

Program Analysis and Transformation

Search and Reduce Redundant Patterns in ROOPLPPC

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Abstract

The Pendulum Instruction Set Architecture (PISA) was first introduced in 1995 by Carlin James Vieri and is a reversible assembly language. The assembly language has later been improved and several high-level languages has been build upon it. One of those languages is the extension to the reversible object-oriented programming language (ROOPL) ROOPL++ presented in 2018. One of the issues with ROOPL++ was the amount of produced target code. In this paper we compile source code for a small program counting from 1..100, analyse the possibility of redundant target code and points out where an optimization could be done.

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1 Introduction

1.1 Assembly language

To communicate with the hardware of a computer, one should speak its language. Each Central Processor Unit (CPU) understands its own machine language. This language is known as instructions, stored as bytes in memory. Each instruction has its own unique numeric code called its operation code or opcode for short. A set of instructions is the vocabulary of the language [11, p.76]. An example in MIPS Assembly Language [11] is the instruction that says add \$s1(register:17) and \$s2(register:18) registers together and store the result into \$t0 (register:8), which is encoded by the following hex code:

0232 4020

This not readable for the blunt eye which is why we have a program called an assembler. An assembler is a program that reads the text of an assembly language program and converts the assembly into machine code [6, p.11].

The assembly language origins back to Birkbeck College 1946-1962, where the creation was credited to Kathleen Booth [1]. Kathleen Booth was a PhD whom both visited with John Von Neumann with the famous The Von Neumann Architecture [3], helped with the design of multiple machines and was one of the founders of the Birkbeck department of computer science.

The assembly language is a symbolic programming language, closest to machine code [2]. An assembly language program is stored as plain text. The text consists of a set of instructions which is processed chronological. Each assembly instruction is equal to one machine instruction for example could above addition be shown as:

add \$t0, \$s1, \$s2

1.1.1 Example program

ForITo100.asm

1	J main	<i>; for int i = 0; i < 100; i++</i>
2		<i>; count += i</i>
3	loop_i:	
4	ADD \$a0, \$a0, \$zero	<i>; count += i</i>
5	ADDI \$a1, \$a1, 1	<i>; i++</i>
6	SLT \$t0, \$a1, \$a2	
7	BEQ \$t0, 1, loop_i	<i>; i < 100</i>
8	JR \$ra	<i>; return</i>
9		
10	main:	
11	ADDI \$a0, \$zero, 0	<i>; count = 0</i>
12	ADDI \$a1, \$zero, 0	<i>; i = 0</i>
13	ADDI \$a2, \$zero, 100	<i>; max</i>
14	JAL loop_i	

1.2 Reversible computing

A reversible computing system has, at any time, at most a single previous computation state as well as a single next computation state, and thus a reversible computing system [7]. It comes with the promise of reduced energy dissipation, when erasure of information is left out of the program.

The inspiration of reversible computing dates back to 1867 and the study of thermodynamics where James Clark Maxwell made a thought experiment also known as Maxwell's Demon. In the experiment he questions that of the second law of thermodynamics which says:

[..] It is impossible in a system enclosed in an envelope which permits neither change of volume nor passage of heat, and in which both the temperature and the pressure are everywhere the same, to produce any inequality of temperature or pressure without expenditure of work [8, p.16].

The experiment was later published in 1872 in a book by Maxwell: Theory of Heat [12], while the connection between thermodynamics and computations was first seen in 1949 by John von Neumann. It was in one of his lectures, where he spoke about computations, and the must of a minimum thermodynamic energy dissipation. A minimum which he determines to [5, p.20][8, p.18]:

$k_B T \ln N$, k_B as the Boltzmann's constant, T as the temperature and $N = 2$.

Rolf Landauer realize that modern computers with irreversible processes must dissipate that minimum energy as von Neumann described if the erasure of a bit occurs thus resulting in at least the increase of entropy by $k_B \ln 2$ [5, p.20][8, p.18]. He also states that reversible operations does not produce the dissipation and irreversible operations can avoid the dissipation by storing information of the computational history. At last Landauer states that the stored history must be erased irreversibly which would just postpone the dissipation of entropy, That last statement is later proven wrong by Charles Bennett [8, p.19].

In 1970 Charles Bennett looks at Landauers last statement and decides to make an experiment. He creates a reversible program consisting of two halves. The first which provides the calculations intended and the second which undid the calculations from the first halves thus ending the program in its starting point. In the experiment he uses a Turing Machine[10] and shows that the information produced by the intended calculation could be used to undo the calculation instead of just be thrown away. With that experiment Bennett had shown that a reversible process would not just postpone the dissipation of entropy it would be able to remove it from the equation [8, p.18].

From Bennetts experiment he came up with a description for an "enzymatic Turing machine" in which reversible logically operations could be executed [8, p.19]. To fullfill the promise of reduced energy dissipation their was a final need of physically logic devices to perform the reversible operations on. Fredkin, Toffoli and Feynmann all aided this need by introducing reversibly logic-gates [8, p.19,22].

1.3 Pendulum microprocessor

Pendulum is a reversible microprocessor, invented by Carlin James Vieri at MIT in 1995. The invention took offset in the existing MIPS R2000 architecture [11][4, p.29]. Vieri's motivation was to create a reversibly processor which would avoid destruction of information and reduce the energy dissipation shown in thermodynamics[1.2] and discussed by Charles Bennet [8]. For this he would focus on memory access, datapath operations on stored values and control flow operations.

The processor has three registers used in the control flow:

- 1 The program counter (PC) for storing address of the current instruction
- 2 The branch register (BR) for storing jump offsets
- 3 The direction bit (DIR) for keeping track of the execution direction.

PC is incremented/decremented by the value stored in DIR, thus changing DIR between 1 & -1, will decide in which direction the instructions will be executed. When the DIR is -1, all instructions is inverted [4, p.21].

Branch instructions like branch or jump is in normal architectures not reversible, that is because the come-from instruction is not stored anywhere, thus the goto instruction not knowing who called it. This could be handled by storing the PC just before the branch/jump in a special register. In later versions of the Pendulum ISA architecture paired branches is introduced, such that each goto instruction should have branch instruction to the come-from.

If/then statements is in need of an exit condition known as assert.

if e1 then s1 else s2 fi e2

For-loop is in need of an entry, loop and exit condition. Where the e1 should only be true upon entry and e2 only on exit.

from e1 do s1 loop s2 until e2

Subroutines in encased between a top and a bottom, which both contains a branch to each other. It follows that the subroutine is skipped when executing instructions sequentially.

top: BRA bot

<..routine definition goes here..>

bot: BRA top

Memory access is always an exchange. The exchange instruction swaps register value with the value in memory at an address specified by another register [4, p.32].

1.4 Motivation

First of the professor Robert Glück, which gave the inspiration and idea by introducing ROOPL and the two masters thesis of Tue Haulund and Martin Holm Cservenka. Next the motivation for this paper comes from the evaluation in the Masters Thesis of Martin Holm Cservenka [14, p.72], in which he shows the blow up of a compiled ROOPL++ program. From this point I couldn't leave the thought, that maybe the compiler left possible redundant patterns, in which one could reduce or simply remove. With tools like PendVM and the ROOPL compiler at hand the task was straight forward: Write a simple program first directly in the Pendulum Assembly Language and then compare it to a similar compiled ROOPL++ program, find if any unnecessary redundant patterns and reduce/remove them from the program.

1.5 Statement

A separate program which takes the target code of compiled ROOPL++ program, reduce some patterns which is redundant and returns a new file of target code without those patterns.

1.6 Outline

This paper consists of four chapters:

Chapter 1 is the introductory chapter and gives a short introduction to the history of assembly and reversible computing.

