

# Binary Search Tree ADT

In this laboratory you will:

- Create an implementation of the Binary Search Tree ADT using a linked tree structure
- Examine how an index can be used to retrieve records from a database file and construct an indexing program for an accounts database
- Create operations that compute the height of a tree and output the data items in a tree whose keys are less than a specified key
- Analyze the efficiency of your implementation of the Binary Search Tree ADT

## Objectives

## Overview

In this laboratory, you examine how a binary tree can be used to represent the hierarchical search process embodied in the binary search algorithm.

The binary search algorithm allows you to efficiently locate a data item in an array provided that each array data item has a unique identifier, called its **key**, and that the array data items are stored in order based on their keys. Given the following array of keys,

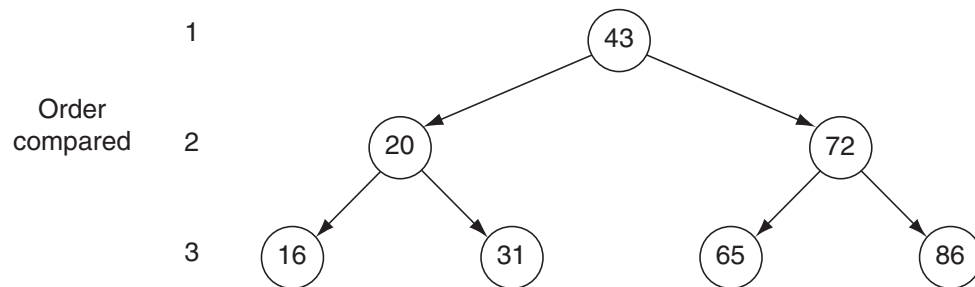
Index	0	1	2	3	4	5	6
Key	16	20	31	43	65	72	86

a binary search for the data item with key 31 begins by comparing 31 with the key in the middle of the array, 43. Because 31 is less than 43, the data item with key 31 must lie in the lower half of the array (entries 0–2). The key in the middle of this subarray is 20. Because 31 is greater than 20, the data item with key 31 must lie in the upper half of this subarray (entry 2). This array entry contains the key 31. Thus, the search terminates with success.

Although the comparisons made during a search for a given key depend on the key, the relative order in which comparisons are made is invariant for a given array of data items. For instance, when searching through the previous array, you always compare the key that you are searching for with 43 before you compare it with either 20 or 72. Similarly, you always compare the key with 72 before you compare it with either 65 or 86. The order of comparisons associated with this array is shown below.

Index	0	1	2	3	4	5	6
Key	16	20	31	43	65	72	86
Order compared	3	2	3	1	3	2	3

The hierarchical nature of the comparisons that are performed by the binary search algorithm is reflected in the following tree.



Observe that for each key  $K$  in this tree, all of the keys in  $K$ 's left subtree are less than  $K$  and all of the keys in  $K$ 's right subtree are greater than  $K$ . Trees with this property are referred to as **binary search trees**.

When searching for a key in a binary search tree, you begin at the root node and move downward along a branch until either you find the node containing the key or you reach a leaf node without finding the key. Each move along a branch corresponds to an array subdivision in the binary search algorithm. At each node, you move down to the left if the key you are searching for is less than the key stored in the node, or you move down to the right if the key you are searching for is greater than the key stored in the node.

## Binary Search Tree ADT

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### Data Items

The data items in a binary search tree are of generic type DT. Each data item has a key (of generic type KF) that uniquely identifies the data item. Data items usually include additional data. Objects of type KF must support the six basic relational operators. Objects of type DT must provide a functional `getKey()` that returns a data item's key.

### Structure

The data items form a binary tree. For each data item D in the tree, all the data items in D's left subtree have keys that are less than D's key and all the data items in D's right subtree have keys that are greater than D's key.

### Operations

`BSTree ()`

*Requirements:*

None

*Results:*

Constructor. Creates an empty binary search tree.

`~BSTree ()`

*Requirements:*

None

*Results:*

Destructor. Deallocates (frees) the memory used to store a binary search tree.

`void insert ( const DT &newDataItem ) throw ( bad_alloc )`

*Requirements:*

Binary search tree is not full.

*Results:*

Inserts `newDataItem` into a binary search tree. If a data item with the same key as `newDataItem` already exists in the tree, then updates that data item's nonkey fields with `newDataItem`'s nonkey fields.

