



# Lab Report - 04

Course No: 206

Course Title: Digital Logic Design

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Lab Report - 04Name of Experiment :

Construct and test various adders and sub-traction circuit.

Equipment :

1. 2 input AND Gate
2. 3 input AND Gate
3. 2 input OR Gate
4. 4 input OR Gate
5. X-OR Gate
6. Not Gate
7. 3 input OR Gate

A	B	S	C
0	0	0	0
1	0	1	0
1	1	0	1
0	1	1	1

A	B	S	C	o
0	0	0	0	0
1	0	1	0	0
0	1	1	0	0
1	1	0	1	0

Description:

An adder is a digital circuit that performs addition of numbers. In many computers and other kinds of processors adders are used in the arithmetic Logic units or other signed numbers representations require more logic around the basic adders. There are two types of adders; ① Half adders

② full adders.

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Half adder: The half adder circuit has two inputs ( $x$  and  $y$ ) which add two input digit and generates a carry and a sum. Half adder circuit doesn't consider the previous carry.

Full adder: The full adder circuit has three inputs ( $x$ ,  $y$  and  $z$ ) where  $z$  is a previous carry and ( $x$  and  $y$ ) are a literal. The full adder generates a carry and sum. It also considers the previous carry.

# Half Adders

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This is the truth table of Half adders

$x$	$y$	$C$	$S$
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

result

$$S = x'y + xy' = x \oplus y$$

$$C = xy$$

This is the truth table of Full adders

$x$	$y$	$z$	$C$	$S$
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

K-map of carry

$x \backslash yz$	00	01	11	10
0	0	0	1	0
1	0	1	1	1

$$C = xz + xy + yz$$

K-map of Sum

$x \backslash yz$	00	01	11	10
0	0	1	0	1
1	1	0	1	0

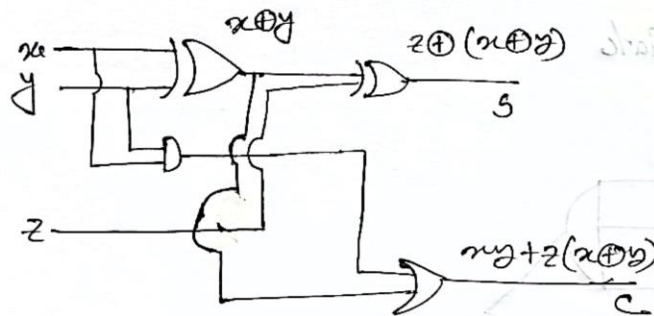
$$S = x'y'z + x'yz' + xy'z' + xyz$$



# Circuit of full adder using half adder:

## Equipment

- ① 2 AND Gate
- ② 2 XOR Gate
- ③ OR Gate



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Simplification Full adders using half adders