Chapter 2 presents two programming languages The Pendulum Assembly Language and ROOPL. A small program is introduced in both languages and compared at the assembly level.

Chapter 3 analyze patterns within the assembly language and search for redundancy.

Chapter 4 evaluates the results from the analysis and presents a conclusion and suggestions for further work.

2 Programming languages

2.1 Pendulum Assembly Language

Pendulum Instruction Set Architecture(PISA) Assembly Language or a shorthand PAL, is a reversible language. It assembles by the Pendulum microprocessor [4, p.48]. In this paper we use the Pendulum virtual machine PendVM [9], which executes programs written in PAL. Pendulum instructions is almost identically to the conventional RISC(Reduced Instruction Set Computing) processor. Thus reversible it introduces some new features.

Branch register is normally zero, if the branch register is not zero, the PC increments by the value in the register [5, p.278]. When this happens the instruction at the destination executes and the branch register is cleared. When implementing subroutines one must use SWAPBR which allows direct access to the branch register, and by that, store the value at the beginning and pop at the end of the routine. It must follow that the subroutine negates the value in the branch register, such that the next SWAPBR will branch back to the location it came from. The branch at the location cancels out the branch register and the PC continues sequentially.

2.1.1 Example program

ForITo100.pal

```
1  ;; main
2  ;;; increment a from [1..n]
3  subtop:  BRA subbot
4  main:    SWAPBR $2          ; entry/exit point
5           NEG $2            ; negate offset to return caller
6           EXCH $2 $1        ; push return offset to stack
7           ADDI $30 100      ; a += n
8           BRA swap          ; set limit ($28) += a, set a = 0
9  looptop: BNE $30 $0 loopbot ; from a = 0 do
10           ADDI $30 1        ; a += 1
11  loopbot: BNE $30 $28 looptop; until a = limit loop body
12           SUB $28 $30       ; set limit = 0
13           ADDI $30 -100     ; a -= n
14           EXCH $2 $1        ; pop return address
15  subbot:  BRA subtop
```

The entire program is shown in the Appendix 7. We have in section 1.1.1 seen how a similar for-loop is written in the irreversible assembly language MIPS. Now let us take a look on the for-loop in the reversible assembly language PAL.

First off the main method is wrapped within a top and a bot. Next we store the offset, so on the end of the method we are able to return to the caller. Now the looptop is checked once like from a = 0 then proceed to the body. From here on the body is executed once and once again until the criteria in loopbot is true.

2.2 Reversible Object-Oriented Programming

Reversible Object-Oriented Programming (ROOPL) and its successor ROOPL++ which expanded the language with dynamic memory was created by Tue Haulund and Martin Cservenka is build with inspiration from the reversible programming language Janus and compiles to the Pendulum Assembly language. The latest extension of the compiler is accessible at github [\[13\]](#).

simplePrg.rplpp

```
1 class Program
2     int nodeCount
3     int limit
4     method main()
5         limit += 100
6         from nodeCount = 0 do
7             skip
8         loop
9             nodeCount += 1
10            until nodeCount = limit
11            nodeCount -= limit
12            limit -= 100
```

This simple program is similar to the two earlier shown assembly programs. Though when compiled the number of instructions explodes. In Appendix 8 the full list of instructions is shown, it sums up to near 400 lines of program.

The program could be divided into parts:

Part	Lines	Description
Static	4	DATA instruction
Malloc	205	Method for memory allocation
Main	134	Main method equal two the other assembly programs
Program structure	54	START .. FINISH

With the above division, its clear that even without the malloc method, the compiled program is still way bigger than the simple self-written PAL program.

A closer look on the main method shows that 26 lines holds a bunch of if-statements with named macros as **cmp** og **f**. The entire entry macro counts 57 lines including the special if-statements. The initialization and clean-up is 20 and 35 lines, where the loop-body is 14 lines.

Part	Lines
1_ main_ 0 to entry	20
entry to test	57
test	14
after exit	35

In the next chapter the focus is on the main method and the program structure. We look into the possibility of redundancy and search for patterns which is unnecessary for the program.

3 Analysis of redundancy

In this section we analyze the possibility of redundant target code after compilation of the ROOPL++ program introduced in section 2.2. The analysis is split into two parts.

The first part will be a stepwise approach going through the following states:

Discover patterns which is repeated multiple times throughout the target code

Isolate the patterns into subroutines to make the target code more readable

Group subroutines by purpose

Try to reduce the groups, for example by introducing new instructions

The second part describes methods for reducing redundancy by eliminating or replacing redundant patterns found in the first part.

3.1 First part - patterns

This is the first part of the analysis, where we try to identify patterns which is occurring multiple times throughout the target code.

3.1.1 Getting data from memory

Multiple times we'll see a pattern for exchange between a register value and a place in memory. We look into an example starting between entry and the first **cmp**.

The pattern goes like this: Put the address of nodeCount into register 7. Use the address in register 7 to exchange the nodeCount in memory with the zero value in register 8. Register 8 now holds the value of nodeCount. This part is reached several times, once for each time nodeCount is not 100. This exchange is placed 6 times in the code.

We isolate the pattern by introducing a subroutine count. Count can replace the 6 redundant patterns:

subtop:	BRA	subbot
count:	SWAPBR	\$2
	NEG	\$2
	EXCH	\$2 \$1
	ADD	\$7 \$3
	ADDI	\$7 2
	EXCH	\$8 \$7
	ADDI	\$7 -2
	SUB	\$7 \$3
	EXCH	\$2 \$1
subbot:	BRA	subtop

We see that the exchange part takes up 5 lines, where the subroutine takes 10 +1 for the call. Exchanges done more than 2 times could line wise be subroutines. Another benefit by isolating exchanges is the readability in the actual main method.

This pattern is not only seen when retrieving the nodeCount, it is seen every time memory and a register has to communicate. This exchange is the same as changing the register value in \$r1 with the value in memory of the stack pointer + some offset. One could formalize a method m with three arguments: m(r1, sp, offset). Why this could be a place to introduce a new instruction.

3.1.2 Special if-statements

Throughout the target code, we seen multiple auto-generated if-statements, with labels like **cmp** and **f**. Lets start by isolating the areas with special if-statements.

subtop_if_1:	BRA	subbot_if_1
if_1:	SWAPB	\$2
	NEG	\$2
	EXCH	\$2 \$1
cmp_top_15:	BNE	\$8 \$0 cmp_bot_16
	XORI	\$9 1
cmp_bot_16:	BNE	\$8 \$0 cmp_top_15
f_top_17:	BEQ	\$9 \$0 f_bot_18
	XORI	\$10 1
f_bot_18:	BEQ	\$9 \$0 f_top_17
	XOR	\$6 \$10
f_bot_18_i:	BEQ	\$9 \$0 f_top_17_i
	XORI	\$10 1
f_top_17_i:	BEQ	\$9 \$0 f_bot_18_i
cmp_bot_16_i:	BNE	\$8 \$0 cmp_top_15_i
	XORI	\$9 1
cmp_top_15_i:	BNE	\$8 \$0 cmp_bot_16_i
	EXCH	\$2 \$1
subbot_if_1:	BRA	subtop_if_1

At first glance we see that the purpose is to set \$6 at one or zero. Simple if-statement could possibly replace the above both complicated and hard-to-read set of instructions. Let's try to figurer out the parts. Let's say if $8 = 0$, then XOR \$6 by \$10, where \$10 is the same as 1. This could be written as below.

```
iftop_3:          BNE    $8 $0 ifbot_3
                  XORI    $6 1
ifbot_3:          BNE    $8 $0 iftop_3
```

If this holds, we could, when approaching the part where the special if-statement occurs, take the first line and let it be the condition, find the XOR which is not encapsulated within a label, exchange the XOR with XORI and exchange the second register value with a 1.

