# Program Analysis and Transformation Final Assignment

Benjamin Brandt Ohrt, zpn492 June 2, 2019

#### Abstract

The Pendulum Instruction Set Architecture (PISA) was first introduced in 1995 by Carlin James Vieri and is a reversible assembly language. The assembly language has later been improved and several high-level languages has been build upon it. One of those languages is the extension to the reversible object-oriented programming language (ROOPL) ROOPL++ presented in 2018. One of the issues with ROOPL++ was the amount of produced target code. In this paper we compile source code for the data structure of a binary tree, analyse the possibility of redundant target code and points out where an optimization could be done.

# Contents

1	Introduction	3
	1.1 Assembly language	3
	1.1.1 Example program	3
	1.2 Reversible computing	4
	1.3 Pendulum microprocessor	5
	1.4 Motivation	6
	1.5 Outline	6
<b>2</b>	Programming languages	7
	2.1 Pendulum Assembly Language	7
	2.1.1 Example program	7
	2.2 Reversible Object-Oriented Programming	8
3	Analysis of redundancy	9
	3.1 First part - patterns	10
	3.1.1 Getting data from memory	10
	3.1.2 Special if-statements	11
	3.2 Second part - methods for reduced redundancy	12
	3.2.1 PendVM - OUT	12
	3.2.2 PendVM - EXCHI	13
	3.2.3 Algorithm - Memory exchange	14
	3.2.4 Algorithm - Special if-statements	14
	3.2.5 Algorithm - Remove redundancy	14
4	Results	16
5	Data structures	17
•	5.1 Binary tree	17
•		
6	Conclusion	17
7	Further work	<b>17</b>
	7.0.1 Instruction operands - [OVERVEJ]	17
	7.0.2 Pendulum operation	18
	7.1 Register values	19
	7.2 Pendulum	20
8	Appendix A	21
9	Appendix B	23
-	9.1 Full program	23
	9.1.1 Malloc	31

#### 1 Introduction

# 1.1 Assembly language

A CPU understands its own machine language. Instructions in machine language are numbers stored as bytes in memory. Each instruction has its own unique numeric code called its operation code or opcode for short. An example is the instruction that says add EAX and EBX registers together and store the result back into EAX is encoded by the following hex code:

```
03 C3
```

This not readable for the blunt eye. Which is why we have a program called an assembler. An assembler is a program that reads the text of a assembly language program and converts the assembly into machine code. [6, p.11].

The assembly language origins back to Birkbeck College 1946-1962, where the creation was credited to Kathleen Booth.[1] Kathleen Booth was a PhD whom both visited with John Von Neumann with the famous The Von Neumann Architecture[3], helped with the design of multiple machines and was one the founders of the Birkbeck department of computer science.

The assembly language is a symbolic programming language, closest to machine code. [2] An assembly language program is stored as plain text. The text consists of a set of instructions which is processed chronological. Each assembly instruction is equal to one machine instruction for example could above addition be shown as:

```
add EAX EBX
```

With the assembly language words as add can be used as mnemonic for the instruction add and so fourth. [6, p.11].

#### 1.1.1 Example program

#### ForITo100.asm

```
J main
                                     for int i = 0; i < 100; i++
 1
 2
                                        count \neq i * 2
3
   loop_i:
  MUL $t0, $a1, 2
   ADD $a0, $a0, $t0
                                     count += i * 2
   ADDI $a1, $a1, 1
6
                                     i++
   SLT $t0, $a1, $a2
                                     i < 100
   |BEQ $t0, 1, loop_i
   JR $ra
9
                                     return
10
11
   main:
   |\mathbf{ADDI} \$ a0, \$ zero, 0
12
                                     count = 0
   |ADDI $a1, $zero, 0
                                    i = 0
   ADDI $a2,
14
               $zero, 100
                                    max
15
   JAL loop_i
```

# 1.2 Reversible computing

A reversible computing system has, at any time, at most a single previous computation state as well as a single next computation state, and thus a reversible computing system. [7] It comes with the promise of reduced energy dissipation, when erasure of information is left out of the program.

