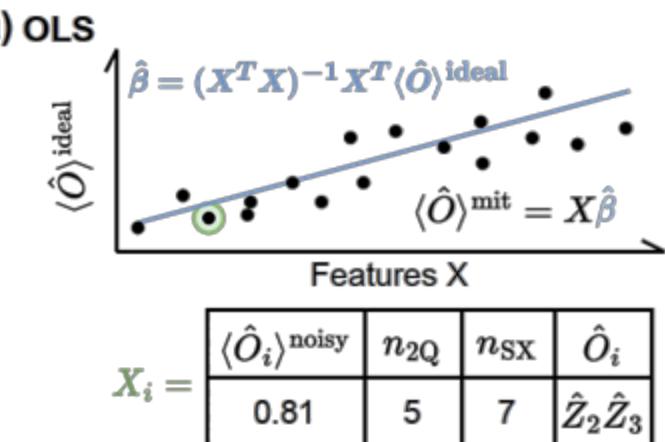


c) Multi-layer perceptron (MLP)

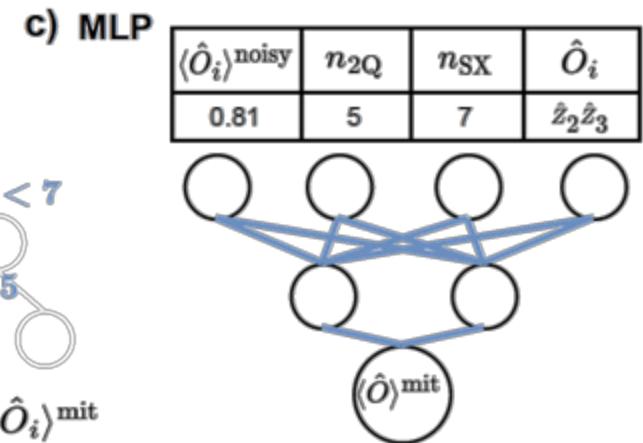
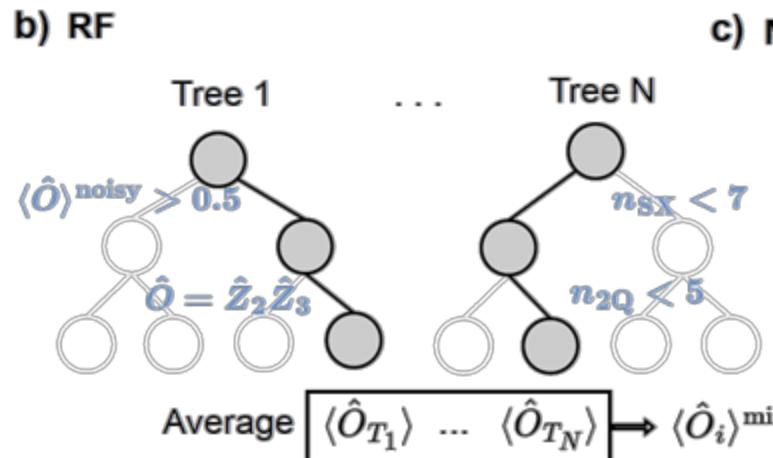


Benchmark performance of variety of ML models

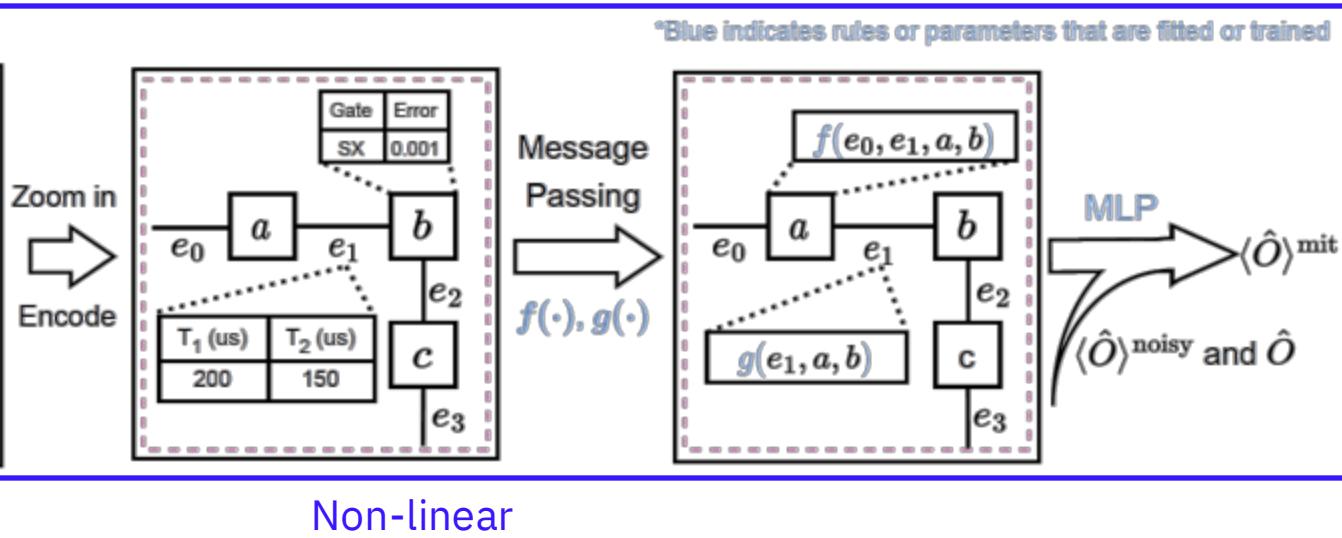
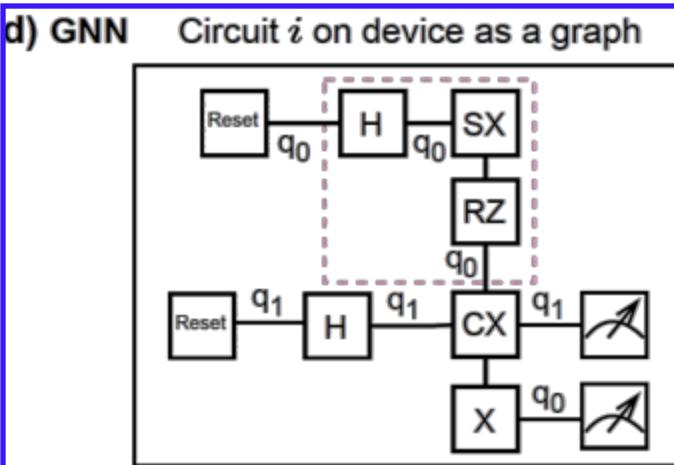
a) Ordinary least square (OLS)



b) Random forest regression (RF)
[new]

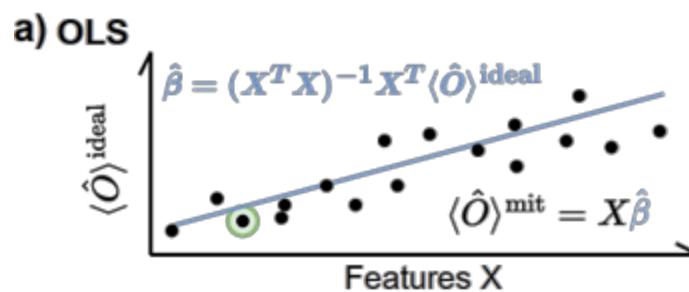


c) Multi-layer perceptron (MLP)

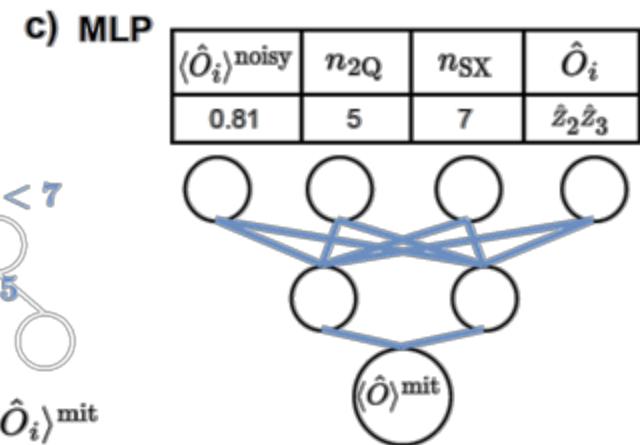
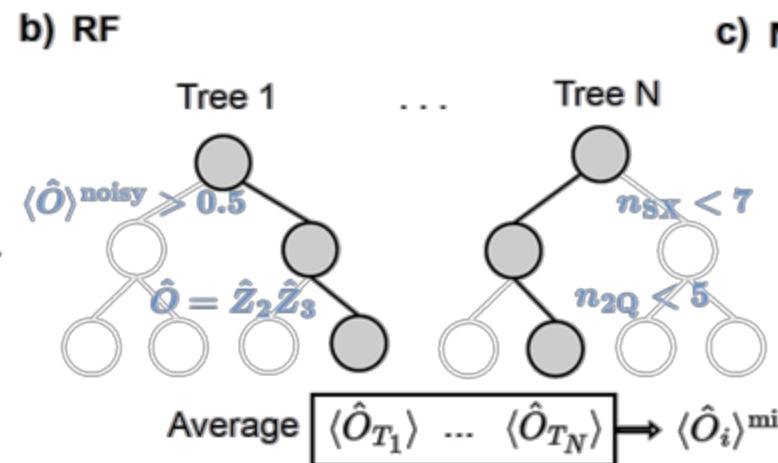


Benchmark performance of variety of ML models

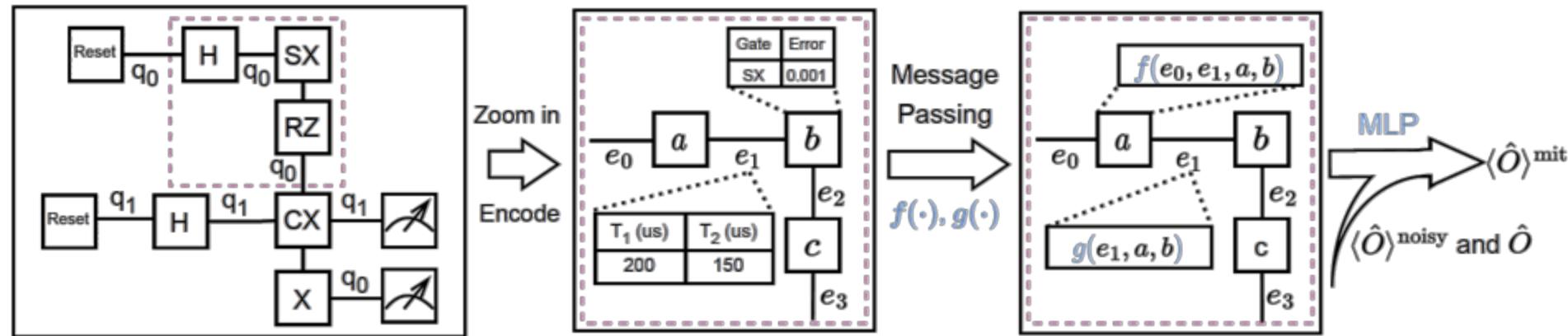
- a) Ordinary least square (OLS)
- b) Random forest regression (RF)
[new]
- c) Multi-layer perceptron (MLP)
- d) Graph neural network (GNN)
[new]



