

COMP 3270 FALL 2018
Programming Project: Autocomplete

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Date Submitted: 11-26-18

1. **Pseudocode:** Understand the strategy provided for *TrieAutoComplete*. State the algorithm for the functions precisely using numbered steps that follow the pseudocode conventions that we use. Provide an approximate efficiency analysis by filling the table given below, for your algorithm.

Add

- Pseudocode:

```
Add(word: string, weight: double)
1   if word is null
2       throw an exception
3   if weight < 0
4       throw an exception
5   Node curr = root of tree
6   Node nextNode = null
7   char index = '-'
8   for i to word.length
9       index = the character in word at index i
10      nextNode = the child of curr with character index
11      if nextNode is null
12          instantiate nextNode with character index,
13              parent curr, and given weight
14          add new node to children map
15      if curr's subtree max weight < weight
16          curr's subtree max weight = weight
17      point curr to nextNode
18  set curr's word value
19  set curr's weight
20  set that curr is a word
```

- Complexity analysis:

Step #	Complexity stated as $O(_)$
1	$O(1)$
2	$O(1)$
3	$O(1)$
4	$O(1)$
5	$O(1)$
6	$O(1)$
7	$O(1)$
8	$O(n)$
9	$O(n)$
10	$O(n)$
11	$O(n)$
12	$O(n)$
13	$O(n)$
14	$O(n)$
15	$O(n)$
16	$O(n)$
17	$O(1)$
18	$O(1)$
19	$O(1)$

Complexity of the algorithm = $O(n)$

topMatch

- Pseudocode:

```
topMatch(prefix: string)
1   if prefix is null
2       throw an exception
3   nodeQueue = new priority queue of Nodes using a
    reverse weight comparator
4   Node curr = root of tree
5   char index = '-'
6   boolean wordExists = true
7   string empty = ""
8   String topMatch = ""
9   for i to prefix.length
10      index = the character in the word at index i
11      if a child of curr contains the value of index
12          point curr to that child
13      else
14          wordExists = false
15          break
16  if (wordExists is false)
17      return empty
18  while (curr is a word and curr's weight < curr's
    subtree max weight)
19      for every node in curr's children
20          add that node to nodeQueue
21      point curr to the head of queue and remove
    element from queue
22  topMatch = curr's word value
23  return topMatch
```

- Complexity analysis:

Step #	Complexity stated as $O(_)$
1	$O(1)$
2	$O(1)$
3	$O(1)$
4	$O(1)$
5	$O(1)$
6	$O(1)$
7	$O(1)$
8	$O(1)$
9	$O(n)$
10	$O(n)$
11	$O(n)$
12	$O(n)$
13	$O(n)$
14	$O(n)$
15	$O(n)$
16	$O(1)$
17	$O(1)$
18	$O(n)$
19	$O(n^2)$
20	$O(n^2)$
21	$O(n)$
22	$O(1)$
23	$O(1)$

Complexity of the algorithm = $O(n^2)$

topMatches

Pseudocode:

```
topMatches(prefix: string, k: integer)
1   if prefix is null
2       throw an exception
3   Node curr = root of tree
4   char index = '-'
4   boolean matchExists = true
5   nodeQueue = new priority queue of Nodes using a
    reverse weight comparator
6   emptyList = new ArrayList of strings
7   topMatches = new ArrayList of Nodes
8   topMatchesString = new ArrayList of strings
9   if k = 0
10      return emptyList
11   for i to prefix.length
12       index = the character in the word at index i
13       point curr to its child with the value of index if
        possible
14       if curr is null
15           return emptyList
16   if curr is not null
17       add curr to nodeQueue
18   while nodeQueue is not empty
19       point curr to head of nodeQueue and remove that
        node from queue
20       for every node in curr's children
21           add that node to nodeQueue
22       if the size of topMatches >= k
23           sort topMatches in descending order of
            value
24           break
25       if curr points to a word
26           add curr to topMatches
27   for every node in topMatches
28       add that node's word to topMatchesString
29   return topMatchesString
```

