

**Swinburne University of Technology***Faculty of Science, Engineering and Technology***FINAL EXAM COVER SHEET**

**Subject Code:** COS30008  
**Subject Title:** Data Structures & Patterns  
**Due date:** June 3, 2021, 13:00  
**Lecturer:** Dr. Markus Lumpe

**Your name:** Zoie Tad-y **Your student id:** 102884743

Check	Wed 08:30	Wed 10:30	Wed 16:30	Thurs 08:30	Thurs 10:30	Thurs 14:30	Thurs 16:30	Fri 08:30	Fri 10:30	Fri 14:30
Tutorial		X								

Marker's comments:

Problem	Marks	Time Estimate in minutes	Obtained
1	50	20	
2	54	15	
3	42	10	
4	60	15	
5	8+128=136	60	
Total	342	120	

This test requires approx. 2 hours and accounts for 50% of your overall mark.

**Problem 1****(50 marks)**

Answer the following questions in one or two sentences:

- a. How can we construct a tree where all subtrees have the same degree? (4 marks)

**1a)**

Predefine pointers to N number of nodes for each node created for a tree and make sure that the tree is strictly balanced. Degree being the number of child nodes for a specific node, setting a predefined definition that each node created will always point to either N number of nodes or 0 will ensure that each subtree will have the same degree.

- b. What are reference data members and how do we initialize them? (2 marks)

**1b)**

Reference data members are "variables" that serve as an alias to an existing value stored in memory. We can initialise a reference member by using the type followed by "&" and the name of the variable reference, and equating them to a variable.

- c. What is the difference between l-value and r-value references? (6 marks)

**1c)**

L value references point towards or reference to a specific section in memory that may contain value, r-value references are simply references to value that is short lived and is not stored in memory. In most reference and even earlier early c++ discussion, r value references are simply referred to as the opposite of l value references. Typically l value references are in the left hand side of the assignment operator, and r value references are found in the right hand side of assignment operator. However l values may also appear on the right hand side of the when it is being assigned to another l value reference. R value references can never be modified or assigned with another value.

- d. What is an object adapter? (6 marks)

**1d)**

An Object adapter is a wrapper around existing objects that allows them to collaborate. Certain definitions of certain objects prevent them from working with the functionality of other objects, in the event that we need that objects functionality to work with another object we create adapters to transform or format one or two of the objects to make them seemingly compatible.

- e. What is a key concept of an abstract data types? (4 marks)

**1e)**

Abstract data types are data types that defined by their functionality, not strictly how they are constructed declaratively. Being abstract means that it exists as a thought or idea, and being an ADT is just that, for example two stacks that a programtically defined differently are still considered stacks as long as they adhere to the abstract definition of what a stack is and can do.

f. How do we define mutual dependent classes in C++? (4 marks)

1f)

We can use forward declaration, declare at least one of the classes in the definition of the other through references or pointers.

g. What must a value-based data type define in C++? (2 marks)

1g)

Value based data types must define copy constructors.

h. What is the difference between copy constructor and assignment operator and how do we guarantee safe operation? (8 marks)

1h)

Copy constructors creates new instances of the a given object with the same information that object has through assigning a spearate memory block for the new object, assignment operators assigns the entirety of one object to another another object without allocating new memory space. To ensure safe operation deleting the old instances, or freeing the memory space allocated from the old instance should be done to prevent memory leaks.

i. What is the best-case, average-case, and worse-case for a lookup in a binary tree? (6 marks)

1i)

Worst case is  $O(n)$  where each node is visited, best case is  $O(1)$  where the node being looked up is the root, and average case if  $O(\log n)$  where approx half the nodes are visited in completing the look up.

j. You are given a set of  $n-1$  numbers out of  $n$  numbers. How do we find the missing number  $n_k$ ,  $1 \leq k \leq n$ , in linear time? (8 marks)

1j)