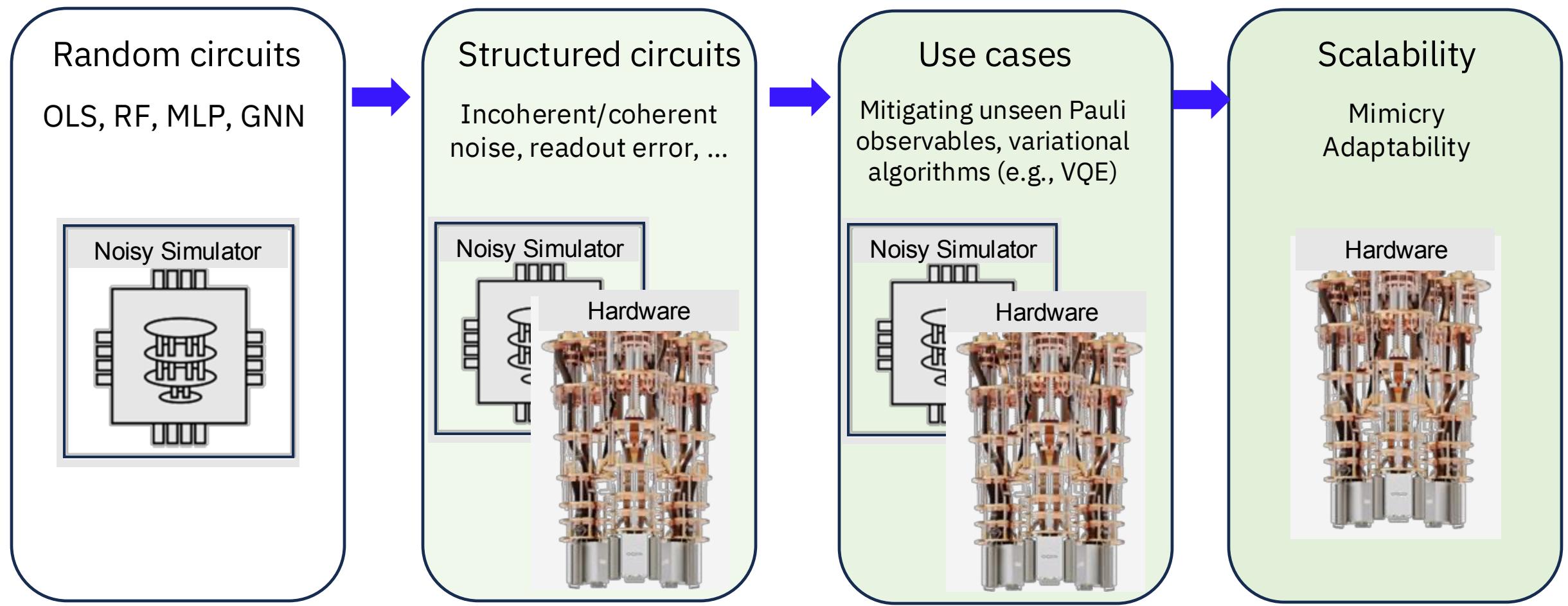
$$X_i = \begin{array}{|c|c|c|c|}\hline & \langle \hat{O}_i \rangle^{\text{noisy}} & n_{2Q} & n_{\text{SX}} & \hat{O}_i \\ \hline & 0.81 & 5 & 7 & \hat{Z}_2 \hat{Z}_3 \\ \hline \end{array}$$



d) GNN Circuit i on device as a graph



Progression

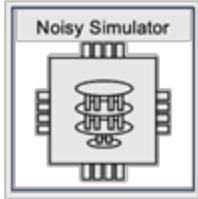


4 qubits
Classical sims available

100+ qubits
Classical sims not available

Testing the waters

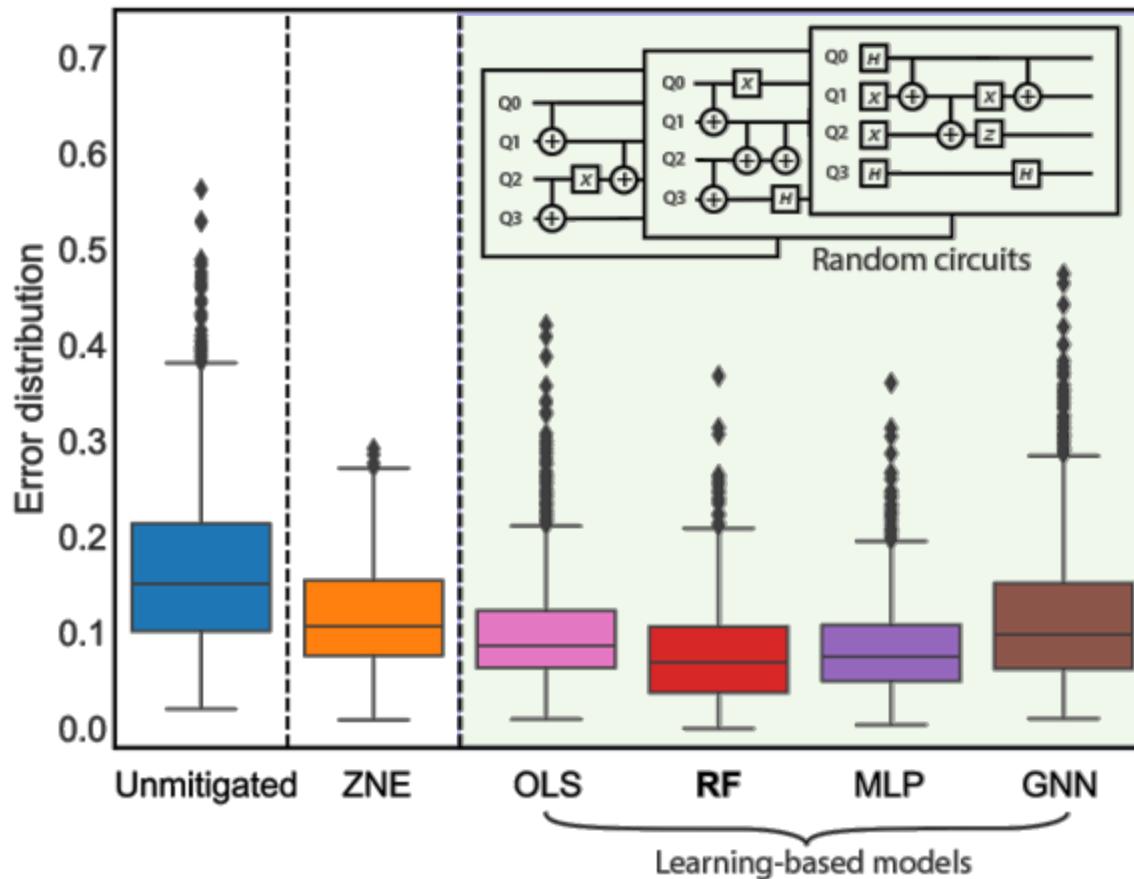
Start small: Performance on small random circuits



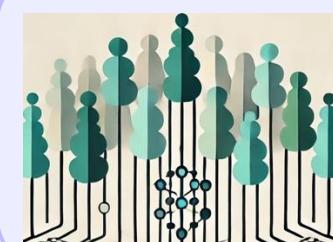
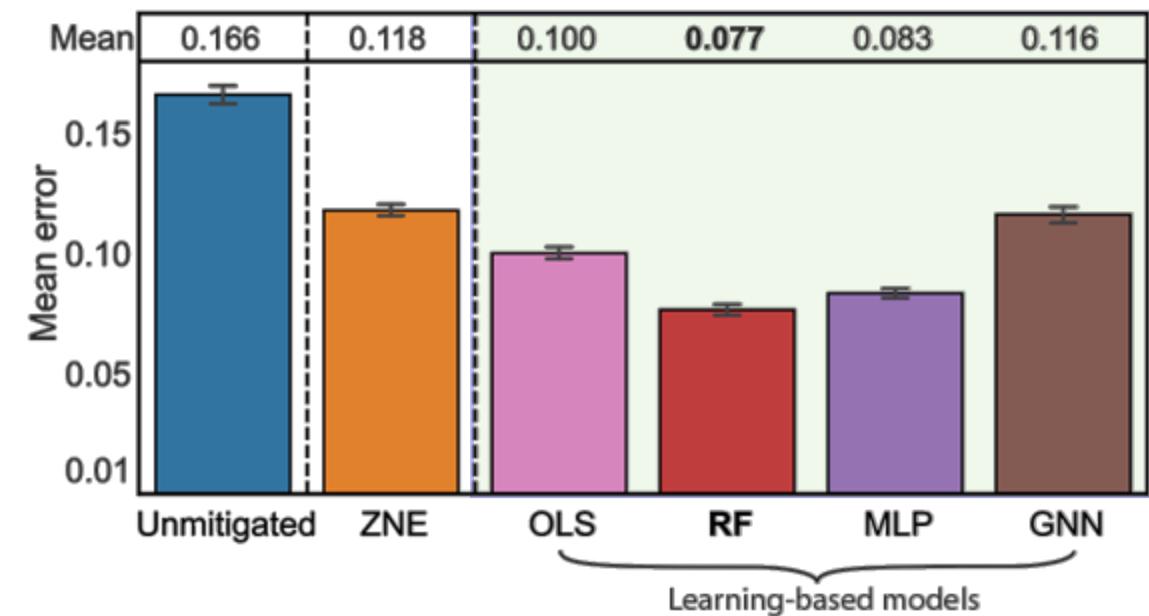
Circuits: 5,000 training and 2,000 benchmark random 4Q circuits, with 2Q gate depths from 0 to 18

Measure: All 2^4 single-Z observables

Execution: Simulation device-measured incoherent noise + SPAM errors. Ideal values computed.



ZNE: Digital ZNE only, no readout error mitigation.



ML-QEM outperforms digital ZNE
Random forest (RF) top performer

Performance on Trotterized circuits

Circuits:

First-order Trotterized
1D 4Q TFIM.

Train:

14 Trotter steps
300 circuits per step,
each different J/h

Test:

28 Trotter steps
300 circuits per step,
each different J/h

Measure:

Random Pauli basis,
weight-1 observables

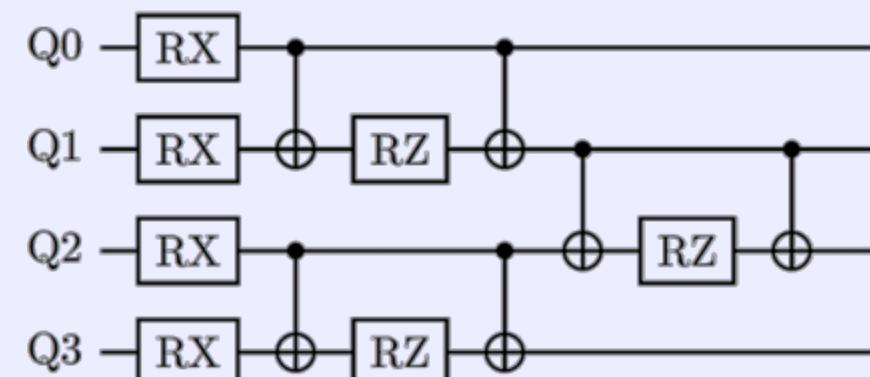
Transverse-field Ising model (TFIM) in 1D



$$\hat{H} = -J \sum_j \hat{Z}_j \hat{Z}_{j+1} + h \sum_j \hat{X}_j = -J \hat{H}_{ZZ} + h \hat{H}_X$$

J : coupling strength

h : transverse-field strength



Circuit for a single step in
first-order Trotter time
expansion

Performance on Trotterized circuits

Circuits:

First-order Trotterized
1D 4Q TFIM.