- Complexity analysis:

Step #	Complexity stated as $O(_)$
1	$O(1)$
2	$O(1)$
3	$O(1)$
4	$O(1)$
5	$O(1)$
6	$O(1)$
7	$O(1)$
8	$O(1)$
9	$O(1)$
10	$O(1)$
11	$O(n)$
12	$O(n)$
13	$O(n)$
14	$O(n)$
15	$O(n)$
16	$O(1)$
17	$O(1)$
18	$O(n)$
19	$O(n)$
20	$O(n^2)$
21	$O(n^2)$
22	$O(n)$
23	$O(n \log(n))$
24	$O(1)$
25	$O(n)$
26	$O(n)$
27	$O(n)$
28	$O(n)$
29	$O(1)$

Complexity of the algorithm = $O(n^2)$

2. **Testing:** Complete your test cases to test the *TrieAutoComplete* functions based upon the criteria mentioned below.

Test of correctness:

Assuming the trie already contains the terms {"ape, 6", "app, 4", "ban, 2", "bat, 3", "bee, 5", "car, 7", "cat, 1"}, you would expect results based on the following table:

Query	k	Result
""	-	Car
"a"	-	Ape
"ap"	-	Ape
"b"	-	Bee
"ba"	-	Bat
"c"	-	Car
"ca"	-	Car
"cat"	-	Cat
"d"	-	""
" "	-	""
""	8	{"car", "ape", "bee", "app", "bat", "ban", "cat"}
""	1	{"car"}
""	2	{"car", "ape"}
""	3	{"car", "ape", "bee"}
"a"	1	{"ape"}
"ap"	1	{"ape"}
"b"	2	{"bee", "bat"}
"ba"	2	{"bee", "bat"}
"d"	100	{}

Test cases have been provided in the file AutocompleteTest.java.

3. **Analysis:** Answer the following questions. Use data wherever possible to justify your answers, and keep explanations brief but accurate:

NOTE: Whenever fourletterwords.txt and fourletterwordshalf.txt are compared in any of the following graphs, note that the letter “a” in fourletterwordshalf is considered synonymous to the letter “n” in fourletterwords.

- i. What is the order of growth (big-Oh) of the number of compares (in the worst case) that each of the operations in the *Autocompletor* data type make?