The inspiration of reversible computing dates back to 1867 and the study of thermodynamics where James Clark Maxwell made a thought experiment also known as Maxwell's Demon. In the experiment he questions that of the second law of thermodynamics which says:

[..] It is impossible in a system enclosed in an envelope which permits neither change of volume nor passage of heat, and in which both the temperature and the pressure are everywhere the same, to produce any inequality of temperature or pressure without expenditure of work.[8, p.16]

The experiment was later published in 1872 in a book by Maxwell: Theory of Heat[11], but the connection between thermodynamics and computations was first seen in 1949 by John von Neumann, where he talks about a computation must have a minimum thermodynamic energy dissipation which he determines to[5, p.20][8, p.18]:

 $k_BTlnN$ ,  $k_B$  as the Boltzmann's constant, T as the temperature and N=2.

Rolf Landauer realize that modern computers with irreversible processes must dissipate that minimum energy as von Neumann described if the erasure of a bit occures thus resulting in atleast the increase of entropy by  $k_B ln 2.[5, p.20][8, p. 18]$  He also states that reversible operations does not produce the dissipation and irreversible operations can avoid the dissipation by storing information of the computational history. At last Landauer states that the stored history must be erased irreversibly which would just postpone the dissipation of entropy, That last statement is later proven wrong by Charles Bennett.[8, p.19]

In 1970 Charles Bennett looks at Landauers last statement and decides to make an experiment. He creates a reversible program consisting of two halves. The first which provided the calculations intended and the second which undid the calculations from the first halves thus ending the program in its starting point. In the experiment he uses a Turing Machine[10] and shows that the information produces by the intended calculation could be used to undo the calculation instead of just be thrown away. With that experiment Bennett had shown that a reversible process would not just postpone the dissipation of energy it would be able to remove it from the equation.[8, p.18]

From Bennetts experiment he came up with a description for an "enzymatic Turing machine" in which reversible logically operations could be executed[8, p.19]. To fullfill the promise of reduced energy dissipation their was final need of physically logic devices to perform the reversible operations on. Fredkin, Toffoli and Feynmann all aided this need by introducing reversibly logic-gates.[8, p. 19, 22]

# 1.3 Pendulum microprocessor

Pendulum is a reversible microprocessor, invented by Carlin James Vieri at MIT in 1995. The invention took offset in the existing MIPS R2000 architecture. [REF til ARK][4, p. 29] Vieri's motivation was to create a reversibly processor which would avoid destruction of information and reduce the energy dissipation shown in thermodynamics [1.2] and discussed by Charles Bennet. [8] For this he would focus on memory access, datapath operations on stored values and control flow operations.

The processor has three registers for used in the control flow:

- 1 The program counter (PC) for storing address of the current instruction
- 2 The branch register (BR) for storing jump offsets
- 3 The direction bit (DIR) for keeping track of the execution direction.

PC is incremented/decremented by the value stored in DIR, thus changing DIR between 1 & -1, will decide in which direction the instructions will be executed. When the DIR is -1, all instructions is inverted. [4, Vieri - Chapter 3, p. 21]

Control flow - Branch instructions like branch or jump is in normal architectures not reversible, that is because the come-from instruction is not stored anywhere, thus the goto instruction not knowing who called it. This could be handled by storing the PC just before the branch/jump in a special register. In later versions of the Pendulum ISA architecture paired branches is introduced, such that each goto instruction should have branch instruction to the come-from.

Control flow - If/then statements is in need of an exit condition known as assert.

```
if e1 then s1 else s2 fi e2
```

**Control flow - for-loop** is in need of an entry, loop and exit condition. Where the el should only be true upon entry and e2 only on exit.

```
from e1 do s1 loop s2 until e2
```

Control flow - subrutines in encased between a top and a bottom, which both contains a branch to eachother. It follows that the subrutine is skipped when executing instructions sequentially.

```
top: BRA bot

<...rutine definition goes here...>

bot: BRA top
```

**Memory access** is always an exchange. The exchange instruction swaps register value with the value in memory at an address specified by another register. [4, p. 32]

- 1.4 Motivation
- 1.5 Outline

# 2 Programming languages

# 2.1 Pendulum Assembly Language

Pendulum Instruction Set Architecture(PISA) Assembly Language or a shorthand PAL, is a reversible language. It assembles by the Pendulum microprocessor.[4, p. 48] In this paper we use the Pendulum virtual machine PendVM[9], which executes programs written in PAL. Pendulum instructions is almost identically to the conventional RISC(Reduced Instruction Set Computing) processor. Thus reversible it introduces some new features.

