Program Analysis and Transformation

Final Assignment

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Abstract

The Pendulum Instruction Set Architecture (PISA) was first introduced in 1995 by Carlin James Vieri and is a reversible assembly language. The assembly language has later been improved and several high-level languages has been build upon it. One of those languages is the extension to the reversible object-oriented programming language (ROOPL) ROOPL++ presented in 2018. One of the issues with ROOPL++ was the amount of produced target code. In this paper we compile source code for the data structure of a binary tree, analyse the possibility of redundant target code and points out where an optimization could be done.

Contents

1 Introduction

1.1 Assembly language

A CPU understands its own machine language. Instructions in machine language are numbers stored as bytes in memory. Each instruction has its own unique numeric code called its operation code or opcode for short. An example is the instruction that says add EAX and EBX registers together and store the result back into EAX is encoded by the following hex code:

03 C3

This not readable for the blunt eye. Which is why we have a program called an assembler. An assembler is a program that reads the text of a assembly language program and converts the assembly into machine code. [6, p.11].

The assembly language origins back to Birkbeck College 1946-1962, where the creation was credited to Kathleen Booth.[1] Kathleen Booth was a PhD whom both visited with John Von Neumann with the famous The Von Neumann Architecture[3], helped with the design of multiple machines and was one the founders of the Birkbeck department of computer science.

The assembly language is a symbolic programming language, closest to machine code.[2] An assembly language program is stored as plain text. The text consists of a set of instructions which is processed chronological. Each assembly instruction is equal to one machine instruction for example could above addition be shown as:

add EAX EBX

With the assembly language words as add can be used as mnemonic for the instruction add and so fourth. [6, p.11].

1.1.1 Example program

ForITo100.asm

```
1  J main                          ; for int i = 0; i < 100; i++
2                                  ;     count += i * 2
3  loop_i:
4  MUL $t0, $a1, 2
5  ADD $a0, $a0, $t0               ; count += i * 2
6  ADDI $a1, $a1, 1                ; i++
7  SLT $t0, $a1, $a2
8  BEQ $t0, 1, loop_i              ; i < 100
9  JR $ra                          ; return
10
11 main:
12 ADDI $a0, $zero, 0              ; count = 0
13 ADDI $a1, $zero, 0              ; i = 0
14 ADDI $a2, $zero, 100            ; max
15 JAL loop_i
```

1.2 Reversible computing

A reversible computing system has, at any time, at most a single previous computation state as well as a single next computation state, and thus a reversible computing system.[7] It comes with the promise of reduced energy dissipation, when erasure of information is left out of the program.

The inspiration of reversible computing dates back to 1867 and the study of thermodynamics where James Clark Maxwell made a thought experiment also known as Maxwell's Demon. In the experiment he questions that of the second law of thermodynamics which says:

> [..] It is impossible in a system enclosed in an envelope which permits neither change of volume nor passage of heat, and in which both the temperature and the pressure are everywhere the same, to produce any inequality of temperature or pressure without expenditure of work.[8, p.16]

The experiment was later published in 1872 in a book by Maxwell: Theory of Heat[11], but the connection between thermodynamics and computations was first seen in 1949 by John von Neumann, where he talks about a computation must have a minimum thermodynamic energy dissipation which he determines to[5, p.20][8, p.18]:

> k_BTlnN, k_B as the Boltzmann's constant, T as the temperature and $N = 2$.

Rolf Landauer realize that modern computers with irreversible processes must dissipate that minimum energy as von Neumann described if the erasure of a bit occures thus resulting in atleast the increase of entropy by k_Bln2.[5, p.20][8, p. 18] He also states that reversible operations does not produce the dissipation and irreversible operations can avoid the dissipation by storing information of the computational history. At last Landauer states that the stored history must be erased irreversibly which would just postpone the dissipation of entropy, That last statement is later proven wrong by Charles Bennett.[8, p.19]

In 1970 Charles Bennett looks at Landauers last statement and decides to make an experiment. He creates a reversible program consisting of two halves. The first which provided the calculations intended and the second which undid the calculations from the first halves thus ending the program in its starting point. In the experiment he uses a Turing Machine[10] and shows that the information produces by the intended calculation could be used to undo the calculation instead of just be thrown away. With that experiment Bennett had shown that a reversible process would not just postpone the dissipation of energy it would be able to remove it from the equation.[8, p.18]

