Regression Final

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Introduction

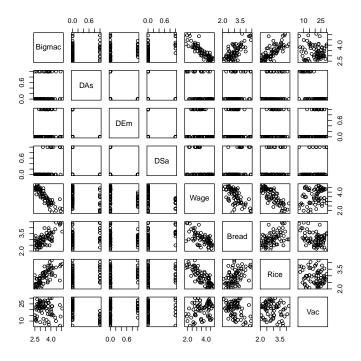
Regression final assignment using R

The complete source for this assignment is available on Github:

https://github.com/zollie/PASS

Problem 5.5

```
> ubs <- read.csv("~/R/PASS/Regression/RegressionFinal/ubs.csv")
> ubs$Region = factor(ubs$Region)
> head(ubs)
       City Region DAs DEm DSa Bigmac Wage Bread Rice Vac
1 Amsterdam NaWeOc 0
                         0
                             0 2.944 4.263 2.303 2.398
     Athens NaWeOc 0 0 0 3.401 3.829 2.565 3.296
                                                            22
 \hbox{3 Auckland NaWeOc} \quad \hbox{0} \quad \hbox{0} \quad \hbox{0} \quad \hbox{2.944 3.786 2.944 2.565} \quad \hbox{21} \\
   Bangkok Asia 1 0 0 3.807 2.653 3.761 3.296
5 Barcelona NaWeOc 0 0 0 3.045 4.119 2.833 2.079
    Beijing Asia 1 0 0 3.784 2.625 3.951 3.434
\mathbf{a}
> pairs(cbind(ubs$Bigmac,
               ubs$DAs, ubs$DEm, ubs$DSa,
               ubs$Wage, ubs$Bread,
               ubs$Rice, ubs$Vac),
        labels=cbind("Bigmac",
                      "DAs", "DEm", "DSa",
                      "Wage", "Bread",
                      "Rice", "Vac"))
```



There seems to be clear linear relationships with Wage and Bigmac (negative), Bread and Bigmac, and Rice and Bigmac. The predictive power for Vac of Bigmac is less clear.

There seems to be some correlation between Wage and Bread, and Wage and Rice.

b

```
> model_b <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread+Rice+Vac, data=ubs)
> stu_b <- rstudent(model_b)
> summary(model_b)
```

Call:

```
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
Vac, data = ubs)
```

Residuals:

Coefficients:

Estimate Std. Error t value Pr(>|t|)

```
(Intercept) 3.929449
                                     6.223 3.99e-08 ***
                         0.631421
DAs
            -0.207525
                         0.114411
                                    -1.814
                                             0.0743 .
DEm
             -0.104153
                         0.094352
                                    -1.104
                                             0.2737
DSa
                                     1.531
                                             0.1306
             0.181246
                         0.118389
Wage
            -0.576032
                         0.084254
                                    -6.837 3.37e-09 ***
             0.309707
                         0.074294
                                     4.169 9.25e-05 ***
Bread
Rice
             0.102046
                         0.088928
                                     1.148
                                             0.2554
             0.015415
                         0.005814
                                     2.651
                                             0.0101 *
Vac
```

Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ 1

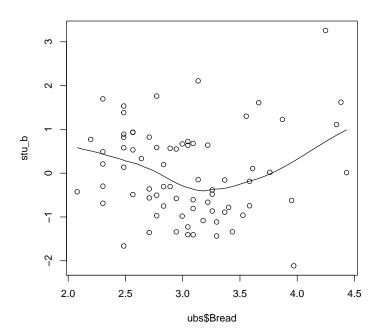
Residual standard error: 0.2331 on 65 degrees of freedom

Multiple R-squared: 0.8807, Adjusted R-squared: 0.8678

F-statistic: 68.54 on 7 and 65 DF, p-value: < 2.2e-16

> plot(ubs\$Bread, stu_b)

> scatter.smooth(ubs\$Bread, stu_b, span=.75)



The zero mean assumption can be tested with a loess line as above.

The constant variance assumption can be checked by ensuring the studentized

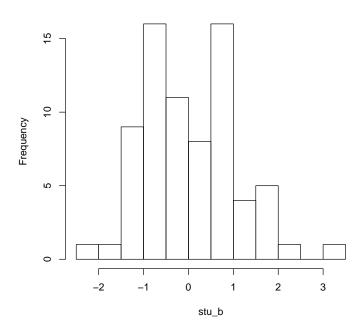
residuals are distributed evenly about the mean. That is, they have a mean of 0 and a standard deviation of 1.

