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Karlsruher Institut für Technologie (KIT)
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Exam in “Machine Vision”

Date of exam: September 9, 2022
Time of exam: 8:00–9:00

Question 1

(6 points)

Let f , g , and h be arbitrary functions $\mathbb{R} \rightarrow \mathbb{C}$. We denote with $f * g$ the convolution of two functions, with $f \cdot g$ the point-wise product of two functions, and with $\mathcal{F}\{g\}$ the Fourier transform of a function. Which of the following terms are equal? Each correct answer yields +2 points, each wrong answer -1 point. The whole task will be awarded with at least 0 points.

(1) $\mathcal{F}\{g\} + \frac{1}{2}\mathcal{F}\{h\}$

(2) $\frac{1}{4}\mathcal{F}\{2g + h\}$

(3) $\mathcal{F}\{3g \cdot f + g \cdot 3h\}$

(4) $f * h + 2g * f$

(5) $f * (2g + h)$

(6) $3\mathcal{F}\{g * (f + h)\}$

(7) $3\mathcal{F}\{g\} * \mathcal{F}\{f + h\}$

(8) $\mathcal{F}\{g + \frac{1}{2}h\}$

(9) $\mathcal{F}\{f \cdot (2g + h)\}$



Question 2**(6 points)**

The picture below shows a small gradient image with 5 by 6 pixels. Each pixel is illustrated as a box. The gradient of each pixel is given by the pair of numbers $\frac{\partial g}{\partial u}, \frac{\partial g}{\partial v}$. Apply double-thresholding with the two thresholds 3 and 4 to find the edge pixels. Mark each edge pixel with a circle (o) and each non-edge pixel with a cross (x). You will obtain $+\frac{1}{5}$ point for each correct pixel and $-\frac{1}{5}$ point for each incorrect pixel. Pixels that are not marked will not be considered. The whole task will not be awarded with negative points.

3,0	2,1	3,-1	3,-3	1,-2	0,-4
2,0	1,1	2,-1	2,-2	2,-2	2,-3
3,1	0,1	2,-3	3,-3	3,-3	3,-2
3,2	0,0	0,-2	2,-2	4,-2	2,-1
2,3	1,3	-1,1	2,-1	2,0	2,0