From Bennetts experiment he came up with a description for an "enzymatic Turing machine" in which reversible logically operations could be executed[8, p.19]. To fullfill the promise of reduced energy dissipation their was final need of physically logic devices to perform the reversible operations on. Fredkin, Toffoli and Feynmann all aided this need by introducing reversibly logic-gates.[8, p. 19, 22]

1.3 Pendulum microprocessor

Pendulum is a reversible microprocessor, invented by Carlin James Vieri at MIT in 1995. The invention took offset in the existing MIPS R2000 architecture.[REF til ARK][4, p. 29] Vieri's motivation was to create a reversibly processor which would avoid destruction of information and reduce the energy dissipation shown in thermodynamics[1.2] and discussed by Charles Bennet.[8] For this he would focus on memory access, datapath operations on stored values and control flow operations.

The processor has three registers for used in the control flow:

1 The program counter (PC) for storing adress of the current instruction

2 The branch register (BR) for storing jump offsets

3 The direction bit (DIR) for keeping track of the execution direction.

PC is incremented/decremented by the value stored in DIR, thus changing DIR between 1 & -1, will decide in which direction the instructions will be executed. When the DIR is -1, all instructions is inverted.[4, Vieri - Chapter 3, p. 21]

Control flow - Branch instructions like branch or jump is in normal architectures not reversible, that is because the come-from instruction is not stored anywhere, thus the goto instruction not knowing who called it. This could be handled by storing the PC just before the branch/jump in a special register. In later versions of the Pendulum ISA architecture paired branches is introduced, such that each goto instruction should have branch instruction to the come-from.

Control flow - If/then statements is in need of an exit condition known as assert.

if e1 **then** s1 **else** s2 **fi** e2

Control flow - for-loop is in need of an entry, loop and exit condition. Where the e1 should only be true upon entry and e2 only on exit.

from e1 **do** s1 **loop** s2 **until** e2

Control flow - subrutines in encased between a top and a bottom, which both contains a branch to eachother. It follows that the subrutine is skipped when executing instructions sequentially.

top: BRA bot

<..rutine definition goes here..>

bot: BRA top

Memory access is always an exchange. The exchange instruction swaps register value with the value in memory at an address specified by another register.[4, p. 32]

1.4 Motivation

1.5 Outline

2 Programming languages

2.1 Pendulum Assembly Language

Pendulum Instruction Set Architecture(PISA) Assembly Language or a shorthand PAL, is a reversible language. It assembles by the Pendulum microprocessor.[4, p. 48] In this paper we use the Pendulum virtual machine PendVM[9], which executes programs written in PAL. Pendulum instructions is almost identically to the conventional RISC(Reduced Instruction Set Computing) processor. Thus reversible it introduces some new features.

Branch register is normally zero, if the branch register is not zero, the PC increments by the value in the register.[REF - PENDULUM 248] When is happens it the instruction at the destination executes and the branch register is cleared. When implementing subroutines one must use SWAPBR which allows direct access to the branch register, and therefor an exchange the value. It must follow that the subrutine negates the value in the branch register, such that the next SWAPBR will branch back to the location it came from. The branch at the location cancels out the branch register and the PC continues sequentially. SWAPBR has also the capability of performing switch statements. [REF - PENDULUM p. 281] START and FINISH marks the beginning and end of a program. BRA is an unconditional jump.

2.1.1 Example program

ForITo100.pal

```
1  ;; main
2  ;;; increment a from [1..n]
3  subtop:   BRA subbot
4  main:     SWAPBR $2            ; entry/exit point
5            NEG $2               ; negate offset to return caller
6            EXCH $2 $1           ; push return offset to stack
7            ADDI $30 100         ; a += n
8            BRA swap             ; set limit ($28) += a, set a = 0
9  looptop:  BNE $30 $0 loopbot   ; from a = 0 do
10           ADDI $30 1           ; a += 1
11 loopbot:  BNE $30 $28 looptop  ; until a = limit loop body
12           SUB $28 $30          ; set limit = 0
13           ADDI $30 -100        ; a -= n
14           EXCH $2 $1           ; pop return address
15 subbot:   BRA subtop
```

The entire program is shown in the Appendix 7. We have in section 1.1.1 seen how a similar for-loop is written in the irreversible assembly language MIPS. Now lets take a look on the for-loop in the reversible assembly language PAL.

