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numberofRBN = 2000; (*number of RBN's with the same topology*)
numberofexps = 50; (*number of topologies to test*)
numperms = 5000; (*random permutations of the updating functions to test*)
n = 5; (*number of nodes*) k = 3; (*in-degree*)

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complexityRBNtrimmed = Table[0, numberofexps];
complexityBoolFun = Table[0, numberofexps];
complexityRBN = Table[0, numberofRBN];

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(*generate the updating functions*)
Do[booleanfunction = {}; booleanfunctionMatrix = {}; Clear[a];
A = Table[a[i], {i, 1, k}];
For[i = 0, i < n, i++,
f = BooleanFunction[RandomInteger[{0, (2^k - 1)}], k];
AppendTo[booleanfunction, f];
AppendTo[booleanfunctionsMatrixList,
Boole[BooleanTable[BooleanConvert[Apply[f, A], "NOR"], A]]] ×
AppendTo[booleanfunctionMatrix, BooleanConvert[Apply[f, A], "NOR"]];

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r = 0; (*generate the topology*)
Do[r++; iterations = 1;
Mnodes = Table[Table[0, n], n];
For[i = 1, i ≤ n, i++, Flag = 0;
While[Flag < k, position = RandomInteger[{1, n}];
If[Mnodes[[i, position]] == 0, Mnodes[[i, position]] = 1; Flag++]];
Matrixnodes = Transpose[Mnodes];

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(*generate the dynamics of the network*)
inputstates = Tuples[{0, 1}, n]; (*possible input states*)
outputstates = Table[Table[0, iterations], 2^n]; (*output states*)
For[q = 1, q ≤ 2^n, q++,
neighbors = Table[0, k]; (*positions of the k-neighbors*)
For[i = 1, i ≤ iterations, i++,
statesnodes = Table[0, n]; (*states of the nodes*)
For[j = 1, j ≤ n, j++, (*run over the nodes*) Flag = 0;
For[p = 1, p ≤ n, p++, (*find the k-neighbors*)
If[Matrixnodes[[p, j]] == 1, Flag++;
neighbors[[Flag]] = p]];
For[m = 1, m ≤ k, m++,
(*run over the in-degrees*) a[m] = inputstates[[q, neighbors[[m]]]];
statesnodes[[j]] = FullSimplify[booleanfunctionMatrix[[j]]];
(*transform the states of the nodes into the state of the network*)
outputstates[[q]] = FullSimplify[Boole[statesnodes]];
inputstates[[q]] = FullSimplify[Boole[statesnodes]]];

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(*measure the complexity of the RBN*)
If[First[Flatten[outputstates]] == 0,
codedynamics = "0" <> ToString[FromDigits[Flatten[outputstates]]],
codedynamics = ToString[FromDigits[Flatten[outputstates]]];
complexityRBN[[r]] = StringBDM[codedynamics], numberofRBN];

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(*measure the complexity of the updating functions*)
rg = booleanfunctionsMatrixList; mat = Flatten[rg];
perms = RandomChoice[Permutations[Table[i, {i, n}]], numperms];
isos = DeleteDuplicates[Permute[rg, #] & /@ perms];
complexityiso = Table[0, Length[isos]];
Do[flatten = Flatten[isos[[L]]];
If[First[flatten] == 0,
output = "0" <> ToString[FromDigits[flatten]], output = ToString[FromDigits[flatten]]];
complexityiso[[L]] = StringBDM[output], {L, Length[isos]}];
complexityBoolFun[[y]] = Min[complexityiso];

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(*mean complexity of the RBN's*)
complexityRBNtrimmed[[y]] = TrimmedMean[complexityRBN,
{(Length[Select[complexityRBN, # ≤ Quantile[complexityRBN, 1/4] &])]/Length[complexityRBN],
(Length[Select[complexityRBN, # ≥ Quantile[complexityRBN, 3/4] &])]/
Length[complexityRBN]}], {y, numberofexps}]

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Export[NotebookDirectory[] <> "C(f)_min.txt", complexityBoolFun];
Export[NotebookDirectory[] <> "C(BN)_trim.txt", complexityRBNtrimmed];

```