# Edexcel GCE

## Core Mathematics C1
### Advanced Subsidiary

Friday 5 June 2009 – Afternoon

Time: 1 hour 30 minutes

Examiner's use only

Team Leader's use only

| Question Number | Leave Blank |
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| 1 | |
| 2 | |
| 3 | |
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**Materials required for examination**
Mathematical Formulae
(Orange or Green)

**Items included with question papers**
Nil

**Calculators may NOT be used in this examination.**

## Instructions to Candidates

In the boxes above, write your centre number, candidate number, your surname, initials and signature.
Check that you have the correct question paper.
Answer ALL the questions.
You must write your answer for each question in the space following the question.

## Information for Candidates

A booklet 'Mathematical Formulae and Statistical Tables' is provided.
Full marks may be obtained for answers to ALL questions.
The marks for individual questions and the parts of questions are shown in round brackets: e.g. **(2)**.
There are 11 questions in this question paper. The total mark for this paper is 75.
There are 28 pages in this question paper. Any blank pages are indicated.

## Advice to Candidates

You must ensure that your answers to parts of questions are clearly labelled.
You should show sufficient working to make your methods clear to the Examiner.
Answers without working may not gain full credit.

*Turn over*

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1. Simplify

   (a) $\left(3\sqrt{7}\right)^2$

   **(1)**

   (b) $\left(8+\sqrt{5}\right)\left(2-\sqrt{5}\right)$

   **(3)**

**(Total 4 marks)**

2. Given that $32\sqrt{2} = 2^a$, find the value of $a$.

(3)

(Total 3 marks)

**3.** Given that $y = 2x^3 + \dfrac{3}{x^2}$, $x \neq 0$, find

(a) $\dfrac{dy}{dx}$

**(3)**

(b) $\int y \, dx$, simplifying each term.

**(3)**

**Question 3 continued**

4. Find the set of values of $x$ for which

(a) $4x - 3 > 7 - x$

**(2)**

(b) $2x^2 - 5x - 12 < 0$

**(4)**

(c) **both** $4x - 3 > 7 - x$ **and** $2x^2 - 5x - 12 < 0$

**(1)**

**Question 4 continued**

**5.** A 40-year building programme for new houses began in Oldtown in the year 1951 (Year 1) and finished in 1990 (Year 40).

The numbers of houses built each year form an arithmetic sequence with first term $a$ and common difference $d$.

Given that 2400 new houses were built in 1960 and 600 new houses were built in 1990, find

(a) the value of $d$,

**(3)**

(b) the value of $a$,

**(2)**

(c) the total number of houses built in Oldtown over the 40-year period.

**(3)**

**Question 5 continued**

**Q5**

**(Total 8 marks)**

**6.** The equation $x^2 + 3px + p = 0$, where $p$ is a non-zero constant, has equal roots.

Find the value of $p$.

**(4)**

**Question 6 continued**

H 3 4 2 6 2 A 0 1 1 2 8

**7.** A sequence $a_1, a_2, a_3, \ldots$ is defined by

$$a_1 = k,$$

$$a_{n+1} = 2a_n - 7, \quad n \geqslant 1,$$

where $k$ is a constant.

(a) Write down an expression for $a_2$ in terms of $k$.

**(1)**

(b) Show that $a_3 = 4k - 21$.

**(2)**

Given that $\displaystyle\sum_{r=1}^{4} a_r = 43$,

(c) find the value of $k$.

**(4)**

**Question 7 continued**

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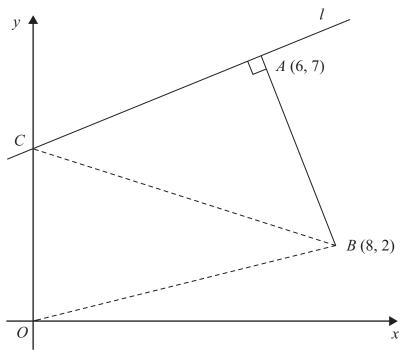
**8.**



**Figure 1**

The points *A* and *B* have coordinates (6, 7) and (8, 2) respectively.

The line *l* passes through the point *A* and is perpendicular to the line *AB*, as shown in Figure 1.

(a)  Find an equation for *l* in the form $ax + by + c = 0$, where *a*, *b* and *c* are integers.

**(4)**

Given that *l* intersects the *y*-axis at the point *C*, find

(b)  the coordinates of *C*,

**(2)**

(c)  the area of $\triangle OCB$, where *O* is the origin.

**(2)**

**Question 8 continued**

H 3 4 2 6 2 A 0 1 5 2 8

**Question 8 continued**

**Question 8 continued**

(Total 8 marks)

Q8

**9.**

$$f(x) = \frac{\left(3 - 4\sqrt{x}\right)^2}{\sqrt{x}}, \quad x > 0$$

(a) Show that $f(x) = 9x^{-\frac{1}{2}} + Ax^{\frac{1}{2}} + B$, where $A$ and $B$ are constants to be found.