$$S = x'y'z + x'yz' + xy'z' + xyz$$

$$= z'(x'y + xy') + z(x'y' + xy)$$

$$= z'(x \oplus y) + z(x \oplus y)'$$

$$= z \oplus (x \oplus y) \quad [\text{Combine two half adders}]$$

01	11	10	00	$\Sigma$
1	1	0	0	0
1	1	1	0	1

$$C = xy + yz + zx$$

$$= xy + yz(x + x') + xz$$

$$= xy + xyz + x'yz + xz$$

$$= xy + x'yz + xyz + xz$$

$$= xy + x'yz + xz(y + 1)$$

$$= xy + x'yz + xz \cdot 1$$

$$= xy + x'yz + xz(y + y')$$

$$= xy + x'yz + xyz + xy'z$$

11	10	00	$\Sigma$
1	1	0	0
1	0	1	1

$$= xy(1+z) + x'yz + xy'z$$

$$= xy + x'yz + xy'z$$

$$= xy + z(x'y + xy')$$

$$= xy + z(x \oplus y) \quad [\text{combine two half adders}]$$

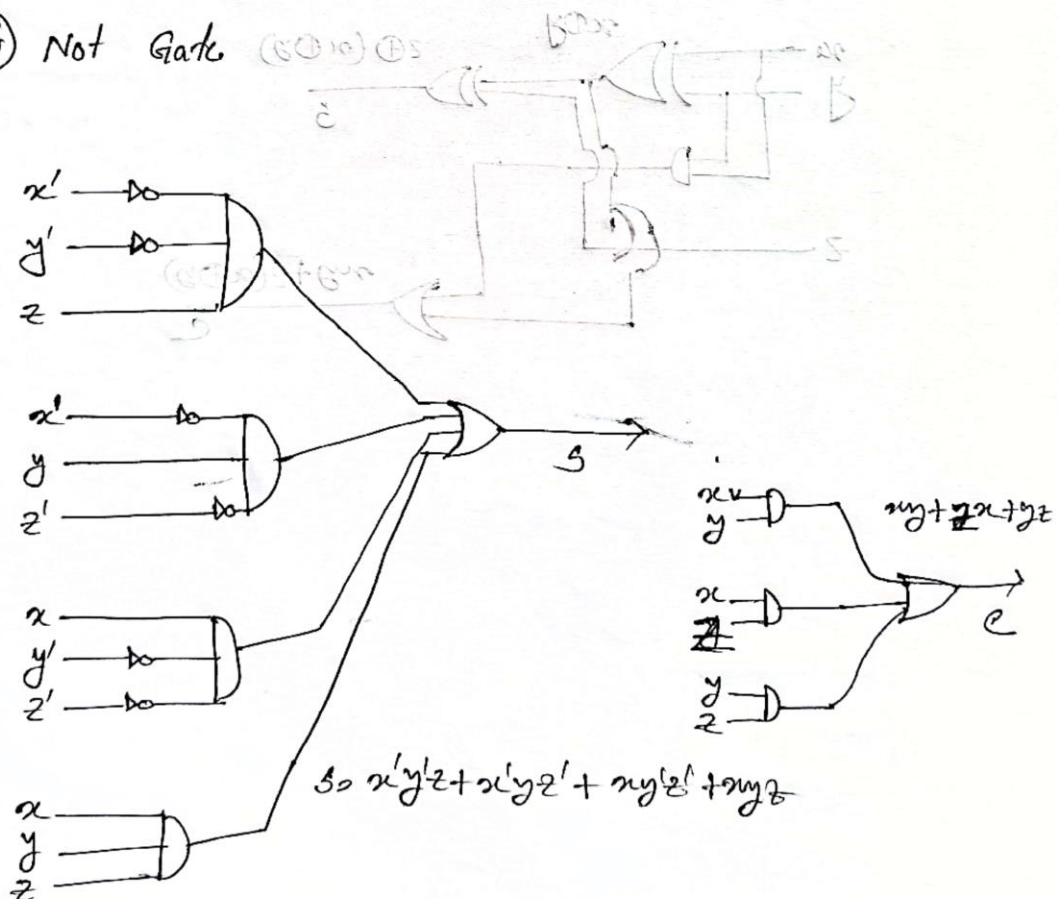
So, we can say, Full adder make with two half adders.