We can convert both sets, set one being the given  $n-1$  numbers, and the other being the general set of  $n$  numbers, to its canonical form by sorting which is  $O(n \log n)$  and then traverse both at the same time, when the values do not match the that means the value at that index on the general set of  $n$  numbers is the missing number. Linear traversal is  $O(n)$  so the entire process is  $O(n \log n) + O(n)$ , drop  $O(n \log n)$  since  $O(n)$  is larger, hence  $O(n)$

```
1
2 // COS30008, Final Exam, 2021
3
4 #pragma once
5
6 #include <stdexcept>
7
8 template<typename T>
9 class TTreePostfixIterator;
10
11 template<typename T>
12 class TTree
13 {
14 private:
15
16     T fKey;
17     TTree<T>* fLeft;
18     TTree<T>* fMiddle;
19     TTree<T>* fRight;
20
21     TTree() : fKey(T()) // use default constructor to initialize fKey
22     {
23         fLeft = &NIL; // loop-back: The sub-trees of a TTree object with
24         fMiddle = &NIL; // no children point to NIL.
25         fRight = &NIL;
26     }
27
28     void addSubTree( TTree<T>** aBranch, const TTree<T>& aTTree )
29     {
30         if ( !(*aBranch)->empty() )
31         {
32             delete *aBranch;
33         }
34
35         *aBranch = const_cast<TTree<T>*>(&aTTree);
36     }
37
38 public:
39
40     using Iterator = TTreePostfixIterator<T>;
41
42     static TTree<T> NIL; // sentinel
43
44     // getters for subtrees
45     const TTree<T>& getLeft() const { return *fLeft; }
46     const TTree<T>& getMiddle() const { return *fMiddle; }
47     const TTree<T>& getRight() const { return *fRight; }
48
49     // add a subtree
50     void addLeft( const TTree<T>& aTTree ) { addSubTree( &fLeft, aTTree ); }
51     void addMiddle( const TTree<T>& aTTree ) { addSubTree( &fMiddle, aTTree ); }
52     void addRight( const TTree<T>& aTTree ) { addSubTree( &fRight, aTTree ); }
```

```
53
54     // remove a subtree, may through a domain error
55     const TTree<T>& removeLeft() { return removeSubTree( &fLeft ); }
56     const TTree<T>& removeMiddle() { return removeSubTree( &fMiddle ); }
57     const TTree<T>& removeRight() { return removeSubTree( &fRight ); }
58
59     // Problem 1: TTree Basic Infrastructure
60
61     private:
62
63     // remove a subtree, may through a domain error
64     const TTree<T>& removeSubTree(TTree<T>** aBranch)
65     {
66         if (*aBranch == &NIL)
67         {
68             throw std::domain_error("Branch does not exist");
69         }
70
71         *aBranch = &NIL;
72     }
73
74     public:
75
76     // TTree 1-value constructor
77     TTree(const T& aKey) :fKey(aKey), fLeft(&NIL), fMiddle(&NIL), fRight(&NIL)
78     {}
79
80     // destructor (free sub-trees, must not free empty trees)
81     ~TTree()
82     {
83         if (empty())
84         {
85             throw domain_error("Empty TTree");
86         }
87         delete fLeft;
88         delete fMiddle;
89         delete fRight;
90
91     }
92
93
94     // return key value, may throw domain_error if empty
95     const T& operator*() const
96     {
97         if (empty())
98         {
99             throw std::domain_error("Empty Tree");
100         }
101
102         return fKey;
103     }
104
```

```
105 // returns true if this TTree is empty
106 bool empty() const
107 {
108     return this == &NIL;
109 }
110
111 // returns true if this TTree is a leaf
112 bool leaf() const
113 {
114     return fLeft->empty() && fMiddle->empty() && fRight->empty();
115 }
116
117 // Problem 2: TTree Copy Semantics
118
119 // copy constructor, must not copy empty TTree
120 TTree(const TTree<T>& aOtherTTree)
121 {
122     if (aOtherTTree.empty())
123     {
124         throw domain_error("Empty Tree.");
125     }
126
127     if (!aOtherTTree.empty())
128     {
129         fKey = aOtherTTree.fKey;
130
131         addRight(aOtherTTree.getRight());
132         addMiddle(aOtherTTree.getMiddle());
133         addLeft(aOtherTTree.getLeft());
134     }
135 }
136
137 // copy assignment operator, must not copy empty TTree
138 TTree<T>& operator=(const TTree<T>& aOtherTTree)
139 {
140     if (aOtherTTree.empty())
141     {
142         throw domain_error("Empty Tree.");
143     }
144
145     if (this != &aOtherTTree)
146     {
147         delete fLeft;
148         delete fMiddle;
149         delete fRight;
150
151         fKey = aOtherTTree.fKey;
152
153         addRight(aOtherTTree.getRight());