First off the main method is wrapped within a top and a bot. Next we store the offset, so on the end of the method we are able to return to the caller. Now the looptop is checked once like from a = 0 then proceed to the body. From here on the body is executed once and once again until the criteria in loopbot is true.

2.2 Reversible Object-Oriented Programming

Reversible Object-Oriented Programming (ROOPL) and its predecessor ROOPL++ which expanded the language with dynamic memory was created by Tue Haulund and Martin Cservenka. It is build with inspiration from the reversible programming language Janus and compiles to the Pendulum Assembly language.

simplePrg.rplpp

```
1  class Program
2      int nodeCount
3      int limit
4      method main()
5          limit += 100
6          from nodeCount = 0 do
7              skip
8          loop
9              nodeCount += 1
10         until nodeCount = limit
11         nodeCount -= limit
12         limit -= 100
```

This simple program is similar to the two earlier shown assembly programs. Though when compiled the number of instructions explodes. In Appendix 8 the full list of instructions is shown, it sums up to near 400 lines of program.

Lets divide the program into bites:

Part	Lines	Description
Static	4	DATA instruction
Malloc	205	Method for memory allocation
Main	134	Main method equal two the other assembly programs
Program structure	50	START .. FINISH

With the above division, its clear the that even without the malloc method, the compiled program is still way bigger than the simple self-written PAL program. So lets take a closer look on what

3 Analysis of redundancy

In this is section we analyse the possibility of redundant target code after compilation of a ROOPL++ program. First we define a smaller area of *redundancy*:

> Redundancy is several immediate instructions in a row which all affect the same register. For example is the two instructions below seen as redundant:
>
> ADDI $3 10
>
> ADDI $3 8
>
> Instead the target code could have used a single instruction:
>
> ADDI $3 18

Now lets look at a successfull analysis:

> Identify redundancy (if any) in the target code
>
> Describe a method for reducing redundancy.
>
> Show that a program p written in ROOPL++ have the same result as the program p' which is copy of p but with above method applied.

3.1 Reduction

For the task of a successfull analysis we need an algorithm in which can find *redundancy*, merge and remove instruction and atlast update the stack point with the new immediate value. This algorithm can be applied to an existing PAL program, which means, that is first useful, when a ROOPL++ program has been compiled to target code. Thus the algorithm must take a .PAL file and produce a .PAL file.

```
remove_redundancy(filepath fp):
    /* read is a function which takes a filepath
     * and returns a array of elements, where each
     * element is a line the the file.
     * map(func1, l[]) applies func1 to every element of l */

    lines = map(parse_inst, read(fp))

    lastRegister = ''
    lastInstruction = 0
    removeableLines[]

    for i = 0 to length(lines)
      if lines[i][0] == 'ADDI' then
        if lastRegister == lines[i][1] then
           lines[lastInstruction][2] += lines[i][2]
           insert(removeableLines, i)
        else
           lastRegister = lines[i][1]
           lastInstruction = i
      else
          lastRegister = ''
          lastInstruction = 0

    /* Remove all redundant instructions, update stack pointer */
    lines = removeLinesAdjustSP(lines, removeableLines)

    /* write is a function which takes an array
     * and writes a line for each element to a named file */

    write(lines, 'reduced.pal')

/* A method to divide an instruction
 * into opcode, arg0, arg1, arg2 */
parse_inst(instruction):
   return split(instruction, '␣')
```

3.2 Tools

PendVM[9] is a virtual machine on which we can run PAL programs. It does not support methods to save the results of an executed program, which is why i have expanded one of the opcodes: OUT.

OUT is now able to write or append a register value to the text-file static_ storage.text. For now ROOPL has not been expanded which means, that using the OUT functionality requeries three steps:

The immediate value in ADDI just after START has to incremented by the value of need OUT instructions.

The immediate value in ADDI just before FINISH has to incremented by the value of need OUT instructions.

OUT instruction has be manually inserted into the resulting .pal file of a compiled ROOPL++ program.

