Affix the authentification label over this field.

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Exam in "Machine Vision"

Date of exam:	August 19, 2024
Time of exam:	10:30-11:30

Question 1 (6 points)

Derive a filter mask to calculate the third order derivative $\frac{\partial^3 g}{(\partial u)^3}$ of a gray value function g.

Question 2 (3+3 points)

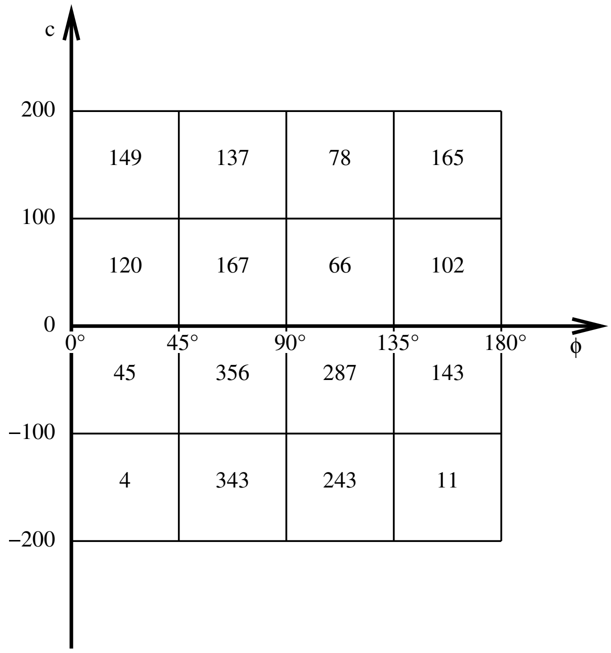
Assume a pinhole camera with a focal length $f_{camera} = 5\ mm$ and an imager with a resolution that is descibed by its scaling factor to be $\alpha = \beta = 1000\ \frac{1}{mm}$. We are observing a plane that is orthogonal to the optical axis of the camera at depth $z = 1000\ mm$ and on which a band-bounded pattern with a cutoff frequency of $k_{cutoff} = 2\ \frac{1}{mm}$ is painted.

(a) Calculate the cutoff frequency of the pattern that is projected to the image plane.

(b) Check whether the Shannon-Nyquist sampling theorem is met.

Question 3 (2+2+2 points)

For a certain image the Hough transform was used to calculate the accumulator array in parameter space that is depicted in the figure below.



(a) Which line does the Hough transform calculate? Provide the angle ϕ of the unit normal vector and the offset of the line c.

(b) Name one advantage and one disadvantage of such a coarse partitioning of the parameter space.

Remark: The term coarse partitioning means that the parameter space is split only in a small number of large cells.

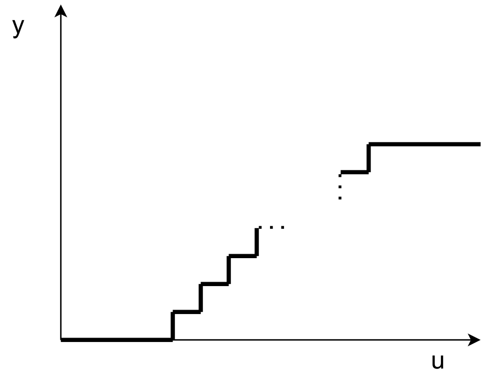
(c) Explain briefly why we can ignore angles ϕ in the interval between 180° and 360°.

Question 4 (6 points)

Assume an RGB color image. We want to apply the white balance procedure described in the lecture to the image. Our reference area contains four pixels with the RGB values $(0.4, 0.4, 0.2), (0.5, 0.3, 0.4), (0.5, 0.4, 0.4), (0.6, 0.5, 0.2)$. Calculate the correction factors and apply them to the RGB values $(0.5, 0.3, 0.3)$, $(1.0, 1.0, 0.9)$.

Question 5 (2+2+2+3 points)

Consider a gray value image as the one shown below on the left. It consists of a black area on the left, a light gray area on the right, and a gray value ramp between, i.e. the gray value increases linearly from left to right with a gray value difference of $d > 0$ between neighboring pixels. In the right image, the gray values (y) from one row are shown.



(a) Which partitioning do we obtain when we apply the connected components labeling algorithm and treat gray values as similar as long as their gray values do not differ more than $\frac{d}{2}$?

(b) Which partitioning do we obtain when we apply the connected components labeling algorithm and treat gray values as similar as long as their gray values do not differ more than $2d$?

(c) Which partitioning do we obtain when we apply k-means-clustering with $k = 2$? Assume that k-means-clustering finds the global optimum.

(d) For the case discussed in part (c) calculate the gray values of the two prototype gray values. Assume that the gray value of the dark area is 0, the gray value of the light gray area is 240, the width of the image is 300, the width of the black area is 100, and the width of the gray value ramp is 100. The height of the picture is 180.

Question 6 (4 points)

Given the camera matrix $\mathbf{A}$. Project point $(\mathbf{x}, \mathbf{y}, \mathbf{z}) = (-0.5, 1, 2)$ into image space.

$$\mathbf{A} = \begin{pmatrix} 600 & 0 & 300 \\ 0 & 400 & 300 \\ 0 & 0 & 1 \end{pmatrix}$$

Question 7 (8 points)

Assume a binary classification task with the three training examples

$$\vec{x}^{(1)} = \begin{pmatrix} 1 \\ 1 \end{pmatrix},\ d^{(1)} = -1$$
$$\vec{x}^{(2)} = \begin{pmatrix} 1 \\ 2 \end{pmatrix},\ d^{(2)} = +1$$
$$\vec{x}^{(3)} = \begin{pmatrix} 3 \\ 1 \end{pmatrix},\ d^{(3)} = +1$$

Calculate the hard margin support vector machine with dot product kernel. Provide the weight vector $\vec{w}$, the bias weight b and the margin ρ.

Remark: All three training examples are support vectors. You may use this assumption in your answer without proving it.

Question 8 (8 points)

Complete the Python function below to calculate an integral image. The input to the function is a gray value image with shape $[v,\, u]$ and the output of the function is expected to have the same shape.

Note: An integral image I_{int} based on image I is defined as:
$I_{int}[v,u] = \sum_{i=0}^{i \leq v} \sum_{j=0}^{j \leq u} I[i, j]$.

```
def integral_image(image:  np.ndarray):
  integral = np.zeros_like(image, dtype=np.float64)
```

Question 9 (7 points)

The graph below represents the major computation steps of a transformer-encoder-based architecture for image classification.
Use the provided computation steps and fill in their corresponding letters into the box.

Note: You may use some boxes multiple times, and it's NOT necessary to use all of them.

A: Positional Embedding	**B**: MLP	**C**: Patch Extraction
D: Decision-Tree	**E**: Argmax/Softmax	**F**: CNN
G: Transformer Encoder	**H**: LSTM	**I**: Patch Embedding
J: Multi-Head-Attention	**K**: Norm