



# Strategic PMU Placement for Secure and Resilient Power Grids

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# Introduction

- **Power Grid:** electrical network that delivers power from generators to loads
- **Network:** a bus topology where every element is connected through a line (bus)
- **Phasor Measurement Unit (PMU):** a device used to measure voltage and current in phase and amplitude

It is capable to deliver measurement by using Global Positioning System GPS, taking up to 60 measurements per second.

Cost per PMU: roughly \$40,000

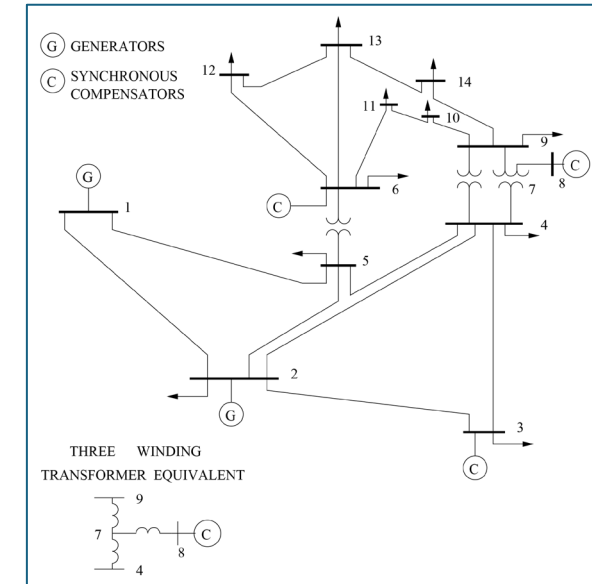
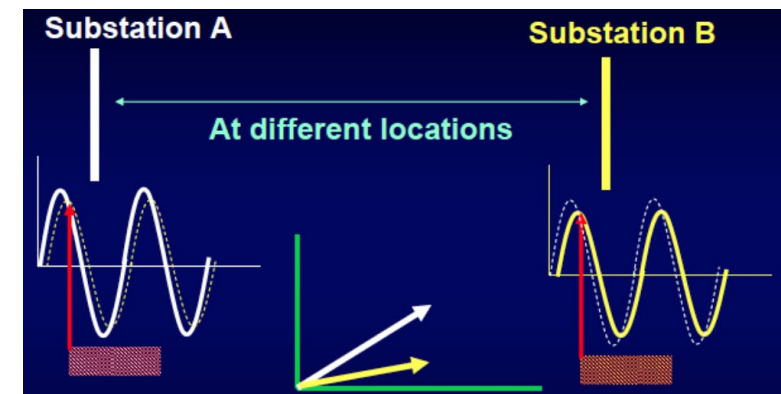


Figure 1: Ali R. Al-Roomi (2015). Power Flow Test Systems Repository [<https://al-roomi.org/power-flow>]. Halifax, Nova Scotia, Canada: Dalhousie University, Electrical and Computer Engineering



# Motivation

- Power Grids are crucial in current society, lot of power is demanded, and generators can only produce a limited level of power.
- Bus network systems are designed to produce and provide the power to the needed areas

These networks to work efficiently, they need to be monitored and accurately acquire them power data.

- PMUs with their synchronized phasor measurements can monitor and facilitate maintenance of the power network
- But, due to the high cost per PMU device, there cannot be a PMU per node.

- ✓ Designing a strategy to optimize the allocation of PMUs to ensure observability while considering:
  - Cost per PMU
  - Network topology
  - Types of nodes/buses

