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n = 6; (*number of nodos*) k = 3; (*in-degree*) numexp = 100000; (*number of random digraphs to
generate*) numperms = 1000; (*number of random permutations*)
complexity = Table[0, numexp]; (*list for K-complexity (1-D representation)*)
complexitymat = Table[0, numexp]; (*list for K-complexity (adjacency matrix)*)
entropy = Table[0, numexp]; (*list for entropy values*)

(*create the random digraph*)
Do[Mnodes = {};(*adjacency matrix*)
For[i = 1, i <= n, i++
AppendTo[Mnodes, Table[0, n]]]
For[i = 1, i <= n, i++, flag = 0;
While[flag < k, position = RandomInteger[{1, n}];
If[Mnodes[[i, position]] == 0, Mnodes[[i, position]] = 1; flag++,]];
matadj = Transpose[Mnodes]; (*random digraph*)
Export[NotebookDirectory[] <> ToString[1] <> "file_name.txt", matadj];

(*generate the isomorphisms*)
perms = Cycles[{#}] & /@ RandomChoice[Permutations[Table[i, {i, n}]], numperms];(*generators of
permutations*)
matpermuted = DeleteDuplicates[Permute[Table[Permute[matadj[[i]], #], {i, n}], #] & /@ perms]
;(*permuted matrices*)
complexitypermut = Table[Null, Length[matpermuted] + 1]; (*list for K-complexity (1-D
representation) permuted*)
complexitymatpermut = Table[Null, Length[matpermuted] + 1]; (*list for K-complexity (adjacency
matrix) permuted*)
entropypermut = Table[Null, Length[matpermuted] + 1]; (*list for entropy values permuted*)

(*complexity of the random graph*)
matadjflatten = Flatten[matadj]; (*1-D representation of the random graph*)
If[First[matadjflatten] == 0, output = "0" <> ToString[FromDigits[matadjflatten]], output =
ToString[FromDigits[matadjflatten]]];
complexitypermut[[1]] = StringBDM[output] // N;
complexitymatpermut[[1]] = BDM[matadj, 4] // N;
entropypermut[[1]] = Entropy[output] // N;

(*measure the complexity of the isomorphisms*)
Do[rg = matpermuted[[1]];
mat = Flatten[rg];
If[First[mat] == 0, output = "0" <> ToString[FromDigits[mat]], output =
ToString[FromDigits[mat]]];
complexity[[1 + 1]] = StringBDM[output] // N;
complexitymat[[1 + 1]] = BDM[rg, 4] // N;
entropy[[1 + 1]] = Entropy[output] // N;
If[ IsomorphicGraphQ[AdjacencyGraph[matrix], AdjacencyGraph[matpermuted[[1]]]] == False,
Abort[]] (*check isomorphism*)
, {1, 1, Length[matpermuted]]}
(*the complexity is the minimum value*)
complexity[[1]] = {1, Min[complexitypermut]};
complexitymat[[1]] = {1, Min[complexitymatpermut]};
entropy[[1]] = {1, Min[entropypermut]};
Export[NotebookDirectory[] <> ToString[1] <> "Vecinos_red.txt", matadj];
, {1, 1, numexp}]

(*order the complexities by increasing value*)
sorted = Sort[complexity, #1[[2]] < #2[[2]] &] ;
list = Flatten[First[sorted][[#]]] & /@ Table[i, {i, Length[sorted]}];
data = Flatten[Take[sorted][[#]], {2, 2}] & /@ Table[i, {i, Length[sorted]}];

sortedmat = Sort[complexitymat, #1[[2]] < #2[[2]] &];
listmat = Flatten[First[sortedmat][[#]]] & /@ Table[i, {i, Length[sortedmat]}];
datamat = Flatten[Take[sortedmat][[#]], {2, 2}] & /@ Table[i, {i, Length[sortedmat]}];

sortedent = Sort[entropy, #1[[2]] < #2[[2]] &] // N;
listent = Flatten[First[sortedent][[#]]] & /@ Table[i, {i, Length[sortedent]}];
dataent = Flatten[Take[sortedent][[#]], {2, 2}] & /@ Table[i, {i, Length[sortedent]}];

(*plot the results*)
ListLinePlot[{Rescale[data, {0, Max[data]}], Rescale[datamat, {0, Max[datamat]}],
Rescale[dataent, {0, Max[dataent]}], TargetUnits -> {"experimento", "C(red)"}, AxesLabel ->
Automatic, PlotRange -> All, PlotLegends -> {"K-Complexity (1-D representation)", "K-Complexity
(adjacency matrix)", "Entropy"}, Frame -> True, GridLines -> Automatic, FrameLabel -> {"Ordered
Digraphs", "C(D)"}]

(*draw some of the digraphs by increasing order of complexity*)
numdig = 27; (*number of digraphs to plot*) r = 1; (*flag*)
Table[If[net == Round[(numexp*r/numdig)] || net == 1,
state = Import[NotebookDirectory[] <> ToString[list[[net]]] <> "file_name.txt", "Lines"]; r++;
AdjacencyGraph[ToExpression[state], PlotLabel -> "Digraph " <> ToString[lista[[net]]],
VertexStyle -> RGBColor[1, .78, .72], EdgeStyle -> Black]
, {net, 1, numexp}] /. Null -> Sequence[]

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