3.2 Second part - methods for reduced redundancy

In this section we upgrade PendVM [9] the virtual machine on which we can run PAL programs. We further introduce some new algorithms to reduce the target code of a compiled ROOPL++ program.

Main algorithm of the section is `remove_redundancy` which we'll later apply to sample programs for testing.

3.2.1 PendVM - OUT

PendVM does not support methods to save the results of an executed program, which is why i have expanded one of the instructions: `OUT`.

`OUT` is now able to write or append a register value to the text-file `static_storage.txt`. For now ROOPL has not been expanded which means, that using the `OUT` functionality requires three steps:

The immediate value in `ADDI` just after `START` has to be incremented by the value of need `OUT` instructions. (update stack pointer)

The immediate value in `ADDI` just before `FINISH` has to be incremented by the value of need `OUT` instructions. (update stack pointer)

`OUT` instruction has to be manually inserted into the resulting `.pal` file of a compiled ROOPL++ program.

The expansion of PendVM exists of the following files:

pendvm.h

```
int i_out(WORD r, WORD u1, WORD u2);
```

pal_parse.c

```
("OUT", {REG, REG, NIL}, i_out)
```

machine.c

```
int
i_out(WORD r, WORD u1, WORD u2)
{
    char buf[...];
    sprintf(buf, '%d', m->reg[r1]);
    const char *p = buf;

    FILE *file;
    file = fopen('static_storage.txt', m->reg[r2]);
    fputs(p, file);
    fclose(file);
    return 0;
}
```

3.2.2 PendVM - EXCHI

Now what we have seen is that the exchange of memory and register values is a 5 line procedure, occurring multiple times within the target code of a ROOPL++ program. Which is why i want to introduce a new instruction called EXCHI, it takes the 3 arguments, two registers and an immediate. First register will get its value swapped with the value in the memory of position of the second register + immediate. The expansion of PendVM exists of the following files:

pendvm.h

```
int i_exchi(WORD WORD WORD);
```

pal_parse.c

```
("EXCHI", {REG, REG, IMM}, i_exchi)
```

machine.c

```
int
i_exchi(WORD rd, WORD ra, WORD u1)
{
    WORD tmp;
    /* ra is the stack pointer
     * u1 is the offset */
    MEMORY *loc = mem_get(m->reg[ra]+u1);

    if (loc->type == MEM_INST) {
        pendvm_error("....");
        return -4; /* "exchange with instruction" error */
    }

    tmp=m->reg[rd];
    m->reg[rd]=loc->value;
    loc->value=tmp;
    return 0;
}
```

3.2.3 Algorithm - Memory exchange

Find the pattern:	
ADD	\$r1 \$r2
ADDI	\$r1 imm
EXCH	\$r3 \$r1
ADDI	\$r1 -imm
SUB	\$r1 \$r2
Replace it with:	
EXCHI	\$r3 \$r2 imm

3.2.4 Algorithm - Special if-statements

Find the pattern:	
cmp_top_x	inst_x
cmp_bot_x	inst_x
<... >	
XOR	\$r1 \$r2
<... >	
cmp_bot_x_i	inst_x_i
cmp_top_x_i	inst_x_i
Replace it with:	
if_top_x:	inst_x
XORI	\$r1 1
if_bot_x:	inst x

3.2.5 Algorithm - Remove redundancy

For the task of a successful analysis we need an algorithm in which we can find redundancy, merge and remove instruction and at last update the stack point with the new immediate value. This algorithm can be applied to an existing PAL program, which means, that it is first useful, when a ROOPL++ program has been compiled to target code. Thus the algorithm must take a .PAL file and produce a .PAL file.

This algorithm will open a .pal file copy its content and run the algorithms memory_exchange and special if-statements. The end result is stored in the file: reduced.pal.


```

int main(int arg, char *args[])
{
    filehandler.input_file=fopen(args[1], "r");
    if(!filehandler.input_file) {
        printf("%s: Unable to open input file %s.\n", "", args[1]);
        exit(1);
    }
    fclose(filehandler.input_file);

    /* memory exchange */
    apply(1, args[1]);
    /* special if-statements */
    apply(2, "reduced.pal");

    return 0;
}

int apply(int method, const char *file) {
    int action;
    initialize(file);

    if(method == 1) {
        /* loop to load instruction memory */
        while(getinst()) {
            /* check for memory exchange pattern */
            action = memory_exchange();

            if(action == 0)
                fputs(buffer.line, filehandler.output_file);
        }
    } else {
        while(getinst()) {
            /* check for special if-statements */
            action = special_if_statements();

            if(action == 0)
                fputs(buffer.line, filehandler.output_file);
        }
    }
    fclose(filehandler.input_file);
    fclose(filehandler.output_file);
}

```

The program `remove_redundancy` is implemented in C and compiles with the GCC 8.2.1 20181127.

`GCC remove_redundancy.c`

After compilation it's runnable on `.pal` files.

`./a.out <filename>.pal`

The program creates two files. First the `tmp.pal` which is used to hold states within the program, the second is `reduced.pal`, which is the reduced program of `<filename>.pal`. The program is divided into two states, first is when we search for patterns of memory exchange, second is when we search for patterns of special if-statements.

The full sourcecode is available in the appendix 10.

4 Evaluation

In this section we evaluate results of the described algorithm `remove_redundancy` and discuss possible scenarios where the algorithm won't apply. The produced program `p'` of the algorithm is tested against the original program `p` created by the ROOPL++ compiler and a similar handwritten program. The focus is on the instruction count and PendVM steps. To prove that the programs produce similar results, the output `1..100` is stored in a `.txt` file.

Program	PendVM step	main lines	start lines	Description
<code>p</code>	6572	134	50	Original program produced by the ROOPL++ compiler
<code>p'</code>	2102	50	42	A reduced version of <code>p</code> , where the algorithm <code>remove_redundancy</code> has been applied
<code>p''</code>	1328	41	5	The example PAL program from the section of Pendulum Assembly Language: <code>ForITo100.pal</code>

On this simple program counting from `1..100`, we have reduced the needed steps in PendVM to one third of the original needed steps. Furthermore the number of lines have been reduced which should be reflected on the readability.

4.1 Scenarios which is not supported

The pattern below is seen in Martin Cservenka's program `BinaryTree.pal`. It's not supported by the algorithm `remove_redundancy`.

Find the pattern:	
<code>cmp_top_x</code>	<code>inst_x</code>
<code>cmp_bot_x</code>	<code>inst_x</code>
<...>	
EXCH	<code>\$rx \$ry</code>
<...>	
ANDX	<code>\$rz \$rw</code>
<...>	
XOR	<code>\$r1 \$r2</code>
<...>	
<code>cmp_bot_x_i</code>	<code>inst_x_i</code>
<code>cmp_top_x_i</code>	<code>inst_x_i</code>

We have also seen that `DATA` instruction as well as `jmp` macros which refer to a specific line has to be updated after the production of `p'`. This is also a step which is missing in `remove_redundancy`.

5 Conclusion

In this paper we searched for redundancy in the target code of a compiled ROOPL++ program. We have found patterns of redundancy regarding memory exchange and special if-statements. The paper shows an algorithm, which works on simple programs without DATA and jmp instructions. On those programs, the algorithm reduces the redundant patterns resulting in fewer lines of instruction as well as fewer computational steps within the virtual machine PendVM.

While the algorithm works great with smaller programs, running it on Cservenka's BinaryTree.pal or RTM.pal results in broken programs.

6 Further work

Getting closer to a complete algorithm, one should focus on updating line-numbers of DATA instructions and jmp labels, which has changed after patterns have been reduced.

Multiple places in the code, we'll see more than one ADDI instructions of the same register but with different immediate value. Those lines could be merged together.