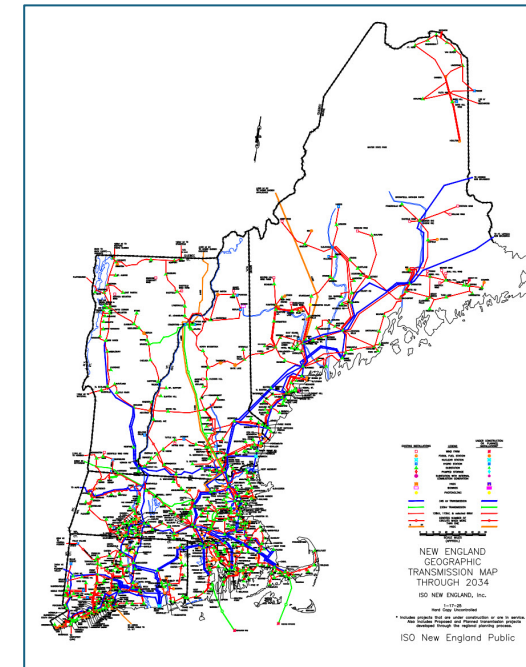
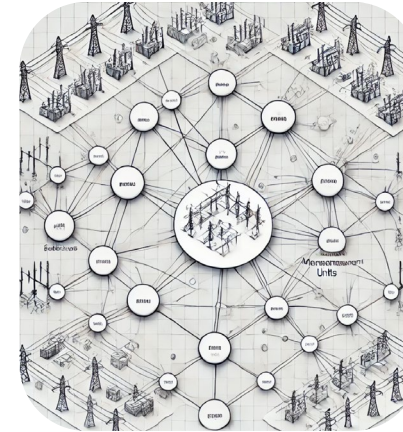
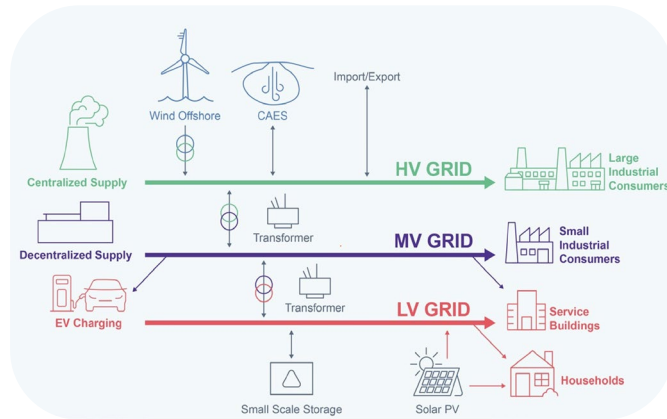


Figure 3: New England Geographic Transmission Line, ISO New England Inc,

# Research Overview



Modern Power  
Grid Observability Issues due  
to insufficient Monitoring  
Devices

Phasor  
Measurement  
Units (PMUs)  
Collecting  
Data

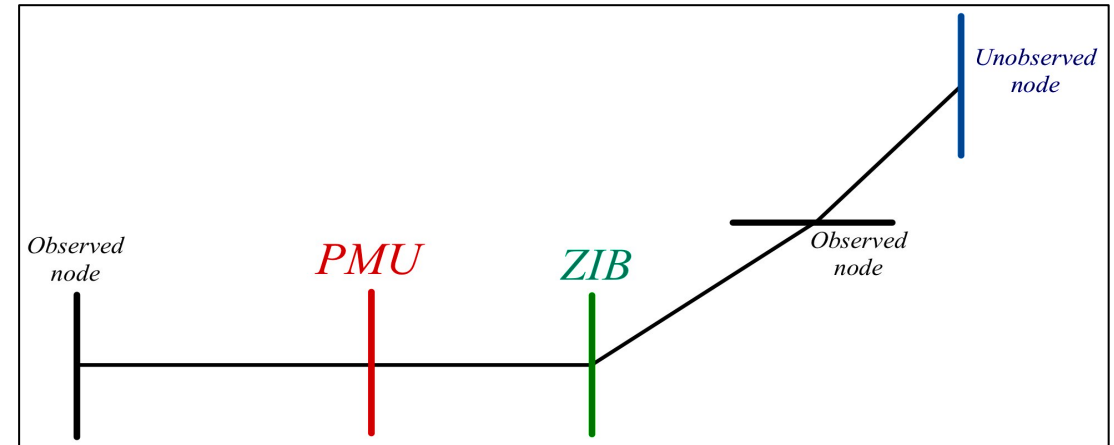
Optimal  
Placement of  
PMUs for Grid  
Control



# Preliminary Definitions

- Observability: the ability to measure a system's inputs and output data:
- PMU facilitates observability for the node it resides and adjacent nodes
- Power grids will require at **least** 100% observability on any network.
- Incrementation of observability percentage will:
  - Increase the number of PMU needed
  - Increase monitoring around CN
  - Increase the total cost

Observability depth system:



- Zero injection Bus (ZIB): buses that don't consume nor produce power
- Critical Node (CN): node that is directly connected to a generator



# Notation

- Bus-Node connection and constrains.

