# Diffusion Transformer (DiT)

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In this note, we will explain how Diffusion Transformer (DiT) works in this seminal paper<sup>1</sup>. We intent to explain it from two parts: the training stage and the inference stage.

### 1 The Inference Stage

Firstly we discuss how to generate images in inference stage, which consists the three components: diffusion process, transformer model, and VAE decoder. In the Fig 1, we present the entire process of how to generate 8 images given 8 labels. Firstly we generate noise tensor with size 8\*4\*32\*32, feed that into diffusion transformer with 8 labels, repeated this operation a number of times (so called number of diffusion steps). Top line is the stretch of diffusion process and we omit the details of how diffusion works in this overview diagram. After diffusion and transformer, we have 16\*4\*32\*32 tensors, and feed the first chunk of tensor 8\*4\*32\*32 to VAE decoder. Finally we obtain the 8 RGB images with size 8\*3\*256\*256. In the notes, we are talking about generating 8 images. Note that the following explanation and diagram is mainly based on the implementation 2



Figure 1: The Process to Generate Images with DiT Given The Class Labels

### 1.1 Latent Diffusion Transformer

In the Fig 2, we present the overall structure of diffusion Transformer model. There are three inputs to transformer: noise with size 16 \* 4 \* 32 \* 32, labels with size 8 and time step t. For the noise part, note that in the implementation, generate noise 8 \* 4 \* 32 \* 32 tensor, and then concatenate those two noise tensor to have tensor 16 \* 4 \* 32 \* 32. Just

<sup>&</sup>lt;sup>1</sup>https://arxiv.org/pdf/2212.09748

<sup>&</sup>lt;sup>2</sup>https://github.com/facebookresearch/DiT?tab=readme-ov-file

make it clear this subtle difference with above section. Labels is a vector, for example [207, 360, 387, 974, 88, 979, 417, 279], where 207 refers dog label. t refer to diffusion step, which is also feed into transformer.

For the noise tensor 16 \* 4 \* 32 \* 32 input, the first step is called patch embedding, which essentially is 2D-convolutional layer with kernel size (2,2) and stride (2,2), thus each channel is converted to  $\frac{32}{2} * \frac{32}{2} = 256$  numbers. To encode positional information, there is the positional embedding table with size 256 \* 1152, in which each row 1152-dim vector is representing each position. we add patch embedding with positional embedding to generate 16 \* 256 \* 1152 tensor as one source of inputs to DiT Block.

For label [207, 360, 387, 974, 88, 979, 417, 279], in the implementation, this 8-dim vector is padded with another null labels to generate 16-dim vector as  $[207, 360, 387, 974, 88, 979, 417, 279, 1000, 1000, \cdots, 1000]$ . Convert this label vector to label embedding 16\*1152 by extracting 16 row from label embedding table with size 1001\*1152, here 1001 is the number of class (Imagenet 1000 class, one extra is null class, I guess) and 1152 is the dimension of label embedding.

For time step t, which is 16-dim vector, essentially is  $[5, 5, \dots, 5]$  if we set the total number of time step as 6 in the diffusion process. Convert this 16-dim t vector to time embedding 16\*1152 matrix. In the time embedding block, there is time embedding, fully connected layer, SiLu normalization layers.

Add the label embedding matrix and the time embedding matrix to obtain the matrix with size 16 \* 1152 as another source of inputs to feed into DiT Block.

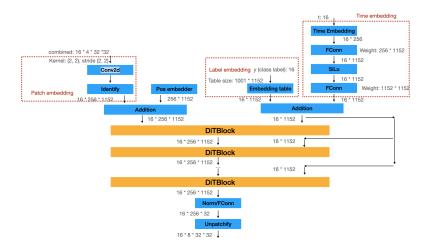


Figure 2: Latent Diffusion Transformer

In the Fig 3, we present what is insider of the DiT block and how those two sources of inputs are used. The top of the Fig 3 shows the inputs and outputs of DiT Block. The inputs to DiT Block are the addition of noise embedding and positional embedding with size of 16\*256\*1152 and the addition of the label embedding and time embedding with size of 16\*1152. The output is a tensor with size of 16\*256\*1152. To facilitate the following discussion, we denoted the addition of the noise embedding and position embedding as  $\mathbf{x}$  and the addition of the label embedding and the time embedding as  $\mathbf{o}$ .