Finally these reduction algorithms should be implemented within the ROOPL compiler, raising the chance, that future developments would result in updates of the algorithms.

7 Appendix A

ForITo100.pal

```
1  ;; increment a from [1..n]
2  subtop:  BRA subbot
3  main:    SWAPBR $2          ; entry/exit point
4           NEG $2             ; negate offset to return caller
5           EXCH $2 $1         ; push return offset to stack
6           ADDI $30 100       ; a += n
7           BRA swap           ; set limit ($28) += a, set a = 0
8  looptop: BNE $30 $0 loopbot ; from a = 0 do
9           ADDI $30 1         ; a += 1
10 loopbot: BNE $30 $28 looptop; until a = limit loop body
11           SUB $28 $30       ; set limit = 0
12           ADDI $30 -100     ; a -= n
13           EXCH $2 $1        ; pop return address
14 subbot:   BRA subtop
15 ;; swap(int a, int b)
16 subtop_3: BRA subbot_3
17 swap:     SWAPBR $2
18           NEG $2
19           EXCH $2 $1
20           ADD $28 $30
21           SUB $30 $28
22           EXCH $2 $1
23 subbot_3:  BRA subtop_3
```

8 Appendix B

prg.pal

```
1  ;; pendulum pal file
2  top:      BRA      start
3  l_r_nodeCount: DATA 0
4  l_r_limit: DATA 0
5  l_Program_vt: DATA 214
6  l_malloc_top: BRA    l_malloc_bot
7  l_malloc: SWAPBR $2
8           NEG      $2
9           ADDI     $9 2
10          XOR      $8 $0
11          ADDI     $1 1
12          EXCH     $6 $1
```

13		ADDI	\$1 1
14		EXCH	\$7 \$1
15		EXCH	\$2 \$1
16		ADDI	\$1 -1
17		BRA	l_malloc1
18		ADDI	\$1 1
19		EXCH	\$2 \$1
20		EXCH	\$7 \$1
21		ADDI	\$1 -1
22		EXCH	\$6 \$1
23		ADDI	\$1 -1
24		XOR	\$8 \$0
25		ADDI	\$9 -2
26	l_malloc_bot:	BRA	l_malloc_top
27	l_malloc1_top:	BRA	l_malloc1_bot
28		ADDI	\$1 1
29		EXCH	\$2 \$1
30		SUB	\$17 \$8
31		XOR	\$17 \$4
32	l_malloc1:	SWAPBR	\$2
33		NEG	\$2
34		EXCH	\$2 \$1
35		ADDI	\$1 -1
36		XOR	\$17 \$4
37		ADD	\$17 \$8
38		EXCH	\$19 \$17
39		XOR	\$18 \$19
40		EXCH	\$19 \$17
41		XOR	\$13 \$9
42		SUB	\$13 \$7
43	cmp_top_1:	BGEZ	\$13 cmp_bot_2
44		XORI	\$14 1
45	cmp_bot_2:	BGEZ	\$13 cmp_top_1
46		XOR	\$10 \$14
47	cmp_bot_2_i:	BGEZ	\$13 cmp_top_1_i
48		XORI	\$14 1
49	cmp_top_1_i:	BGEZ	\$13 cmp_bot_2_i
50		ADD	\$13 \$7
51		XOR	\$13 \$9
52	l_o_test:	BEQ	\$10 \$0 l_o_test_false
53		XORI	\$10 1
54		ADDI	\$8 1
55		EXCH	\$19 \$17
56		XOR	\$18 \$19
57		EXCH	\$19 \$17

58	RL	\$9 1
59	EXCH	\$10 \$1
60	ADDI	\$1 -1
61	EXCH	\$11 \$1
62	ADDI	\$1 -1
63	EXCH	\$12 \$1
64	ADDI	\$1 -1
65	EXCH	\$14 \$1
66	ADDI	\$1 -1
67	EXCH	\$16 \$1
68	ADDI	\$1 -1
69	EXCH	\$17 \$1
70	ADDI	\$1 -1
71	EXCH	\$18 \$1
72	ADDI	\$1 -1
73	EXCH	\$20 \$1
74	ADDI	\$1 -1
75	EXCH	\$21 \$1
76	ADDI	\$1 -1
77	EXCH	\$22 \$1
78	ADDI	\$1 -1
79	EXCH	\$23 \$1
80	ADDI	\$1 -1
81	BRA	l_malloc1
82	ADDI	\$1 1
83	EXCH	\$23 \$1
84	ADDI	\$1 1
85	EXCH	\$22 \$1
86	ADDI	\$1 1
87	EXCH	\$21 \$1
88	ADDI	\$1 1
89	EXCH	\$20 \$1
90	ADDI	\$1 1
91	EXCH	\$18 \$1
92	ADDI	\$1 1
93	EXCH	\$17 \$1
94	ADDI	\$1 1
95	EXCH	\$16 \$1
96	ADDI	\$1 1
97	EXCH	\$14 \$1
98	ADDI	\$1 1
99	EXCH	\$12 \$1
100	ADDI	\$1 1
101	EXCH	\$11 \$1
102	ADDI	\$1 1

103		EXCH	\$10 \$1
104		RR	\$9 1
105		ADDI	\$8 -1
106		XORI	\$10 1
107	l_o_assert_true:	BRA	l_o_assert
108	l_o_test_false:	BRA	l_o_test
109	cmp_top_5:	BEQ	\$18 \$0 cmp_bot_6
110		XORI	\$20 1
111	cmp_bot_6:	BEQ	\$18 \$0 cmp_top_5
112		XOR	\$11 \$20
113	cmp_bot_6_i:	BEQ	\$18 \$0 cmp_top_5_i
114		XORI	\$20 1
115	cmp_top_5_i:	BEQ	\$18 \$0 cmp_bot_6_i
116	l_i_test:	BEQ	\$11 \$0 l_i_test_false
117		XORI	\$11 1
118		ADD	\$6 \$18
119		SUB	\$18 \$6
120		EXCH	\$12 \$6
121		EXCH	\$12 \$17
122		XOR	\$12 \$6
123		XORI	\$11 1
124	l_i_assert_true:	BRA	l_i_assert
125	l_i_test_false:	BRA	l_i_test
126		ADDI	\$8 1
127		RL	\$9 1
128		EXCH	\$10 \$1
129		ADDI	\$1 -1
130		EXCH	\$11 \$1
131		ADDI	\$1 -1
132		EXCH	\$12 \$1
133		ADDI	\$1 -1
134		EXCH	\$14 \$1
135		ADDI	\$1 -1
136		EXCH	\$16 \$1
137		ADDI	\$1 -1
138		EXCH	\$17 \$1
139		ADDI	\$1 -1
140		EXCH	\$18 \$1
141		ADDI	\$1 -1
142		EXCH	\$20 \$1
143		ADDI	\$1 -1
144		EXCH	\$21 \$1
145		ADDI	\$1 -1
146		EXCH	\$22 \$1
147		ADDI	\$1 -1

