

**Institut für Mess- und Regelungstechnik  
mit Maschinenlaboratorium  
Karlsruher Institut für Technologie  
(KIT)  
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**Exam in “Machine Vision”**

Date of exam: February 14, 2019  
Time of exam: 10:30-11:30

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Question 1

(2+2+2 points)

Assume, we observe Moiré patterns in an image. Which of the following ideas can be used to avoid the Moiré patterns? Explain your answers briefly by referring to the sampling theorem.

- (a) convolute the image with a Gaussian filter
- (b) increase the focal length of the camera
- (c) reduce the distance between camera and observed object



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Question 2

(7 points)

Describe how we could simplify the Hough transform in order to use graylevel gradient information for the estimation of graylevel edges. Which benefits would such an approach yield over the standard Hough transform.



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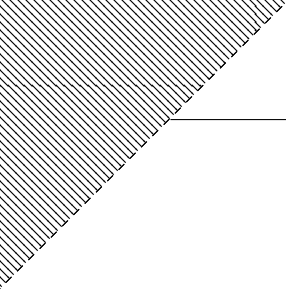
Question 3

(4+3 points)

Given are the points  $\vec{x}_1 = (-1, 7)^T$  and  $\vec{x}_2 = (7, 1)^T$ . You are supposed to find parameters  $\vec{n}$  and  $c$  for the line connecting these two points using the line representation from the lecture (Hesse normal form).

- (a) How many solutions for  $\vec{n}$  exist? Calculate one. What is the corresponding  $c$ ?
- (b) Now, we want to find this line using the total least squares approach. What are the values for  $\alpha, \beta$  and  $\gamma$  in the following Eigenvalue problem?

$$\begin{pmatrix} \alpha & \beta \\ \beta & \gamma \end{pmatrix} \cdot \vec{n} = \lambda \cdot \vec{n}$$



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#### Question 4

(9 points)

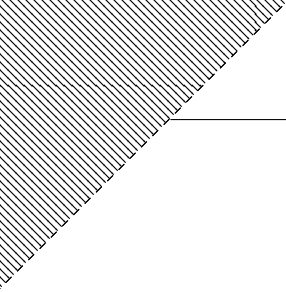
Implement a MATLAB function which determines the correction factors  $c_R$ ,  $c_B$  in order to perform a white balance on an input RGB image. The brightest pixel in the image is assumed to be white and should be used as reference pixel to calculate the correction factors. First of all, determine the reference pixel. Afterwards, calculate the correction factors and return them to the user. Keep in mind that the pixel values are stored as an 8-bit unsigned integer for each channel. Below, we provide the function header of the MATLAB function

*Remark:* The brightness (luminance)  $L$  of an RGB value is calculated as weighted sum of the RGB values:

$$L = 0.299 \cdot R + 0.587 \cdot G + 0.114 \cdot B$$

```
function [c_R, c_B] = white_balance_factors(image)
% calculate the white balance correction factors from an RGB image
% use brightest pixel as reference pixel
% image is an 8-bit encoded unsigned integer RGB image
% add your code below this line
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Question 5

(3+3 points)

Are the following statements true or false? Justify your answers briefly. Provide a counterexample if a statement is false.

- (a) If we turn an image by  $90^\circ$  and apply connected components labeling (CCL) on the rotated image we obtain the same partitioning of the image into segments as if we apply CCL on the original image.
- (b) If we remove the topmost row of an image and apply CCL on the remainder we obtain the same partitioning of the remaining image as if we would apply CCL on the complete image and ignore the topmost row afterwards.



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Question 6

(7 points)

Assume a pinhole camera that is described by its matrix of intrinsic parameters

$$A = \begin{pmatrix} 1000 & 0 & 500 \\ 0 & 1000 & 500 \\ 0 & 0 & 1 \end{pmatrix} \text{ and a circle on the plane } z = 10 \text{ with center at position}$$

$(x, y, z) = (3, -1, 10)$  and radius 2. Derive to which geometric curve this circle is mapped in the image of the camera. Describe the shape, position, and size of the curve.  $(x, y, z)$  refer to coordinates in the camera coordinate system.



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Question 7

(3+3+3 points)

Derive for each of the following kernel functions  $K(x,y)$  its respective nonlinear transformation  $\Phi(x)$  such that  $K(x,y) = \langle \Phi(x), \Phi(y) \rangle$ . You may assume  $0 < x, y < 1$ .

(a)  $K(x,y) = (x \cdot y + 1)^2$

(b)  $K(x,y) = \cos(x - y)$

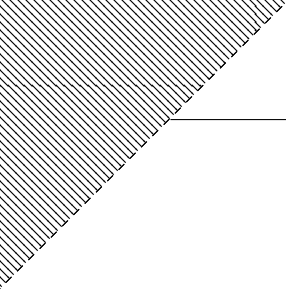
(c)  $K(x,y) = \frac{1}{1-x^2y^2}$

*Remark:*

$$\cos(\theta \pm \psi) = \cos(\theta)\cos(\psi) \mp \sin(\theta)\sin(\psi)$$

*Remark:*

$$\sum_{k=0}^{\infty} a_0 q^k = \frac{a_0}{1-q} \quad \text{for any } 0 < q < 1, a_0 \in \mathbb{R}$$



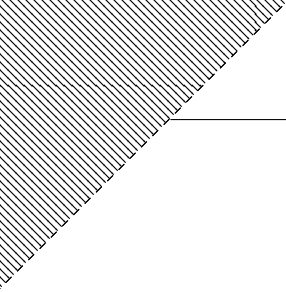
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**Question 8****(6 points)**

Assume a cascade classifier with three classification stages  $c_1$ ,  $c_2$ , and  $c_3$ . We are facing four images  $I_1$ ,  $I_2$ ,  $I_3$ , and  $I_4$  which are applied to the cascade classifier. The classification results are shown in the following table. Enter the output of the cascade classifier (either  $+1$  or  $-1$ ) for each image in the table. Furthermore, enter to the table which stages are evaluated for each image and which stages are not evaluated.

image	classification output			output of cascade	stages evaluated	stages not evaluated
	$c_1$	$c_2$	$c_3$			
$I_1$	$+1$	$-1$	$-1$			
$I_2$	$+1$	$+1$	$+1$			
$I_3$	$-1$	$+1$	$+1$			
$I_4$	$+1$	$-1$	$+1$			





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Question 9

(3 points)

Name three regularization techniques for the training of convolutional networks.

*Remark:* If more than three answers are given, only the first three answers count.

