

Logistic Regression

Assignment 1

Kevin Zollicoffer

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Question 1

$$\log\left(\frac{\mu}{1-\mu}\right)$$

Question 2

The Gaussian link function is an identity function, $g(\mu)$, where g maps its input back to the same input. The Gaussian link function can handle negative numbers. Its distribution is Normal, or Gaussian.

In the logit case, a natural log can not be negative (neither can $\frac{\mu}{1-\mu}$). It has a Binomial distribution.

Question 3

$$(82/157)/(431/825) = 1.00$$

Question 4

$$xb_{white} = .25268$$

$$xb_{los} = -.02998$$

$$xb_{con} = -.59868$$

$$odds = (xb_{white})(0) + (xb_{con}) + (xb_{los})(10) + (xb_{con})$$

$$odds = (.25268)(0) + (-.59868) + (-.02998)(10) + (-.59868)$$

$$odds = (-.59868) + (-0.89848)$$

$$odds = -1.49716$$

$$p = 1/(1 + \exp(-xb))$$

$$p = 1/(1 + \exp(1.49716))$$

$$p = 1/(1 + 4.468979)$$

$$p = 1/5.468979$$

$$p = .18$$

Question 5

$$a3 = \text{sqrt}(1.59199)$$

$$a3 = 1.26$$

Question 6

$$CI_{95} = \beta + / - 1.96 * SE(\beta)$$

$$CI_{95l} = -3.344039 - 1.96 * 1.26$$

$$CI_{95l} = -5.81$$

$$CI_{95u} = -3.344039 + 1.96 * 1.26$$

$$CI_{95u} = -.87$$

$$CI_{95} = [-5.81 : -.87]$$

Question 7

Yes, because the interval does not cross 0.

Question 8

$$\text{odds}_f = \exp(-2.31 * 0 + 1.00436) = \exp(1.00436) = 2.73$$

Question 9

Let μ be the probability of success of some event y

$$\mu = \text{Pr}(y == 1)$$

The likelihood or odds of this event occurring is the ratio of success to failure, or

$$\left(\frac{\mu}{1-\mu}\right)$$

Question 10

Given a matrix of form

$$m = \begin{bmatrix} A & B \\ C & D \end{bmatrix},$$

$$odds = \frac{AD}{BC}$$

$$risk = \frac{AD+CD}{BC+CD}$$

The table as given in the question is:

$$m = \begin{bmatrix} 4 & 8 \\ 3 & 5 \end{bmatrix}$$

However the odds and risk ratios for x , not y were asked for so we transpose this matrix

$$m^T = \begin{bmatrix} 4 & 3 \\ 8 & 5 \end{bmatrix}$$

Therefore

$$odds = \frac{4*5}{8*3} = \frac{20}{24} = .83$$

$$risk = \frac{4*5+8*5}{3*8+3*5} = \frac{60}{39} = 1.54$$