Inside of DiT block there are normalization layer, traditional multi-head attention layer, fully connected layer, GELU normalization layer. One novelty inside of this block is so called adaptive layer normalization. Firstly apply SiLu normalization and fully connected on embedding  $\bf o$  to obtain the large matrix with size 16\*6912, then chunk this large matrix to six parts and each part with size 16\*1152, divided those six parts into two groups msa and mlp. Inside each group three small matrix with size 16\*1152 are corresponding shift, scale and gate. The following roughly capture how shift, scale and gate are used.

$$\mathbf{x} = \mathbf{x} + \text{gate} * \text{attn}(\text{modulate}(\text{scale} * \mathbf{x} + \text{shift}))$$
 (1)

Here modulate is just some function.

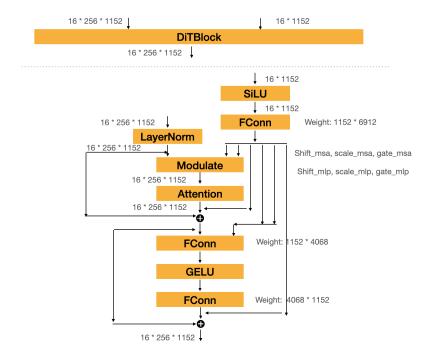


Figure 3: DiT Block

After the 28 repeated DiT block, there are normalization layer, fully connected layer, and unpatchify layer. The final output of diffusion transformer is 16 \* 32 \* 32 size.

#### 1.2 Backward Diffusion Process

Following the previous section, we extract one transformer block as the Fig 4

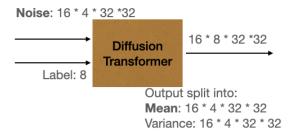


Figure 4: Transformer Block

The input are noise with size 16 \* 4 \* 32 \* 32 and label with size 8 and the output is the size 16 \* 8 \* 32 \* 32, which consists of two parts: the mean 8 \* 4 \* 32 \* 32 and the variance 8 \* 4 \* 32 \* 32. At this point, let's denote the noise as  $\mathbf{x}_t$  and the mean as  $\epsilon$ .

• Compute  $\mathbf{x}_0$ , based on  $\mathbf{x}_t = \sqrt{\bar{\alpha}_t}\mathbf{x}_0 + \sqrt{1-\bar{\alpha}_t}\epsilon$ , we have

$$\mathbf{x}_0 = \sqrt{\frac{1}{\bar{\alpha}_t}} \mathbf{x}_t - \sqrt{\frac{1 - \bar{\alpha}_t}{\bar{\alpha}_t}} * \epsilon \tag{2}$$

• Compute  $\tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0)$  and  $\tilde{\beta}_t$  based on the  $q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0) = \mathcal{N}(\mathbf{x}_{t-1}; \tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0), \tilde{\beta}_t I)$  where

$$\tilde{\beta}_{t} = \beta_{t} * \frac{1 - \bar{\alpha}_{t-1}}{1 - \bar{\alpha}_{t}}$$

$$\tilde{\mu}_{t}(\mathbf{x}_{t}, \mathbf{x}_{0}) = \frac{\beta_{t} \sqrt{\bar{\alpha}_{t-1}}}{1 - \bar{\alpha}_{t}} \mathbf{x}_{0} + \frac{(1 - \bar{\alpha}_{t-1})\sqrt{\alpha_{t}}}{1 - \bar{\alpha}_{t}} \mathbf{x}_{t}$$
(3)

Actually if we plug  $\mathbf{x}_0 = \sqrt{\frac{1}{\bar{\alpha}_t}}\mathbf{x}_t - \sqrt{\frac{1-\bar{\alpha}_t}{\bar{\alpha}_t}} * \epsilon$  to the  $\tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0)$ , which yields

$$\tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0) = \frac{1}{\bar{\alpha}_t} (\mathbf{x}_t - \frac{1 - \alpha_t}{\sqrt{1 - \bar{\alpha}_t}} \epsilon)$$
(4)

In the implementation, the authors computed  $\mathbf{x}_0$  first and then compute  $\tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0)$ , maybe because they would like to re-use some functions.