add: $O(n)$

topMatch: $O(n^2)$

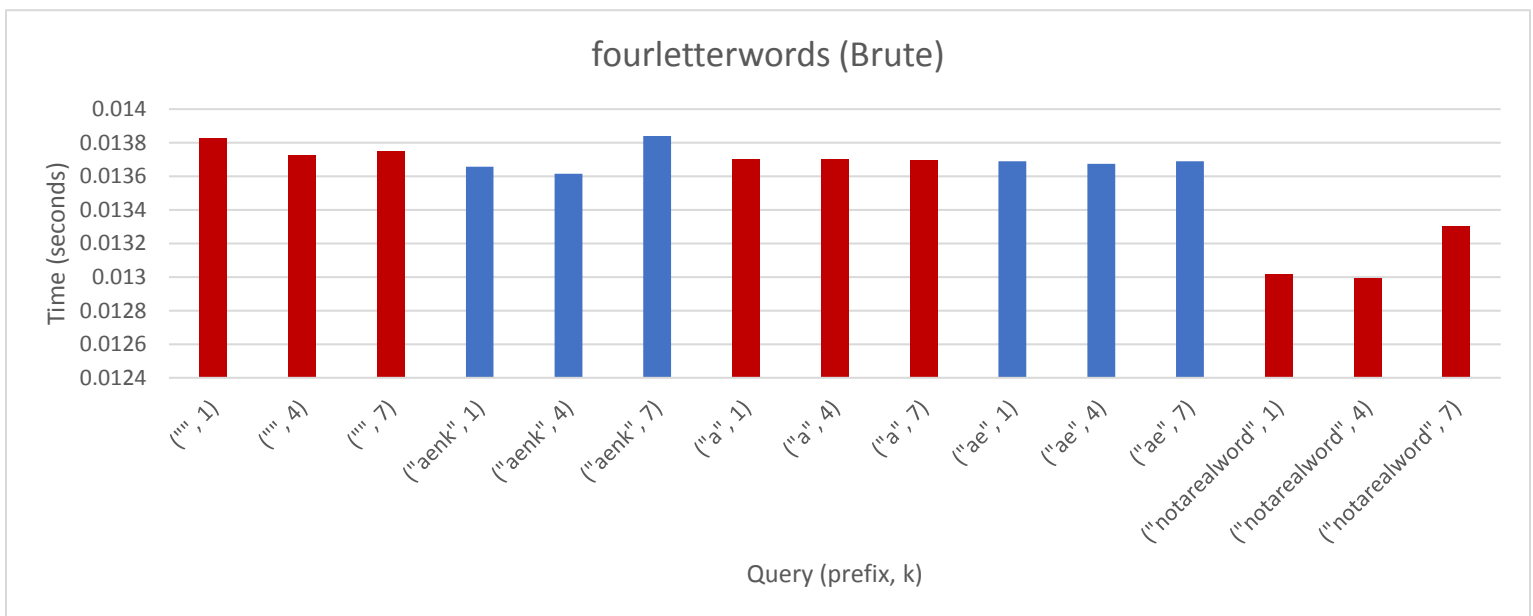
topMatches: $O(n^2)$

This information is presented above in Problem 1.

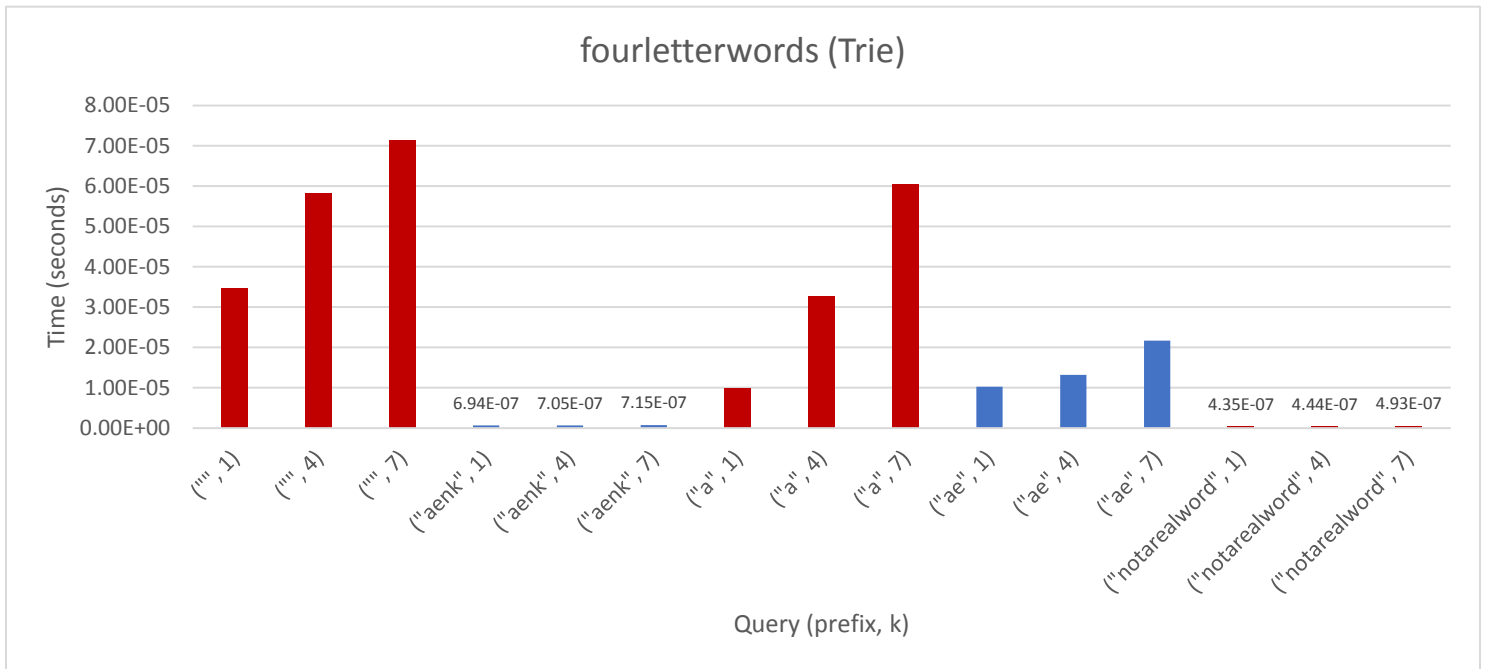
- ii. How does the runtime of *topMatches()* vary with k, assuming a fixed prefix and set of terms? Provide answers for *BruteAutocomplete* and *TrieAutocomplete*. Justify your answer, with both data and algorithmic analysis.