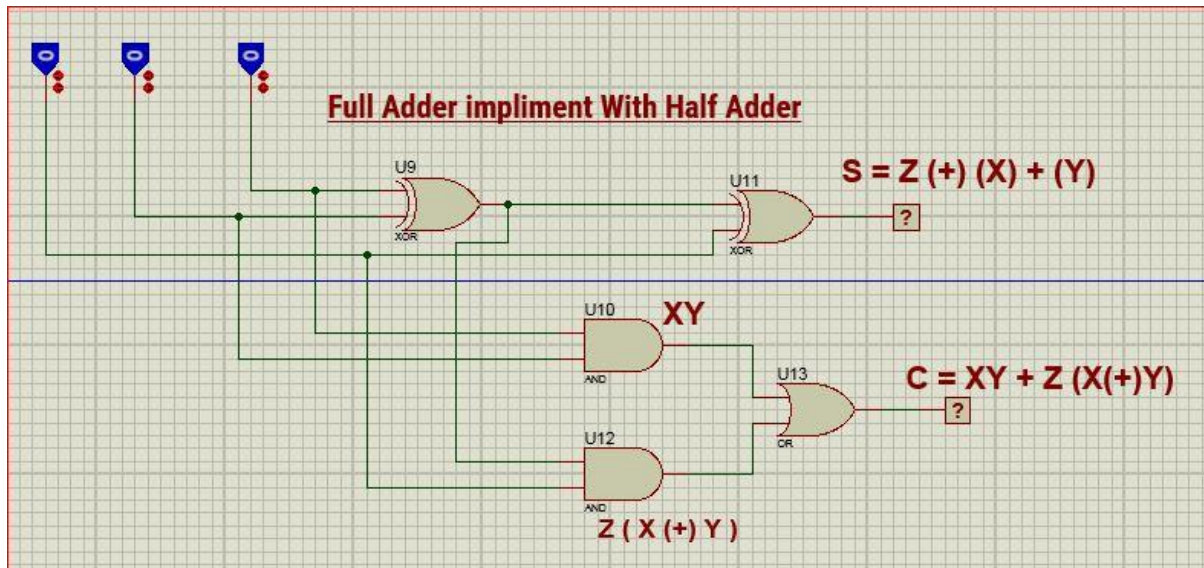
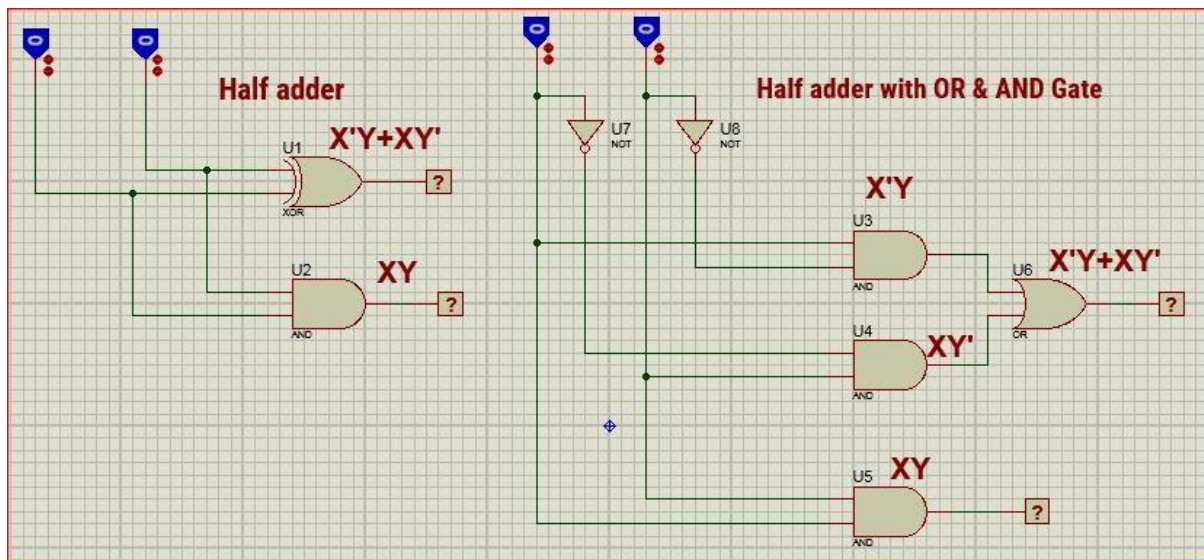


