Final Exam Section 1 Fall 2015, Part B

Computer Science Department, SJSU CS146: Data Structures and Algorithms Instructor: Katerina Potika

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Section	Points		
Question 1	Out of 6		
Question 2	Out of 16		
Question 3	Out of 10		
Question 4	Out of 16		
Total	Out of 48		

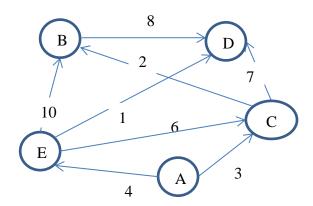
Duration 1 hour. Closed Books. Good luck!

Question 1

[6pts] Suppose that we define a different kind of graph, where we have weights on the vertices and not the edges. Does the shortest-paths problem make sense for this kind of graph? If so, give a precise and formal description of the problem and an application. If not, explain why not. Note we are not asking for an algorithm, just what the problem is or that it makes no sense.

Question 2

Use the following graph for this problem. Where needed and not determined by the algorithm, assume that any algorithm begins at node A.



a. Give both the adjacency matrix and adjacency list representations of this graph. (Specify which is which for full credit.)[3 pts/each]

Adjacency Matrix

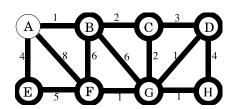
Adjacency Lists

- b. Give a valid topological sorting of the vertices in the graph.[4pts]
- c. Step through Dijkstra's Algorithm to calculate the single source shortest path from A to every other vertex. You need to show your steps in a table for full credit.[6pts]

Set S A B C D E

Question 3

Suppose we want to find the minimum spanning tree of the following graph.



(a) [5pts] Run Prim's algorithm; whenever there is a choice of nodes, always use alphabetic ordering (e.g., start from node A). Fill the next table showing the intermediate values of the priority queue for each vertex.

А	В	С	D	E	F	G	Н
0	∞	∞	8	8	8	8	∞

(b) [5pts] Run Kruskal's algorithm on the same graph. Show how the disjoint-sets data structure looks at every intermediate stage (use connected components).

Question 4

Identify a Celebrity

We call a person a celebrity among a group of n people, if that person knows nobody but is known to everybody else. The problem is to identify a celebrity by only asking questions to people of the form: "Do you know him/her?"

How would you model this problem with a directed graph that is represented with an adjacency matrix? In particular, answer the following questions [1pts/each]:

- (a) Who are the vertices of this graph?
- (b) What is the meaning of a directed edge in this graph?
- (c) What is a celebrity in our model (what property does it have)?
- (d) What is the equivalent (in graph terms) to the defined question? (how would reformulate it)
- (e) What do we want to minimize?
- (f) Can a group have more than one celebrity?

Design an efficient algorithm to identify a celebrity or determine that the group has no such person. How many questions does this algorithm need in the worst case? Justify **[10pts]**.

Hint: Think about exactly what information a single edge provides after answering the question.

SCRATCH PAPER