Branch register is normally zero, if the branch register is not zero, the PC increments by the value in the register. [REF - PENDULUM 248] When is happens it the instruction at the destination executes and the branch register is cleared. When implementing subroutines one must use SWAPBR which allows direct access to the branch register, and therefor an exchange the value. It must follow that the subrutine negates the value in the branch register, such that the next SWAPBR will branch back to the location it came from. The branch at the location cancels out the branch register and the PC continues sequentially. SWAPBR has also the capability of performing switch statements. [REF - PENDULUM p. 281] START and FINISH marks the beginning and end of a program. BRA is an unconditional jump.

#### 2.1.1 Example program

#### ForITo100.pal

```
1
   ; ; main
2
   ;;; increment \ a \ from \ [1..n]
 3
              BRA subbot
   subtop:
4
   main:
              SWAPBR $2
                                    ; entry/exit point
5
              NEG $2
                                     negate offset to return caller
                                     push return offset to stack
6
              EXCH $2 $1
 7
              ADDI $30 100
                                     a \neq = n
8
                                    ; set\ limit\ (\$28)\ +=\ a, set\ a=0
              BRA swap
9
              BNE $30 $0 loopbot; from a = 0 do
   looptop:
              ADDI $30 1
10
                                      a \neq 1
              BNE $30 $28 looptop; until \ a = limit \ loop \ body
11
   loopbot:
                                    ; set limit = 0
12
              SUB $28 $30
13
              ADDI $30 -100
                                     a -= n
              EXCH $2 $1
14
                                      pop return address
15
   subbot:
              BRA subtop
```

The entire program is shown in the Appendix 8. We have in section 1.1.1 seen how a similar for-loop is written in the irreversible assembly language MIPS. Now lets take a look on the for-loop in the reversible assembly language PAL.

First off the main method is wrapped within a top and a bot. Next we store the offset, so on the end of the method we are able to return to the caller. Now the looptop is checked once like from a=0 then proceed to the body. From here on the body is executed once and once again until the criteria in loopbot is true.

# 2.2 Reversible Object-Oriented Programming

Reversible Object-Oriented Programming (ROOPL) and its predecessor ROOPL++ which expanded the language with dynamic memory was created by Tue Haulund and Martin Cservenka. It is build with inspiration from the reversible programming language Janus and compiles to the Pendulum Assembly language.

#### simplePrg.rplpp

```
1
   class Program
2
        int nodeCount
 3
        int limit
 4
        method main()
5
            limit += 100
6
            from nodeCount = 0 do
 7
                skip
8
            loop
9
               nodeCount += 1
10
            until nodeCount = limit
11
            nodeCount -= limit
            limit = 100
12
```

This simple program is similar to the two earlier shown assembly programs. Though when compiled the number of instructions explodes. In Appendix 9 the full list of instructions is shown, it sums up to near 400 lines of program.

Lets divide the program into bites:

zets arriae the program mee stees.					
Part	Lines	Description			
Static	4	DATA instruction			
Malloc	205	Method for memory allocation			
Main	134	Main method equal two the other assembly programs			
Program structure	54	START FINISH			

With the above division, its clear the that even without the malloc method, the compiled program is still way bigger than the simple self-written PAL program.

Now lets take a closer look on the main method. We see that 26 lines holds a bunch of if-statements with nameded macros as **cmp** og **f**. The entire entry macro counts 57 lines including the special if-statements. The initialization and clean-up is 20 and 35 lines, where the loop-body is 14 lines.

Part	Lines
1_ main_ 0 to entry	20
entry to test	57
test	14
after exit	35

In the next chapter the focus is on the main method and the program structure. We look into the possibility of redundancy and search for patterns which is unnecessary for the program.

# 3 Analysis of redundancy

In this is section we analyse the possibility of redundant target code after compilation of the ROOPL++ program introduced in section 2.2. The analysis is split into two parts.

The first part will be a stepwise approach going through the following states:

Discover patterns which is repeated multiple times through out the target code.

Isolate the patterns into subroutines to make the target code more readable.

Group subroutines by purpose

Try to reduce the groups, for example by introducing new instructions.