Train:

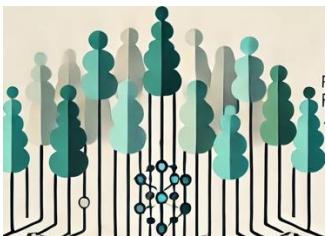
14 Trotter steps
300 circuits per step,
each different J/h

Test:

28 Trotter steps
300 circuits per step,
each different J/h

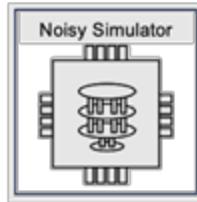
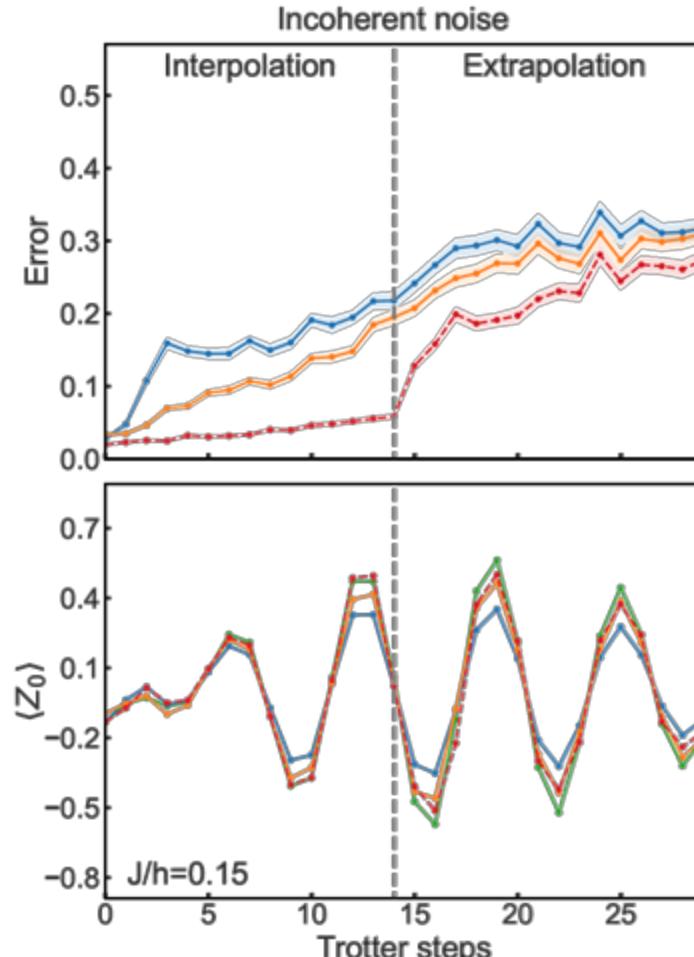
Measure:

Random Pauli basis,
weight-1 observables



Testing results in both interpolation and extrapolation regimes.

— Unmitigated — ZNE -.- RF — Ideal



Performance on Trotterized circuits

Circuits:

First-order Trotterized
1D 4Q TFIM.

Train:

14 Trotter steps
300 circuits per step,
each different J/h

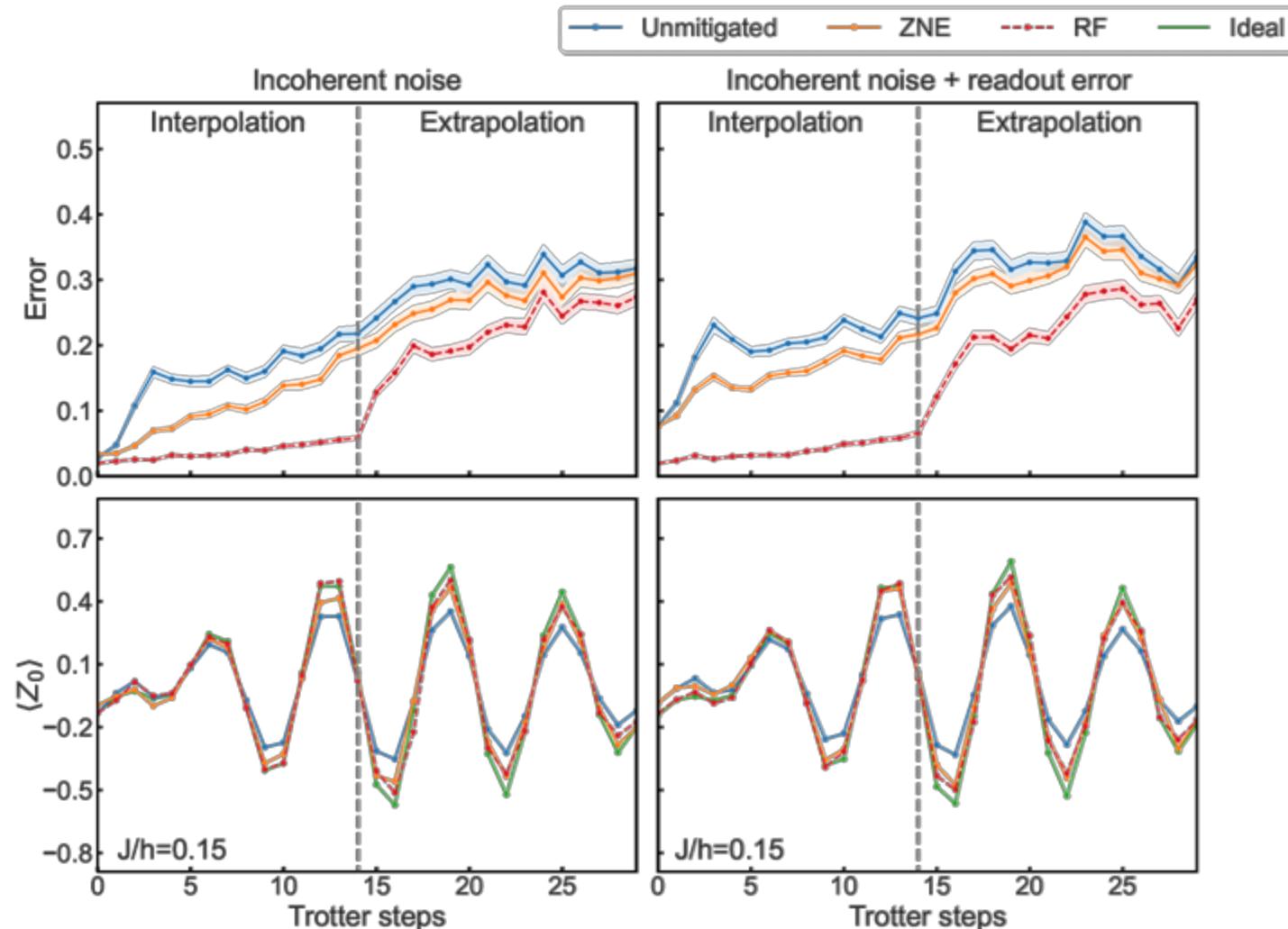
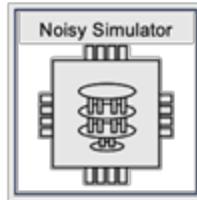
Test:

28 Trotter steps
300 circuits per step,
each different J/h

Measure:

Random Pauli basis,
weight-1 observables

Testing results in both interpolation and extrapolation regimes.



Performance on Trotterized circuits

Circuits:

First-order Trotterized

1D 4Q TFIM.

Train:

14 Trotter steps

300 circuits per step,
each different J/h

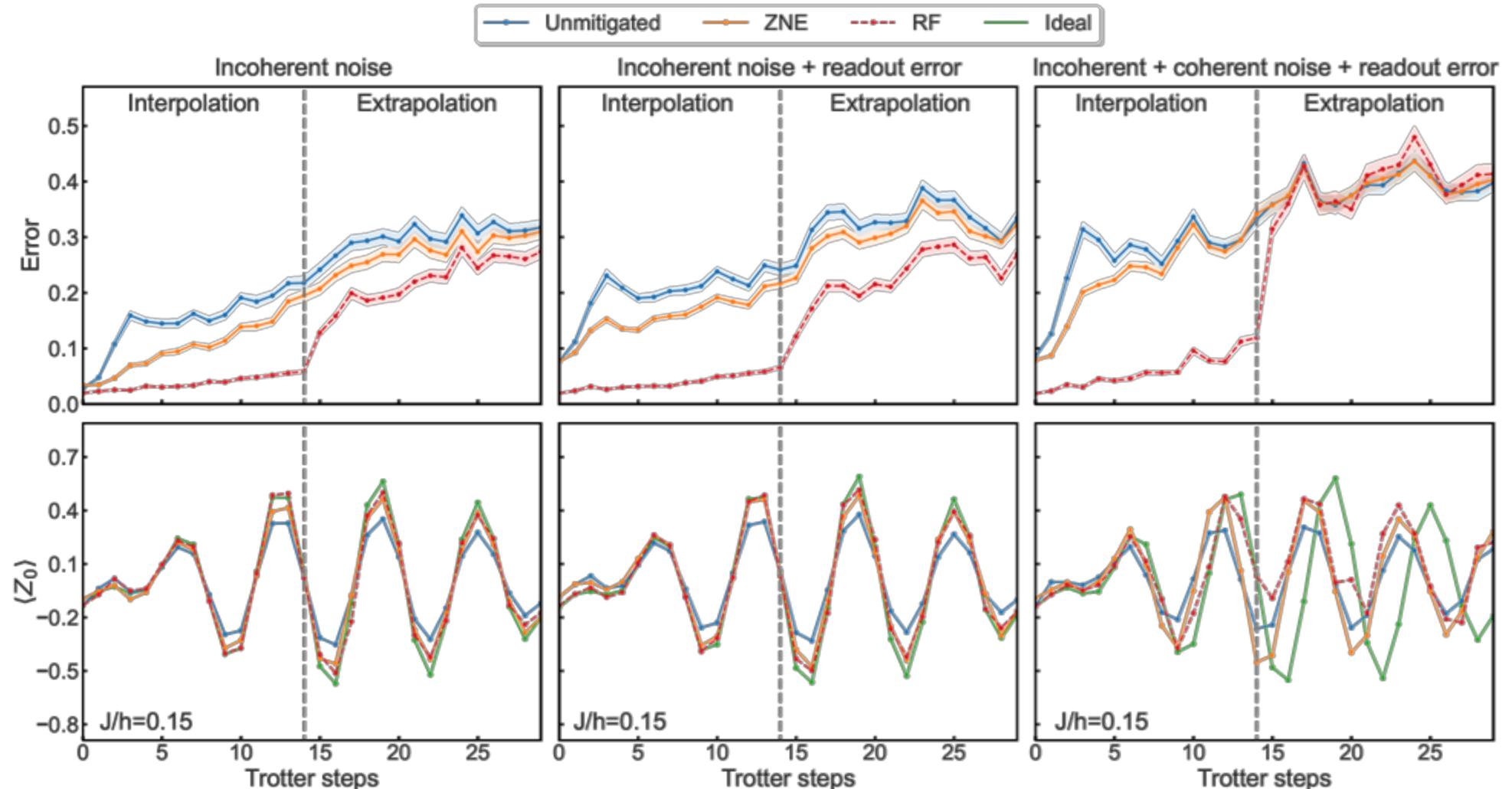
Test:

28 Trotter steps

300 circuits per step,
each different J/h

Measure:

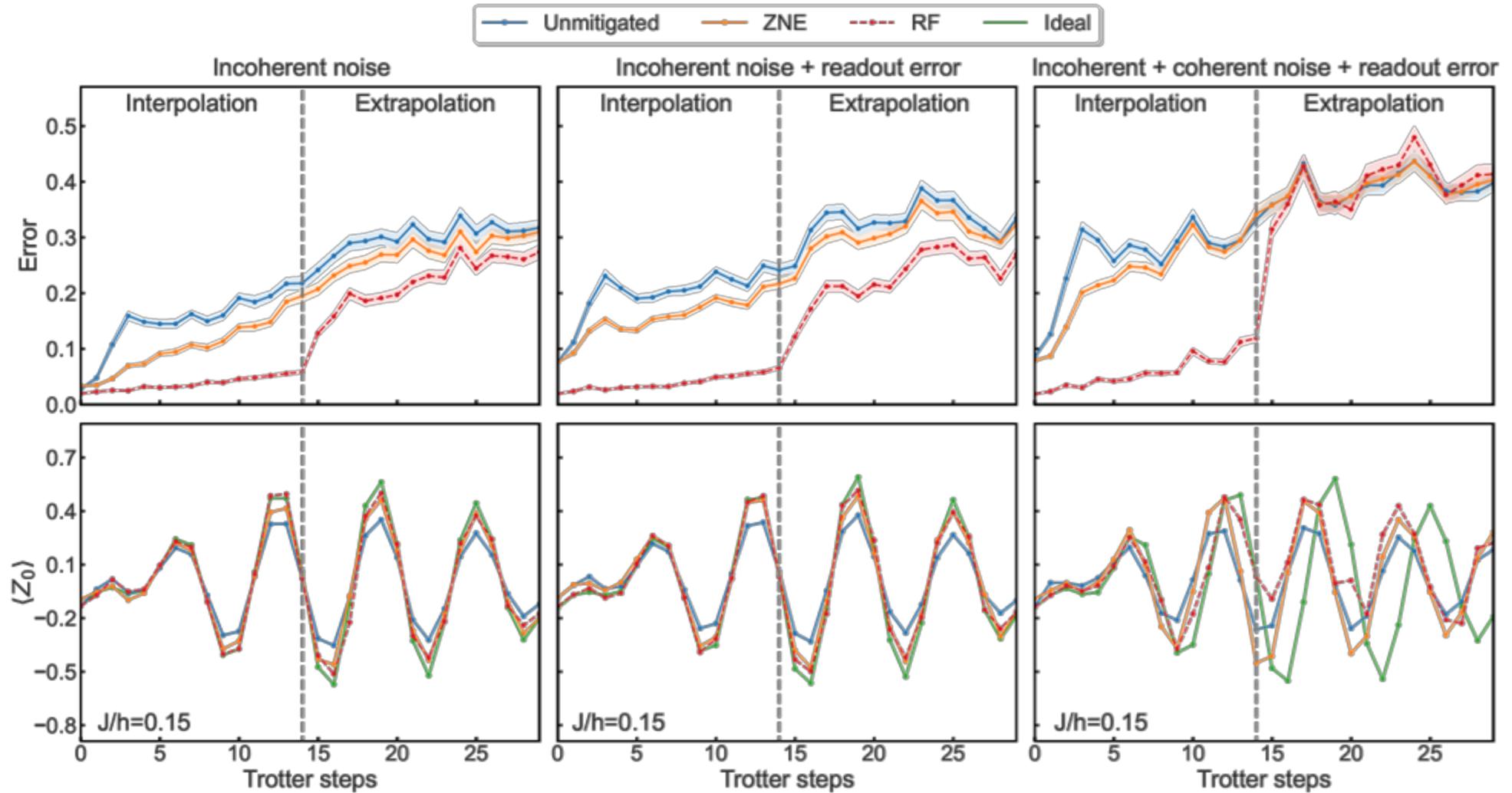
Random Pauli basis,
weight-1 observables



Performance on Trotterized circuits

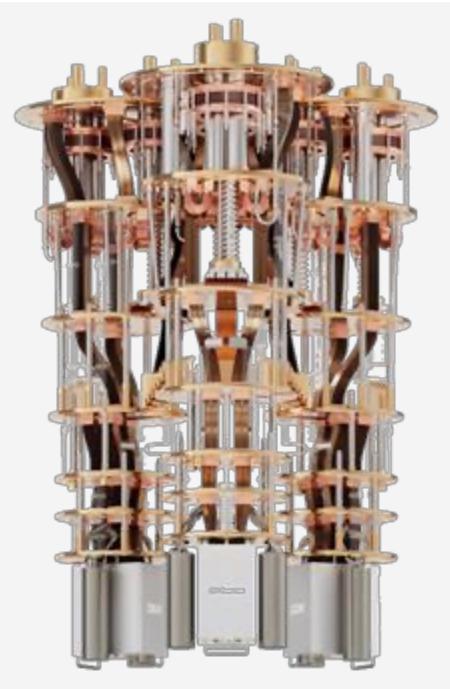
ML-QEM with random forest outperforms digital ZNE

It wins even in extrapolation when there is no coherent error

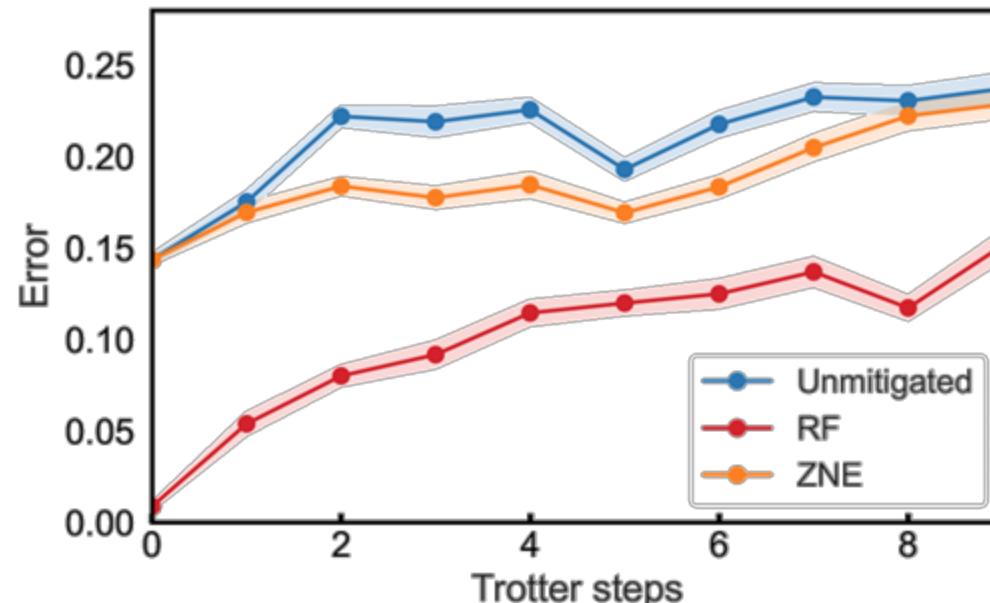


Performance on Trotterized circuits on hardware

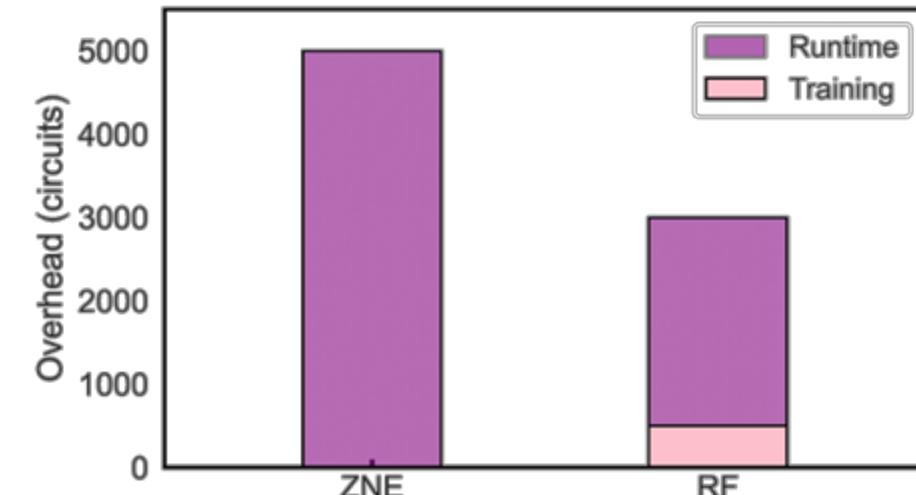
Results from
[ibm_algiers](#)



Circuits: 500 training, 2500 testing circuits
Hardness: We compute ideal expectation values.
Execution: Device (Subject to incoherent + coherent noise + readout error)



Compared to MVP ZNE with only 2 noise factors, RF has **50% lower runtime overhead**, and **40% lower overall overhead**



0.7 QPU hours to generate all training data*

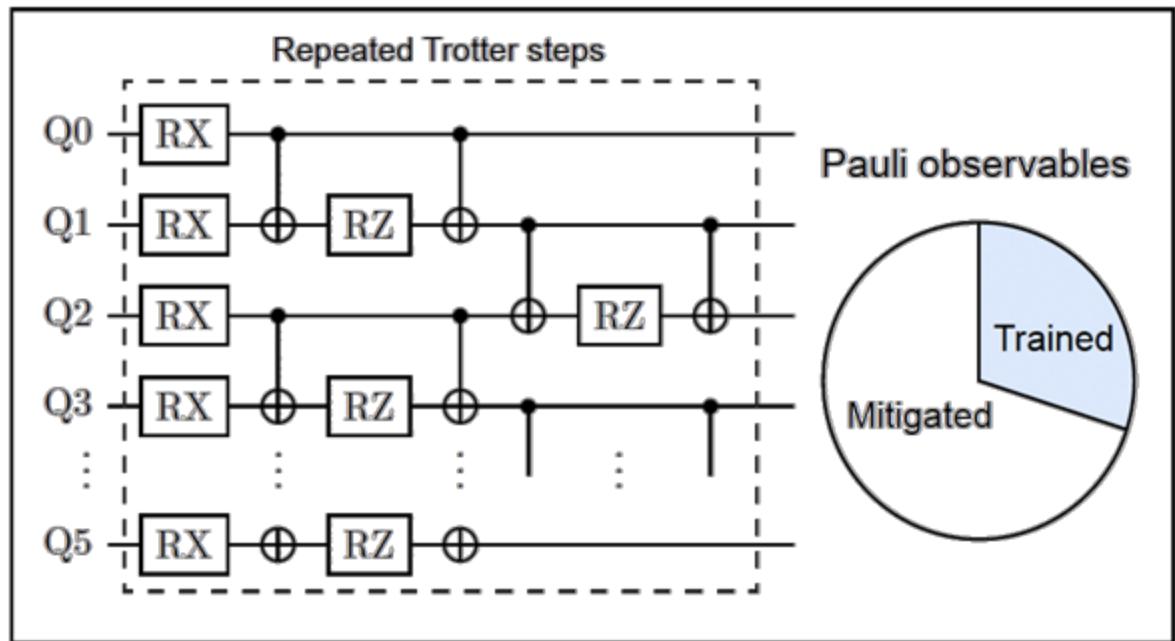
ML-QEM with random forest **outperforms digital ZNE** on hardware

In addition to **higher runtime efficiency**, we observe **higher overall efficiency**

*Estimate based on 10k shots and a conservative sampling rate of 2 kHz:

Y. Kim, A. Eddins, S. Anand et al., Nature 618, 500–505 (2023)

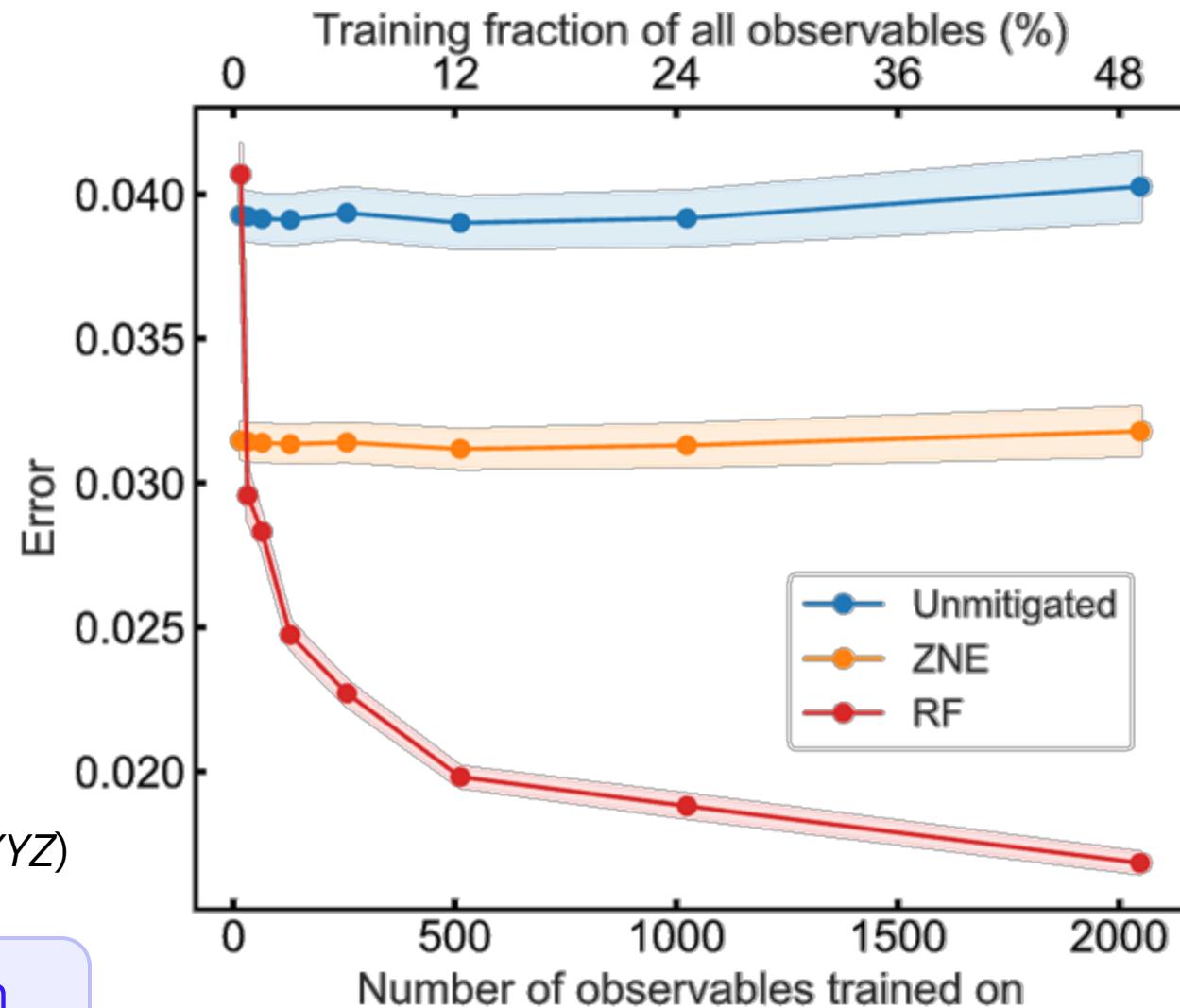
Mitigating observables not seen in training



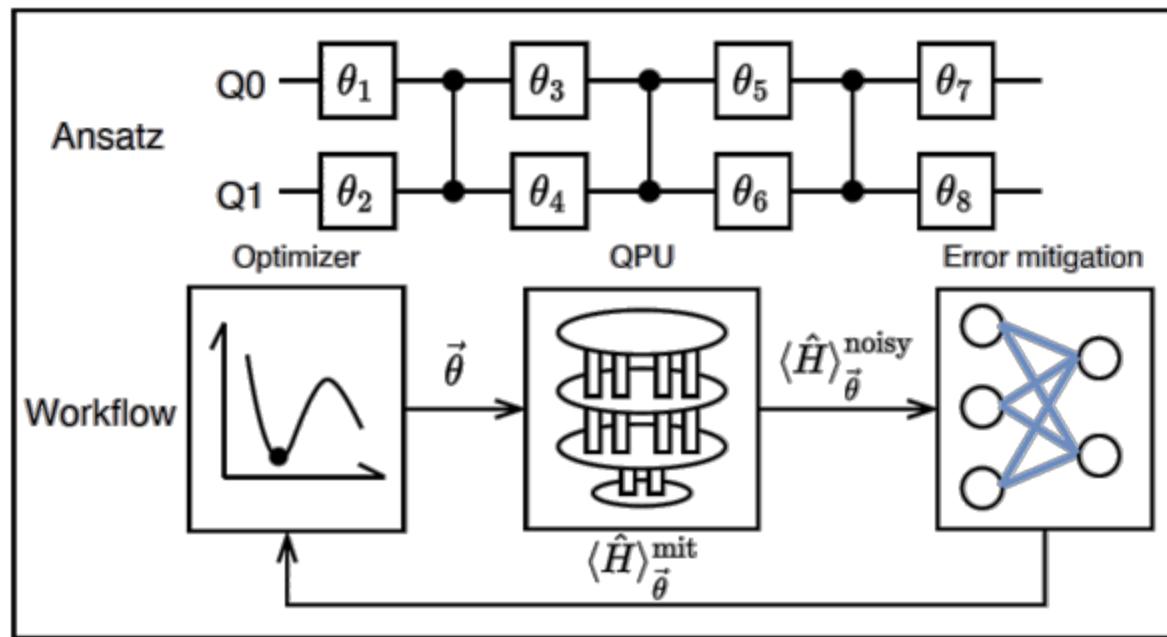
Train: on a portion of all Pauli observables (e.g., $XXIZYX$) measured on the 6Q 1D TFIM with 5 Trotter steps

Test: on the remaining of the Pauli observables (e.g., $YIIXYZ$)

ML-QEM only needs to train on a very small fraction to outperform digital ZNE



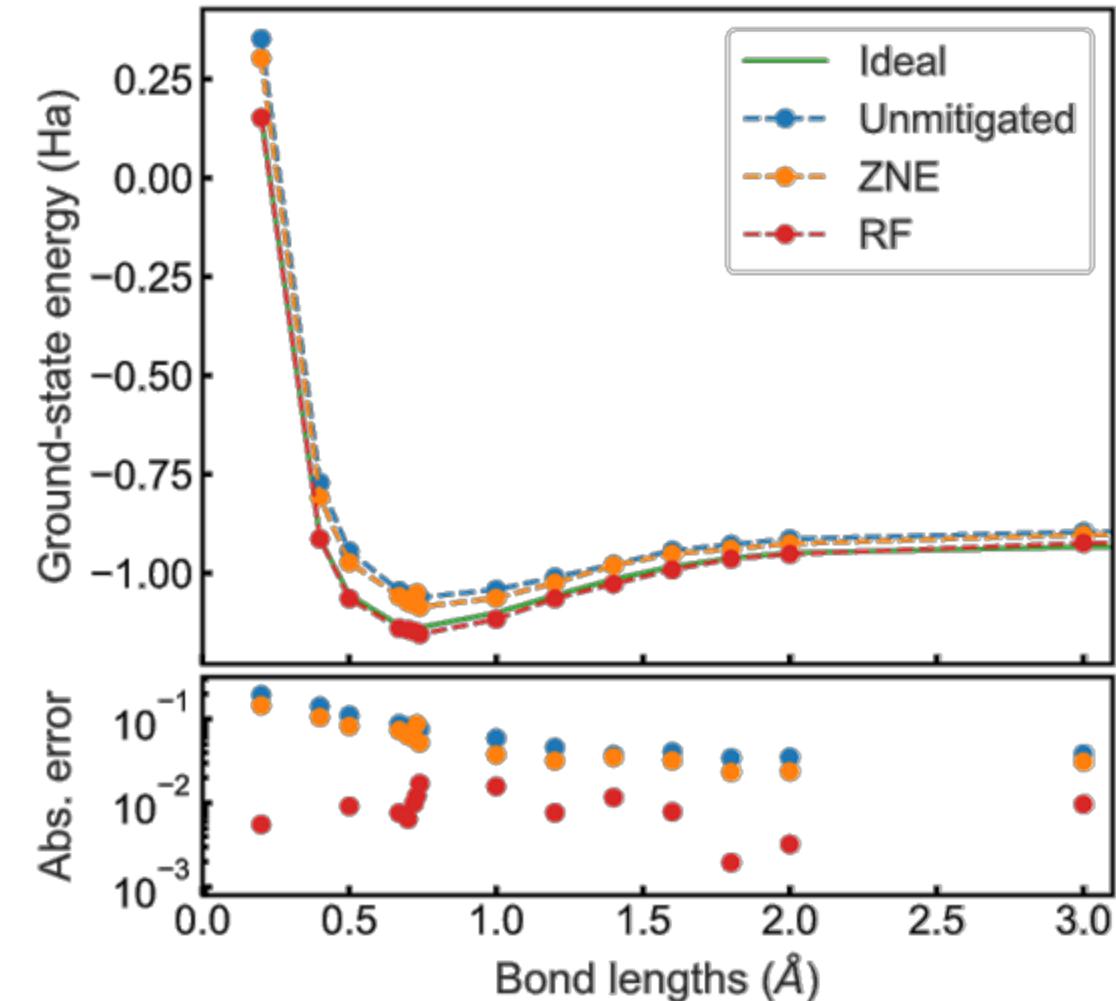
Enhancing variational algorithms (e.g., VQE)



Train: on 2000 2Q two-local ansatz with randomly sampled parameters measured in either XX or ZZ

One trained model for all bond lengths

Run VQE to find the ground-state energy of H_2 molecule whose Hamiltonian is composed of XX , ZI , IZ , ZZ terms



ML-QEM outperforms digital ZNE

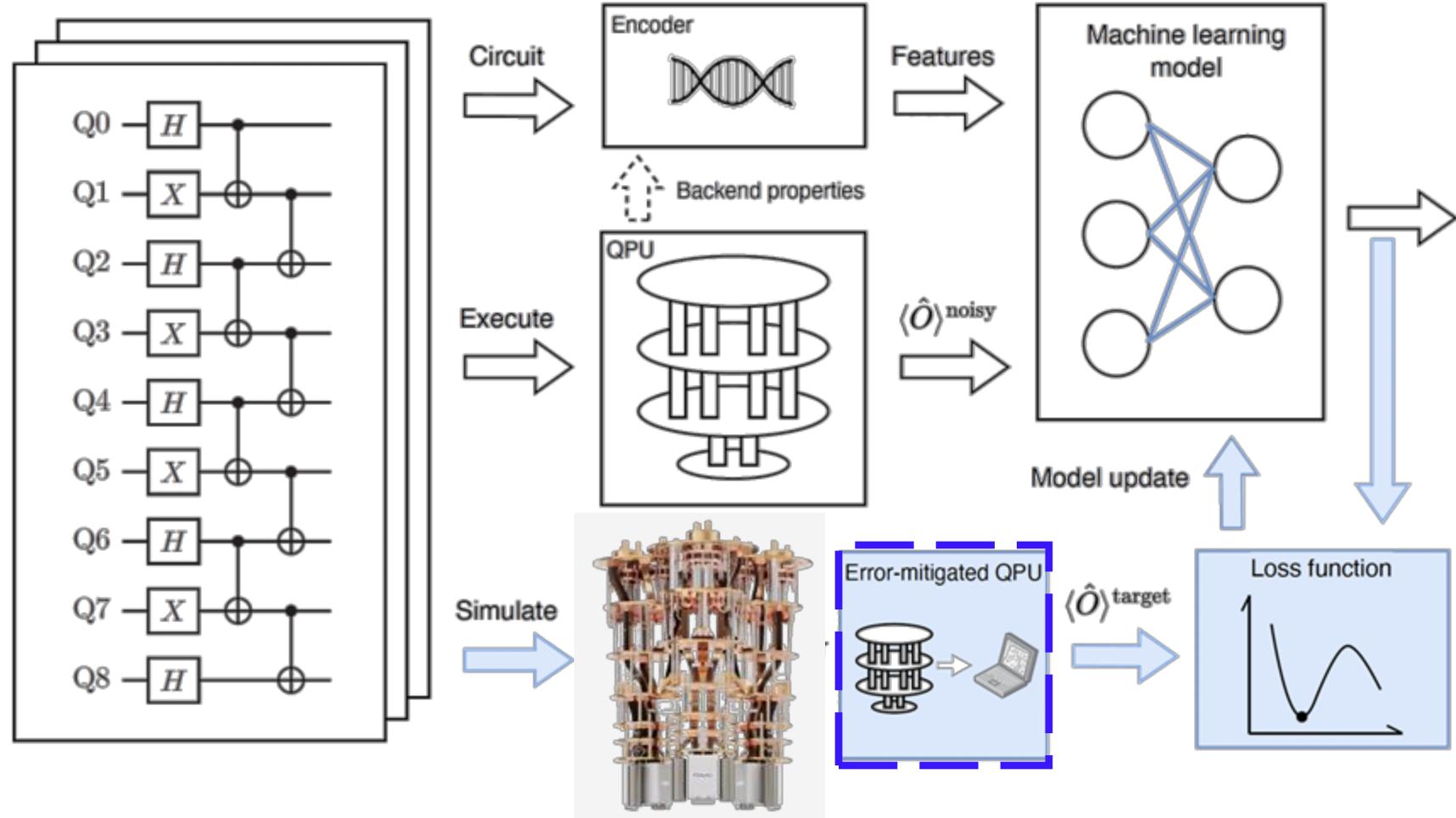
Scaling & Adaptability

Scalability through mimicry

Setting:

100Q+ circuits
No classical sims available

Aim:
Produce results matching gold-standard conventional method (e.g., ZNE, PEC, PEA) but **with higher runtime efficiency.**



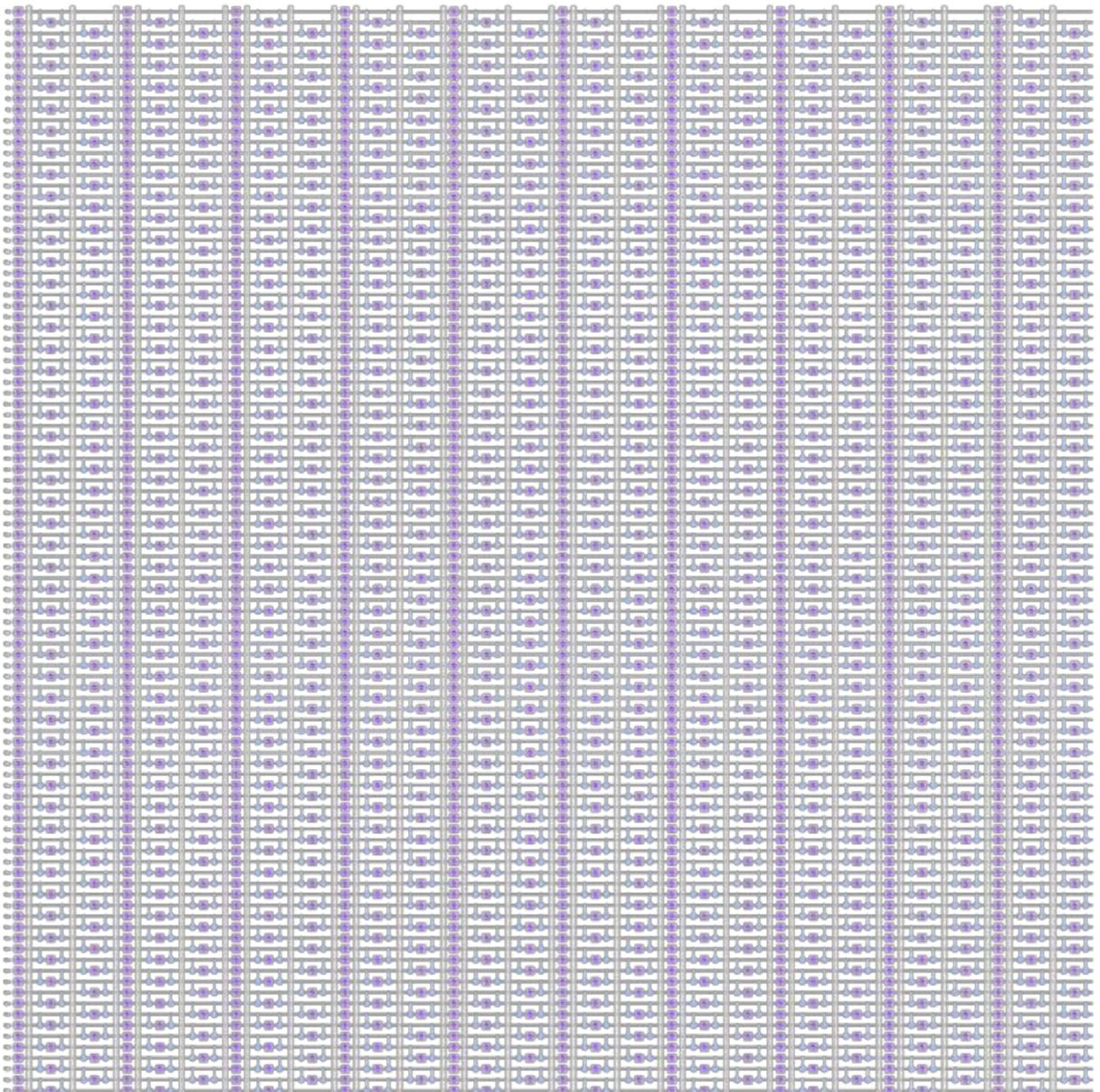
Example: Mimicry on a 100-qubit experiment



ibm_brisbane

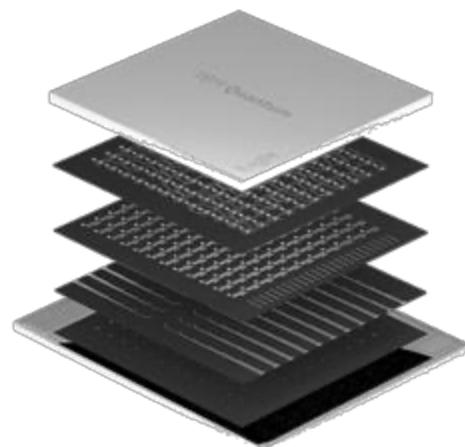
Circuits: 100-qubit Trotterized 1D transverse-field Ising model (TFIM) experiment up to 10 Trotter steps (**40 CNOT depth, ~2000 CNOTs**) with twirling.

Measure: $\langle Z \rangle$ expectation values

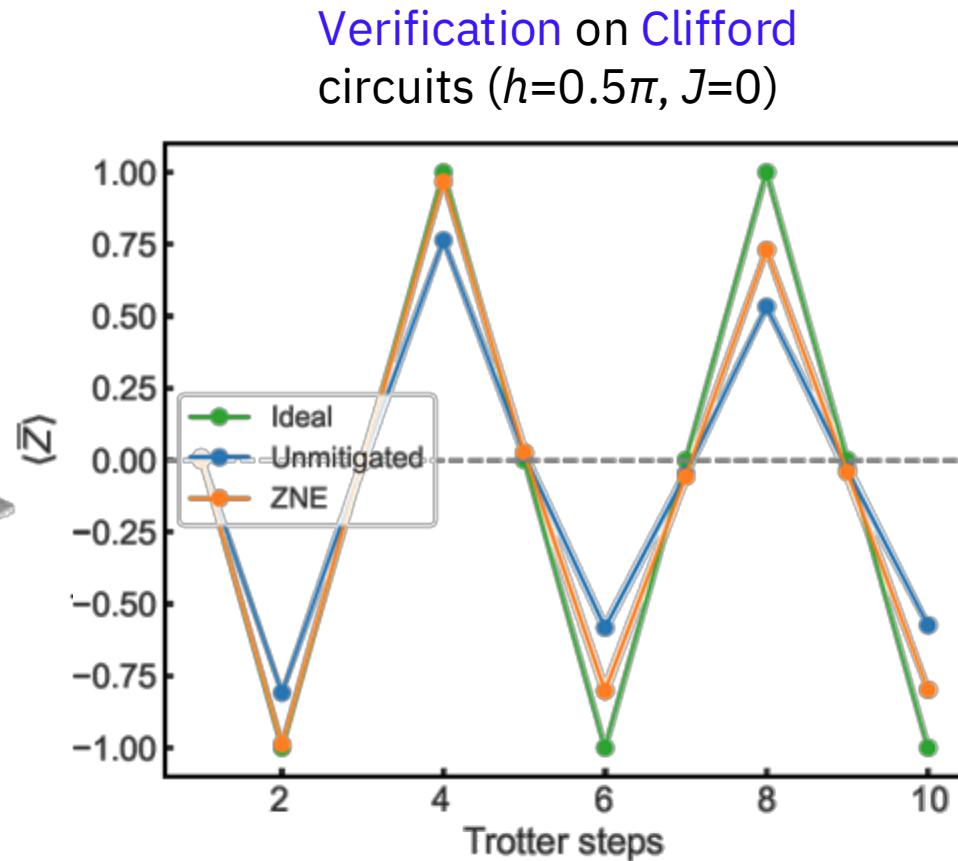


Mimicry on a 100-qubit experiment

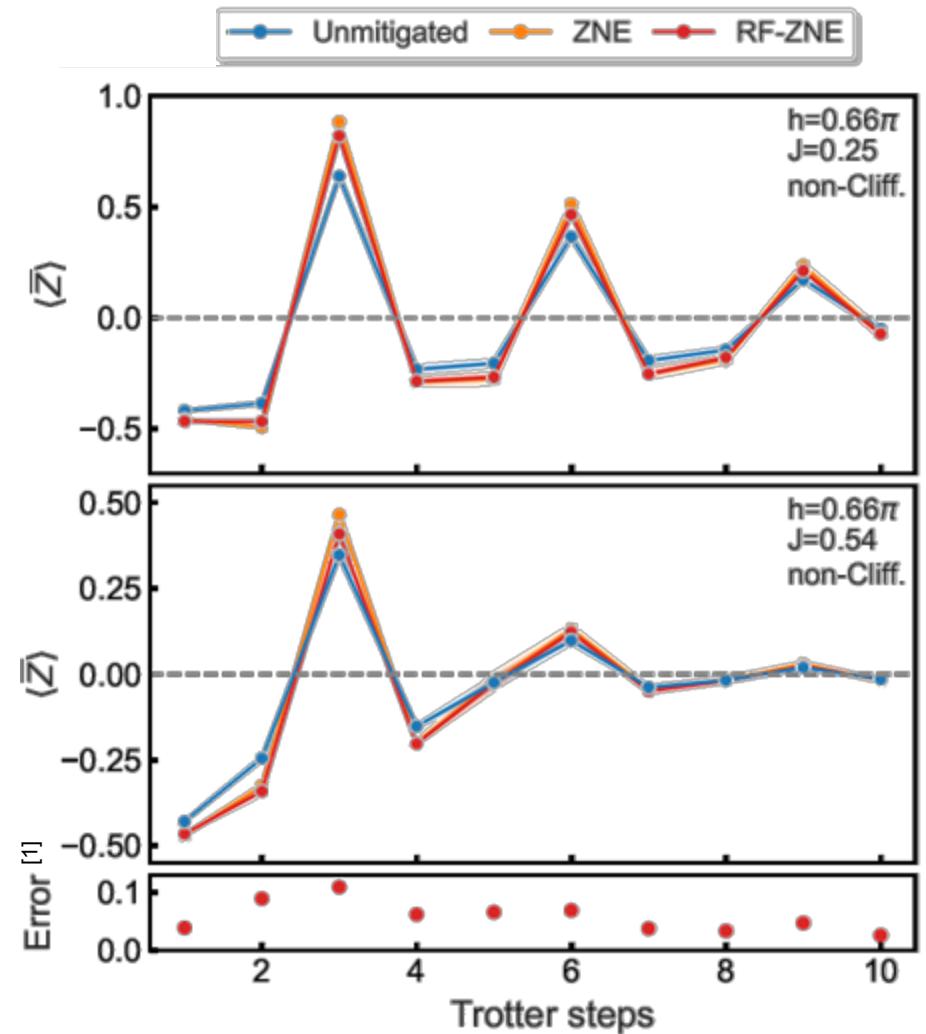
100 training, 400 testing circuits in total



ibm_brisbane
(with twirling)

