

Matrix Algebra Review
Assignment 1
Points – 30

1.1

Vector Operations

$$\mathbf{u} = [-1 \quad 0 \quad 1] \quad \text{and} \quad \mathbf{v} = \begin{bmatrix} 2 \\ 4 \\ 6 \end{bmatrix}$$

- a. Find $\mathbf{u}^t = \text{transpose}(\mathbf{u})$. (Include the correct orientation as row or column.) (2 pts.)
- b. Find $\mathbf{v}^t = \text{transpose}(\mathbf{v})$. (Include the correct orientation as row or column.) (2 pts.)
- c. Find $\mathbf{u} \cdot \mathbf{v}$ (inner product). (2 pts.)
- d. Find $\mathbf{v} \times \mathbf{u}$ (outer product). (2 pts.)

1.2

Matrix Operations

$$\mathbf{A} = \begin{bmatrix} 1 & 0 & -1 \\ 2 & 1 & 0 \\ 0 & 1 & 2 \end{bmatrix} \quad \mathbf{B} = \begin{bmatrix} 1 & 0 \\ 1 & 1 \\ 1 & 0 \end{bmatrix} \quad \mathbf{C} = \begin{bmatrix} 2 & 0 & 0 \\ 0 & 1 & -1 \\ 0 & -1 & 1 \end{bmatrix}$$

- a. Find $\mathbf{B}^t = \text{transpose}(\mathbf{B})$. (2 pts.)
- b. Find $\mathbf{A} \mathbf{B}$. (2 pts.)
- c. Find $\mathbf{A} - \mathbf{C}$. (2 pts.)
- d. Find $\mathbf{C} \mathbf{A}$. (2 pts.)

1.3

Quadratic Form

$$\mathbf{A} = \begin{bmatrix} 2 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 1 & 0 \end{bmatrix} \quad \mathbf{b} = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$$

- a. Find $\mathbf{b}^t \mathbf{A} \mathbf{b}$. (5 pts.)

1.4

Solution of a set of linear equations

$$x + y - z = 0$$

$$x - y + z = 2$$

$$2x - 3y + z = -1$$

- a. Solve for x , y and z (**9 pts.**)