154         addMiddle(aOtherTTree.getMiddle());
155         addLeft(aOtherTTree.getLeft());
156     }
```

```
157     }
158     return *this;
159 }
160
161 // clone TTree, must not copy empty trees
162 TTree<T>* clone() const
163 {
164     if (!empty())
165     {
166         return new TTree(*this);
167     }
168 }
169
170 // Problem 3: TTree Move Semantics
171
172 // TTree r-value constructor
173 TTree(T&& aKey) :fKey(aKey), fLeft(&NIL), fMiddle(&NIL), fRight(&NIL)
174 {}
175
176 // move constructor, must not copy empty TTree
177 TTree(TTree<T>&& aOtherTTree)
178 {
179     if (aOtherTTree.empty())
180     {
181         throw domain_error("Empty Tree.");
182     }
183
184     if (this != &aOtherTTree)
185     {
186         fKey = aOtherTTree.fKey;
187         fRight = std::move(aOtherTTree.getRight());
188         fMiddle = std::move(aOtherTTree.getMiddle());
189         fLeft = std::move(aOtherTTree.getLeft());
190     }
191     return *this;
192 }
193
194
195 // move assignment operator, must not copy empty TTree
196 TTree<T>& operator=(TTree<T>&& aOtherTTree)
197 {
198     if (aOtherTTree.empty())
199     {
200         throw domain_error("Empty Tree.");
201     }
202
203     if (this != &aOtherTTree)
204     {
205         delete fLeft;
206         delete fMiddle;
207         delete fRight;
208     }
```

```
209         fKey = aOtherTTree.fKey;
210
211         fRight = std::move((aOtherTTree.getRight()));
212         fMiddle = std::move((aOtherTTree.getMiddle()));
213         fLeft = std::move((aOtherTTree.getLeft()));
214
215     }
216     return *this;
217 }
218
219 // Problem 4: TTree Postfix Iterator
220
221 // return TTree iterator positioned at start
222 Iterator begin() const
223 {
224     return Iterator(&this);
225 }
226
227 // return TTree iterator positioned at end
228 Iterator end() const
229 {
230     return begin().end();
231 }
232 };
233
234 template<typename T>
235 TTree<T> TTree<T>::NIL;
236
```



```
1
2 // COS30008, Final Exam, 2021
3
4 #pragma once
5
6 #include "TTree.h"
7
8 #include <stack>
9
10 template<typename S>
11 struct TTreeFrontier
12 {
13     size_t stage;                // frontier stages: 0, 1, 2
14     const TTree<S>* node;        // frontier TTree node
15
16     TTreeFrontier( const TTree<S>* aNode ) :
17         node(aNode),            // TTree node
18         stage(0)                // 0 - start right
19     {}
20 };
21
22 template<typename T>
23 class TTreePostfixIterator
24 {
25 private:
26     const TTree<T>* fTTree;      // 3-way tree
27     std::stack<TTreeFrontier<T>> fStack; // DFS traversal stack
28
29     using Frontier = TTreeFrontier<T>;
30
31     // push subtree starting with aNode
32     void push_nodes(const TTree<T>* aNode)
33     {
34         fStack.push(aNode);
35     }
36
37 public:
38
39     using Iterator = TTreePostfixIterator<T>;
40
41     Iterator operator++(int)
42     {
43         Iterator old = *this;
44
45         ++(*this);
46
47         return old;
48     }
49
50     bool operator!=( const Iterator& aOtherIter ) const
51     {
52         return !(*this == aOtherIter);
53     }
54 }
```

```
53     }
54
55     // iterator constructor
56     TTreePostfixIterator(const TTree<T>* aTTree)
57     {
58         fTTree = aTTree;
59
60         constTTree<T>* lNode = fTTree;
61
62         push_nodes(lNode);
63
64         while (!lNode.empty())
65         {
66
67             if (!lNode.GetRight()->empty())
68                 push_nodes(lNode.GetRight());
69             if (!lNode.GetMiddle()->empty())
70                 push_nodes(lNode.GetMiddle());
71             if (!lNode.GetLeft()->empty())
72                 push_nodes(lNode.GetLeft());
73
74             lNode = lNode.GetLeft();
75         }
76     }
77
78
79     // iterator dereference
80     const T& operator*() const
81     {
82         return *(fStack.top());
83     }
84
85     // prefix increment
86     Iterator& operator++()
87     {
88         fStack.pop();
89         return *this;
90     }
91
92     // iterator equivalence
93     bool operator==(const Iterator& aOtherIter) const
94     {
95         return fTTree == aOtherIter.fTTree;
96     }
97
98     // auxiliaries
99     Iterator begin() const
100    {
101        return Iterator(fTTree);
102    }
103    Iterator end() const
104    {
```

---

```
105     Iterator iter = *this;
106
107     iter.fStack = std::stack<const TTree<T>*>();
108
109     return iter;
110 }
111 };
112
```