The second part It also describes methods for reducing redundancy. Within this we define a smaller area of redundancy:

Redundancy is the same instruction occurring multiple times in a row in which all affect the same register. For example is the two instructions below seen as redundant:

ADDI \$3 10

ADDI \$3 8

Instead the target code could have used a single instruction:

ADDI \$3 18

# 3.1 First part - patterns

This is the first part of the analysis, where we try to identify patterns which is occurring multiple times throughout the target code.

#### 3.1.1 Getting data from memory

Multiple times we'll see that, the pattern for exchange between a register value and the place in memory. We look into an example starting between entry and the first **cmp**.

The pattern goes like this: Put the address of nodeCount into register 7. Use the address in register 7 to exchange the nodeCount in memory with the zero value in register 8. Register 8 now holds the value of nodeCount. This part is reached several times, once for each time nodeCount is not 100. This exchange is done 6 times.

We isolate the pattern by introducing a subrutine count. Count can can replace the 6 redundant patterns:

```
subtop: BRA subbot
        SWAPBR
count:
                  $2
                  $2
        NEG
        EXCH
                  $2 $1
        ADD
                  $7 $3
        ADDI
                  $7 2
                  $8 $7
        EXCH
        ADDI
                  \$7 -2
        SUB
                  $7 $3
        EXCH
                  $2 $1
subbot: BRA subtop
```

We see that the exchange part takes up 5 lines, where the subroutine takes 10 + 1 for the call. Which means all exchanges which are done more than 2 times could line wise be subroutines. Another benefit by isolating exchanges is the readability in the actual main method.

This pattern is not only seen when retrieving the nodeCount, it is seen every time memory and a register has to communicate. But this is the same as change the register value r1 with the value in memory of the stack pointer + some offset. One could formalize a method m with three arguments: m(r1, sp, offset). Why this could by a place to introduce a new instruction.

#### 3.1.2 Special if-statements

Through out the target code, we seen multiple if-statements, properly auto-generated, with labels like **cmp** and **f**. Lets start by isolating the areas with special if-statements.

```
BRA subbot_if_1
subtop_if_1:
if_{-1}:
                           SWAPBR $2
                           NEG $2
                           EXCH $2 $1
                           BNE
                                    $8 $0 cmp_bot_16
cmp_top_15:
                                    $9 1
                           XORI
cmp\_bot\_16:
                           BNE
                                    $8 $0 cmp_top_15
                                    $9 $0 f_bot_18
f_{top_{17}}:
                           BEQ
                           XORI
                                    $10 1
                                    9 \ f_{top_{1}}
                           BEQ
f_bot_18:
                           XOR
                                    $6 $10
f_bot_18_i:
                           BEQ
                                    9 \ f_{top_{1}7_{i}}
                           XORI
                                    $10 1
f_{top_17_i}:
                           BEQ
                                    $9 $0 f_bot_18_i
                           BNE
                                    $8 $0 cmp_top_15_i
cmp_bot_16_i:
                                    $9 1
                           XORI
                           BNE
                                    $8 $0 cmp_bot_16_i
cmp\_top\_15\_i:
                           EXCH $2 $1
subbot_if_1:
                           BRA subtop_if_1
```

At first glance we see that the purpose is to set \$6 at one or zero. Which means that a simple if-statement could possibly replace the above both complicated and hard-to-read set of instructions. Lets try to figurer out the parts. Lets say if 8 == 0, then XOR \$6 by \$10, where \$10 in is the same as 1. This could be written as below.

$iftop_3:$	$\operatorname{BNE}$	\$8	\$0	$ifbot_3$
	XORI	\$6	1	
$ifbot_3:$	BNE	\$8	\$0	$iftop\_3$

If this holds, we could when approaching the part where the special if-statement occures take the first line and let it be the condition, find the XOR which is not encapsulated within a label, exchange the XOR with XORI and exchange the second register value with a 1.

# 3.2 Second part - methods for reduced redundancy

In this section we upgrade PendVM[9] the virtual machine on which we can run PAL programs. We further introduce some new algorithm which can applies on the target code of a compiled ROOPL++ program.

Main algorithm of the section is remove\_ redundancy which we'll later apply to sample programs for testing.

#### 3.2.1 PendVM - OUT

PendVM does not support methods to save the results of an executed program, which is why i have expanded one of the instructions: OUT.