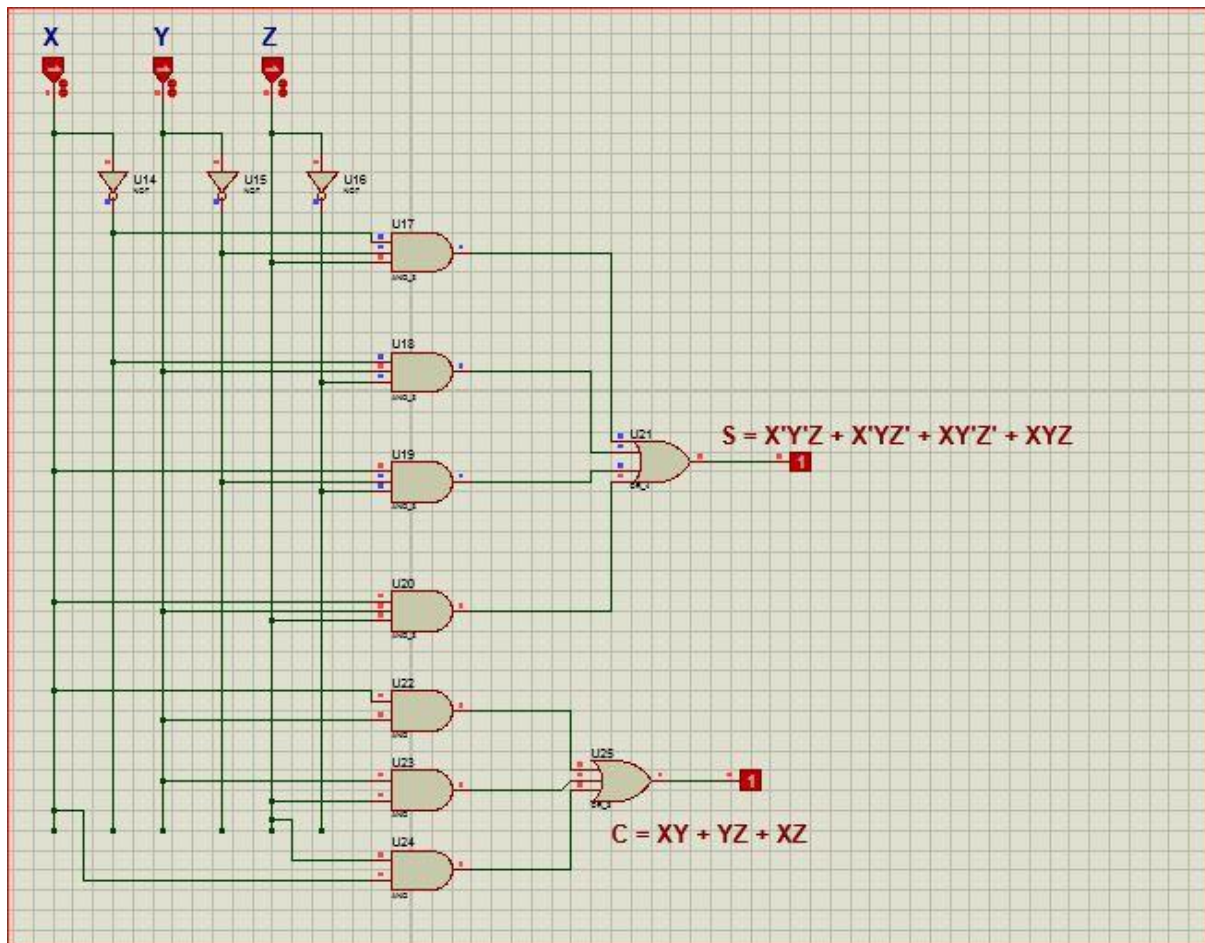
## Full adder using Basic Gates

### Equipment :-

- 3 input AND Gate
- 3 input OR Gate
- 4 input OR Gate
- 2 input AND Gate
- Not Gate







Full Adder Using Basic Gates

Description:-

A subtractor logic circuit for calculating the difference between two numbers. The minuend and the numbers to be subtracted.