$i, j \rightarrow$  bus index

$\Omega_B \rightarrow$  Set of all busses

$\Omega_{ij} \rightarrow$  Set of bus  $i$  connected to  $j$

$\gamma_i \rightarrow$  Observability, integer variable

$$a_i = \begin{cases} 1 & \text{node contains a PMU} \\ 0 & \text{else} \end{cases}$$

$c \rightarrow$  cost per PMU

$n \rightarrow$  number of PMU channels used

$C_i \rightarrow$  total PMU cost based on  $n$

- Consideration of ZIBs:

$\Omega_Z \rightarrow$  Set of ZIBs

$\Omega_{Za} \rightarrow$  Set of adjacent buses to ZIBs

$\Omega_n \rightarrow$  Set of normal Buses (Not ZIBs or CN)

- Consideration of critical nodes:

$\Omega_C \rightarrow$  Set of critical nodes

$$\begin{aligned}
 & \text{Critical nodes} \\
 & a_i + \sum_{j \in \Omega_{ij}^l} a_j \geq 1 + \gamma_i \quad \forall i \in \Omega_c \\
 & \text{Normal Buses} \\
 & a_i + \sum_{j \in \Omega_{ij}^l} a_j \geq 1 \quad \forall i \in \Omega_n \\
 & \text{Abnormal buses (not in normal set, not CN)} \\
 & \sum_{j \in \Omega_{ia}^l} \left( a_a + \sum_{j \in \Omega_{aj}^l} a_j \right) \geq |\Omega_{za}| - 1 \quad \forall i \in \Omega_{za}
 \end{aligned}$$

# Methodology

## Objective Functions

Minimization of PMU's based on cost

$$C_i = (1 + 0.1 * n)c$$

$$\min OF = \sum_{i \in \Omega_B} C_i * a_i$$

Maximizing Observability

$$\gamma_i \geq 1$$

$$\max OBS = \sum_{i \in \Omega_B} \gamma_i$$

Critical nodes

$$a_i + \sum_{j \in \Omega_{ij}^l} a_j \geq 1 + \gamma_i \quad \forall i \in \Omega_c$$

Normal Buses

$$a_i + \sum_{j \in \Omega_{ij}^l} a_j \geq 1 \quad \forall i \in \Omega_n$$

Abnormal buses (not in normal set, not CN)

$$\sum_{j \in \Omega_{ia}^l} \left( a_a + \sum_{j \in \Omega_{aj}^l} a_j \right) \geq |\Omega_{za}| - 1 \quad \forall i \in \Omega_{za}$$





# Optimal PMU placement in 30-IEEE

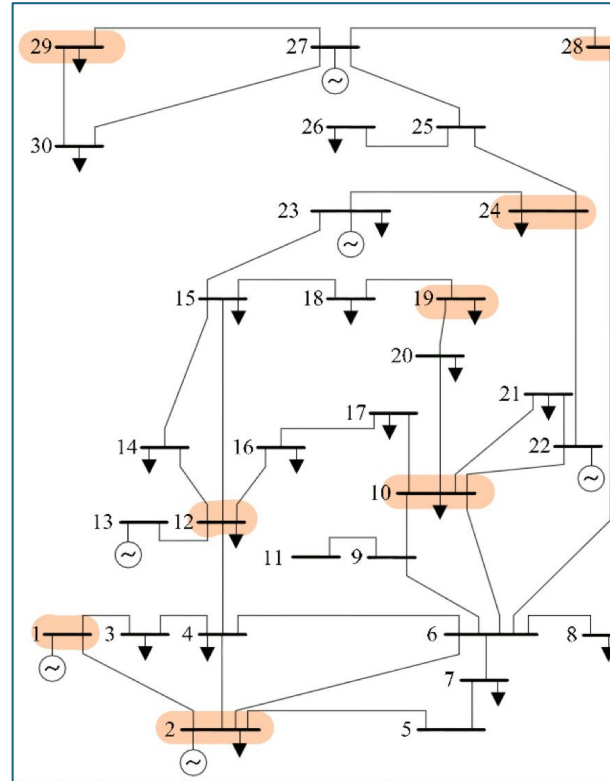
## Observations:

Minimum number of PMUs needed to obtain 100% observability in the IEE-30 bus system