• Output sample based on t value

$$t = 0, \text{ sample} = \tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0)$$
  

$$t \neq 0, \text{ sample} = \tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0) + \tilde{\beta}_t * \text{ noise}$$
(5)

For the variance part, there are different strategies on how to compute variance either fixed or learned from models<sup>3</sup>.

So far we roughly present the structure of how to generate an image based on diffusion process if we can decode the sample 16\*4\*32\*32 through VAE decode, which will be discussed in the next section.

We include the Fig 5 to detail understand how the diffusion process is exactly implemented in the code base<sup>4</sup>.

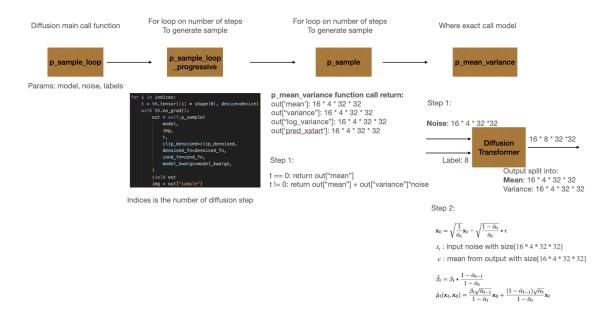


Figure 5: Diffusion Process in Implementation

We include some code explanation related the above process in the Appendix section 3.

<sup>&</sup>lt;sup>3</sup>Improved Denoising Diffusion Probabilistic Models

<sup>&</sup>lt;sup>4</sup>https://github.com/facebookresearch/DiT?tab=readme-ov-file

### 1.3 VAE Decoder

In the Fig 6, we present the entire network structure of VAE decoder model. After diffusion transformer stage, we have the de-noised (terminology in diffusion model) tensor with size of 16\*8\*32\*32. We ignore the half part of that matrix and feed the another half of matrix 8\*4\*32\*32 to VAE decoder model <sup>5</sup>. The first step is Post quantization convolutional layer, which I guess conducts operation on value level. After that, there is 2D convolutional layer, Unet Middle block, four Up Decoder Block, group normalization layer, SiLu, and convolutional layer. The final output of this network is 8 RGB images, that is, a tensor with size 8\*3\*256\*256.

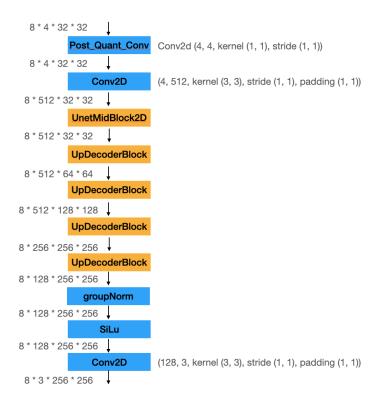


Figure 6: VAE Decoder Model

The Fig 7 shows the block structure for Unet Middle Block, which consists of some conventional layers such as group normalization layer, convolutional layer, attention layer and others. In this block, as seen the dimension of the tensor remains the same.

<sup>&</sup>lt;sup>5</sup>https://huggingface.co/stabilityai/sd-vae-ft-mse

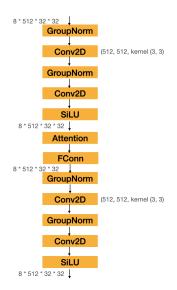


Figure 7: Unet Middle Block

The Fig 8 shows the block structure of Up Decoder Block, similarly which consists of some conventional layers and up sampling layer. One thing to note is that in this block spatial dimension is two time scaled up. In the implementation, up sampling layer is essentially using torch interpolate function with mode as nearest. The following is one of up sampling examples on the input 2\*2 matrix with the scale factor 2 and the mode being nearest.

$$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 1 & 2 & 2 \\ 1 & 1 & 2 & 2 \\ 3 & 3 & 4 & 4 \\ 3 & 3 & 4 & 4 \end{bmatrix}$$
 (6)

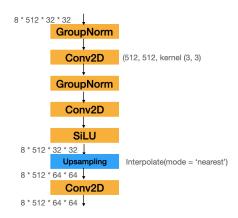


Figure 8: Up Decoder Block

## 2 The Training Stage

To be updated.