The independence assumption can be checked with a quick glance at a residual scatter plot to ensure there are no non-random patterns.

The normality assumption can be checked with histograms and QQ plots as below.

> hist(stu_b)

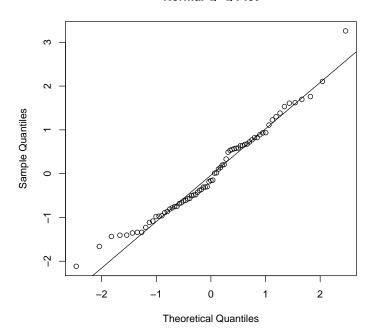
Histogram of stu_b



To check the constant vriance assumption we can use a histogram \dots

- > qqnorm(stu_b)
- > qqline(stu_b)

Normal Q-Q Plot



```
\mathbf{c}
> DasWage <- ubs$DAs*ubs$Wage
> DasBread <- ubs$DAs*ubs$Bread
> DasRice <- ubs$DAs*ubs$Rice
> DasVac <- ubs$DAs*ubs$Vac
> DemWage <- ubs$DEm*ubs$Wage
> DemBread <- ubs$DEm*ubs$Bread
> DemRice <- ubs$DEm*ubs$Rice
> DemVac <- ubs$DEm*ubs$Vac
> DsaWage <- ubs$DSa*ubs$Wage
> DsaBread <- ubs$DSa*ubs$Bread
> DsaRice <- ubs$DSa*ubs$Rice
> DsaVac <- ubs$DSa*ubs$Vac
> model_c <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread+Rice
                +Vac+DasWage+DasBread+DasRice+DasVac
                +DemWage+DemBread+DemRice+DemVac+DsaWage
                +DsaBread+DsaRice+DsaVac, data=ubs)
> summary(model_c)
Call:
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
```

```
Vac + DasWage + DasBread + DasRice + DasVac + DemWage + DemBread +
DemRice + DemVac + DsaWage + DsaBread + DsaRice + DsaVac,
data = ubs)
```

Residuals:

Min 1Q Median 3Q Max -0.32656 -0.12469 -0.01427 0.10780 0.49710

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
                        0.996793
(Intercept) 3.683085
                                   3.695 0.000522 ***
DAs
            -0.738972
                                  -0.506 0.614749
                        1.459567
DEm
            0.555744
                       1.383537
                                   0.402 0.689532
DSa
            -0.984978
                       2.907659
                                  -0.339 0.736134
Wage
            -0.478023
                        0.154255
                                  -3.099 0.003106 **
Bread
            0.082348
                        0.107430
                                   0.767 0.446765
Rice
            0.221956
                        0.122558
                                  1.811 0.075804 .
Vac
            0.022065
                        0.007127
                                   3.096 0.003131 **
                                  -0.551 0.583933
DasWage
            -0.103942
                        0.188635
DasBread
            0.567501
                        0.183594
                                  3.091 0.003176 **
DasRice
            -0.463639
                        0.202251
                                 -2.292 0.025882 *
DasVac
            0.054241
                        0.021818
                                  2.486 0.016104 *
                                  -0.240 0.811278
DemWage
            -0.051375
                        0.214087
DemBread
            0.208266
                        0.175752
                                  1.185 0.241303
DemRice
            -0.011267
                        0.203540
                                  -0.055 0.956064
DemVac
            -0.045066
                        0.015387
                                  -2.929 0.005005 **
DsaWage
            -0.130008
                        0.460941
                                  -0.282 0.779005
DsaBread
            0.690651
                        0.189595
                                  3.643 0.000614 ***
DsaRice
            -0.160711
                        0.384538
                                 -0.418 0.677684
DsaVac
            -0.007723
                        0.013443 -0.575 0.568045
___
```

Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ 1

Residual standard error: 0.1903 on 53 degrees of freedom

Multiple R-squared: 0.9351, Adjusted R-squared: 0.9119

F-statistic: 40.21 on 19 and 53 DF, p-value: < 2.2e-16

The 3 interactions with largest p-value are ...

- 1. DemWage
- 2. DemRice
- $3.\ {\bf DsaWage}$

```
\mathbf{d}
```

```
> model_d <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread+Rice+Vac+DasWage+DasBread+DasRice+DasVac+Dem
> summary(model_d)
```

Call:

```
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
Vac + DasWage + DasBread + DasRice + DasVac + DemBread +
DemVac + DsaBread + DsaRice + DsaVac, data = ubs)
```

Residuals:

Min 1Q Median 3Q Max -0.32589 -0.12401 -0.01427 0.10882 0.49611

Coefficients:

```
Estimate Std. Error t value Pr(>|t|)
             0.707313 5.476 1.06e-06 ***
(Intercept) 3.873477
      -0.929363
             1.256451 -0.740 0.46259
DEm
       0.282447
             0.565201
                   0.500 0.61922
DSa
             0.898657 -1.950 0.05615 .
      -1.752632
      -0.511492
             0.100893 -5.070 4.66e-06 ***
Wage
       0.075781
             0.102562
                   0.739 0.46306
Bread
Rice
       Vac
      DasWage
       DasBread
DasRice
      DasVac
      1.417 0.16210
      0.224488
DemBread
             0.158454
      DemVac
DsaBread
      0.714585
             DsaRice
      -0.076633
             0.179529 -0.427 0.67112
             0.012880 -0.564 0.57475
DsaVac
      -0.007269
```

Signif. codes: 0 $\hat{a}\ddot{A}\ddot{Y}***\hat{a}\ddot{A}\acute{Z}$ 0.001 $\hat{a}\ddot{A}\ddot{Y}**\hat{a}\ddot{A}\acute{Z}$ 0.01 $\hat{a}\ddot{A}\ddot{Y}*\hat{a}\ddot{A}\acute{Z}$ 0.05 $\hat{a}\ddot{A}\ddot{Y}.\hat{a}\ddot{A}\acute{Z}$ 0.1 $\hat{a}\ddot{A}\ddot{Y}$ $\hat{a}\ddot{A}\acute{Z}$ 1

```
Residual standard error: 0.1854 on 56 degrees of freedom
Multiple R-squared: 0.935, Adjusted R-squared: 0.9164
F-statistic: 50.33 on 16 and 56 DF, p-value: < 2.2e-16
```

> anova(model_d, model_c)

Analysis of Variance Table

```
Model 1: Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice + Vac + DasWage + DasBread + DasRice + DasVac + DemBread + DemVac + DsaBread + DsaRice + DsaVac
```

```
Model 2: Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice + Vac + DasWage +
    DasBread + DasRice + DasVac + DemWage + DemBread + DemRice +
    DemVac + DsaWage + DsaBread + DsaRice + DsaVac
 Res.Df
            RSS Df Sum of Sq
                                  F Pr(>F)
      56 1.9243
      53 1.9198 3 0.0045205 0.0416 0.9886
2
The p-value of .9886 > .05 therefore we cannot reject H_0. We can remove the 3
interactions with the largest p-value as statistically DemWage = DemRice =
DsaWage = 0
\mathbf{e}
> model_e <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread
                +Rice+Vac+DasBread+DasRice+DasVac
                +DemBread+DemVac+DsaBread, data=ubs)
> summary(model_e)
Call:
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
    Vac + DasBread + DasRice + DasVac + DemBread + DemVac + DsaBread,
    data = ubs)
Residuals:
    Min
               1Q Median
                                 3Q
                                         Max
-0.31559 -0.11941 -0.00559 0.10736 0.49558
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 4.110961
                        0.553962
                                  7.421 5.23e-10 ***
            -1.512860
                        0.632105 -2.393 0.019894 *
DAs
DEm
             0.212223
                       0.542260
                                  0.391 0.696935
DSa
            -2.219990 0.508840
                                 -4.363 5.23e-05 ***
Wage
            -0.541401
                        0.071295 -7.594 2.67e-10 ***
Bread
             0.065805
                        0.098576
                                  0.668 0.507019
Rice
             0.189425
                        0.073788
                                  2.567 0.012809 *
Vac
             0.020716
                        0.005185
                                 3.995 0.000182 ***
            0.608153
                        0.163987
                                   3.709 0.000463 ***
DasBread
DasRice
            -0.394569
                        0.137903 -2.861 0.005830 **
DasVac
             0.057814
                       0.019994
                                  2.892 0.005358 **
DemBread
             0.226347
                        0.154589
                                  1.464 0.148451
DemVac
            -0.042906
                        0.012967 -3.309 0.001600 **
DsaBread
            0.729123
                        0.153530
                                  4.749 1.35e-05 ***
Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ 1
```