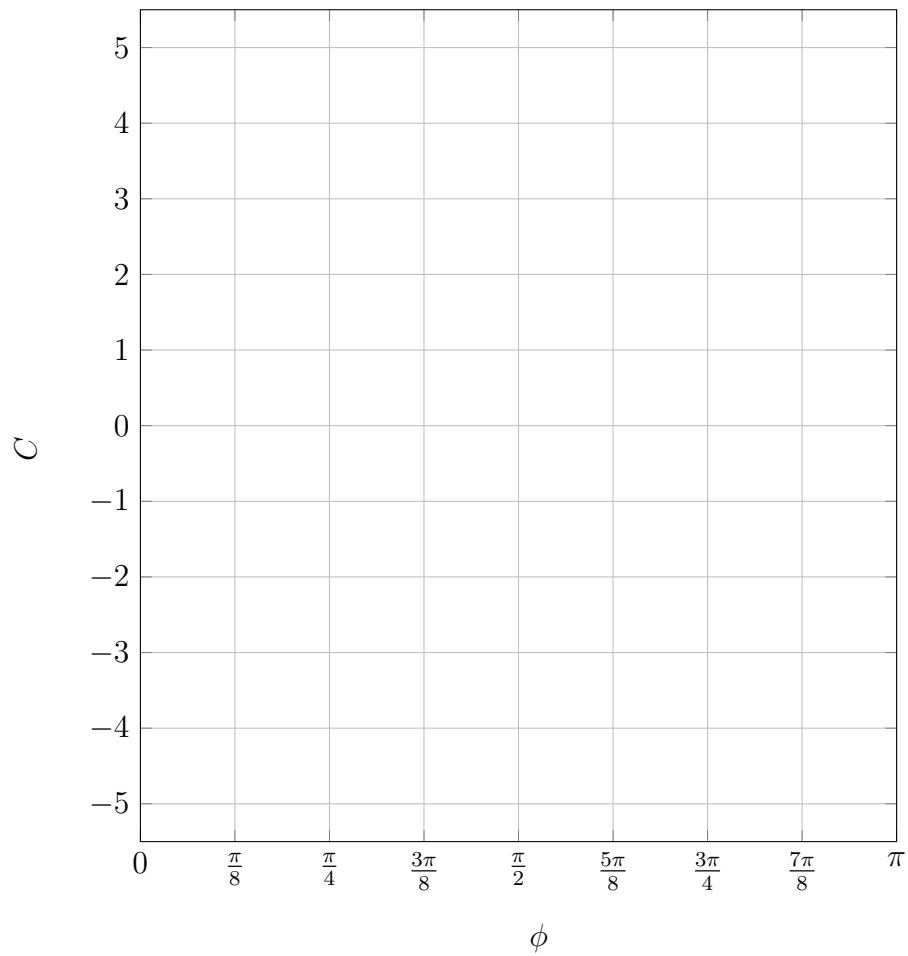
Question 3

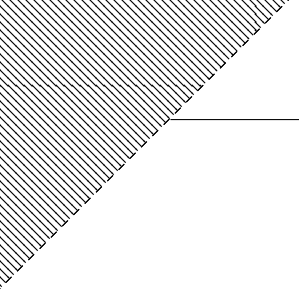
(8 points)

The image I shows a 4-by-6 pixel image. The two pixels highlighted in gray are edge pixels. Transform the two edge pixels into Hough space and draw the corresponding curves in the graph below. For each edge pixel provide a formula that describes the curve in Hough space.

$I :$

	0	1	2	3	4	5
0						
1						
2						
3						



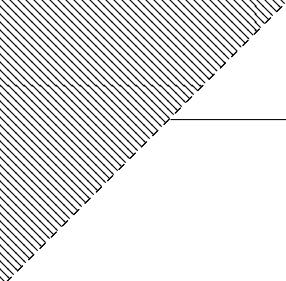


Question 4

(8 points)

We want to apply the mean-shift algorithm for image segmentation to a small gray value image with 12 pixels. The gray values of the 12 pixels are shown in the drawing below. Apply the mean-shift algorithm for the pixel with the gray value 15. Consider for the set S all pixels which have gray values that deviate no more than at most 5.1. For each iteration of the mean-shift algorithm provide the previous reference color/gray value c , the set S , and the new reference c . State explicitly when the mean-shift algorithm terminates.

65	56	21	7
89	72	15	4
8	2	10	3

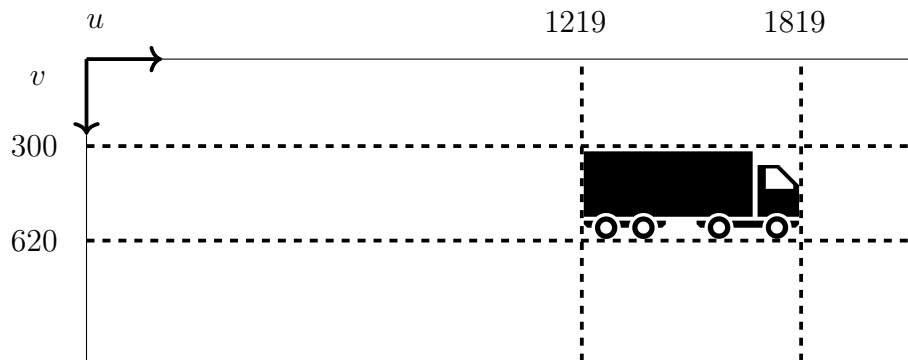


Question 5

(6+4 points)

Assume a setup in which a camera is mounted on the roof of an automated vehicle. The camera can be modeled using the pinhole camera model with the parameters given by matrix A . The camera is mounted such that the x - and z -axes of the camera coordinate system are parallel to the ground plane. Instance segmentation on a certain camera image yields a bounding box of a truck as given in the picture below.

$$A = \begin{pmatrix} 550 & 0 & 1040 \\ 0 & 550 & 510 \\ 0 & 0 & 1 \end{pmatrix}$$



- (a) Assume that the ground plane is given as $y = 2$ m in the camera coordinate system. Determine the distance to the truck.

