6.5 Lab: Subset Selection Methods

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6.5 Lab: Subset Selection Methods

Here we would use the Hitters data.

• is.na() function can be used to identify the missing observations. It returns a vector of the same length as the input vector, TRUE means the value is missing whereas FALSE means it is not missing.

```
library(ISLR)
fix(Hitters)
names(Hitters)
   [1] "AtBat"
##
                     "Hits"
                                  "HmRun"
                                              "Runs"
                                                           "RBI"
                                                                        "Walks"
   [7] "Years"
                     "CAtBat"
                                  "CHits"
                                              "CHmRun"
                                                           "CRuns"
                                                                        "CRBI"
## [13] "CWalks"
                     "League"
                                              "PutOuts"
                                  "Division"
                                                           "Assists"
                                                                        "Errors"
## [19] "Salary"
                     "NewLeague"
dim(Hitters)
## [1] 322
sum(is.na(Hitters$Salary))
```

[1] 59

So we know from here that the Salary column has 59 missing values, then try to remove them

```
Hitters=na.omit(Hitters)
```

The regsubsets() function (part of the leaps library) performs best subset selection by identifying the best model that contains a given number of predictors, where best is quantified using RSS.

```
library(leaps)
regfit.full=regsubsets(Salary~.,Hitters)
summary(regfit.full)
```

```
## Subset selection object
## Call: regsubsets.formula(Salary ~ ., Hitters)
## 19 Variables (and intercept)
               Forced in Forced out
##
## AtBat
                   FALSE
                               FALSE
## Hits
                   FALSE
                               FALSE
## HmRun
                   FALSE
                               FALSE
## Runs
                   FALSE
                               FALSE
## RBI
                   FALSE
                               FALSE
## Walks
                   FALSE
                               FALSE
## Years
                   FALSE
                               FALSE
## CAtBat
                   FALSE
                               FALSE
## CHits
                   FALSE
                               FALSE
## CHmRun
                   FALSE
                               FALSE
## CRuns
                   FALSE
                               FALSE
## CRBI
                   FALSE
                               FALSE
## CWalks
                   FALSE
                               FALSE
## LeagueN
                   FALSE
                               FALSE
## DivisionW
                   FALSE
                               FALSE
## PutOuts
                   FALSE
                               FALSE
## Assists
                   FALSE
                               FALSE
## Errors
                   FALSE
                               FALSE
## NewLeagueN
                   FALSE
                               FALSE
## 1 subsets of each size up to 8
## Selection Algorithm: exhaustive
             AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
##
      (1)
                                                                                  "*"
  1
   2
      (1)
             11 11
                   "*"
                                               11 11
                                                                                  "*"
##
             11 11
                   "*"
                                                                                  "*"
  3
      (1)
##
      (1)
             11 11
                                                                                  "*"
                   "*"
                                                                                  "*"
## 5
      (1)
##
  6
      (1)
                                               11 11
                                                                                  "*"
      (1)""
                                                                    الياا
                                                                                  11 11
## 7
                               11 11
                                    " " "*"
                                                      11 11
                                                                                  ......
## 8
      (1)"*"
##
             CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
## 1
            11 11
                             11 11
                                        11 11
                                                 11 11
      (1)
                             11 11
                                        11 11
      (1)""
## 2
## 3
      (1)
                    11 11
                             11 11
                                        "*"
             11 11
                             11 * 11
                                        11 * 11
## 4
      (1)
      (1)""
                             "*"
                                        "*"
## 5
## 6
      (1)""
                             "*"
                                        "*"
      (1)""
                             "*"
                                        "*"
## 7
      (1)"*"
                    11 11
                             "*"
                                        "*"
                                                 11 11
```

The asterisk indicates that a given variable is included in the corresponding model. In this case, the best two-variable model contains only in Hits and CRBI.

By default, regsubsets() only reports results up to the best eight-variable model. But the nvmax option can be used in order to return as many variables as are desired.

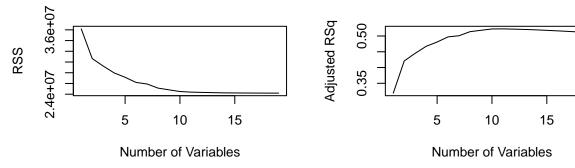
```
regfit.full=regsubsets(Salary~.,data=Hitters, nvmax=19)
reg.summary=summary(regfit.full)
reg.summary$rsq
```

[1] 0.3214501 0.4252237 0.4514294 0.4754067 0.4908036 0.5087146 0.5141227

```
## [8] 0.5285569 0.5346124 0.5404950 0.5426153 0.5436302 0.5444570 0.5452164 ## [15] 0.5454692 0.5457656 0.5459518 0.5460945 0.5461159
```

Here, reg.summary\$rsq can be used to get \mathbb{R}^2 , we can also plot those parameters:

```
par(mfrow=c(2,2))
plot(reg.summary$rss,xlab="Number of Variables",ylab="RSS",type="1")
plot(reg.summary$adjr2,xlab="Number of Variables",ylab="Adjusted RSq",type="1")
```



The points() command works like the plot() command, except that it puts points on a plot that has already been created, instead of creating a new plot.