The expansion of PendVM exists of the following files:

```
int i_out(WORD, WORD, WORD);
```

pendvm.h

```
("OUT", {REG, REG, NIL}, i_out)
```

pal_ parse.c

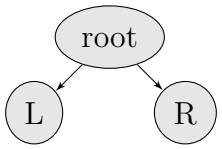
```
int
i_out(WORD r, WORD u1, WORD u2)
  {
  char buf[..];
  sprintf(buf, '%d', m->reg[r1]);
  const char *p = buf;

  FILE *file;
  file = fopen('static_storage.txt', m->reg[r2]);
  fputs(p, file);
  fclose(file);
  return 0;
  }
```

machine.c

4 Data structures

4.1 Binary tree

A binary tree in computer science is a data structure, which is either empty or consist of a root node, where each node has atmost two children. You could see the binary tree as a tuple of the single node root and the two binary trees L & R.



Simple binary tree, with the a root node and two binary trees L & R as children to the root.

Their are different types of binary tree all with their own properties. fx A full binary tree is one where every node either have zero or two child-nodes. A perfect binary tree is one, where all interior nodes have two children and all leaves have none. the A balanced binary tree is one where L & R of every node only differ in height with no more than one. [REF-Introduction to algorithms]

Properties of binary tree is fx maximum height, number of nodes, number of leafs and so on. Operations of different sort can be used of a binary tree some of em is:

Traversal: Search for a node

Insertion: Insert a new node

Deletion: Remove an existing node

5 Conclusion

6 Further work

6.0.1 Instruction operands - [OVERVEJ]

Machine code instructions vary, but in general each instruction itself will have fixed number of operands (0 to 3). Operands can have the following types:[6, p. 12]

register: These operands refer directly to the content of the CPU-register.

memory: These refer to data in memory. The address of the data may be a constant hardcoded into the instruction or may be computed using values of registers. Address are always offsets from the beginning of a segment.

immediate: These fixed values that are listed in the instruction itself. They are stored in the instruction itself (in code segment), not in the data segment.

implied: These operands are not explicitly shown. For example the increment instruction adds one to the register or memory. The one is implied.

6.0.2 Pendulum operation

Operation type					
R	op	rsd	rs	sh/rot	func
bit	6	5	5	5	11
J	j/cf	Target			
bit	6	26			
B	j/b op	ra	rb	offset	
bit	6	5	5	16	
I	op	rsd	immediate		
bit	6	5	21		

Jump instructions other than j and all conditional branches uses B-type instruction encoding and specify two registers and an offset.

Immediate instructions, I-type, specify one register and a 21 bit signed or unsigned, depending on the opcode, immediate value.

Instruction	
ADD	
SUB	
ADDI	
AND	
ANDI	
BEQ	
BGEZ	
BGEZAL	
BGTZ	
BLEZ	Branch on less than or equal to zero
BLTZ	Branch on less than zero
BLTZAL	Branch on less than than zero and link
BNE	Branch on not equal
CF	Come-from

6.1 Pendulum

, with exception of two constraints:

> Memory access is always an exchange. The exchange instruction swaps register value with the value in memory at an address specified by another register.[4, p. 32]

> Non-sequential instructions like jumps to another macro must have a return address. This is needed to keep the reversibility. [4, p. 36] Say an instruction is reached by one jump, then that instruction only needs to keep track a single destination. In case an instruction is reached from multiple other instructions, it needs to keep track of which instruction that made the jump.[4, p. 25]

7 Appendix A

ForITo100.pal

```
1  ;;; increment a from [1..n]
2  subtop:   BRA subbot
3  main:     SWAPBR $2           ; entry/exit point
4            NEG $2              ; negate offset to return caller
5            EXCH $2 $1          ; push return offset to stack
6            ADDI $30 100        ; a += n
7            BRA swap            ; set limit ($28) += a, set a = 0
8  looptop:  BNE $30 $0 loopbot  ; from a = 0 do
9            ADDI $30 1          ; a += 1
10 loopbot:  BNE $30 $28 looptop ; until a = limit loop body
11           SUB $28 $30         ; set limit = 0
12           ADDI $30 -100       ; a -= n
13           EXCH $2 $1          ; pop return address
14 subbot:   BRA subtop
15 ;; swap(int a, int b)
16 subtop_3: BRA subbot_3
17 swap:     SWAPBR $2
18           NEG $2
19           EXCH $2 $1
20           ADD $28 $30
21           SUB $30 $28
22           EXCH $2 $1
23 subbot_3: BRA subtop_3
24 ;; increment (int a)
25 subtop_2: BRA subbot_2
26 incr:     SWAPBR $2
27           NEG $2
28           EXCH $2 $1
29           ADDI $30 1
30           EXCH $2 $1
31 subbot_2: BRA subtop_2
32 ;; write (int a, int mode)
33 subtop_1: BRA subbot_1
34 write:    SWAPBR $2
35           NEG $2
36           EXCH $2 $1
37           OUT $30 $31
38           EXCH $2 $1
39 subbot_1: BRA subtop_1
```