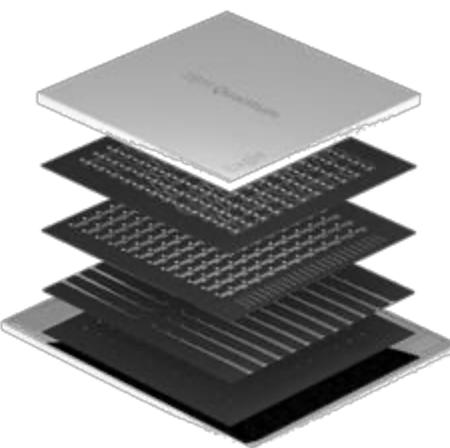


Mimicry on non-Clifford circuits with different J/h



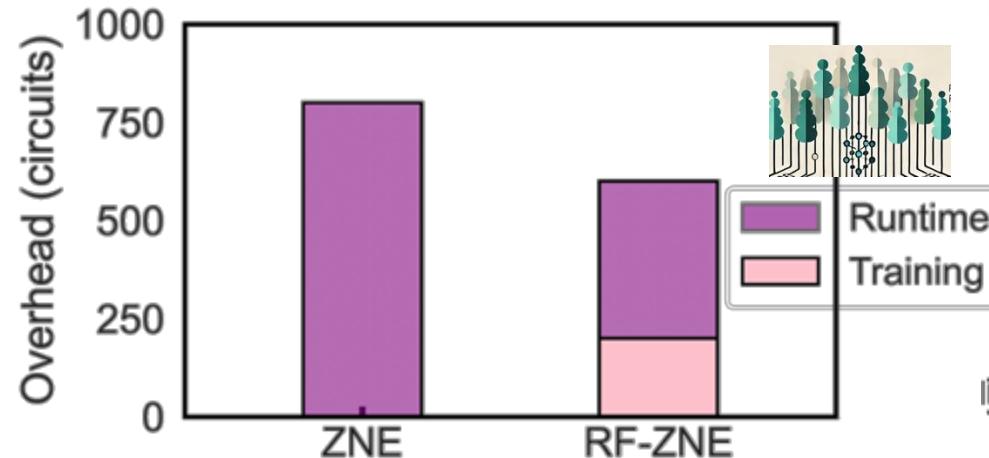
[¹] Errors are between ZNE and RF-ZNE, also averaged over 40 different J/h at each step Z. Minev, IBM Quantum (50)

Mimicry on a 100-qubit experiment



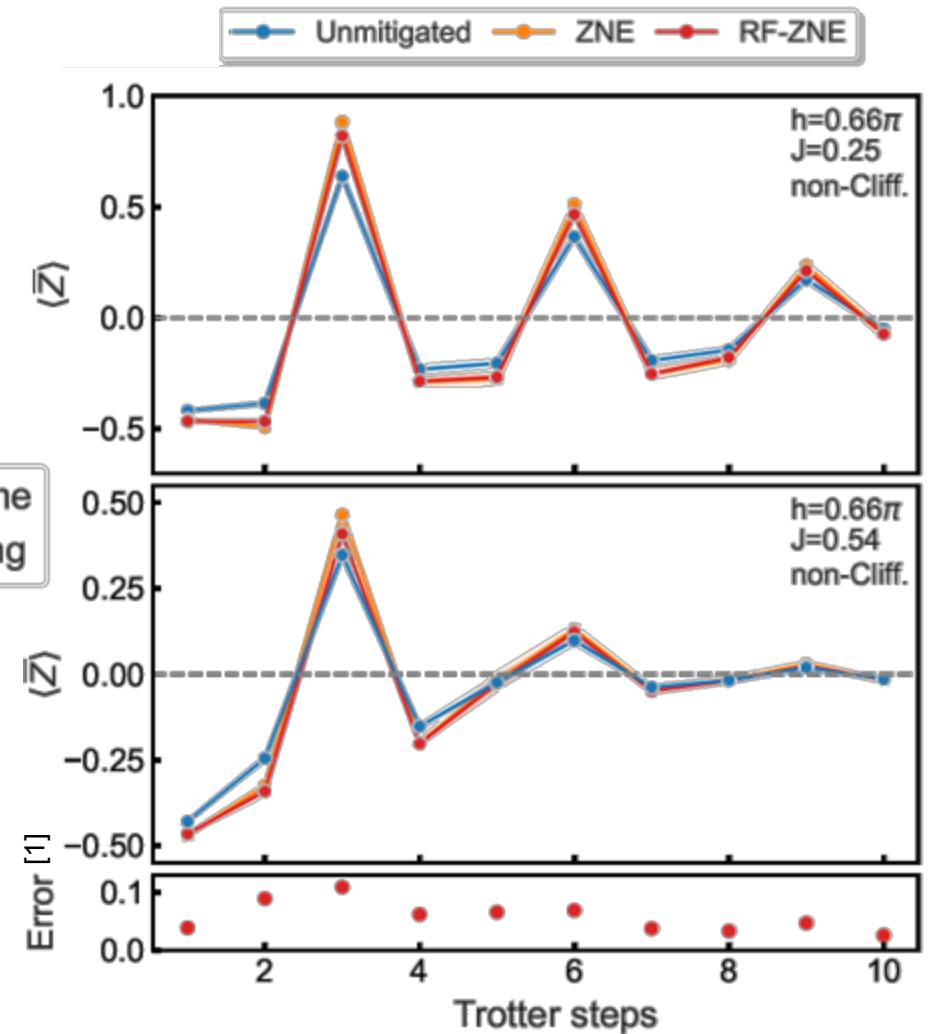
100 training, 400 testing circuits in total

Compared to ZNE with 2 noise factors,
Runtime overhead of RF-ZNE is 50% lower
Overall overhead of RF-ZNE is 25% lower



0.14 QPU hours to generate all training data
(excluding randomized compiling)^[2]

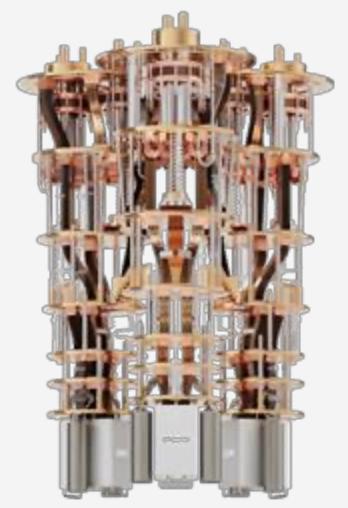
Mimicry on non-Clifford
circuits with different J/h



^[2] Estimate based on 10k shots and a conservative sampling rate of 2 kHz: Y. Kim, A. Eddins, S. Anand et al., Nature 618, 500–505 (2023)

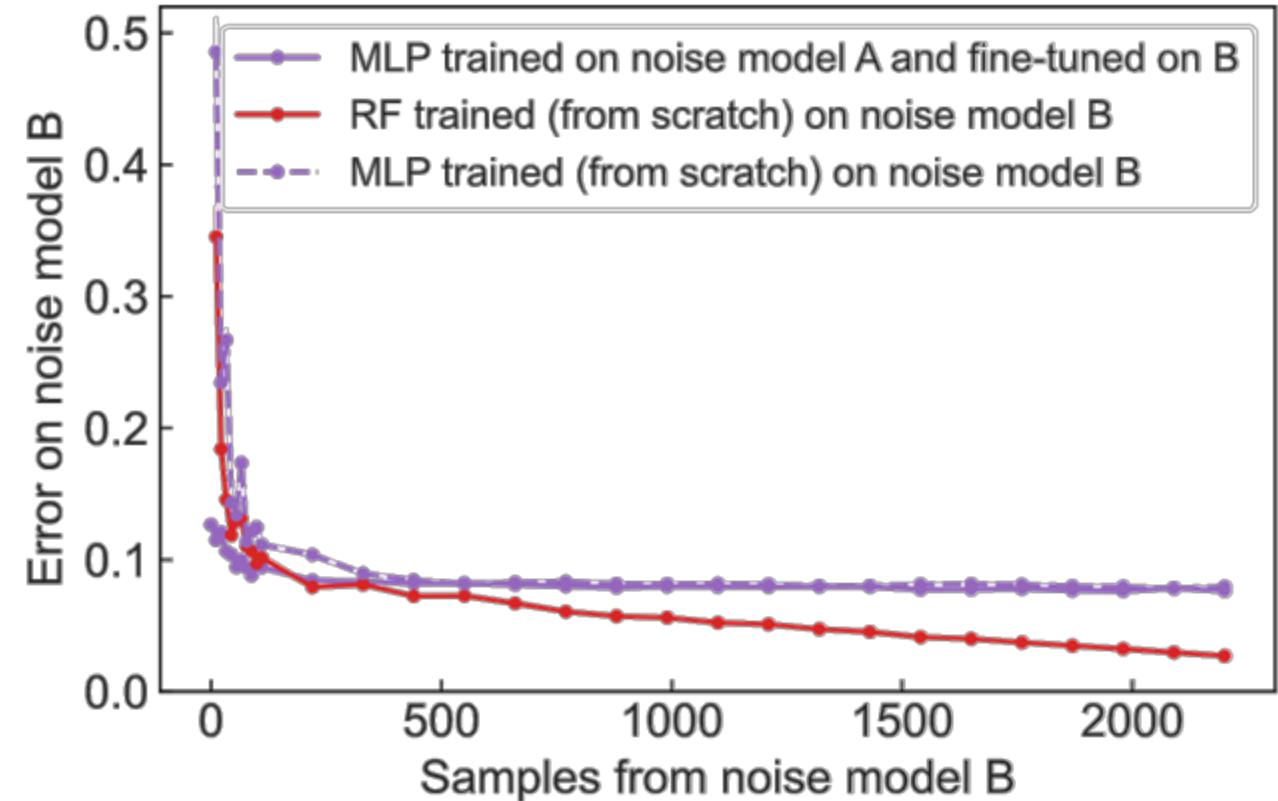
^[1] Errors are between ZNE and RF-ZNE, also averaged over 40 different J/h at each step

Adapt to device noise drift



MLP can be fine-tuned on a different noise model after initial training, results in faster convergence than training new MLP from scratch

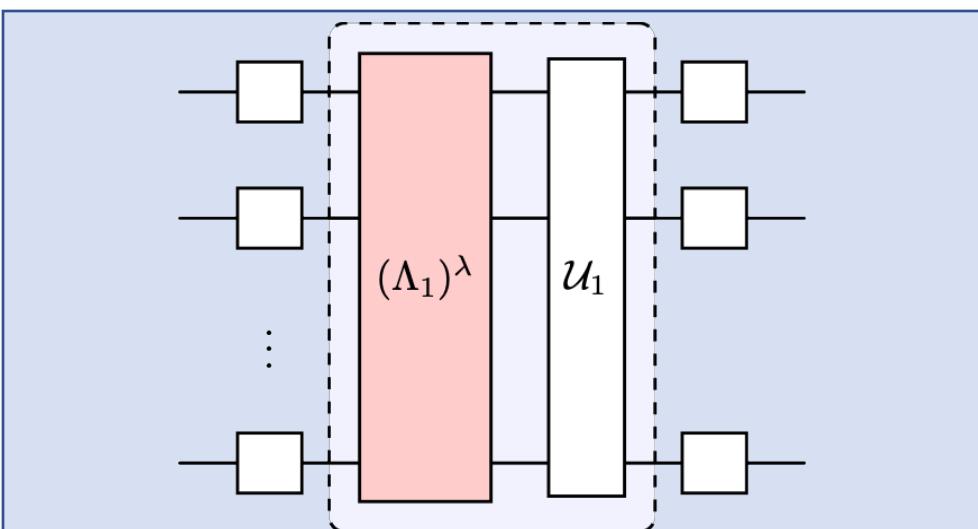
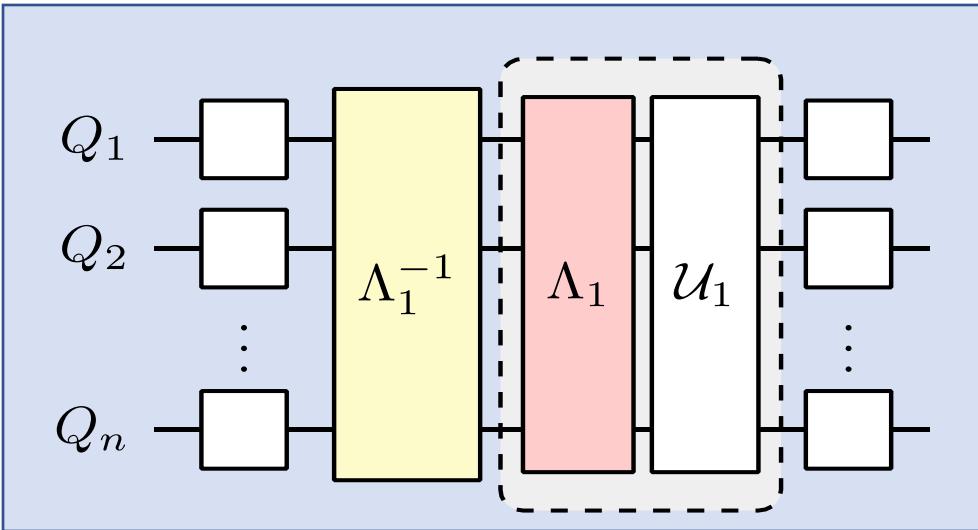
RF trained from scratch converges very quickly, demonstrates good efficiency in training an updated RF model



MLP and RF can efficiently adapt to time-varying noise models

Why could ML-QEM be working?