Half subtractor:-

The half subtractor is also a building block for subtracting two binary numbers. It has two inputs and two outputs. This circuit is used to subtract two single bit binary numbers  $A$  and  $B$ . The  $D = \text{Sub}$  and  $B = \text{borrow out}$  are two output states of half subtractor.

Full subtractor:-

The full subtractor is used to subtract three 1-bit numbers  $A$ ,  $B$ , and  $C$ , which are minuend, subtrahend and borrow respectively. The full subtractor has three input states and two output states.  $\text{Sub} = D$  and  $\text{borrow} = B$



# Half Subtractor

A	B	Bn	D
0	0	0	0
0	1	1	1
1	0	0	1
1	1	0	0

Half Subtractor implement with K-map of Borrow

B	0	1
A	0	1
0	0	1
1	0	0

$$B = \bar{A}B$$

Half Subtractor implement with K-map of (D)

B	0	1
A	0	1
0	0	1
1	1	0

$$D = \bar{A}B + A\bar{B} = A \oplus B$$



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# Full Subtractor

A	B	C	Bn	D
0	0	0	0	0
0	0	1	1	1
0	1	0	1	1
0	1	1	1	0
1	0	0	0	1
1	0	1	0	0
1	1	0	0	0
1	1	1	1	1

$(A, B) \rightarrow \text{Input}$

$C \Rightarrow \text{Previous Borrow}$

## K-map for Borrow

A \ BC	00	01	11	10
0	0	1	1	1
1	0	0	1	0

$$\text{Borrow} = A'C + BC + A'B$$

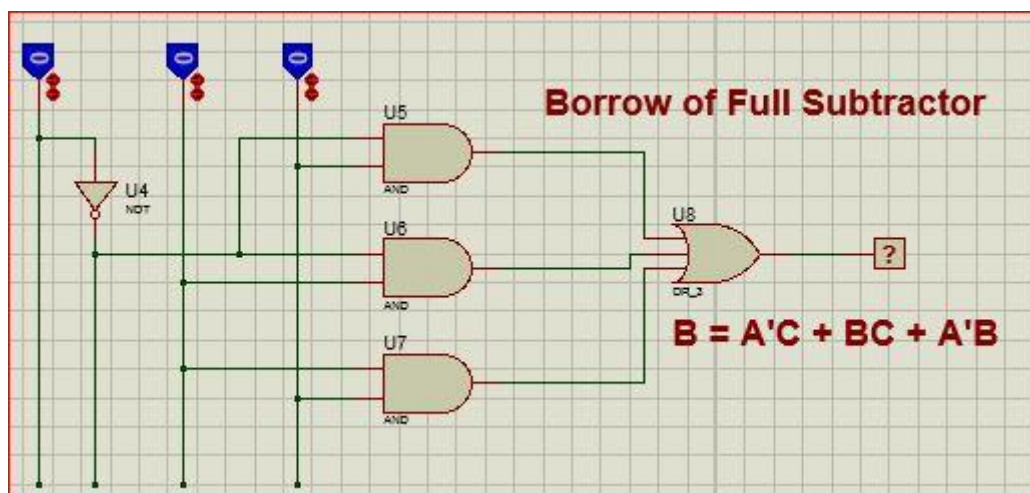
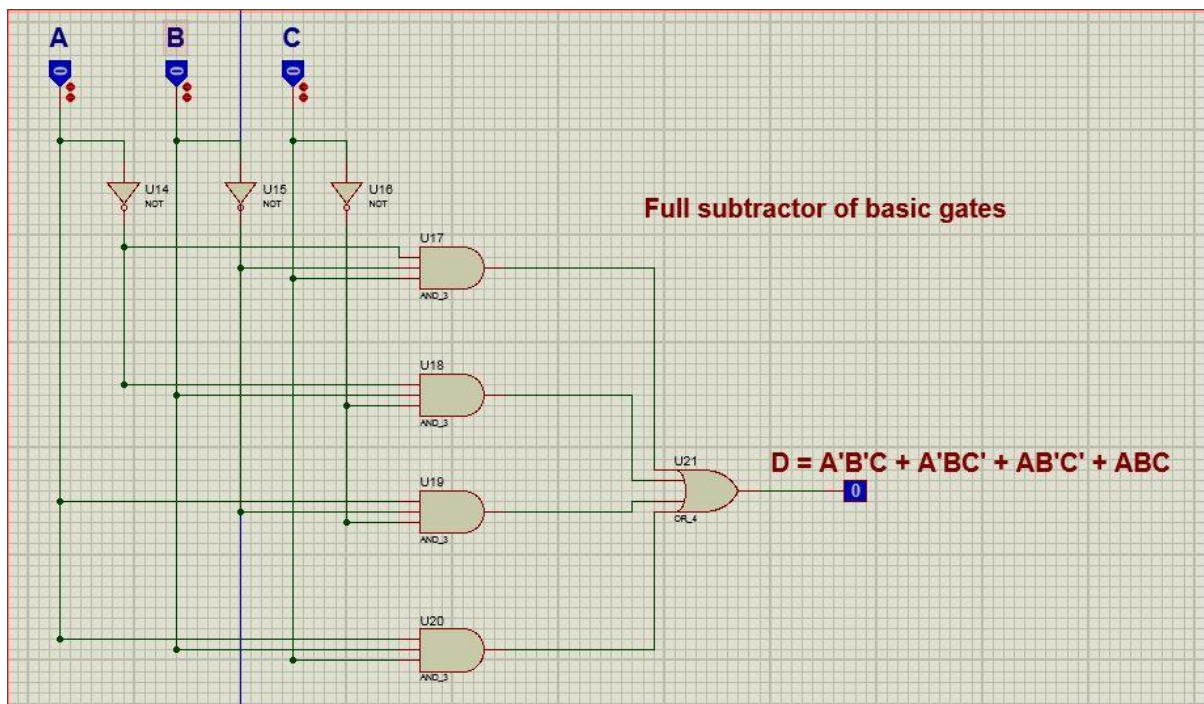
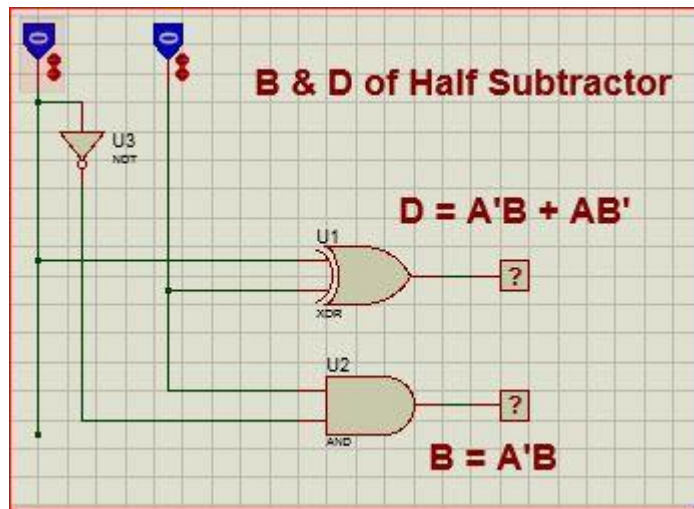
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Ques

K-map for  $D = \text{Sub}$

$A \backslash BC$	00	01	11	10
0	0	1	0	1
1	1	0	1	0

$$D = A'B'C + A'BC' + AB'C' + ABC$$





Conclusion:

1. we have learnt how to implement subtraction and Full subtraction.
2. we also know how to work Half adders and how to get full adders from two half adders.
3. we learnt that, Half adder is an adder which adds two binary digits together, resulting in a sum and carry.
4. we also learnt Half subtraction is another type of combinational circuit which is used to perform subtraction of two bits.
5. we also know, how to implement Half adder, full adder, and Half subtraction and full subtraction using in protues & software.