The which.max() function can be used to identify the location of the maximum point of a vector.

```
which.max(reg.summary$adjr2)
```

[1] 11

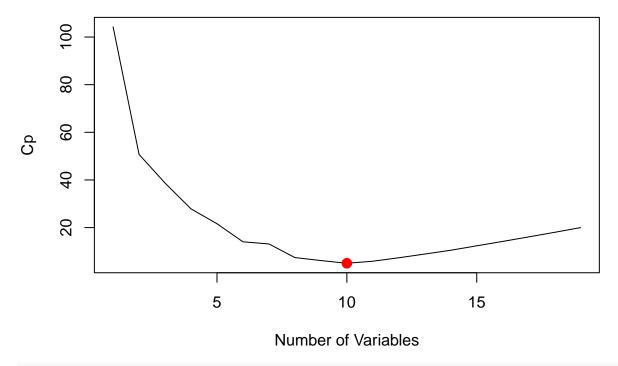
```
# points(11,reg.summary$adjr2[11], col="red",cex=2,pch=20)
```

Some extension of plotting:

```
plot(reg.summary$cp,xlab="Number of Variables",ylab="Cp",type='1')
which.min(reg.summary$cp)
```

[1] 10

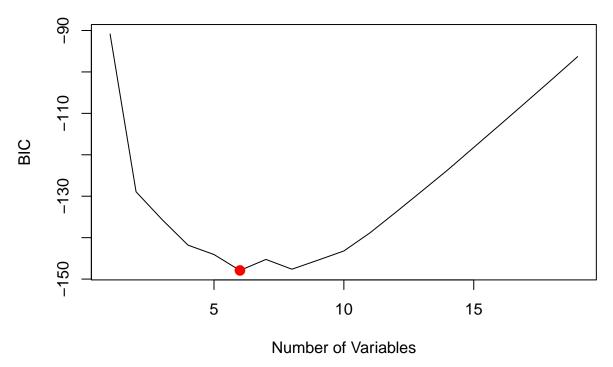
```
points(10,reg.summary$cp[10],col="red",cex=2,pch=20)
```



which.min(reg.summary\$bic)

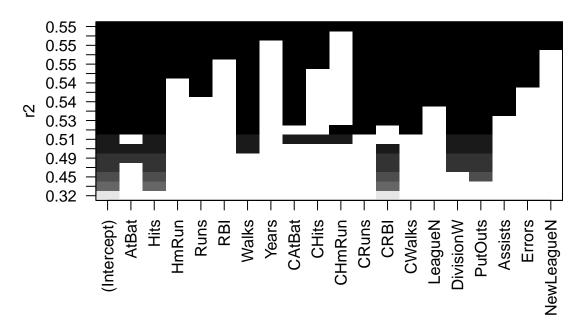
[1] 6

```
plot(reg.summary$bic,xlab="Number of Variables",ylab="BIC",type='1')
points(6,reg.summary$bic[6],col="red",cex=2,pch=20)
```

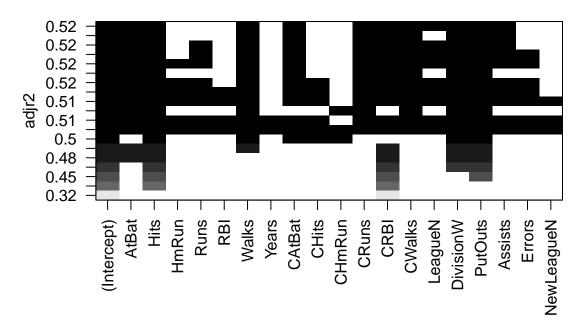


The regsubsets() function has a built-in plot() command which can be used to display the selected variables for the best model with a given number of predictors, can we can change the ranking criteria of those plots.