OUT is now able to write or append a register value to the text-file static\_storage.text. For now ROOPL has not been expanded which means, that using the OUT functionality requeries three steps:

The immediate value in ADDI just after START has to incremented by the value of need OUT instructions.

The immediate value in ADDI just before FINISH has to incremented by the value of need OUT instructions.

OUT instruction has be manually inserted into the resulting pal file of a compiled ROOPL++ program.

The expansion of PendVM exists of the following files:

```
int i_out (WORD, WORD, WORD);
```

pendvm.h

```
("OUT", {REG, REG, NIL}, i_out)
```

pal\_ parse.c

```
int
i_out(WORD r, WORD u1, WORD u2)
{
  char buf[..];
  sprintf(buf, '%d', m->reg[r1]);
  const char *p = buf;

FILE *file;
  file = fopen('static_storage.txt', m->reg[r2]);
  fputs(p, file);
```

```
fclose(file);
return 0;
}
```

machine.c

#### 3.2.2 PendVM - EXCHI

Now what we have seen is that the exchange of memory and register values is a 5 line procedure, which is occuring multiple times within the target code of a ROOPL++ program. Which is why i want to introduce a new instruction called EXCHI, it takes the 3 arguments, two registers and an immediate. First register will get its value swapped with the value in the memory of position of the second register + immediate. The expansion of PendVM exists of the following files:

```
int i_exchpi (WORD, WORD, WORD);
```

pendvm.h

```
\label{eq:chi}  (\text{"EXCHI"}, \text{ } \{\text{REG}, \text{ } \text{REG}, \text{ } \text{IMM}\}, \text{ } \text{i}_{-}\text{exchi}\,)
```

pal\_ parse.c

```
int
i_exchi(WORD rd, WORD ra, WORD u1)
{
WORD tmp;
/* ra is the stack pointer
   * u1 is the offset */
MEMORY *loc = mem_get(m->reg[ra]+u1);

if (loc->type == MEM_INST) {
   pendvm_error("..");
   return -4; /* "exchange with instruction" error */
}

tmp=m->reg[rd];
m->reg[rd]=loc->value;
loc->value=tmp;
return 0;
}
```

machine.c

#### 3.2.3 Algorithm - Memory exchange

Find the	pattern	<del>-</del> :
ADD ADDI EXCH	\$r1 \$r3	\$r2 imm \$r1
ADDI SUB		-imm \$r2
Replace i EXCHI		 \$r2_imm

#### 3.2.4 Algorithm - Special if-statements

Find the pa	ttern:
cmp_top_x	$inst_{-}x$
$cmp\_bot\_x$	$inst{}x$
<>	
XOR	\$r1 \$r2
<>	
$cmp\_bot\_x\_i$	$inst{}x{}i$
$cmp\_top\_x\_i$	$inst{}x{}i$
Replace it	with:
if_top_x:	instx
XORI	\$r1 1
$if_bot_x$ :	inst x

#### 3.2.5 Algorithm - Remove redundancy

For the task of a successfull analysis we need an algorithm in which can find *redundancy*, merge and remove instruction and atlast update the stack point with the new immediate value. This algorithm can be applied to an existing PAL program, which means, that is first useful, when a ROOPL++ program has been compiled to target code. Thus the algorithm must take a .PAL file and produce a .PAL file.

```
remove_redundancy(filepath fp):
    /* read is a function which takes a filepath
     * and returns a array of elements, where each
     * element is a line the the file. */
     file = read(fp)
    /* Replace patterns with simplifications */
     call memory_exchange (file)
     call special_if_statements (file)
    /* map(func1, l[]) applies func1
     * to every element of l */
     lines = map(parse_inst, file)
     lastRegister = ','
     lastInstruction = 0
     removeableLines []
     for i = 0 to length(lines)
       if lines[i][0] in {'ADDI', 'EXCHI'} then
         if lastRegister = lines[i][1] then
            lines [lastInstruction][2] += lines[i][2]
            insert (removeableLines, i)
         else
            lastRegister = lines[i][1]
            lastInstruction = i
       else
           lastRegister = ','
           lastInstruction = 0
     /* Remove all redundant instructions, update stack pointer */
     lines = removeLinesAdjustSP(lines, removeableLines)
     /* write is a function which takes an array
      * and writes a line for each element to a named file */
     write(lines, 'reduced.pal')
/* A method to divide an instruction
* into opcode, arg0, arg1, arg2 */
parse_inst (instruction):
   return split (instruction, '_')
```

#### 4 Results

Now we apply all our new tools to the target code, after we'll see the difference instructions and for test purpose, we'll write the values of nodeCount from 1..100 to a .txt file both for the program p which was created by the ROOPL++ compiler and the program p' which is the reduced program of p.

