import numpy as np

data = [

[1, 1, 1, 1, 0, 1, 1, 1, 1, 0],

[1, 1, 1, 1, 1, 1, 1, 0, 1, 1],

[1, 1, 1, 0, 1, 1, 1, 1, 0, 0],

[1, 1, 0, 1, 1, 1, 1, 0, 1, 1],

[1, 0, 1, 1, 0, 1, 1, 1, 1, 0]

]

theta\_A, theta\_B = 0.6, 0.5

threshold = 1e-4

max\_iterations = 5

iteration = 0

while iteration < max\_iterations:

iteration += 1

prev\_theta\_A, prev\_theta\_B = theta\_A, theta\_B

P\_A, P\_B = [], []

for seq in data:

h = sum(seq)

t = len(seq) - h

L\_A = (theta\_A \* h) \* ((1 - theta\_A) \* t)

L\_B = (theta\_B \* h) \* ((1 - theta\_B) \* t)

denom = L\_A + L\_B

P\_A\_i = L\_A / denom if denom > 0 else 0.5

P\_B\_i = L\_B / denom if denom > 0 else 0.5

P\_A.append(P\_A\_i)

P\_B.append(P\_B\_i)

total\_heads\_A = sum(P\_A[i] \* sum(data[i]) for i in range(len(data)))

total\_flips\_A = sum(P\_A[i] \* len(data[i]) for i in range(len(data)))

theta\_A = total\_heads\_A / total\_flips\_A if total\_flips\_A else prev\_theta\_A

total\_heads\_B = sum(P\_B[i] \* sum(data[i]) for i in range(len(data)))

total\_flips\_B = sum(P\_B[i] \* len(data[i]) for i in range(len(data)))

theta\_B = total\_heads\_B / total\_flips\_B if total\_flips\_B else prev\_theta\_B

if abs(theta\_A - prev\_theta\_A) < threshold and abs(theta\_B - prev\_theta\_B) < threshold:

break

print(f"Stopped after {iteration} iterations.")

print(f"Estimated theta\_A: {theta\_A:.6f}")

print(f"Estimated theta\_B: {theta\_B:.6f}")