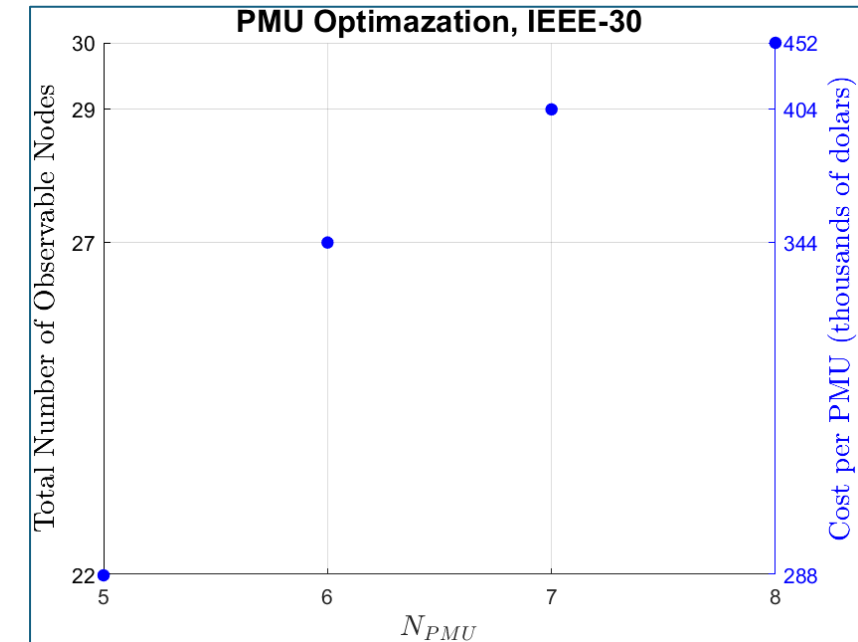
- $N_{PMU} = 8$

Cost per PMU varies based on the number of channels needed at the node it resides.

- Final cost based in  $N_{PMU}$ :
  - Total cost:  $C = \text{Cost based on channel} * c$
  - $c =$  is the cost per PMU (i.e.  $c = \$43,400$ )



$$N_{PMU} = 8$$







# Optimal PMU placement in 57-IEEE

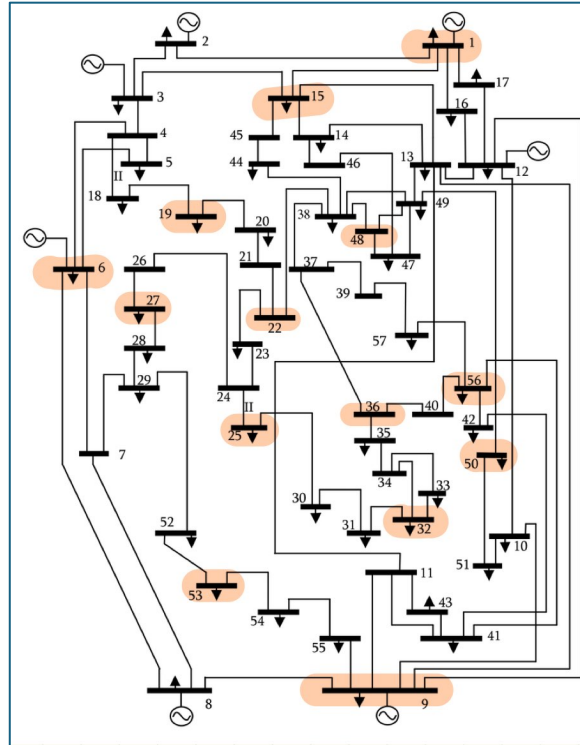
## Observations:

Minimum number of PMUs needed to obtain 100% observability in the IEE-30 bus system