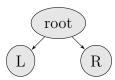
Program	PendVM step	main lines	start lines	Description
p	6572	134	50	Original program produced
				by the ROOPL++ compiler
p'	2102	50	42	A reduced version of p,
				where the algorithm re-
				move_ redundancy has been
				applied
p"	1328	41	5	The example PAL program
				from the section of Pen-
				dulum Assembly Language:
				ForITo100.pal

On this simple program counting from 1..100, we have reduced the needed steps in PendVM to one third of the original need steps. Furthermore the number of lines have been reduced which should be reflected on the readability.

#### 5 Data structures

#### 5.1 Binary tree

A binary tree in computer science is a data structure, which is either empty or consist of a root node, where each node has atmost two children. You could see the binary tree as a tuple of the single node root and the two binary trees L & R.



Simple binary tree, with the a root node and two binary trees L & R as children to the root.

Their are different types of binary tree all with their own properties. fx A full binary tree is one where every node either have zero or two child-nodes. A perfect binary tree is one, where all interior nodes have two children and all leaves have none. the A balanced binary tree is one where L & R of every node only differ in height with no more than one. [REF-Introduction to algorithms]

Properties of binary tree is fx maximum height, number of nodes, number of leafs and so on. Operations of different sort can be used of a binary tree some of em is:

Traversal: Search for a node

**Insertion:** Insert a new node

**Deletion:** Remove an existing node

#### 6 Conclusion

#### 7 Further work

#### 7.0.1 Instruction operands - [OVERVEJ]

Machine code instructions vary, but in general each instruction itself will have fixed number of operands (0 to 3). Operands can have the following types:[6, p. 12]

register: These operands refer directly to the content of the CPU-register.

**memory:** These refer to data in memory. The address of the data may be a constant hardcoded into the instruction or may be computed using values of registers. Address are always offsets from the beginning of a segment.

**immediate:** These fixed values that are listed in the instruction itself. They are stored in the instruction itself (in code segment), not in the data segment.

**implied:** These operands are not explicitly shown. For example the increment instruction adds one to the register or memory. The one is implied.

#### 7.0.2 Pendulum operation

Operation type					
R	op	rsd	rs	sh/rot	func
bit	6	5	5	5	11
J	j/cf	Target			
bit	6	26			
В	j/b op	ra	rb	offset	
bit	6	5	5	16	
I	op	rsd	immediate		
bit	6	5	21		

Jump instructions other than j and all conditional branches uses B-type instruction encoding and specify two registers and an offset.

Immediate instructions, I-type, specify one register and a 21 bit signed or unsigned, depending on the opcode, immediate value.

Instruction

ADD

SUB

ADDI

AND

ANDI

BEQ

**BGEZ** 

**BGEZAL** 

**BGTZ** 

BLEZ Branch on less than or equal to zero

BLTZ Branch on less than zero

BLTZAL Branch on less than than zero and link

BNE Branch on not equal

CF Come-from

# 7.1 Register values

Before entry

Register	Value
1	2462
2	0
3	2464
6	1
7	0
8	0
9	0
10	0
11	0
12	0

```
BRA subbot_if_2
subtop_if_2:
if_{-2}:
                          SWAPBR $2
                          NEG $2
                          EXCH $2 $1
                          BNE
cmp\_top\_19:
                                  $8 $10 cmp_bot_20
                          XORI
                                  $11 1
                                  $8 $10 cmp_top_19
cmp\_bot\_20:
                          BNE
f_top_21:
                          BEQ
                                  $11 $0 f_bot_22
                          XORI
                                  $12 1
f_bot_22:
                                  11 \ f_{top_2} 
                          BEQ
                          XOR
                                  $6 $12
f_bot_22_i:
                                  $11 $0 f_top_21_i
                          BEQ
                          XORI
                                  $12 1
f_top_21_i:
                          BEQ
                                  $11 $0 f_bot_22_i
cmp\_bot\_20\_i:
                          BNE
                                  $8 $10 cmp_top_19_i
                          XORI
                                  $11 1
                          BNE
                                  $8 $10 cmp_bot_20_i
cmp_top_19_i:
                          EXCH $2 $1
subbot_if_2:
                          BRA subtop_if_2
```