# 3 Appendix

## 3.1 Implementation notes for diffusion process

From the previous notes, we have

$$\mathbf{x}_t = \sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} * \epsilon \tag{7}$$

that is,

$$\mathbf{x}_0 = \sqrt{\frac{1}{\bar{\alpha}_t}} \mathbf{x}_t - \sqrt{\frac{1 - \bar{\alpha}_t}{\bar{\alpha}_t}} * \epsilon \tag{8}$$

Given  $\mathbf{x}_t$  and  $\mathbf{x}_0$ , we know  $\mathbf{x}_{t-1}$  is from the following posterior distribution

$$q(\mathbf{x}_{t-1}|\mathbf{x}_t, \mathbf{x}_0) = \mathcal{N}(\mathbf{x}_{t-1}; \tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0), \tilde{\beta}_t I)$$
(9)

where  $\tilde{\mu}_t(\mathbf{x}_t, \mathbf{x}_0)$  and  $\tilde{\beta}_t$  can be computed as

$$\tilde{\beta}_{t} = \beta_{t} * \frac{1 - \bar{\alpha}_{t-1}}{1 - \bar{\alpha}_{t}}$$

$$\tilde{\mu}_{t}(\mathbf{x}_{t}, \mathbf{x}_{0}) = \frac{\beta_{t} \sqrt{\bar{\alpha}_{t-1}}}{1 - \bar{\alpha}_{t}} \mathbf{x}_{0} + \frac{(1 - \bar{\alpha}_{t-1})\sqrt{\alpha_{t}}}{1 - \bar{\alpha}_{t}} \mathbf{x}_{t}$$
(10)

```
# calculations for posterior q(x_{t-1} \mid x_t, x_0)
self.posterior_variance = (
            betas * (1.0 - self.alphas_cumprod_prev) / (1.0 - self.
                                                    alphas_cumprod)
       )
self.posterior_mean_coef1 = (
            betas * np.sqrt(self.alphas_cumprod_prev) / (1.0 - self.
                                                    alphas_cumprod)
self.posterior_mean_coef2 = (
            (1.0 - self.alphas_cumprod_prev) * np.sqrt(alphas) / (1.0 -
                                                    self.alphas_cumprod)
def q_posterior_mean_variance(self, x_start, x_t, t):
        Compute the mean and variance of the diffusion posterior:
            q(x_{t-1} | x_t, x_0)
        assert x_start.shape == x_t.shape
        posterior_mean = (
            _extract_into_tensor(self.posterior_mean_coef1, t, x_t.shape) *
                                                     x_start
            + _extract_into_tensor(self.posterior_mean_coef2, t, x_t.shape)
        posterior_variance = _extract_into_tensor(self.posterior_variance,
                                               t, x_t.shape)
        posterior_log_variance_clipped = _extract_into_tensor(
            {\tt self.posterior\_log\_variance\_clipped}, \ {\tt t, \ x\_t.shape}
        assert (
            posterior_mean.shape[0]
            == posterior_variance.shape[0]
            == posterior_log_variance_clipped.shape[0]
            == x_start.shape[0]
        )
        return posterior_mean, posterior_variance,
                                                posterior_log_variance_clipped
```

$$\mathbf{x}_t = \sqrt{\bar{\alpha}_t} \mathbf{x}_0 + \sqrt{1 - \bar{\alpha}_t} \epsilon \tag{11}$$

In the above code, x\_start is  $\mathbf{x}_0$  in the Eq.11. \_extract\_into\_tensor function extract  $t^{th}$  element from self.sqrt\_alphas\_cumprod and broadcast as the same shape as x\_start, then element-wise product with x\_start.