```
Residual standard error: 0.1816 on 59 degrees of freedom
Multiple R-squared: 0.9342,
                             Adjusted R-squared: 0.9197
F-statistic: 64.47 on 13 and 59 DF, p-value: < 2.2e-16
> anova(model_e, model_d)
Analysis of Variance Table
Model 1: Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice + Vac + DasBread +
   DasRice + DasVac + DemBread + DemVac + DsaBread
Model 2: Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice + Vac + DasWage +
   DasBread + DasRice + DasVac + DemBread + DemVac + DsaBread +
   DsaRice + DsaVac
 Res.Df
          RSS Df Sum of Sq
                            F Pr(>F)
1
     59 1.9464
     56 1.9243 3 0.022104 0.2144 0.886
The p-value of .886 > .05 therefore we cannot reject H_0. We can remove the 3
interactions considered here.
f
> model_f <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread+Rice+
               Vac+DasBread+DasRice+DasVac+DemBread+DemVac+DsaBread, data=ubs)
> summary(model_f)
Call:
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
   Vac + DasBread + DasRice + DasVac + DemBread + DemVac + DsaBread,
   data = ubs)
Residuals:
            1Q Median
                           30
-0.31559 -0.11941 -0.00559 0.10736 0.49558
Coefficients:
          Estimate Std. Error t value Pr(>|t|)
(Intercept) 4.110961 0.553962 7.421 5.23e-10 ***
          -1.512860 0.632105 -2.393 0.019894 *
DAs
DEm
          DSa
          -0.541401
                    0.071295 -7.594 2.67e-10 ***
Wage
                    Bread
          0.065805
Rice
          Vac
         DasBread
```

DasRice -0.394569 0.137903 -2.861 0.005830 **

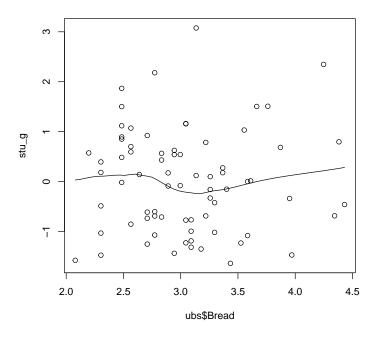
```
DasVac
             0.057814
                        0.019994
                                   2.892 0.005358 **
                                   1.464 0.148451
DemBread
             0.226347
                        0.154589
DemVac
            -0.042906
                        0.012967
                                  -3.309 0.001600 **
DsaBread
             0.729123
                        0.153530
                                   4.749 1.35e-05 ***
Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ 1
Residual standard error: 0.1816 on 59 degrees of freedom
Multiple R-squared: 0.9342,
                                    Adjusted R-squared: 0.9197
F-statistic: 64.47 on 13 and 59 DF, p-value: < 2.2e-16
H_0: DemBread = 0 \ H_a: D_{Em} \neq 0
.1484 > .05 therefore we do not reject H_0
> model_g <- lm(Bigmac ~ DAs+DEm+DSa+Wage+Bread+Rice+
+ Vac+DasBread+DasRice+DasVac+DemVac+DsaBread, data=ubs)
> summary(model_g)
lm(formula = Bigmac ~ DAs + DEm + DSa + Wage + Bread + Rice +
    Vac + DasBread + DasRice + DasVac + DemVac + DsaBread, data = ubs)
Residuals:
     Min
               1Q
                    Median
                                 3Q
                                         Max
-0.27016 -0.12943 0.00022 0.10108 0.51102
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) 3.861757
                        0.532170
                                  7.257 9.12e-10 ***
DAs
            -1.207924
                        0.602473
                                 -2.005 0.049487 *
DEm
             0.876811
                        0.299504
                                  2.928 0.004821 **
                                  -4.073 0.000138 ***
DSa
            -1.991641
                        0.488946
            -0.547934
                        0.071831
                                 -7.628 2.11e-10 ***
Wage
Bread
             0.154348
                        0.078586
                                  1.964 0.054162 .
Rice
             0.195452
                        0.074372
                                  2.628 0.010889 *
Vac
             0.021595
                        0.005199
                                  4.153 0.000105 ***
DasBread
             0.515727
                        0.152786
                                  3.375 0.001297 **
DasRice
            -0.406481
                        0.138969 -2.925 0.004856 **
DasVac
             0.056577
                        0.020165
                                  2.806 0.006759 **
DemVac
            -0.043681
                        0.013079
                                  -3.340 0.001446 **
                                  4.495 3.24e-05 ***
DsaBread
             0.641239
                        0.142652
```

Signif. codes: 0 âĂŸ***âĂŹ 0.001 âĂŸ**âĂŹ 0.01 âĂŸ*âĂŹ 0.05 âĂŸ.âĂŹ 0.1 âĂŸ âĂŹ 1

Residual standard error: 0.1834 on 60 degrees of freedom Multiple R-squared: 0.9318, Adjusted R-squared: 0.9182 F-statistic: 68.36 on 12 and 60 DF, p-value: < 2.2e-16

> stu_g <- rstudent(model_g)
> plot(ubs\$Bread, stu_g)

> scatter.smooth(ubs\$Bread, stu_g, span=.75)



The zero mean regression assumption now appears met.

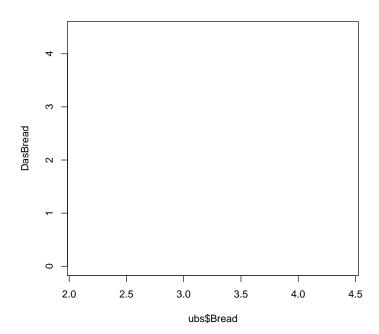
\mathbf{h}

 $\begin{array}{l} Bi\hat{g}mac = 3.861757 - 1.2709D_{As} + .8768D_{Em} - 1.99.16D_{Sa} - .5479Wage + .15348Bread + .195452Rice + .021595Vac + .515727DasBread - .406481DasRice + .056577DasVac - .043681DemVac + .641239DsaBread \end{array}$

i

Yes, the economist is correct. The coefficient for Wage is negative meaning as Wage increases Bigmac decreases all else held constant.

