

Linear Algebra

TOTAL POINTS 5

1. Let two matrices be

1 / 1 point

$$A = \begin{bmatrix} 1 & -4 \\ -2 & 1 \end{bmatrix}, \quad B = \begin{bmatrix} 0 & 3 \\ 5 & 8 \end{bmatrix}$$

What is A + B?

- ☒  $\begin{bmatrix} 1 & -1 \\ 3 & 9 \end{bmatrix}$
- ☐  $\begin{bmatrix} 1 & 7 \\ 7 & 9 \end{bmatrix}$
- ☐  $\begin{bmatrix} 1 & -1 \\ 7 & 9 \end{bmatrix}$
- ☐  $\begin{bmatrix} 1 & -7 \\ -7 & -7 \end{bmatrix}$

✓ Correct

To add two matrices, add them element-wise.

2.

Let  $x = \begin{bmatrix} 5 \\ 5 \\ 2 \\ 7 \end{bmatrix}$

1 / 1 point

What is  $2 * x$ ?

- ☐  $\begin{bmatrix} 5 \\ 5 \\ 2 \\ 1 \\ 7 \\ 2 \end{bmatrix}$
- ☐  $\begin{bmatrix} 10 & 10 & 4 & 14 \end{bmatrix}$
- ☐  $\begin{bmatrix} 5 & 5 & 1 & 7 \\ 2 & 2 & & 2 \end{bmatrix}$
- ☒  $\begin{bmatrix} 10 \\ 10 \\ 4 \\ 14 \end{bmatrix}$

✓ Correct

To multiply the vector x by 2, take each element of x and multiply that element by 2.

3. Let u be a 3-dimensional vector, where specifically

1 / 1 point

$$u = \begin{bmatrix} 2 \\ 1 \\ 8 \end{bmatrix}$$

What is  $u^T$ ?

- ☐  $\begin{bmatrix} 8 & 1 & 2 \end{bmatrix}$
- ☐  $\begin{bmatrix} 2 \\ 1 \\ 8 \end{bmatrix}$
- ☒  $\begin{bmatrix} 2 & 1 & 8 \end{bmatrix}$
- ☐  $\begin{bmatrix} 8 \\ 1 \\ 2 \end{bmatrix}$

✓ Correct

4. Let u and v be 3-dimensional vectors, where specifically

1 / 1 point

$$u = \begin{bmatrix} 4 \\ -4 \\ -3 \end{bmatrix}$$

and

$$v = \begin{bmatrix} 4 \\ 2 \\ 4 \end{bmatrix}$$

What is  $u^T v$ ?

(Hint:  $u^T$  is a

1x3 dimensional matrix, and v can also be seen as a 3x1

matrix. The answer you want can be obtained by taking

the matrix product of  $u^T$  and  $v$ .) Do not add brackets to your answer.

-4

✓ Correct

5. Let A and B be 3x3 (square) matrices. Which of the following

1 / 1 point

must necessarily hold true? Check all that apply.

☒ If  $C = A * B$ , then C is a 3x3 matrix.

✓ Correct

Since A and B are both 3x3 matrices, their product is 3x3. More generally, if A were an  $m \times n$ . matrix, and B a  $n \times o$  matrix, then C would be  $m \times o$ . (In our example,  $m = n = o = 3$ .)

☐  $A * B * A = B * A * B$

☒ If B is the 3x3 identity matrix, then  $A * B = B * A$

✓ Correct

Even though matrix multiplication is not commutative in general ( $A * B \neq B * A$  for general matrices  $A, B$ ), for the special case where  $B = I$ , we have  $A * B = A * I = A$ , and also  $B * A = I * A = A$ . So,  $A * B = B * A$ .

☐  $A * B = B * A$