8 Appendix B

8.1 Full program

prg.pal

```
1  ;; pendulum pal file
2  top:                    BRA     start
3  l_r_nodeCount:          DATA    0
4  l_r_limit:              DATA    0
5  l_Program_vt:           DATA    214
6  l_malloc_top:           BRA     l_malloc_bot
7  l_malloc:               SWAPBR  $2
8                          NEG     $2
9                          ADDI    $9  2
10                         XOR     $8  $0
11                         ADDI    $1  1
12                         EXCH    $6  $1
13                         ADDI    $1  1
14                         EXCH    $7  $1
15                         EXCH    $2  $1
16                         ADDI    $1  -1
17                         BRA     l_malloc1
18                         ADDI    $1  1
19                         EXCH    $2  $1
20                         EXCH    $7  $1
21                         ADDI    $1  -1
22                         EXCH    $6  $1
23                         ADDI    $1  -1
24                         XOR     $8  $0
25                         ADDI    $9  -2
26 l_malloc_bot:           BRA     l_malloc_top
27 l_malloc1_top:          BRA     l_malloc1_bot
28                         ADDI    $1  1
29                         EXCH    $2  $1
30                         SUB     $17 $8
31                         XOR     $17 $4
32 l_malloc1:              SWAPBR  $2
33                         NEG     $2
34                         EXCH    $2  $1
35                         ADDI    $1  -1
36                         XOR     $17 $4
37                         ADD     $17 $8
38                         EXCH    $19 $17
39                         XOR     $18 $19
```

```
40 |                          EXCH   $19 $17
41 |                          XOR    $13 $9
42 |                          SUB    $13 $7
43 | cmp_top_1:               BGEZ   $13 cmp_bot_2
44 |                          XORI   $14 1
45 | cmp_bot_2:               BGEZ   $13 cmp_top_1
46 |                          XOR    $10 $14
47 | cmp_bot_2_i:             BGEZ   $13 cmp_top_1_i
48 |                          XORI   $14 1
49 | cmp_top_1_i:             BGEZ   $13 cmp_bot_2_i
50 |                          ADD    $13 $7
51 |                          XOR    $13 $9
52 | l_o_test:                BEQ    $10 $0 l_o_test_false
53 |                          XORI   $10 1
54 |                          ADDI   $8 1
55 |                          EXCH   $19 $17
56 |                          XOR    $18 $19
57 |                          EXCH   $19 $17
58 |                          RL     $9 1
59 |                          EXCH   $10 $1
60 |                          ADDI   $1 -1
61 |                          EXCH   $11 $1
62 |                          ADDI   $1 -1
63 |                          EXCH   $12 $1
64 |                          ADDI   $1 -1
65 |                          EXCH   $14 $1
66 |                          ADDI   $1 -1
67 |                          EXCH   $16 $1
68 |                          ADDI   $1 -1
69 |                          EXCH   $17 $1
70 |                          ADDI   $1 -1
71 |                          EXCH   $18 $1
72 |                          ADDI   $1 -1
73 |                          EXCH   $20 $1
74 |                          ADDI   $1 -1
75 |                          EXCH   $21 $1
76 |                          ADDI   $1 -1
77 |                          EXCH   $22 $1
78 |                          ADDI   $1 -1
79 |                          EXCH   $23 $1
80 |                          ADDI   $1 -1
81 |                          BRA    l_malloc1
82 |                          ADDI   $1 1
83 |                          EXCH   $23 $1
84 |                          ADDI   $1 1
```

```
85                              EXCH    $22 $1
86                              ADDI    $1 1
87                              EXCH    $21 $1
88                              ADDI    $1 1
89                              EXCH    $20 $1
90                              ADDI    $1 1
91                              EXCH    $18 $1
92                              ADDI    $1 1
93                              EXCH    $17 $1
94                              ADDI    $1 1
95                              EXCH    $16 $1
96                              ADDI    $1 1
97                              EXCH    $14 $1
98                              ADDI    $1 1
99                              EXCH    $12 $1
100                             ADDI    $1 1
101                             EXCH    $11 $1
102                             ADDI    $1 1
103                             EXCH    $10 $1
104                             RR      $9 1
105                             ADDI    $8 -1
106                             XORI    $10 1
107 l_o_assert_true:            BRA     l_o_assert
108 l_o_test_false:             BRA     l_o_test
109 cmp_top_5:                  BEQ     $18 $0 cmp_bot_6