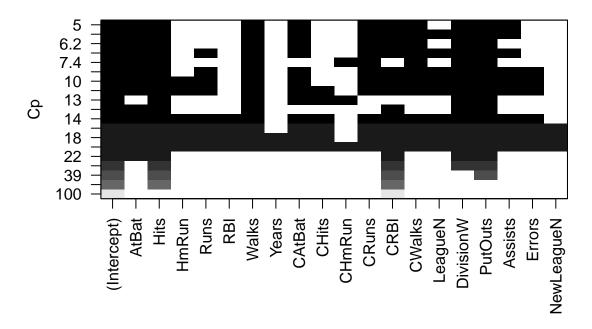
plot(regfit.full,scale="r2")



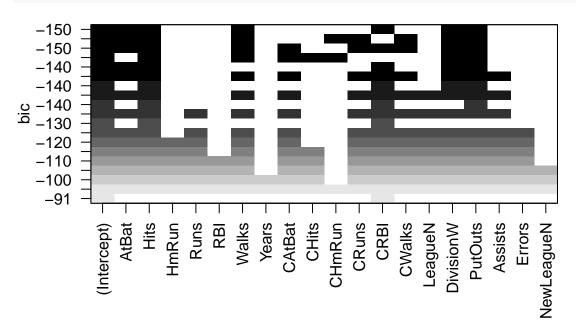
plot(regfit.full,scale="adjr2")



plot(regfit.full,scale="Cp")



plot(regfit.full,scale="bic")