Remark: You can assume that the wheels of the truck are in contact with the ground plane.

- (b) Another, very precise lidar sensor is sensing a distance to the truck as $d = 11$ m. We assume that the mismatch between the lidar measurement and the result from part (a) is caused by an error in the given height of the ground plane. Recalculate the height y of the ground plane such that the distance measurement of the lidar and the content of the image are consistent.



Question 6

(4 points)

Explain why it is impossible to calibrate all intrinsic and extrinsic parameters of a pinhole camera model from a single image of a flat checkerboard.

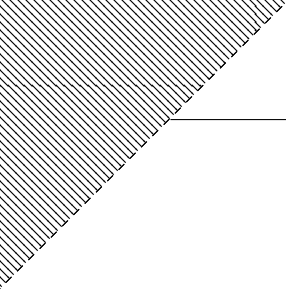
Remark: Compare the number of parameters that need to be estimated and the number of equations that you obtain from a single checkerboard image.



Question 7

(5 points)

Assume you have trained a non-linear support vector machine (SVM). Which pieces of information do you need to store that you can apply the non-linear SVM later on new examples? Correct answers yield +1 point, incorrect answers -1 point. The whole task will be awarded with at least 0 points.



Question 8

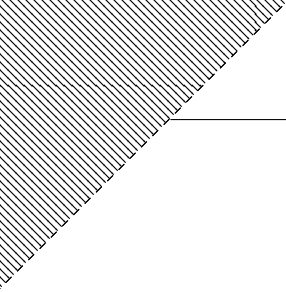
(7 points)

Implement a MATLAB-function that calculates a histogram of oriented gradients (HOG) from the gradients of a gray level image. The gradients are provided in terms of two matrices. The first matrix `dir` contains the direction of the gradient in each pixel. The directions are encoded $\phi \in (-\pi, \pi]$. The second matrix `len` contains the length of the gradient in each pixel. The histogram of oriented gradients should discretize the gradient direction to eight equal sectors as given in the table below. The histogram should be represented as vector with eight entries. Use the gradient length to weight each gradient direction. You don't need to normalize the histogram.

index	bin
1	$(-\pi, -\frac{3\pi}{4}]$
2	$(-\frac{3\pi}{4}, -\frac{\pi}{2}]$
3	$(-\frac{\pi}{2}, -\frac{\pi}{4}]$
4	$(-\frac{\pi}{4}, 0]$
5	$(0, \frac{\pi}{4}]$
6	$(\frac{\pi}{4}, \frac{\pi}{2}]$
7	$(\frac{\pi}{2}, \frac{3\pi}{4}]$
8	$(\frac{3\pi}{4}, \pi]$

Remark: MATLAB-function `ceil(x)` rounds the variable x to the next integer greater or equal x , whereas `floor(x)` rounds the variable x to the next integer less or equal x .

```
function histogram = hog(dir, len)
```

Question 9

(2+2+2 points)

- (a) Why is it impossible to approximate the identity function $x \mapsto x$ (for all $x \in \mathbb{R}$) with a multi layer perceptron with hyperbolic tangent activation function (\tanh)?
- (b) Why is it impossible to approximate the exponential function $x \mapsto e^x$ (for all $x \in \mathbb{R}$) with a multi layer perceptron with ReLU activation function?
- (c) How can we implement the logical NOT-function with a single perceptron with ReLU activation function? The NOT-function maps input $x = 0$ to output $y = 1$ and input $x = 1$ to output $y = 0$. Provide the weights of the perceptron.