148		EXCH	\$23 \$1
149		ADDI	\$1 -1
150		BRA	l_malloc1
151		ADDI	\$1 1
152		EXCH	\$23 \$1
153		ADDI	\$1 1
154		EXCH	\$22 \$1
155		ADDI	\$1 1
156		EXCH	\$21 \$1
157		ADDI	\$1 1
158		EXCH	\$20 \$1
159		ADDI	\$1 1
160		EXCH	\$18 \$1
161		ADDI	\$1 1
162		EXCH	\$17 \$1
163		ADDI	\$1 1
164		EXCH	\$16 \$1
165		ADDI	\$1 1
166		EXCH	\$14 \$1
167		ADDI	\$1 1
168		EXCH	\$12 \$1
169		ADDI	\$1 1
170		EXCH	\$11 \$1
171		ADDI	\$1 1
172		EXCH	\$10 \$1
173		RR	\$9 1
174		ADDI	\$8 -1
175		XOR	\$12 \$6
176		EXCH	\$12 \$17
177		ADD	\$6 \$9
178	l_i_assert:	BNE	\$11 \$0 l_i_assert_true
179		EXCH	\$12 \$17
180		SUB	\$6 \$9
181	cmp_top_7:	BEQ	\$6 \$12 cmp_bot_8
182		XORI	\$21 1
183	cmp_bot_8:	BEQ	\$6 \$12 cmp_top_7
184	cmp_top_9:	BNE	\$12 \$0 cmp_bot_10
185		XORI	\$22 1
186	cmp_bot_10:	BNE	\$12 \$0 cmp_top_9
187		ORX	\$23 \$21 \$22
188		XOR	\$11 \$23
189		ORX	\$23 \$21 \$22
190	cmp_bot_10_i:	BNE	\$12 \$0 cmp_top_9_i
191		XORI	\$22 1
192	cmp_top_9_i:	BNE	\$12 \$0 cmp_bot_10_i

193	cmp_bot_8_i:	BEQ	\$6 \$12 cmp_top_7_i
194		XORI	\$21 1
195	cmp_top_7_i:	BEQ	\$6 \$12 cmp_bot_8_i
196		ADD	\$6 \$9
197		EXCH	\$12 \$17
198	l_o_assert:	BNE	\$10 \$0 l_o_assert_true
199		XOR	\$15 \$9
200		SUB	\$15 \$7
201	cmp_top_3:	BGEZ	\$15 cmp_bot_4
202		XORI	\$16 1
203	cmp_bot_4:	BGEZ	\$15 cmp_top_3
204		XOR	\$10 \$16
205	cmp_bot_4_i:	BGEZ	\$15 cmp_top_3_i
206		XORI	\$16 1
207	cmp_top_3_i:	BGEZ	\$15 cmp_bot_4_i
208		ADD	\$15 \$7
209		XOR	\$15 \$9
210	l_malloc1_bot:	BRA	l_malloc1_top
211	l_main_0_top:	BRA	l_main_0_bot
212		ADDI	\$1 1
213		EXCH	\$2 \$1
214		EXCH	\$3 \$1
215		ADDI	\$1 -1
216	l_main_0:	SWAPBR	\$2
217		NEG	\$2
218		ADDI	\$1 1
219		EXCH	\$3 \$1
220		EXCH	\$2 \$1
221		ADDI	\$1 -1
222		ADD	\$6 \$3
223		ADDI	\$6 3
224		EXCH	\$7 \$6
225		ADDI	\$6 -3
226		SUB	\$6 \$3
227		XORI	\$8 100
228		ADD	\$7 \$8
229		XORI	\$8 100
230		ADD	\$6 \$3
231		ADDI	\$6 3
232		EXCH	\$7 \$6
233		ADDI	\$6 -3
234		SUB	\$6 \$3
235		XORI	\$6 1
236	entry_11:	BEQ	\$6 \$0 assert_13
237		ADD	\$7 \$3

238		ADDI	\$7	2
239		EXCH	\$8	\$7
240		ADDI	\$7	-2
241		SUB	\$7	\$3
242	cmp_top_15:	BNE	\$8	\$0 cmp_bot_16
243		XORI	\$9	1
244	cmp_bot_16:	BNE	\$8	\$0 cmp_top_15
245	f_top_17:	BEQ	\$9	\$0 f_bot_18
246		XORI	\$10	1
247	f_bot_18:	BEQ	\$9	\$0 f_top_17
248		XOR	\$6	\$10
249	f_bot_18_i:	BEQ	\$9	\$0 f_top_17_i
250		XORI	\$10	1
251	f_top_17_i:	BEQ	\$9	\$0 f_bot_18_i
252	cmp_bot_16_i:	BNE	\$8	\$0 cmp_top_15_i
253		XORI	\$9	1
254	cmp_top_15_i:	BNE	\$8	\$0 cmp_bot_16_i
255		ADD	\$7	\$3
256		ADDI	\$7	2
257		EXCH	\$8	\$7
258		ADDI	\$7	-2
259		SUB	\$7	\$3
260		ADD	\$7	\$3
261		ADDI	\$7	2
262		EXCH	\$8	\$7
263		ADDI	\$7	-2
264		SUB	\$7	\$3
265		ADD	\$9	\$3
266		ADDI	\$9	3
267		EXCH	\$10	\$9
268		ADDI	\$9	-3
269		SUB	\$9	\$3
270	cmp_top_19:	BNE	\$8	\$10 cmp_bot_20
271		XORI	\$11	1
272	cmp_bot_20:	BNE	\$8	\$10 cmp_top_19
273	f_top_21:	BEQ	\$11	\$0 f_bot_22
274		XORI	\$12	1
275	f_bot_22:	BEQ	\$11	\$0 f_top_21
276		XOR	\$6	\$12
277	f_bot_22_i:	BEQ	\$11	\$0 f_top_21_i
278		XORI	\$12	1
279	f_top_21_i:	BEQ	\$11	\$0 f_bot_22_i
280	cmp_bot_20_i:	BNE	\$8	\$10 cmp_top_19_i
281		XORI	\$11	1
282	cmp_top_19_i:	BNE	\$8	\$10 cmp_bot_20_i

283		ADD	\$9 \$3	
284		ADDI	\$9 3	
285		EXCH	\$10 \$9	
286		ADDI	\$9 -3	
287		SUB	\$9 \$3	
288		ADD	\$7 \$3	
289		ADDI	\$7 2	
290		EXCH	\$8 \$7	
291		ADDI	\$7 -2	
292		SUB	\$7 \$3	
293	test_12:	BNE	\$6 \$0	exit_14
294		ADD	\$7 \$3	
295		ADDI	\$7 2	
296		EXCH	\$8 \$7	
297		ADDI	\$7 -2	
298		SUB	\$7 \$3	
299		XORI	\$9 1	
300		ADD	\$8 \$9	
301		XORI	\$9 1	
302		ADD	\$7 \$3	
303		ADDI	\$7 2	
304		EXCH	\$8 \$7	
305		ADDI	\$7 -2	
306		SUB	\$7 \$3	
307	assert_13:	BRA	entry_11	
308	exit_14:	BRA	test_12	
309		XORI	\$6 1	
310		ADD	\$6 \$3	
311		ADDI	\$6 2	
312		EXCH	\$7 \$6	
313		ADDI	\$6 -2	
314		SUB	\$6 \$3	
315		ADD	\$8 \$3	
316		ADDI	\$8 3	
317		EXCH	\$9 \$8	
318		ADDI	\$8 -3	
319		SUB	\$8 \$3	
320		SUB	\$7 \$9	
321		ADD	\$8 \$3	
322		ADDI	\$8 3	
323		EXCH	\$9 \$8	
324		ADDI	\$8 -3	
325		SUB	\$8 \$3	
326		ADD	\$6 \$3	
327		ADDI	\$6 2	