**(3)**

(b) Find $f'(x)$.

**(3)**

(c) Evaluate $f'(9)$.

**(2)**
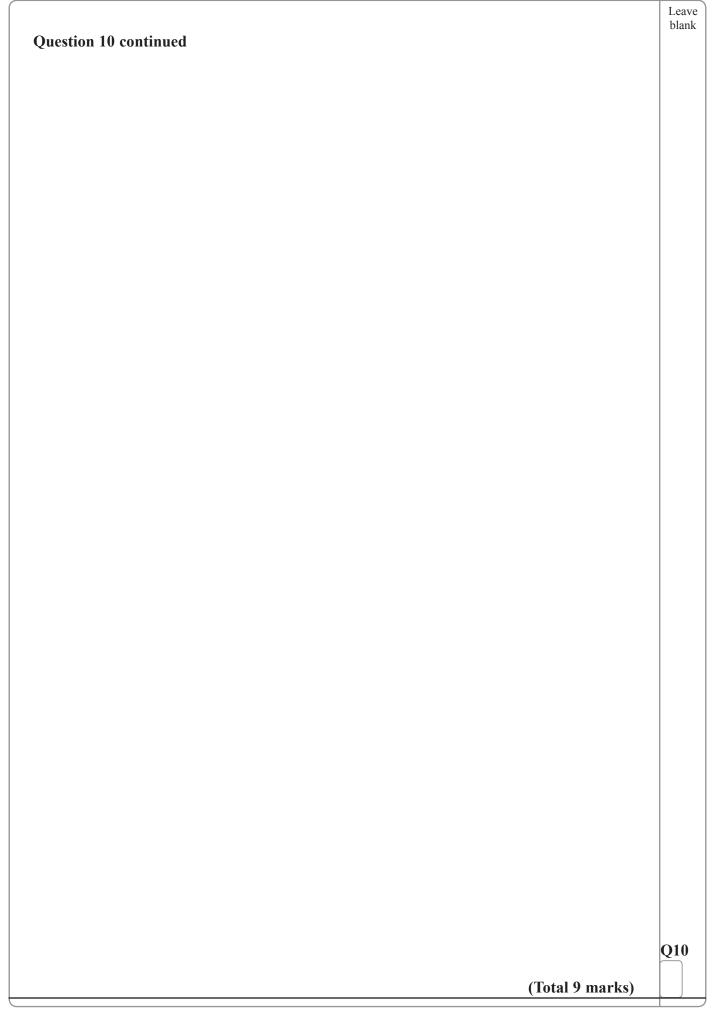
**Question 9 continued**

H 3 4 2 6 2 A 0 1 9 2 8

**Question 9 continued**

**Question 9 continued**

(Total 8 marks)

**Q9**

**10.** (a) Factorise completely $x^3 - 6x^2 + 9x$

(3)

(b) Sketch the curve with equation

$$y = x^3 - 6x^2 + 9x$$

showing the coordinates of the points at which the curve meets the $x$-axis.

(4)

Using your answer to part (b), or otherwise,

(c) sketch, on a separate diagram, the curve with equation

$$y = (x - 2)^3 - 6(x - 2)^2 + 9(x - 2)$$

showing the coordinates of the points at which the curve meets the $x$-axis.

(2)

**Question 10 continued**

H 3 4 2 6 2 A 0 2 3 2 8

**Question 10 continued**

$\text{H 3 4 2 6 2 A 0 2 4 2 8}$

**Question 10 continued**

**(Total 9 marks)**

H 3 4 2 6 2 A 0 2 5 2 8

**11.** The curve $C$ has equation

$$y = x^3 - 2x^2 - x + 9, \quad x > 0$$

The point $P$ has coordinates $(2, 7)$.

(a) Show that $P$ lies on $C$.

**(1)**

(b) Find the equation of the tangent to $C$ at $P$, giving your answer in the form $y = mx + c$, where $m$ and $c$ are constants.

**(5)**

The point $Q$ also lies on $C$.

Given that the tangent to $C$ at $Q$ is perpendicular to the tangent to $C$ at $P$,

(c) show that the $x$-coordinate of $Q$ is $\dfrac{1}{3}\left(2 + \sqrt{6}\right)$.

**(5)**

**Question 11 continued**

H 3 4 2 6 2 A 0 2 7 2 8

**Question 11 continued**

**(Total 11 marks)**

**TOTAL FOR PAPER: 75 MARKS**

**END**

H 3 4 2 6 2 A 0 2 8 2 8