The following observations were made using the given AutocompletorBenchmark class and fourletterwords text file.

BruteAutocomplete: The runtime of topMatches() is nearly the exact same for a fixed prefix and set of terms. This suggests that the runtime of topMatches() in this given implementation is not actually affected the value of k.



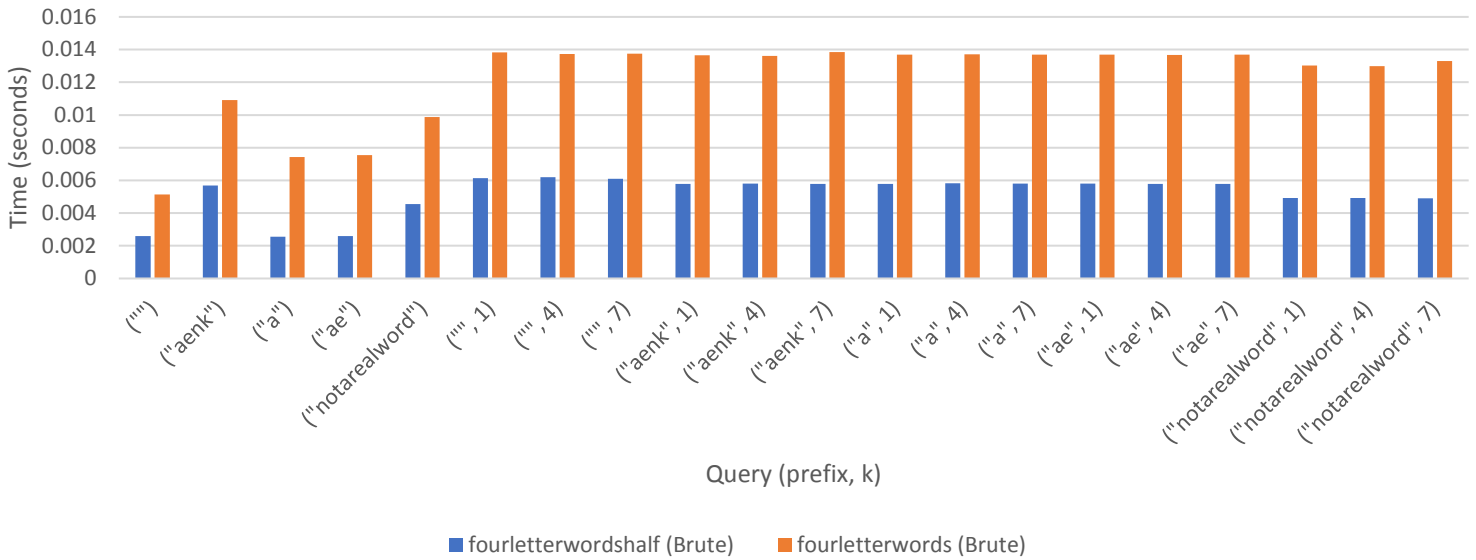
TrieAutocomplete: The runtime of topMatches() consistently increases as the value of k increases. This suggests that increasing values of k are correlated to a slower runtime. This may at least partly be attributed to the fact that TrieAutocomplete has the opportunity to break out of its loop, but BruteAutocomplete cannot do so.