110                             XORI    $20 1
111 cmp_bot_6:                  BEQ     $18 $0 cmp_top_5
112                             XOR     $11 $20
113 cmp_bot_6_i:                BEQ     $18 $0 cmp_top_5_i
114                             XORI    $20 1
115 cmp_top_5_i:                BEQ     $18 $0 cmp_bot_6_i
116 l_i_test:                   BEQ     $11 $0 l_i_test_false
117                             XORI    $11 1
118                             ADD     $6 $18
119                             SUB     $18 $6
120                             EXCH    $12 $6
121                             EXCH    $12 $17
122                             XOR     $12 $6
123                             XORI    $11 1
124 l_i_assert_true:            BRA     l_i_assert
125 l_i_test_false:             BRA     l_i_test
126                             ADDI    $8 1
127                             RL      $9 1
128                             EXCH    $10 $1
129                             ADDI    $1 -1
```

```
130                     EXCH    $11 $1
131                     ADDI    $1 -1
132                     EXCH    $12 $1
133                     ADDI    $1 -1
134                     EXCH    $14 $1
135                     ADDI    $1 -1
136                     EXCH    $16 $1
137                     ADDI    $1 -1
138                     EXCH    $17 $1
139                     ADDI    $1 -1
140                     EXCH    $18 $1
141                     ADDI    $1 -1
142                     EXCH    $20 $1
143                     ADDI    $1 -1
144                     EXCH    $21 $1
145                     ADDI    $1 -1
146                     EXCH    $22 $1
147                     ADDI    $1 -1
148                     EXCH    $23 $1
149                     ADDI    $1 -1
150                     BRA     l_malloc1
151                     ADDI    $1 1
152                     EXCH    $23 $1
153                     ADDI    $1 1
154                     EXCH    $22 $1
155                     ADDI    $1 1
156                     EXCH    $21 $1
157                     ADDI    $1 1
158                     EXCH    $20 $1
159                     ADDI    $1 1
160                     EXCH    $18 $1
161                     ADDI    $1 1
162                     EXCH    $17 $1
163                     ADDI    $1 1
164                     EXCH    $16 $1
165                     ADDI    $1 1
166                     EXCH    $14 $1
167                     ADDI    $1 1
168                     EXCH    $12 $1
169                     ADDI    $1 1
170                     EXCH    $11 $1
171                     ADDI    $1 1
172                     EXCH    $10 $1
173                     RR      $9 1
174                     ADDI    $8 -1
```

```
175                         XOR     $12 $6
176                         EXCH    $12 $17
177                         ADD     $6 $9
178 l_i_assert:             BNE     $11 $0 l_i_assert_true
179                         EXCH    $12 $17
180                         SUB     $6 $9
181 cmp_top_7:              BEQ     $6 $12 cmp_bot_8
182                         XORI    $21 1
183 cmp_bot_8:              BEQ     $6 $12 cmp_top_7
184 cmp_top_9:              BNE     $12 $0 cmp_bot_10
185                         XORI    $22 1
186 cmp_bot_10:             BNE     $12 $0 cmp_top_9
187                         ORX     $23 $21 $22
188                         XOR     $11 $23
189                         ORX     $23 $21 $22
190 cmp_bot_10_i:           BNE     $12 $0 cmp_top_9_i
191                         XORI    $22 1
192 cmp_top_9_i:           BNE     $12 $0 cmp_bot_10_i
193 cmp_bot_8_i:           BEQ     $6 $12 cmp_top_7_i
194                         XORI    $21 1
195 cmp_top_7_i:           BEQ     $6 $12 cmp_bot_8_i
196                         ADD     $6 $9
197                         EXCH    $12 $17
198 l_o_assert:             BNE     $10 $0 l_o_assert_true
199                         XOR     $15 $9
200                         SUB     $15 $7
201 cmp_top_3:              BGEZ    $15 cmp_bot_4
202                         XORI    $16 1
203 cmp_bot_4:              BGEZ    $15 cmp_top_3
204                         XOR     $10 $16
205 cmp_bot_4_i:           BGEZ    $15 cmp_top_3_i
206                         XORI    $16 1
207 cmp_top_3_i:           BGEZ    $15 cmp_bot_4_i
208                         ADD     $15 $7
209                         XOR     $15 $9
210 l_malloc1_bot:          BRA     l_malloc1_top
211 l_main_0_top:           BRA     l_main_0_bot
212                         ADDI    $1 1
213                         EXCH    $2 $1
214                         EXCH    $3 $1
215                         ADDI    $1 -1
216 l_main_0:               SWAPBR  $2
217                         NEG     $2
218                         ADDI    $1 1
219                         EXCH    $3 $1
