

$$\begin{aligned}
f(n) &= L(n-1) + (n-2) \times L(n-2) + \left[ \frac{(n-1)(n-2)}{2} - 1 \right] \times L(n-3) \\
&\quad + \sum_{k=3}^{n-2} \frac{(n+k-3)!}{k!} \times [(n-1)(n-2) - k(k-1)] \times L(n-k-1) \\
&\quad ( \text{Remark : } L(0) \text{ don't is not used} )
\end{aligned}$$

we can compute  $F_k = [(n-1)(n-2) - k(k-1)]$  by an addition with  $F_k = F_{k-1} - 2(k-1)$

and  $\frac{1}{k!}$  recursively by  $\frac{1}{k!} = k \times \frac{1}{(k+1)!}$  ; *only one inversion for  $\frac{1}{n!}$*

So we have 6 multiplications modulus(1 000 000 007) by coefficient:

- one for  $\frac{1}{n!}$
- one for  $\frac{1}{k!}$
- one for  $(n+k-3)!$
- three for the product  $(n+k-3)! \times \frac{1}{k!} \times F_k \times L(n-k-1)$