Physics based methods



ML-QEM

Skip learning quantum noise

Complex general object; We care about the relationship of classical objects. Instead, show similar circuits.

Learn classical output-only relationships

Learn non-linear relationship b/w $\langle O_{\text{noisy}} \rangle$ and $\langle O_{\text{target}} \rangle$ + circuit features directly. Generically hard, but here simple.

Convergence of global noise

Experiment: Empirically, noise effect is to damp same-weight Paulis by very similar amount in most circuits

Theory: $\log(d)$ convergence for random circuits.*

Tailor the noise

We can tailor & simplify the noise (twirl, DD, etc.)

* Dalzell, et al. Random quantum circuits transform local noise into global white noise, Commun. Math. Phys. (2024).

Try it yourself: Code

Code: github.com/qiskit-community/ml-qem

The screenshot shows the GitHub repository page for 'ml-qem'. At the top, there's a navigation bar with links for Code, Issues (3), Pull requests (1), Actions, Projects, Security (1), and Insights. Below the navigation is the repository name 'qiskit-community / ml-qem' and a search bar. The main content area shows a list of recent commits and pull requests:

Author	Commit Message	Time Ago	
zlatko-minev	Added published links to README...	b1eccf8 · 3 months ago	
	.github	Issue 12 Templates for iss...	3 years ago
	blackwater	Update estimator.py	10 months ago
	docs	update figures	3 months ago
	tests	update	2 years ago
	.gitignore	Update .gitignore	2 years ago
	.pylintrc	Issue 8 Tox and docs (#11)	3 years ago
	CONTRIBUTING.md	Issue 8 Tox and docs (#11)	3 years ago

To the right of the commit list is an 'About' section with the following text:

Library for solving quantum computing problems using machine learning

- Readme
- Apache-2.0 license
- Code of conduct
- Activity
- Custom properties
- 33 stars
- 5 watching
- 10 forks

At the bottom of the 'About' section is a link to 'Report repository'.

Docs: qiskit-community.github.io/ml-qem

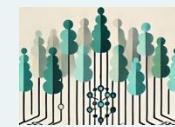
The screenshot shows the ML-QEM documentation page. The title 'ML-QEM' is at the top. Below it is a 'Navigation' section with links to 'Tutorial: NGEM - Neural graph error mitigation', 'Guide: graph encoders', 'Guide: data writing and loading', and 'API References'. There's also a 'Quick search' bar. On the right side, there are sections for 'Installation' (with a command 'pip install ml_qem'), 'Tutorials' (linking to the NGEM tutorial), 'Guides' (links to 'graph encoders' and 'data writing and loading'), and 'API references' (linking to 'API References' and 'Primitives', 'Data', and 'Metrics').

Conclusion: ML-QEM can significantly *accelerate* (reduce cost of) quantum error mitigation without sacrificing *accuracy* even at utility scale.

General framework
(can test other ML and QEM models)

Applicable at utility scale (100Q+)

Best model: RF



Adaptable to noise fluctuation
Cloud deployable
Limit set by conventional methods
Lots more to test and try!

Haoran Liao, Derek Wang, Iskandar Situdikov, Ciro Salcedo, Alireza Seif, **Zlatko Minev**
Nature Machine Intelligence v. 6, p. 1478 (2024); IBM Quantum Team

AI compiling:
arXiv:2405.13196, arXiv:2407.21225S

Slides? zlatko-minev.com/blog   @zlatko_minev

Machine learning for practical quantum error mitigation

Haoran Liao, Derek Wang, Iskandar Situdikov, Ciro Salcedo, Alireza Seif, **Zlatko Minev**

Nature Machine Intelligence v. 6, p. 1478 (2024)

Acknowledgements: Brian Quanz, Patrick Rall, Oles Shtanko, Roland De Putter, Kunal Sharma, Barbara Jones, Sona Najafi, Thaddeus Pelligrini, Grace Harper, Vinay Tripathi, Antonio Mezzacapo, Christa Zoufal, Travis Scholten, Bryce Fuller, Swarnadeep Majumder, Sarah Sheldon, Youngseok Kim, Pedro Rivero, Will Bradbury, Nate Gruver, Minh Tran, Kristan Temme, and the broader IBM Quantum team



Slides?

zlatko-minev.com/blog @zlatko_minev

Derek Wang Iskandar Situdikov

Alireza Seif Zlatko Minev Ciro Salcedo

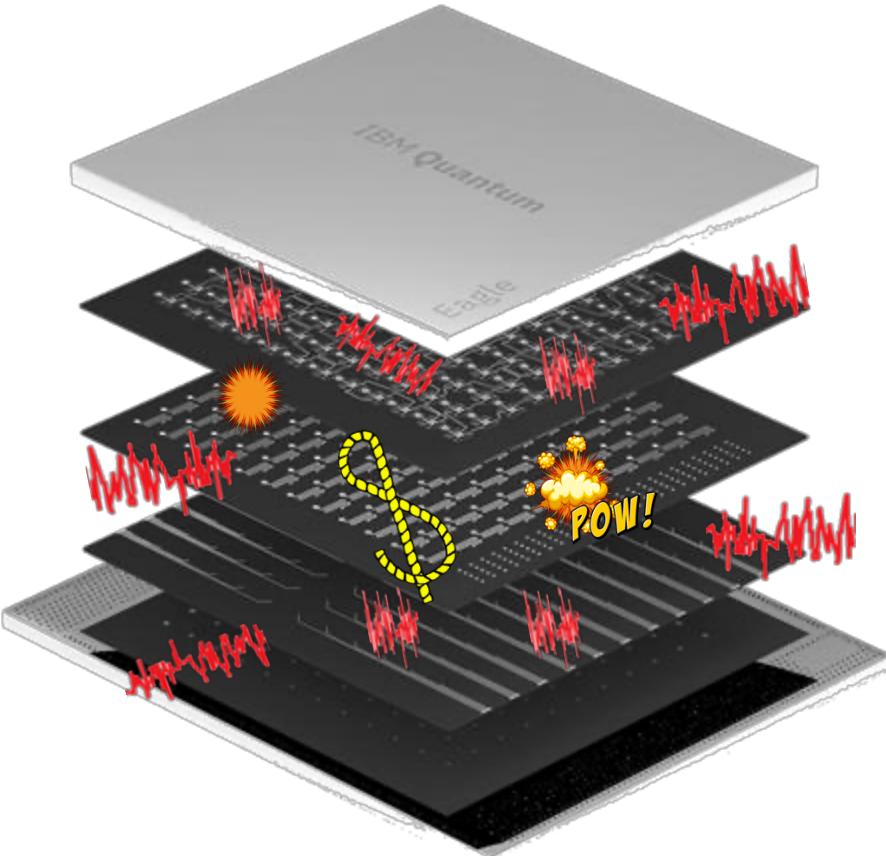
Illustration generated using AI (DALL-E)

EXTRA

Some future directions

1. When trained with different noise parameters and their corresponding noisy expectation values, can we set all noise parameters encoded in GNN to the “good” values (i.e., [set encoded gate error to 0, coherence times to infinity](#)) to predict the ideal expectation values [without ever training on ideal expectation values \(and thus scalable\)](#)?
2. Can we instead regress the ideal and noisy expectation values of small-scale circuits onto the noise parameters [to extract some noise parameters \(e.g., avg. 2q gate error\) of the backend](#), without running benchmarking experiments with additional quantum resources?
3. In ML-QEM, the training set can be optimized in terms of both size and type of the training circuits subject to design principles
4. ML-QEM can be more rigorously benchmarked against leading methods, such as PEC, PEA, and pulse-stretching ZNE

Error mitigation and error correction



Error mitigation: working with what you have

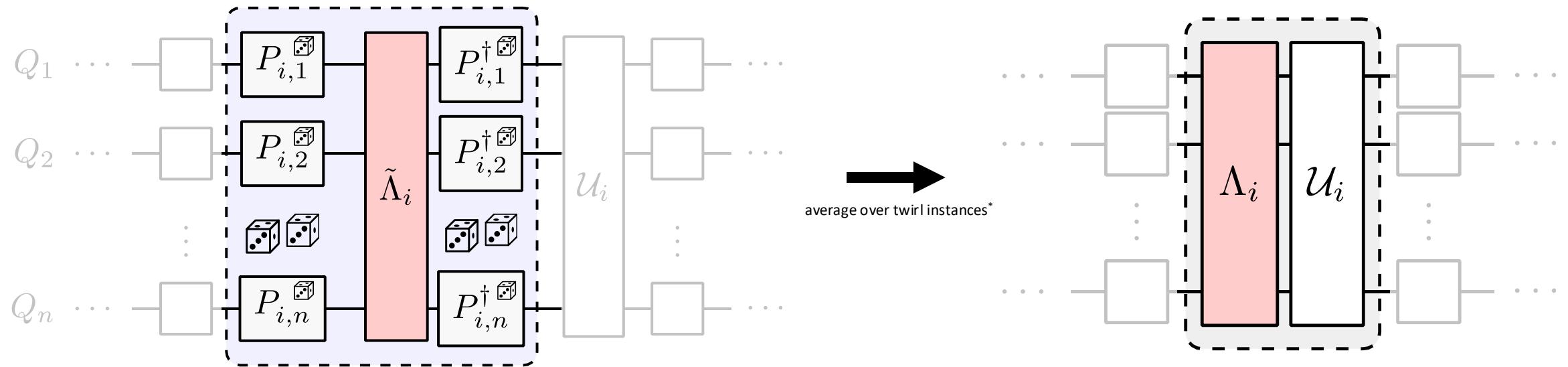
- **benefit** suppress errors on classical results (expectation values)
- **q-cost** no extra qubits or hardware resources needed
- **c-cost** trades classical resources (post-processing) for lower error
- **limitation** bad asymptotic scaling: high number of samples & circuits

Error correction: protecting quantum information

- **benefit** suppress & correct errors to arbitrarily small level
- **q-cost** very large qubit and hardware overhead
- **c-cost** decoding and encoding can be classically costly
- **challenge** requires fault-tolerant operations and readout

Simplify the noise: twirl

twirl reduces to noise $4^n \times 4^n$ matrix to diagonal one with 4^n entries in Pauli basis



(Stochastic) Pauli channel

Twirling references

1. C. H. Bennett, G. Brassard, S. Popescu, B. Schumacher, J. A. Smolin, W. K. Wootters, et al., Phys. Rev. Lett. 76, 722 (1996).
2. E. Knill, arXiv:0404104 (2004).
3. O. Kern, G. Alber, D. L. Shepelyansky, EPJ D 32, 153 (2005).
4. M. R. Geller, Z. Zhou, Physical Review A 88, 012314 (2013).
5. J. J. Wallman, J. Emerson, Physical Review A 94, 052325 (2016)
6. Hashim *et al.*, Phys. Rev. X 11, 041039 (2021)
7. Tutorial: zlatko-minev.com/blog/twirling (2022)
8. ...