6.5.2 Forward and Backward Stepwise Selection

We can also use regsubset() to do a forward or backward stepwise selecction.

```
regfit.fwd=regsubsets(Salary~.,data=Hitters,nvmax=19,method="forward")
summary(regfit.fwd)

## Subset selection object
## Call: regsubsets.formula(Salary ~ ., data = Hitters, nvmax = 19, method = "forward")
## 19 Variables (and intercept)
## Forced in Forced out
```

```
## AtBat
                     FALSE
                                 FALSE
## Hits
                     FALSE
                                 FALSE
## HmRun
                     FALSE
                                 FALSE
## Runs
                     FALSE
                                 FALSE
## RBI
                     FALSE
                                 FALSE
## Walks
                     FALSE
                                 FALSE
## Years
                     FALSE
                                 FALSE
## CAtBat
                     FALSE
                                 FALSE
## CHits
                     FALSE
                                 FALSE
## CHmRun
                     FALSE
                                 FALSE
## CRuns
                     FALSE
                                 FALSE
## CRBI
                                 FALSE
                     FALSE
## CWalks
                     FALSE
                                 FALSE
## LeagueN
                     FALSE
                                 FALSE
## DivisionW
                     FALSE
                                 FALSE
## PutOuts
                     FALSE
                                 FALSE
## Assists
                     FALSE
                                 FALSE
## Errors
                     FALSE
                                 FALSE
## NewLeagueN
                     FALSE
                                 FALSE
## 1 subsets of each size up to 19
## Selection Algorithm: forward
               AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
## 1
      (1)
                                                                                          "*"
                                         . . . . .
                                                                    11 11
                                                                           11 11
                                                                                   .. ..
                                                                                          "*"
                      "*"
## 2
      (1)
## 3
      (1)
                                                                                          "*"
                                                                                   11 11
                                                                                          "*"
## 4
      (1)
                                                                                          "*"
## 5
      (1)
               "*"
## 6
       (1
           )
               "*"
                            11 11
                                   11 11
                                           11 11 411
                                                     .. ..
                                                                    11 11
                                                                                   11 11
                                                                                          "*"
               "*"
## 7
       (1)
                                   11 11
                                                     . .
                                                                                          "*"
## 8
      (1)
                      "*"
                                                            "*"
                                                                                   "*"
                                                                                          "*"
## 9
       (1)
               "*"
                                   11 11
                                                                    11 11
                                                                                          "*"
## 10
        (1)
                      "*"
                            11 11
                                           11
                                                            "*"
                                                                                   "*"
                      "*"
##
        (1)
              "*"
                                                            "*"
                                                                                   "*"
                                                                                          "*"
   11
                                   "*"
                                           "
                                                                           .. ..
                                                                                          "*"
## 12
        (1)
                                                                                          "*"
                                   "*"
                                                            اليواا
                                                                                   11 🕌 11
## 13
        (1)
               "*"
                                   "*"
                                           11
                                                     11 11
                                                                    11 11
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
##
   14
        (1
                                   11 * 11
                                                                                   11 * 11
                                                                                          "*"
## 15
        (1)
                            "*"
                                                           11 * 11
## 16
        (1)
                            "*"
                                   "*"
                                                            "*"
                                                                                   "*"
                                                                                          "*"
            )
               "*"
                            11 * 11
                                   "*"
                                                            11 * 11
                                                                    11 * 11
                                                                                   "*"
                                                                                          "*"
## 17
        (1
                            "*"
                                   "*"
                                         "*" "*"
                                                            "*"
                                                                    "*"
                                                                                   "*"
                                                                                          "*"
## 18
        (1)
               "*"
                                         "*" "*"
                                                                                          "*"
                            "*"
                                   "*"
                                                    || *||
                                                           "*"
                                                                    "*"
                                                                           "*"
## 19
        (1)
##
               CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
##
                       11 11
                                11 11
                                            11 11
                                                     11 11
                                                               11 11
   1
       (1)
                                                      .. ..
##
   2
      (1)
                                 11 11
                                            11 11
                                            "*"
## 3
      (1)
                                 "*"
                                            "*"
       (1)
## 4
                                                      .. ..
                       11 11
                                "*"
                                            "*"
## 5
       (1
           )
                                "*"
                                            "*"
## 6
      (1)
## 7
                       11 11
                                "*"
                                            "*"
      (1)
                                 "*"
                                            "*"
## 8
      (1)
               "*"
                       11 11
                                "*"
                                            "*"
## 9
       (1
           )
                                 "*"
                                            "*"
               "*"
## 10
       (1)
                       "*"
                                 "*"
                                            "*"
                                                                       11 11
## 11
        (1)
                                "*"
                                            "*"
                                                      "*"
                                                                       11 11
## 12
       (1)"*"
                       "*"
```

```
"*"
                                "*"
                                            "*"
                                                      "*"
                                                               "*"
                                                                       11 11
## 14
        (1)
              "*"
                                "*"
                                                                       11 11
                       "*"
                                            "*"
                                                      "*"
                                                               "*"
## 15
        (1)
              "*"
## 16
        (1)
               "*"
                       "*"
                                "*"
                                            "*"
                                                      "*"
                                                               "*"
                       "*"
                                "*"
                                            11 * 11
                                                      11 * 11
## 17
        (1
            )
               "*"
                                                               11 * 11
                                                                       11 * 11
## 18
       (1)
              "*"
                       "*"
                                 "*"
                                            "*"
                                                      "*"
                                                               "*"
                                                                       "*"
## 19
        (1)"*"
                       "*"
                                "*"
                                            "*"
                                                      "*"
                                                               "*"
                                                                       "*"
regfit.bwd=regsubsets(Salary~.,data=Hitters,nvmax=19,method="backward")
summary(regfit.bwd)
## Subset selection object
## Call: regsubsets.formula(Salary ~ ., data = Hitters, nvmax = 19, method = "backward")
## 19 Variables (and intercept)
##
                Forced in Forced out
## AtBat
                     FALSE
                                 FALSE
## Hits
                     FALSE
                                 FALSE
## HmRun
                    FALSE
                                 FALSE
## Runs
                     FALSE
                                 FALSE
## RBI
                     FALSE
                                 FALSE
## Walks
                                 FALSE
                    FALSE
## Years
                    FALSE
                                 FALSE
## CAtBat
                    FALSE
                                 FALSE
## CHits
                     FALSE
                                 FALSE
## CHmRun
                     FALSE
                                 FALSE
## CRuns
                     FALSE
                                 FALSE
## CRBI
                     FALSE
                                 FALSE
## CWalks
                     FALSE
                                 FALSE
## LeagueN
                     FALSE
                                 FALSE
## DivisionW
                     FALSE
                                 FALSE
## PutOuts
                     FALSE
                                 FALSE
## Assists
                     FALSE
                                 FALSE
## Errors
                     FALSE
                                 FALSE
## NewLeagueN
                     FALSE
                                 FALSE
## 1 subsets of each size up to 19
## Selection Algorithm: backward
##
               AtBat Hits HmRun Runs RBI Walks Years CAtBat CHits CHmRun CRuns CRBI
## 1 (1)
                                   11 11
                                         11 11 11 11
                                                                                   "*"
                      "*"
      (1)
               11 11
                                                                                   "*"
## 2
## 3
      (1)
               11 11
                      "*"
                            11 11
                                   11 11
                                         11 11
                                                                           11 11
                                                                                   "*"
                                                                                          .. ..
                                                                                   "*"
                                                                                          11 11
## 4 (1)
               "*"
                                                     11 11
                                                                                          .. ..
## 5
      (1)
               "*"
                                   11 11
                                                                                   "*"
## 6
               "*"
                      "*"
                                                                                   "*"
      (1)
## 7
               "*"
                            11 11
                                   11 11
                                           11
                                                     11 11
                                                           11 11
                                                                    11 11
                                                                           11 11
                                                                                   "*"
                                                                                          11 11
       (1)
                      "*"
                                                                                   "*"
                                                                                          "*"
## 8
      (1)
               "*"
               "*"
                            11 11
                                   11 11
                                                     . .
                                                                    11 11
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
## 9
      (1)
                                   11 11
                                                                                   11 4 11
                                                                                          اليواا
## 10
        (1)
               "*"
                                                           11 🕌 11
## 11
        (1
            )
               "*"
                      "*"
                            11 11
                                   11 11
                                                     11 11
                                                                    11 11
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
                            11 11
                                   "*"
                                                     11 11
                                                                    11 11
                                                                                   "*"
                                                                                          11 * 11
## 12
        ( 1
            )
               "*"
                                                           "*"
                      "*"
                            11 11
                                   "*"
                                                     11 11
                                                                                   "*"
                                                                                          "*"
## 13
        (1)
               "*"
                                                           "*"
                                         11 11
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
## 14
        (1
            )
               "*"
                      11 * 11
                            11 * 11
                                   11 * 11
                                                           11 * 11
                            "*"
                                   "*"
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
            )
               "*"
                      "*"
                                                            "*"
                                                                    "*"
## 15
        ( 1
## 16
        (1)
              "*"
                      "*"
                            "*"
                                   "*"
                                         11 * 11 11 * 11
                                                     11 11
                                                           "*"
                                                                    "*"
                                                                           11 11
                                                                                   "*"
                                                                                          "*"
       (1)"*"
                      "*"
                            "*"
                                   "*"
                                         "*" "*"
                                                           "*"
                                                                    "*"
                                                                                   "*"
                                                                                          "*"
## 17
```