```

```
220                             EXCH    $2 $1
221                             ADDI    $1 -1
222                             ADD     $6 $3
223                             ADDI    $6 3
224                             EXCH    $7 $6
225                             ADDI    $6 -3
226                             SUB     $6 $3
227                             XORI    $8 100
228                             ADD     $7 $8
229                             XORI    $8 100
230                             ADD     $6 $3
231                             ADDI    $6 3
232                             EXCH    $7 $6
233                             ADDI    $6 -3
234                             SUB     $6 $3
235                             XORI    $6 1
236 entry_11:                   BEQ     $6 $0 assert_13
237                             ADD     $7 $3
238                             ADDI    $7 2
239                             EXCH    $8 $7
240                             ADDI    $7 -2
241                             SUB     $7 $3
242 cmp_top_15:                 BNE     $8 $0 cmp_bot_16
243                             XORI    $9 1
244 cmp_bot_16:                 BNE     $8 $0 cmp_top_15
245 f_top_17:                   BEQ     $9 $0 f_bot_18
246                             XORI    $10 1
247 f_bot_18:                   BEQ     $9 $0 f_top_17
248                             XOR     $6 $10
249 f_bot_18_i:                 BEQ     $9 $0 f_top_17_i
250                             XORI    $10 1
251 f_top_17_i:                 BEQ     $9 $0 f_bot_18_i
252 cmp_bot_16_i:               BNE     $8 $0 cmp_top_15_i
253                             XORI    $9 1
254 cmp_top_15_i:               BNE     $8 $0 cmp_bot_16_i
255                             ADD     $7 $3
256                             ADDI    $7 2
257                             EXCH    $8 $7
258                             ADDI    $7 -2
259                             SUB     $7 $3
260                             ADD     $7 $3
261                             ADDI    $7 2
262                             EXCH    $8 $7
263                             ADDI    $7 -2
264                             SUB     $7 $3
```

```
265                             ADD     $9 $3
266                             ADDI    $9 3
267                             EXCH    $10 $9
268                             ADDI    $9 -3
269                             SUB     $9 $3
270 cmp_top_19:                 BNE     $8 $10 cmp_bot_20
271                             XORI    $11 1
272 cmp_bot_20:                 BNE     $8 $10 cmp_top_19
273 f_top_21:                   BEQ     $11 $0 f_bot_22
274                             XORI    $12 1
275 f_bot_22:                   BEQ     $11 $0 f_top_21
276                             XOR     $6 $12
277 f_bot_22_i:                 BEQ     $11 $0 f_top_21_i
278                             XORI    $12 1
279 f_top_21_i:                 BEQ     $11 $0 f_bot_22_i
280 cmp_bot_20_i:               BNE     $8 $10 cmp_top_19_i
281                             XORI    $11 1
282 cmp_top_19_i:               BNE     $8 $10 cmp_bot_20_i
283                             ADD     $9 $3
284                             ADDI    $9 3
285                             EXCH    $10 $9
286                             ADDI    $9 -3
287                             SUB     $9 $3
288                             ADD     $7 $3
289                             ADDI    $7 2
290                             EXCH    $8 $7
291                             ADDI    $7 -2
292                             SUB     $7 $3
293 test_12:                    BNE     $6 $0 exit_14
294                             ADD     $7 $3
295                             ADDI    $7 2
296                             EXCH    $8 $7
297                             ADDI    $7 -2
298                             SUB     $7 $3
299                             XORI    $9 1
300                             ADD     $8 $9
301                             XORI    $9 1
302                             ADD     $7 $3
303                             ADDI    $7 2
304                             EXCH    $8 $7
305                             ADDI    $7 -2
306                             SUB     $7 $3
307 assert_13:                  BRA     entry_11
308 exit_14:                    BRA     test_12
309                             XORI    $6 1
```

```
310                             ADD     $6 $3
311                             ADDI    $6 2
312                             EXCH    $7 $6
313                             ADDI    $6 -2
314                             SUB     $6 $3
315                             ADD     $8 $3
316                             ADDI    $8 3
317                             EXCH    $9 $8
318                             ADDI    $8 -3
319                             SUB     $8 $3