328		EXCH	\$7	\$6
329		ADDI	\$6	-2
330		SUB	\$6	\$3
331		ADD	\$6	\$3
332		ADDI	\$6	3
333		EXCH	\$7	\$6
334		ADDI	\$6	-3
335		SUB	\$6	\$3
336		XORI	\$8	100
337		SUB	\$7	\$8
338		XORI	\$8	100
339		ADD	\$6	\$3
340		ADDI	\$6	3
341		EXCH	\$7	\$6
342		ADDI	\$6	-3
343		SUB	\$6	\$3
344	l_main_0_bot:	BRA	l_main_0_top	
345	start:	BRA	top	
346		START		
347		ADDI	\$4	393
348		XOR	\$5	\$4
349		ADDI	\$5	10
350		XOR	\$7	\$5
351		ADDI	\$4	10
352		ADDI	\$4	-1
353		EXCH	\$7	\$4
354		ADDI	\$4	1
355		ADDI	\$4	-10
356		XOR	\$1	\$5
357		ADDI	\$1	2048
358		ADDI	\$1	-4
359		XOR	\$3	\$1
360		XORI	\$6	3
361		EXCH	\$6	\$3
362		ADDI	\$1	-1
363		EXCH	\$3	\$1
364		ADDI	\$1	-1
365		BRA	l_main_0	
366		ADDI	\$1	1
367		EXCH	\$3	\$1
368		ADDI	\$3	1
369		ADDI	\$3	1
370		EXCH	\$6	\$3
371		XORI	\$7	1
372		EXCH	\$6	\$7

373	XORI	\$7	1
374	ADDI	\$3	−1
375	ADDI	\$3	−1
376	ADDI	\$3	1
377	ADDI	\$3	2
378	EXCH	\$6	\$3
379	XORI	\$7	2
380	EXCH	\$6	\$7
381	XORI	\$7	2
382	ADDI	\$3	−2
383	ADDI	\$3	−1
384	ADDI	\$1	1
385	EXCH	\$6	\$3
386	XORI	\$6	3
387	XOR	\$3	\$1
388	ADDI	\$1	4
389	ADDI	\$1	−2048
390	XOR	\$1	\$5
391	ADDI	\$5	−10
392	XOR	\$5	\$4
393	ADDI	\$4	−393
394	finish :	FINISH	

9 Appendix C

prgReduced.pal

```
1 ;; pendulum pal file
2 top:          BRA    start
3 l_r_nodeCount: DATA  0
4 l_r_limit:    DATA  0
5 l_Program_vt: DATA 214
6 l_malloc_top: BRA    l_malloc_bot
7 l_malloc:     SWAPBR $2
8              NEG     $2
9              ADDI    $9 2
10             XOR     $8 $0
11             ADDI    $1 1
12             EXCH    $6 $1
13             ADDI    $1 1
14             EXCH    $7 $1
15             EXCH    $2 $1
16             ADDI    $1 -1
17             BRA     l_malloc1
18             ADDI    $1 1
19             EXCH    $2 $1
20             EXCH    $7 $1
21             ADDI    $1 -1
22             EXCH    $6 $1
23             ADDI    $1 -1
24             XOR     $8 $0
25             ADDI    $9 -2
26 l_malloc_bot: BRA     l_malloc_top
27 l_malloc1_top: BRA     l_malloc1_bot
28             ADDI    $1 1
29             EXCH    $2 $1
30             SUB     $17 $8
31             XOR     $17 $4
32 l_malloc1:    SWAPBR $2
33             NEG     $2
34             EXCH    $2 $1
35             ADDI    $1 -1
36             XOR     $17 $4
37             ADD     $17 $8
38             EXCH    $19 $17
39             XOR     $18 $19
40             EXCH    $19 $17
41             XOR     $13 $9
```

42		SUB	\$13 \$7
43	cmp_top_1:	BGEZ	\$13 cmp_bot_2
44		XORI	\$14 1
45	cmp_bot_2:	BGEZ	\$13 cmp_top_1
46		XOR	\$10 \$14
47	cmp_bot_2_i:	BGEZ	\$13 cmp_top_1_i
48		XORI	\$14 1
49	cmp_top_1_i:	BGEZ	\$13 cmp_bot_2_i
50		ADD	\$13 \$7
51		XOR	\$13 \$9
52	l_o_test:	BEQ	\$10 \$0 l_o_test_false
53		XORI	\$10 1
54		ADDI	\$8 1
55		EXCH	\$19 \$17
56		XOR	\$18 \$19
57		EXCH	\$19 \$17
58		RL	\$9 1
59		EXCH	\$10 \$1
60		ADDI	\$1 -1
61		EXCH	\$11 \$1
62		ADDI	\$1 -1
63		EXCH	\$12 \$1
64		ADDI	\$1 -1
65		EXCH	\$14 \$1
66		ADDI	\$1 -1
67		EXCH	\$16 \$1
68		ADDI	\$1 -1
69		EXCH	\$17 \$1
70		ADDI	\$1 -1
71		EXCH	\$18 \$1
72		ADDI	\$1 -1
73		EXCH	\$20 \$1
74		ADDI	\$1 -1
75		EXCH	\$21 \$1
76		ADDI	\$1 -1
77		EXCH	\$22 \$1
78		ADDI	\$1 -1
79		EXCH	\$23 \$1
80		ADDI	\$1 -1
81		BRA	l_malloc1
82		ADDI	\$1 1
83		EXCH	\$23 \$1
84		ADDI	\$1 1
85		EXCH	\$22 \$1
86		ADDI	\$1 1

87		EXCH	\$21 \$1
88		ADDI	\$1 1
89		EXCH	\$20 \$1
90		ADDI	\$1 1
91		EXCH	\$18 \$1
92		ADDI	\$1 1
93		EXCH	\$17 \$1
94		ADDI	\$1 1
95		EXCH	\$16 \$1
96		ADDI	\$1 1
97		EXCH	\$14 \$1
98		ADDI	\$1 1
99		EXCH	\$12 \$1
100		ADDI	\$1 1
101		EXCH	\$11 \$1
102		ADDI	\$1 1
103		EXCH	\$10 \$1
104		RR	\$9 1
105		ADDI	\$8 -1
106		XORI	\$10 1
107	l_o_assert_true:	BRA	l_o_assert
108	l_o_test_false:	BRA	l_o_test
109	cmp_top_5:	BEQ	\$18 \$0 cmp_bot_6
110		XORI	\$20 1
111	cmp_bot_6:	BEQ	\$18 \$0 cmp_top_5
112		XOR	\$11 \$20
113	cmp_bot_6_i:	BEQ	\$18 \$0 cmp_top_5_i
114		XORI	\$20 1
115	cmp_top_5_i:	BEQ	\$18 \$0 cmp_bot_6_i
116	l_i_test:	BEQ	\$11 \$0 l_i_test_false
117		XORI	\$11 1
118		ADD	\$6 \$18
119		SUB	\$18 \$6
120		EXCH	\$12 \$6
121		EXCH	\$12 \$17
122		XOR	\$12 \$6
123		XORI	\$11 1
124	l_i_assert_true:	BRA	l_i_assert
125	l_i_test_false:	BRA	l_i_test
126		ADDI	\$8 1
127		RL	\$9 1
128		EXCH	\$10 \$1
129		ADDI	\$1 -1
130		EXCH	\$11 \$1
131		ADDI	\$1 -1

132	EXCH	\$12 \$1
133	ADDI	\$1 -1
134	EXCH	\$14 \$1
135	ADDI	\$1 -1
136	EXCH	\$16 \$1
137	ADDI	\$1 -1
138	EXCH	\$17 \$1
139	ADDI	\$1 -1
140	EXCH	\$18 \$1
141	ADDI	\$1 -1
142	EXCH	\$20 \$1
143	ADDI	\$1 -1
144	EXCH	\$21 \$1
145	ADDI	\$1 -1
146	EXCH	\$22 \$1
147	ADDI	\$1 -1
148	EXCH	\$23 \$1
149	ADDI	\$1 -1
150	BRA	l_malloc1
151	ADDI	\$1 1
152	EXCH	\$23 \$1
153	ADDI	\$1 1
154	EXCH	\$22 \$1
155	ADDI	\$1 1
156	EXCH	\$21 \$1
157	ADDI	\$1 1
158	EXCH	\$20 \$1
159	ADDI	\$1 1
160	EXCH	\$18 \$1
161	ADDI	\$1 1
162	EXCH	\$17 \$1
163	ADDI	\$1 1
164	EXCH	\$16 \$1
165	ADDI	\$1 1
166	EXCH	\$14 \$1
167	ADDI	\$1 1
168	EXCH	\$12 \$1
169	ADDI	\$1 1
170	EXCH	\$11 \$1
171	ADDI	\$1 1
172	EXCH	\$10 \$1
173	RR	\$9 1
174	ADDI	\$8 -1
175	XOR	\$12 \$6
176	EXCH	\$12 \$17