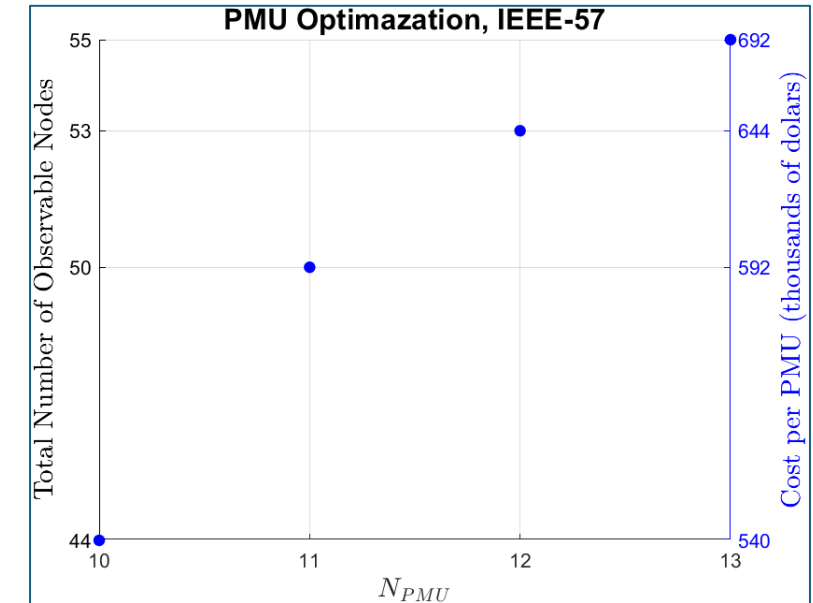
- $N_{PMU} = 8$

Cost per PMU varies based on the number of channels needed at the node it resides.

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$$N_{PMU} = 8$$





# Optimal PMU placement in 118-IEEE

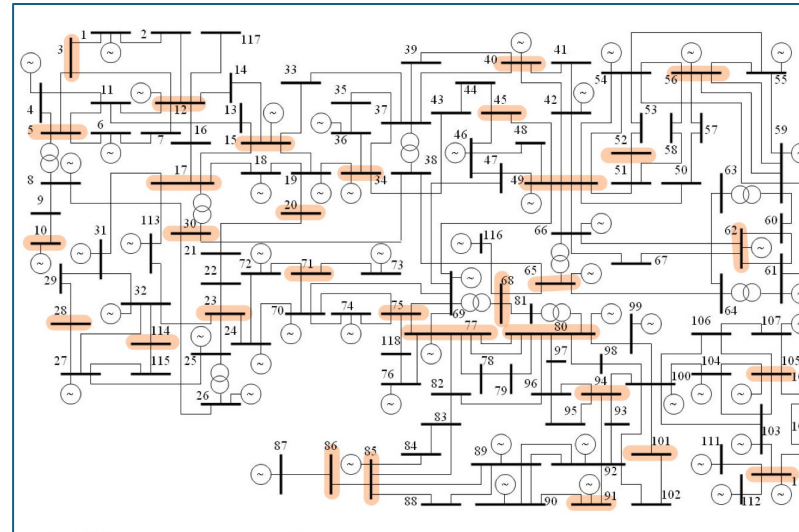
## Observations:

Minimum number of PMUs  
needed to obtain 100%  
observability in the IEEE-30 bus  
system

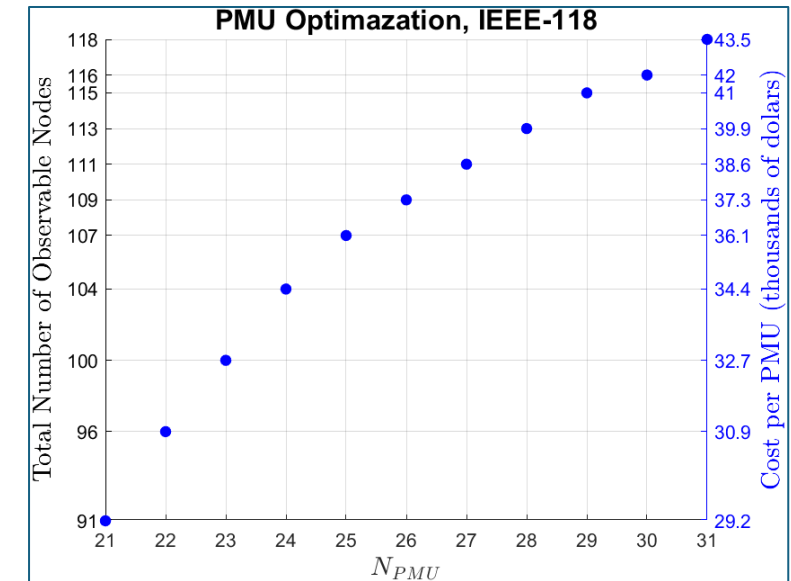
- $N_{PMU} = 31$

Cost per PMU varies based on the  
number of channels needed at the  
node it resides.

- Final cost based in  $N_{PMU}$ :
  - Total cost:  $C = \text{Cost based on channel} * c$
  - $c =$  is the cost per PMU (i.e.  $c = \$43,400$ )



$N_{PMU} = 31$





# Conclusion

- Reflection