320                             SUB     $7 $9
321                             ADD     $8 $3
322                             ADDI    $8 3
323                             EXCH    $9 $8
324                             ADDI    $8 -3
325                             SUB     $8 $3
326                             ADD     $6 $3
327                             ADDI    $6 2
328                             EXCH    $7 $6
329                             ADDI    $6 -2
330                             SUB     $6 $3
331                             ADD     $6 $3
332                             ADDI    $6 3
333                             EXCH    $7 $6
334                             ADDI    $6 -3
335                             SUB     $6 $3
336                             XORI    $8 100
337                             SUB     $7 $8
338                             XORI    $8 100
339                             ADD     $6 $3
340                             ADDI    $6 3
341                             EXCH    $7 $6
342                             ADDI    $6 -3
343                             SUB     $6 $3
344 l_main_0_bot:               BRA     l_main_0_top
345 start:                      BRA     top
346                             START
347                             ADDI    $4 393
348                             XOR     $5 $4
349                             ADDI    $5 10
350                             XOR     $7 $5
351                             ADDI    $4 10
352                             ADDI    $4 -1
353                             EXCH    $7 $4
354                             ADDI    $4 1
```

```
355                             ADDI    $4 -10
356                             XOR     $1 $5
357                             ADDI    $1 2048
358                             ADDI    $1 -4
359                             XOR     $3 $1
360                             XORI    $6 3
361                             EXCH    $6 $3
362                             ADDI    $1 -1
363                             EXCH    $3 $1
364                             ADDI    $1 -1
365                             BRA     l_main_0
366                             ADDI    $1 1
367                             EXCH    $3 $1
368                             ADDI    $3 1
369                             ADDI    $3 1
370                             EXCH    $6 $3
371                             XORI    $7 1
372                             EXCH    $6 $7
373                             XORI    $7 1
374                             ADDI    $3 -1
375                             ADDI    $3 -1
376                             ADDI    $3 1
377                             ADDI    $3 2
378                             EXCH    $6 $3
379                             XORI    $7 2
380                             EXCH    $6 $7
381                             XORI    $7 2
382                             ADDI    $3 -2
383                             ADDI    $3 -1
384                             ADDI    $1 1
385                             EXCH    $6 $3
386                             XORI    $6 3
387                             XOR     $3 $1
388                             ADDI    $1 4
389                             ADDI    $1 -2048
390                             XOR     $1 $5
391                             ADDI    $5 -10
392                             XOR     $5 $4
393                             ADDI    $4 -393
394 finish:                     FINISH
```

8.1.1 Malloc

malloc

```
1  l_malloc_top:          BRA     l_malloc_bot
2  l_malloc:              SWAPBR  $2
3                         NEG     $2
4                         ADDI    $9  2
5                         XOR     $8  $0
6                         ADDI    $1  1
7                         EXCH    $6  $1
8                         ADDI    $1  1
9                         EXCH    $7  $1
10                        EXCH    $2  $1
11                        ADDI    $1  -1
12                        BRA     l_malloc1
13                        ADDI    $1  1
14                        EXCH    $2  $1
15                        EXCH    $7  $1
16                        ADDI    $1  -1
17                        EXCH    $6  $1
18                        ADDI    $1  -1
19                        XOR     $8  $0
20                        ADDI    $9  -2
21 l_malloc_bot:          BRA     l_malloc_top
```

malloc1

```
1  l_malloc1_top:         BRA     l_malloc1_bot
2                         ADDI    $1  1
3                         EXCH    $2  $1
4                         SUB     $17 $8
5                         XOR     $17 $4
6  l_malloc1:             SWAPBR  $2
7                         NEG     $2
8                         ADD     $15 $7
9                         XOR     $15 $9
10 l_malloc1_bot:         BRA     l_malloc1_top
```

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