177		ADD	\$6 \$9
178	l_i_assert:	BNE	\$11 \$0 l_i_assert_true
179		EXCH	\$12 \$17
180		SUB	\$6 \$9
181	cmp_top_7:	BEQ	\$6 \$12 cmp_bot_8
182		XORI	\$21 1
183	cmp_bot_8:	BEQ	\$6 \$12 cmp_top_7
184	cmp_top_9:	BNE	\$12 \$0 cmp_bot_10
185		XORI	\$22 1
186	cmp_bot_10:	BNE	\$12 \$0 cmp_top_9
187		ORX	\$23 \$21 \$22
188		XOR	\$11 \$23
189		ORX	\$23 \$21 \$22
190	cmp_bot_10_i:	BNE	\$12 \$0 cmp_top_9_i
191		XORI	\$22 1
192	cmp_top_9_i:	BNE	\$12 \$0 cmp_bot_10_i
193	cmp_bot_8_i:	BEQ	\$6 \$12 cmp_top_7_i
194		XORI	\$21 1
195	cmp_top_7_i:	BEQ	\$6 \$12 cmp_bot_8_i
196		ADD	\$6 \$9
197		EXCH	\$12 \$17
198	l_o_assert:	BNE	\$10 \$0 l_o_assert_true
199		XOR	\$15 \$9
200		SUB	\$15 \$7
201	cmp_top_3:	BGEZ	\$15 cmp_bot_4
202		XORI	\$16 1
203	cmp_bot_4:	BGEZ	\$15 cmp_top_3
204		XOR	\$10 \$16
205	cmp_bot_4_i:	BGEZ	\$15 cmp_top_3_i
206		XORI	\$16 1
207	cmp_top_3_i:	BGEZ	\$15 cmp_bot_4_i
208		ADD	\$15 \$7
209		XOR	\$15 \$9
210	l_malloc1_bot:	BRA	l_malloc1_top
211	l_main_0_top:	BRA	l_main_0_bot
212		ADDI	\$1 1
213		EXCH	\$2 \$1
214		EXCH	\$3 \$1
215		ADDI	\$1 -1
216	l_main_0:	SWAPBR	\$2
217		NEG	\$2
218		ADDI	\$1 1
219		EXCH	\$3 \$1
220		EXCH	\$2 \$1
221		ADDI	\$1 -1

222		EXCHI	\$7	\$3	3
223		XORI	\$8	100	
224		ADD	\$7	\$8	
225		XORI	\$8	100	
226		EXCHI	\$7	\$3	3
227		XORI	\$6	1	
228	entry_11:	BEQ	\$6	\$0	assert_13
229		EXCHI	\$8	\$3	2
230		OUT	\$8	\$31	
231	iftop_3:	BNE	\$8	\$0	ifbot_3
232		XORI	\$6	1	
233	ifbot_3:	BNE	\$8	\$0	iftop_3
234		EXCHI	\$8	\$3	2
235		EXCHI	\$8	\$3	2
236		EXCHI	\$10	\$3	3
237	iftop_2:	BNE	\$8	\$10	ifbot_2
238		XORI	\$6	1	
239	ifbot_2:	BNE	\$8	\$10	iftop_2
240		EXCHI	\$10	\$3	3
241		EXCHI	\$8	\$3	2
242	test_12:	BNE	\$6	\$0	exit_14
243		EXCHI	\$8	\$3	2
244		XORI	\$9	1	
245		ADD	\$8	\$9	
246		XORI	\$9	1	
247		EXCHI	\$8	\$3	2
248	assert_13:	BRA		entry_11	
249	exit_14:	BRA		test_12	
250		XORI	\$6	1	
251		EXCHI	\$7	\$3	3
252		EXCHI	\$9	\$3	3
253		SUB	\$7	\$9	
254		EXCHI	\$9	\$3	3
255		EXCHI	\$7	\$3	3
256		EXCHI	\$7	\$3	3
257		XORI	\$8	100	
258		SUB	\$7	\$8	
259		XORI	\$8	100	
260		EXCHI	\$7	\$3	3
261	l_main_0_bot:	BRA		l_main_0_top	
262	start:	BRA		top	
263		START			
264		ADDI	\$4	314	
265		XOR	\$5	\$4	
266		ADDI	\$5	10	

267	XOR	\$7	\$5
268	ADDI	\$4	10
269	ADDI	\$4	-1
270	EXCH	\$7	\$4
271	ADDI	\$4	1
272	ADDI	\$4	-10
273	XOR	\$1	\$5
274	ADDI	\$1	2048
275	ADDI	\$1	-4
276	XOR	\$3	\$1
277	XORI	\$6	3
278	EXCH	\$6	\$3
279	ADDI	\$1	-1
280	EXCH	\$3	\$1
281	ADDI	\$1	-1
282	ADDI	\$31	1
283	ADDI	\$30	-1
284	BRA	l_main_0	
285	ADDI	\$31	-1
286	ADDI	\$30	1
287	ADDI	\$1	1
288	EXCH	\$3	\$1
289	ADDI	\$3	1
290	ADDI	\$3	1
291	EXCH	\$6	\$3
292	XORI	\$7	1
293	EXCH	\$6	\$7
294	XORI	\$7	1
295	ADDI	\$3	-1
296	ADDI	\$3	-1
297	ADDI	\$3	1
298	ADDI	\$3	2
299	EXCH	\$6	\$3
300	XORI	\$7	2
301	EXCH	\$6	\$7
302	XORI	\$7	2
303	ADDI	\$3	-2
304	ADDI	\$3	-1
305	ADDI	\$1	1
306	EXCH	\$6	\$3
307	XORI	\$6	3
308	XOR	\$3	\$1
309	ADDI	\$1	4
310	ADDI	\$1	-2048
311	XOR	\$1	\$5

312		ADDI	\$5	−10
313		XOR	\$5	\$4
314		ADDI	\$4	−314
315	finish :	FINISH		

10 Appendix D

remove_redundancy.c

```
1 #include <stdio.h>
2 #include <stdlib.h>
3 #include <string.h>
4
5 /** ***** */
6 /** STRUCTS ***** */
7 /** ***** */
8 /* File & flow handling */
9 struct Controlflow {
10     int patternm;
11     int pattern;
12 } controller;
13
14 struct Buffer {
15     /* The current instruction line */
16     char line[256];
17     char param_set[5][32];
18
19     /* Some list to split
20      * an instruction line
21      * into single paramters */
22     char param_sets[5][5][32];
23
24     /* Previous instruction lines */
25     char previous_lines[5][256];
26 } buffer;
27
28 struct Filehandler {
29     FILE *input_file;
30     FILE *output_file;
31 } filehandler;
32 /** ***** */
33 /** ***** */
34
35 /** ***** */
36 /* functions */
37 /** ***** */
38 int apply();
39 int memory_exchange();
40 int special_if_statements();
41
```

```

42  /** ***** */
43  /* File & flow handling */
44  /** ***** */
45  int initialize(const char *file);
46  int getinst();
47  char* getparam(int idx);
48  int saveline(int idx);
49  int setPreviousLines();
50
51  /** ***** */
52  /** main */
53  /** ***** */
54  int main(int arg, char *args[])
55  {
56      filehandler.input_file=fopen(args[1], "r");
57      if(!filehandler.input_file) {
58          printf("%s: Unable to open input file %s.\n", "", args[1]);
59          exit(1);
60      }
61      fclose(filehandler.input_file);
62
63      /* memory exchange */
64      apply(1, args[1]);
65      /* special if-statements */
66      apply(2, "reduced.pal");
67
68      return 0;
69  }
70
71  int apply(int method, const char *file) {
72      int action;
73      initialize(file);
74
75      if(method == 1) {
76          /* loop to load instruction memory */
77          while(getinst()) {
78              /* check for memory exchange pattern */
79              action = memory_exchange();
80
81              if(action == 0)
82                  fputs(buffer.line, filehandler.output_file);
83          }
84      } else {
85          while(getinst()) {
86              /* check for special if-statements */