- iii. How does increasing the size of the source and increasing the size of the prefix argument affect the runtime of *topMatch* and *topMatches*? (Tip: Benchmark each implementation using fourletterwords.txt, which has all four-letter combinations from aaaa to zzzz, and fourletterwordshalf.txt, which has all four-letter word combinations from aaaa to mzzz. These datasets provide a very clean distribution of words and an exact 1-to-2 ratio of words in source files.)

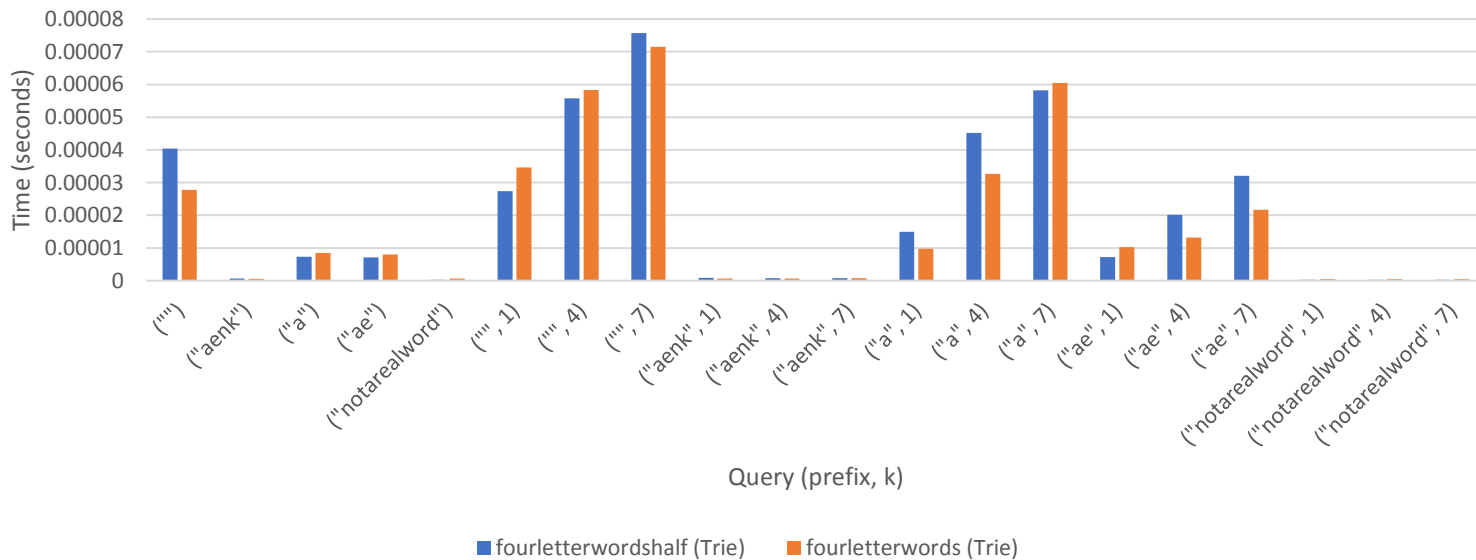
For BruteAutocomplete, increasing the size increases the runtime of topMatch and topMatches in a linear fashion. This is to say that doubling the input will, on average, double the runtime of these functions.

topMatch and topMatches: Source Size Comparison (Brute)



For TrieAutocomplete, increasing the size of the source does not discernibly alter the runtime of topMatch and topMatches. This means that this implementation is far more scalable in comparison to BruteAutocomplete.

topMatch and topMatches: Source Size Comparison (Trie)



4. Graphical Analysis: Provide a graphical analysis by comparing the following:
- The big-Oh for *TrieAutoComplete* after analyzing the pseudocode and big-Oh for *TrieAutoComplete* after the implementation.