13 (1) "*"

"*"

11 🕌 11

11 🕌 11

11 🕌 11

11 🕌 11

```
" * "
        (1)"*"
                                                                                              "*"
## 19
        (1)
                CWalks LeagueN DivisionW PutOuts Assists Errors NewLeagueN
##
                                                        11 11
## 1
       (1
                        11 11
                                  .. ..
                                              11 11
                                                        11 11
                                                                          11 11
##
   2
         1
                                  11 11
##
   3
       (1
                                                        11 11
## 4
       (1
                                              "*"
## 5
       (1
                                                        11 11
## 6
       (1
            )
                                  "*"
## 7
       ( 1
           )
                                  "*"
                                                        11 11
## 8
       (1
           )
## 9
                "*"
                                  "*"
                                              "*"
       ( 1
           )
                        11 11
                                  "*"
## 10
        (1
               "*"
                                  "*"
                                                        "*"
## 11
        (1
## 12
        (1
                                  "*"
                                                        "*"
               "*"
                                  "*"
                                              الياا
                                                        11 🕌 11
## 13
        (
          1
             )
## 14
        ( 1
             )
               "*"
                                  "*"
                                  "*"
               "*"
                                                        "*"
## 15
        (1
             )
                        "*"
                                  "*"
                                                        "*"
## 16
        (1
                        "*"
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                          "*"
##
   17
                        "*"
                                  "*"
## 18
        (1
             )
               "*"
## 19
        (1)
                        "*"
                                  "*"
                                              "*"
                                                        "*"
                                                                          "*"
```

We can notice that the best seven-variable models identified by forward stepwise selection, backward stepwise selection, and best subset selection are different.

```
coef(regfit.full,7)
##
    (Intercept)
                         Hits
                                      Walks
                                                   CAtBat
                                                                   CHits
                                                                                CHmRun
##
     79.4509472
                    1.2833513
                                  3.2274264
                                               -0.3752350
                                                              1.4957073
                                                                            1.4420538
##
      DivisionW
                      PutOuts
## -129.9866432
                    0.2366813
coef(regfit.fwd,7)
##
    (Intercept)
                        AtBat
                                        Hits
                                                     Walks
                                                                    CRBI
                                                                                CWalks
    109.7873062
                   -1.9588851
                                  7.4498772
                                                4.9131401
                                                                           -0.3053070
##
                                                              0.8537622
##
      DivisionW
                      PutOuts
## -127.1223928
                    0.2533404
coef(regfit.bwd,7)
                                                                   CRuns
                                                                                CWalks
##
    (Intercept)
                        AtBat
                                        Hits
                                                     Walks
##
    105.6487488
                   -1.9762838
                                  6.7574914
                                                6.0558691
                                                              1.1293095
                                                                           -0.7163346
##
      DivisionW
                      PutOuts
## -116.1692169
                    0.3028847
```

6.5.3 Choosing Among Models Using the Validation Set Approach and Cross-Validation