`bool retrieve ( KF searchKey, DT &searchDataItem ) const`

*Requirements:*

None

*Results:*

Searches a binary search tree for the data item with key `searchKey`. If this data item is found, then copies the data item to `searchDataItem` and returns `true`. Otherwise, returns `false` with `searchDataItem` undefined.

```
bool remove ( KF deleteKey )
```

*Requirements:*

None

*Results:*

Deletes the data item with key `deleteKey` from a binary search tree. If this data item is found, then deletes it from the tree and returns `true`. Otherwise, returns `false`.

```
void writeKeys () const
```

*Requirements:*

None

*Results:*

Outputs the keys of the data items in a binary search tree. The keys are output in ascending order, one per line.

```
void clear ()
```

*Requirements:*

None

*Results:*

Removes all the data items in a binary search tree.

```
bool isEmpty () const
```

*Requirements:*

None

*Results:*

Returns `true` if a binary search tree is empty. Otherwise, returns `false`.

```
bool isFull () const
```

*Requirements:*

None

*Results:*

Returns `true` if a binary search tree is full. Otherwise, returns `false`.

```
void showStructure () const
```

*Requirements:*

None

*Results:*

Outputs the keys in a binary search tree. The tree is output with its branches oriented from left (root) to right (leaves); that is, the tree is output rotated counterclockwise 90 degrees from its conventional orientation. If the tree is empty, outputs "Empty tree". Note that this operation is intended for debugging purposes only.

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## Laboratory 11: Cover Sheet

Name \_\_\_\_\_ Date \_\_\_\_\_

Section \_\_\_\_\_

Place a check mark in the *Assigned* column next to the exercises your instructor has assigned to you. Attach this cover sheet to the front of the packet of materials you submit following the laboratory.

Activities	Assigned: Check or list exercise numbers	Completed
Prelab Exercise		
Bridge Exercise		
In-lab Exercise 1		
In-lab Exercise 2		
In-lab Exercise 3		
Postlab Exercise 1		
Postlab Exercise 2		
Total		



## Laboratory 11: Prelab Exercise

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Name \_\_\_\_\_ Date \_\_\_\_\_

Section \_\_\_\_\_

**Step 1:** Implement the operations in Binary Search Tree ADT using a linked tree structure. As with the linear linked structures you developed in prior laboratories, your implementation of the linked tree structure uses a pair of classes: one for the nodes in the tree (`BSTreeNode`) and one for the overall tree structure (`BSTree`). Each node in the tree should contain a data item (`dataItem`) and a pair of pointers to the node's children (`left` and `right`). Your implementation should also maintain a pointer to the tree's root node (`root`). Base your implementation on the following declarations from the file *bstree.hs*. An implementation of the `showStructure` operation is given in the file *show11.cpp*.

```
template < class DT, class KF >
class BSTreeNode                                // Facilitator for the BSTree class
{
    private:

        // Constructor
        BSTreeNode ( const DT &nodeDataItem,
                     BSTreeNode *leftPtr, BSTreeNode *rightPtr );

        // Data members
        DT dataItem;           // Binary search tree data item
        BSTreeNode *left,      // Pointer to the left child
        *right;                // Pointer to the right child

    friend class BSTree<DT,KF>;
};

template < class DT, class KF >                // DT : tree data item
class BSTree                                  // KF : key field
{
    public:

        // Constructor
        BSTree ();

        // Destructor
        ~BSTree ();

        // Binary search tree manipulation operations
        void insert ( const DT &newDataItem )    // Insert data item
            throw ( bad_alloc );
        bool retrieve ( KF searchKey, DT &searchDataItem ) const;
                                                    // Retrieve data item
        bool remove ( KF deleteKey );            // Remove data item
        void writeKeys () const;                 // Output keys
        void clear ();                           // Clear tree
};
```

```
// Binary search tree status operations
bool isEmpty () const;           // Tree is empty
bool isFull () const;           // Tree is full

// Output the tree structure -- used in testing/debugging
void showStructure () const;

private:

// Recursive partners of the public member functions -- insert
// prototypes of these functions here.
void showSub ( BSTreeNode<DT,KF> *p, int level ) const;

// Data member
BSTreeNode<DT,KF> *root;    // Pointer to the root node
};
```

**Step 2:** The declaration of the BSTree class in the file *bstree.hs* does not include prototypes for the recursive private member functions needed by your implementation of the Binary Search Tree ADT. Add these prototypes and save the resulting class declarations in the file *bstree.h*.

**Step 3:** Save your implementation of the Binary Search Tree ADT in the file *bstree.cpp*. Be sure to document your code.



## Laboratory 11: Bridge Exercise

Name \_\_\_\_\_ Date \_\_\_\_\_

Section \_\_\_\_\_

Check with your instructor whether you are to complete this exercise prior to your lab period or during lab.

The test program in the file *test11.cpp* allows you to interactively test your implementation of the Binary Search Tree ADT using the following commands.

Command	Action
+key	Insert (or update) the data item with the specified key.
?key	Retrieve the data item with the specified key and output it.
-key	Delete the data item with the specified key.
K	Output the keys in ascending order.
E	Report whether the tree is empty.
F	Report whether the tree is full.
C	Clear the tree.
Q	Quit the test program.

**Step 1:** Prepare a test plan for your implementation of the Binary Search Tree ADT. Your test plan should cover trees of various shapes and sizes, including empty, single branch, and single data item trees. A test plan form follows.

**Step 2:** Execute your test plan. If you discover mistakes in your implementation, correct them and execute your test plan again.

### Test Plan for the Operations in the Binary Search Tree ADT

<i>Test Case</i>	<i>Commands</i>	<i>Expected Result</i>	<i>Checked</i>