Pseudocode:

add: $O(n)$

topMatch: $O(n^2)$

topMatches: $O(n^2)$

Implementation:

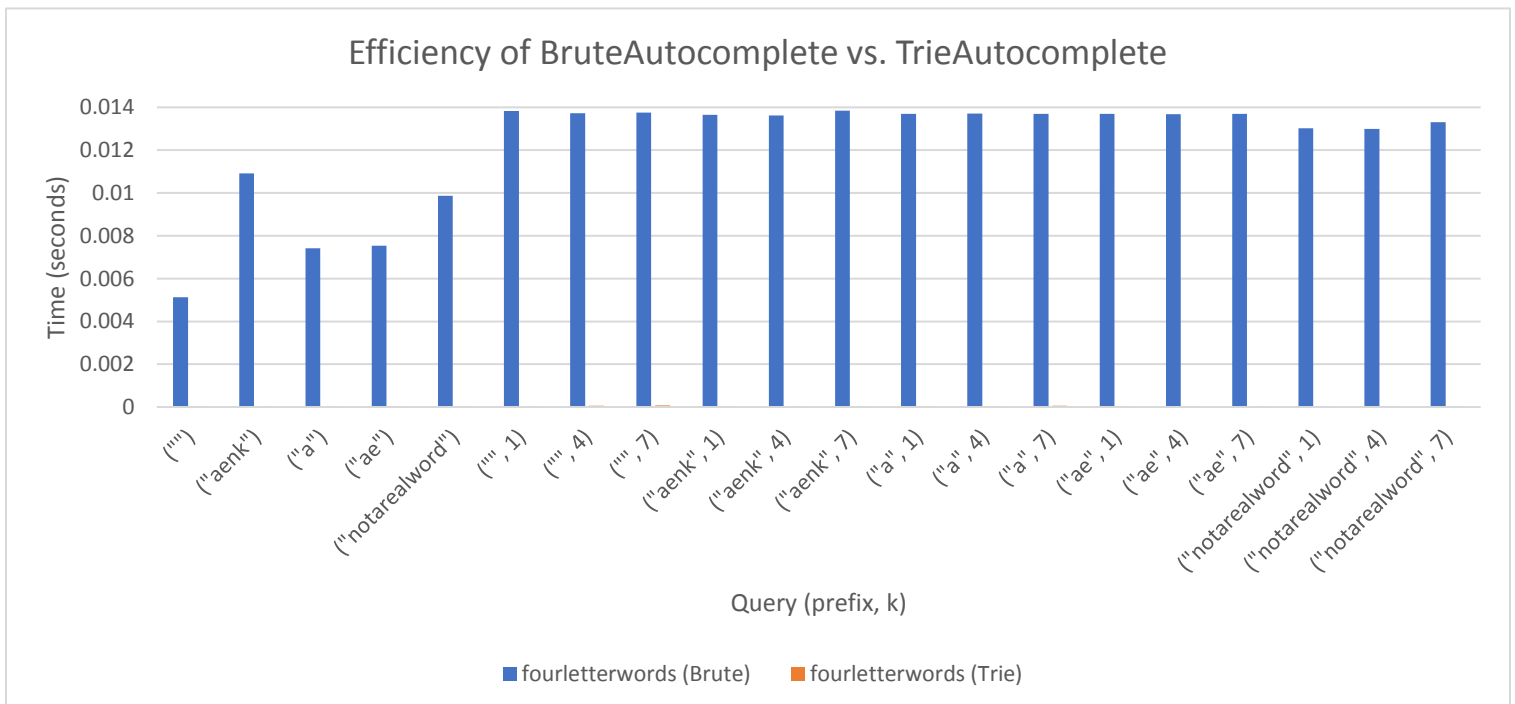
add: $O(n)$

topMatch: $O(n^2)$

topMatches: $O(n^2)$

- Compare the *TrieAutoComplete* with *BruteAutoComplete*.

In all given benchmark cases, TrieAutocomplete is orders of magnitude more efficient than BruteAutocomplete. Note that, when compared to the brute force implementation, the allotted time of the trie strategy is hardly visible in the graph.



The next chart represents the same data but more clearly represents TrieAutocomplete's allotted time when compared to BruteAutocomplete.

