

1.1  $O(n)$

1.2  $O(n)$

### 3.1 Table

Sorting Method	Best Case	Worst Case
Bubble Sort Non-Recursive	$O(n^2)$	$O(n^2)$
Bubble Sort Recursive	$O(n^2)$	$O(n^2)$
Selection Sort (Non-recursive)	$O(n^2)$	$O(n^2)$
Insertion Sort (Non-recursive)	$O(n)$	$O(n^2)$
Merge Sort (Recursive)	$O(n \log(n))$	$O(n \log(n))$
Quick Sort (Recursive)	$O(n \log(n))$	$O(n^2)$

### 3.2 Step by step

4	77	98	30	20	50	77	22	49	2
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**Bubble Sort**

for ( $i < \text{length}$ ), for ( $j < \text{length} - i$ ), push the biggest number to the right

4	77	30	20	50	77	22	49	2	98
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4	30	20	50	77	22	49	2	77	98
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4	20	30	50	22	49	2	77	77	98
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... ..

apply same logic to the rest

**Selection Sort (Non-recursive)**

for ( $i < \text{length}$ ), for ( $i + 1 < j < \text{length} - i$ ), find min and swap with  $i$

2	77	98	30	20	50	77	22	49	4
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2	4	98	30	20	50	77	22	49	77
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2	4	20	30	98	50	77	22	49	77
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... ..

apply same logic to the rest

## Insertion Sort (Non-recursive)

for ( $i < \text{length}$ ), while ( $j > 0$  &&  $\text{array}[j] < \text{array}[j - 1]$ ), insert  $\text{array}[i]$  and shift  $\text{array}[j - 1]$  to the left

4	77	98	30	20	50	77	22	49	2
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4	77	98	30	20	50	77	22	49	2
---	----	----	----	----	----	----	----	----	---

4	77	98	30	20	50	77	22	49	2
---	----	----	----	----	----	----	----	----	---

4	30	77	98	20	50	77	22	49	2
---	----	----	----	----	----	----	----	----	---

4	20	30	77	98	50	77	22	49	2
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... ..

apply same logic to the rest

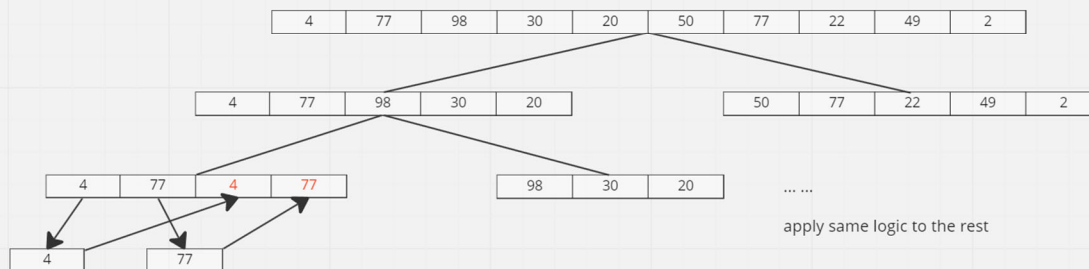
## Merge Sort

**Push:** while ( $\text{floor} < \text{ceiling}$ ),  $\text{mergeSort}(\text{array}, \text{floor}, \text{middle})$ ,  $\text{mergeSort}(\text{array}, \text{middle} + 1, \text{ceiling})$

**Pop:** when base case is reached,  $\text{merge}(\text{left sorted array}, \text{right sorted array})$

**\*merge:** while ( $\text{leftSortedArray.length} > \text{left Index}$  &&  $\text{rightSortedArray.length} > \text{right Index}$ ), compare and put the smaller one to  $\text{newArray}[i]$

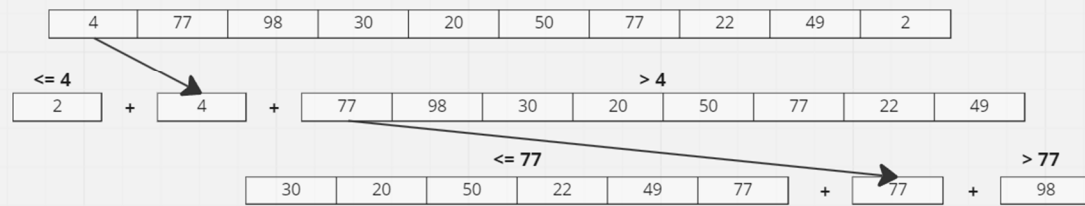
attach the rest of  $\text{leftSortedArray}/\text{rightSortedArray}$  to the end of  $\text{newArray}$



## Quick Sort

**Push:** `index = Partition (array, low, high), quickSort(array, low, index - 1), quickSort(array, index + 1, high)`

**Pop:** each stack push, the whole array is sorted in respective partitions



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apply same logic to the rest