```



```

87         action = special_if_statements();
88
89         if(action == 0)
90             fputs(buffer.line, filehandler.output_file);
91     }
92 }
93 fclose(filehandler.input_file);
94 fclose(filehandler.output_file);
95 }
96
97 int memory_exchange() {
98     int action = 0;
99
100     /* reset on an add */
101     if( !strcasecmp(getparam(0), "ADD") ) {
102         for(int i = 0; i < controller.pattern; i++)
103             fputs(buffer.previous_lines[i],
104                 filehandler.output_file);
105         controller.pattern = 0;
106     }
107
108     /* memory exchange start
109      * save lines */
110     if( !strcasecmp(getparam(0), "ADD")
111         || controller.pattern > 0) {
112         saveline(controller.pattern);
113         controller.pattern += 1;
114         action = 1;
115     }
116
117     /* memory exchange end */
118     if( !strcasecmp(getparam(0), "SUB")
119         && controller.pattern == 5) {
120         char buf[256];
121
122         /* Place previous lines in
123          * param_sets[0..4]
124          *
125          * EXCH within param_sets[2]
126          * ADDI within param_sets[1]
127          * SUB within param_sets[4]
128          */
129         setPreviousLines();
130
131         if( !strcasecmp(buffer.param_sets[2][0], "EXCH") ) {

```

```

132         strcpy( buffer.param_sets[2][4]
133             , " " );
134         sprintf( buf, "%s%s %s %s %s\n", buffer.param_sets[2][4]
135             , "EXCH"
136             , buffer.param_sets[2][1]
137             , buffer.param_sets[4][2]
138             , buffer.param_sets[1][2] );
139         printf( "%s", buf );
140
141         fputs( buf, filehandler.output_file );
142         controller.pattern = 0;
143         action = 1;
144     }
145 }
146
147 /* memory exchange final
148 * if no pattern was regconized
149 * print all five lines */
150 if( controller.pattern == 5 ) {
151     for( int i = 0; i < controller.pattern; i++ )
152         fputs( buffer.previous_lines[i],
153             filehandler.output_file );
154     controller.pattern = 0;
155     action = 1;
156 }
157
158 return action;
159 }
160
161 int special_if_statements() {
162     int action = 0;
163
164     if( strstr( getparam(0), "cmp" ) != NULL
165         && controller.patternm == 0 ) {
166         saveline(0); /* cmp */
167         printf( "%s%s\n", "cmp: ", buffer.previous_lines[0] );
168         controller.patternm = 1;
169     }
170
171     if( !strcasecmp( getparam(0), "XOR" )
172     && controller.patternm == 1 ) {
173         saveline(1); /* xor */
174         printf( "%s%s\n", "xor: ", buffer.previous_lines[1] );
175     }
176

```

```

177     if ( getparam(0)[strlen(getparam(0))-2]== 'i'
178         && strstr(getparam(0), "cmp") != NULL
179         && controller.patternm == 1) {
180         char buf[256];
181         char cls[32];
182         setPreviousLines();
183
184         strcpy(buffer.param_set[4], "_____");
185         strcpy(buffer.param_set[2], "_____");
186
187         char *pp1 = strdup(buffer.param_sets[0][0],
188                         strlen(buffer.param_sets[0][0]) - 1);
189         char *pp2 = strdup(getparam(0), strlen(getparam(0)) - 3);
190         char *pp3 = strdup(buffer.param_sets[0][4],
191                         strlen(buffer.param_sets[0][4]));
192         printf("%s_%s\n", "pp1:_", pp1);
193         printf("%s_%s\n", "pp2:_", pp2);
194
195         if ( !strcasecmp(pp1, pp2) ) {
196             /* if */
197             sprintf(buf, "%s%s%s_%%s_%s_%s\n",
198                     buffer.param_sets[0][0],
199                     getparam(2),
200                     buffer.param_sets[0][1],
201                     buffer.param_sets[0][2],
202                     buffer.param_sets[0][3],
203                     buffer.param_sets[0][4]);
204             fputs(buf, filehandler.output_file);
205
206             /* xori */
207             sprintf(buf, "%s%s_%%s_%s\n", getparam(4), "XORI",
208                     buffer.param_sets[1][1], "1");
209             fputs(buf, filehandler.output_file);
210
211             /* fi */
212             sprintf(buf, "%s:%s%s_%%s_%s_%s\n", pp3, getparam(2),
213                     buffer.param_sets[0][1],
214                     buffer.param_sets[0][2],
215                     buffer.param_sets[0][3],
216                     pp1);
217             fputs(buf, filehandler.output_file);
218
219             controller.patternm = 0;
220         }
221         action = 1;

```

```

222     }
223
224     return action+controller.patternm;
225 }
226
227 int initialize(const char *file) {
228     /* copy input file into
229      * tmp file */
230     filehandler.input_file=fopen( file , "r");
231     filehandler.output_file=fopen("tmp.pal", "w");
232     while(getinst()) {
233         fputs(buffer.line , filehandler.output_file);
234     }
235     fclose(filehandler.output_file);
236     fclose(filehandler.input_file);
237
238     filehandler.input_file = fopen("tmp.pal", "r");
239     filehandler.output_file = fopen("reduced.pal", "w");
240
241     /* make sure file is in valid pendulum format */
242     /* get first line */
243     fgets(buffer.line,256,filehandler.input_file);
244     if( strcmp(buffer.line , ";;_pendulum_pal_file", 20) ) {
245         /* compare with known header */
246         printf("Input_file_not_in_in_Pendulum_pal_format.\n");
247         exit(1);
248     }
249     /* Initialize new file */
250     sprintf(buffer.line , ";;_pendulum_pal_file\n");
251     fputs(buffer.line , filehandler.output_file);
252     return 0;
253 };
254
255 int getinst() {
256     int r = fgets(buffer.line,256,filehandler.input_file);
257
258     /* */
259     int fields=sscanf(buffer.line ,"%s%s%s%s%s" ,
260         buffer.param_set[0] ,
261         buffer.param_set[1] ,
262         buffer.param_set[2] ,
263         buffer.param_set[3] ,
264         buffer.param_set[4]);
265
266     if( fields==0 || fields==EOF ) return 0;

```

```

267
268     return r;
269 };
270
271 char* getparam(int idx) {
272     return buffer.param_set[idx];
273 }
274
275 int saveline(int idx) {
276     strcpy(buffer.previous_lines[idx], buffer.line);
277     return 0;
278 };
279
280 int setPreviousLines() {
281     for(int i = 0; i < 5; i++)
282     {
283         sscanf(buffer.previous_lines[i], "%s%s%s%s%s",
284             buffer.param_sets[i][0],
285             buffer.param_sets[i][1],
286             buffer.param_sets[i][2],
287             buffer.param_sets[i][3],
288             buffer.param_sets[i][4]);
289     }
290     return 0;
291 }

```

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