```
j
 > mWage <- mean(ubs$Wage)</pre>
> mBread <- mean(ubs$Bread)</pre>
 > mRice <- mean(ubs$Rice)</pre>
 > mVac <- mean(ubs$Vac)</pre>
 \hat{Bigmac} = 3.861757 - 1.2709D_{As} + .8768D_{Em} - 1.99.16D_{Sa} - mWage * Wage + 1.8980D_{Em} - 1.8980D_{Sa} - mWage * Wage + 1.8980D_{Em} - 1.8980D_{Sa} - mWage * Wage + 1.8980D_{Em} - 1.8980D_{Em
 .15348*Bread+mRice*Rice+mVac*Vac+.15348*DasBread-mRice*
DasRice + mVac * DasVac - mVac * DemVac + .15348 * DsaBread
> DasBread0 <- DasBread[ubs$DAs==0]</pre>
 > DasBread1 <- DasBread[ubs$DAs==1]</pre>
 > DsaBread0 <- DsaBread[ubs$DSa==0]</pre>
 > DsaBread1 <- DsaBread[ubs$DSa==1]</pre>
 > DasRice0 <- DasRice[ubs$DAs==0]
> DasRice1 <- DasRice[ubs$DAs==1]</pre>
 **I am having trouble producing the predictor effect plots below
> plot(ubs$Bread, DasBread, type="n")
> lines(sort(ubs$Bread[ubs$DasBread==0]), DasBread0[order(ubs$Bread[ubs$DasBread==0])])
 > lines(sort(ubs$Bread[ubs$DasBread==1]), DasBread1[order(ubs$Bread[ubs$DasBread==1])])
```



\mathbf{k}

$$\begin{split} Bi\hat{g}mac &= 3.861757 - 1.2709D_{As} + .8768D_{Em} - 1.99.16D_{Sa} - mWage*Wage + \\ mBread*Bread + .195452*Rice + mVac*Vac + mBread*DasBread - .195452*DasRice + mVac*DasVac - mVac*DemVac + mBread*DsaBread \\ \end{split}$$

i

$$\begin{split} Bi\hat{gmac} &= 3.861757 - 1.2709D_{As} + .8768D_{Em} - 1.99.16D_{Sa} - mWage*Wage + \\ mBread*Bread + mRice*Rice + .021595*Vac + mBread*DasBread - mRice*\\ DasRice + .021595*DasVac - .021595*DemVac + mBread*DasBread \end{split}$$