And see what entry has become, simple 9 lines.

```
$6 $0 assert_13
entry_11:
                           BEQ
                           BRA
                                   get
                                   if_{-}1
                           BRA
                           BRA
                                   get
                           BRA
                                   get
                                   get_lim
                           BRA
                           BRA
                                   if_2
                           BRA
                                   get_lim
```

# 7.2 Pendulum

, with exception of two constraints:

Memory access is always an exchange. The exchange instruction swaps register value with the value in memory at an address specified by another register.[4, p. 32]

Non-sequential instructions like jumps to another macro must have a return address. This is needed to keep the reversibility. [4, p. 36] Say an instruction is reached by one jump, then that instruction only needs to keep track a single destination. In case an instruction is reached from multiple other instructions, it needs to keep track of which instruction that made the jump.[4, p. 25]

# 8 Appendix A

#### ForITo100.pal

```
;;; increment a from [1..n]
2
   subtop:
             BRA subbot
3
   main:
             SWAPBR $2
                                  ; entry/exit point
4
             NEG $2
                                  ; negate offset to return caller
             EXCH $2 $1
5
                                  ; push return offset to stack
              ADDI $30 100
6
                                   ; a += n
 7
             BRA swap
                                  ; set limit ($28) += a, set a = 0
             BNE $30 $0 loopbot; from a = 0 do
8
   looptop:
9
              ADDI $30 1
                                  : a += 1
             BNE $30 $28 looptop; until a = limit loop body
10
   loopbot:
             SUB $28 $30
                                    set limit = 0
11
12
              ADDI \$30 -100
                                  ; a = n
13
             EXCH $2 $1
                                  ; pop return address
14
   subbot:
             BRA subtop
   ;; swap(int a, int b)
15
   subtop_3: BRA subbot_3
16
             SWAPBR $2
17
   swap:
             NFG $2
18
             EXCH $2 $1
19
20
             ADD $28 $30
              SUB $30 $28
21
22
             EXCH $2 $1
23
   subbot_3: BRA subtop_3
24
   ;; increment (int a)
   subtop_2: BRA subbot_2
25
             SWAPBR $2
26
   incr:
27
             NEG $2
28
             EXCH $2 $1
              ADDI $30 1
29
30
             EXCH $2 $1
   subbot_2: BRA subtop_2
31
32
   ;; write (int a, int mode)
   subtop_1: BRA subbot_1
33
34
   write:
             SWAPBR $2
35
             NEG $2
             EXCH $2 $1
36
             OUT $30 $31
37
38
             EXCH $2 $1
   subbot_1: BRA subtop_1
39
```

# 9 Appendix B

# 9.1 Full program

prg.pal

```
;; pendulum pal file
2
                               BRA
   top:
                                        start
   l_r_nodeCount:
                               DATA
                                       0
   l_r_limit:
                               DATA
                                       0
   l_Program_vt:
                               DATA
                                        214
                                        l_malloc_bot
   l_malloc_top:
                               BRA
7
   l_malloc:
                               SWAPBR $2
                               NEG
                                       $2
8
9
                               ADDI
                                       $9 2
                               XOR
                                        $8 $0
10
11
                               ADDI
                                       $1 1
                                       $6 $1
12
                               EXCH
13
                               ADDI
                                        $1 1
                                       $7 $1
14
                               EXCH
                                       $2 $1
15
                               EXCH
                               ADDI
                                       $1 -1
16
                               BRA
                                       l_{-}malloc1
17
18
                               ADDI
                                       $1 1
                               EXCH
                                       $2 $1
19
                               EXCH
                                       $7 $1
20
21
                               ADDI
                                       \$1 -1
                                       $6 $1
22
                               EXCH
23
                               ADDI
                                       $1 -1
24
                               XOR
                                       $8 $0
                                       $9 -2
25
                               ADDI
26
   l_malloc_bot:
                                        l_malloc_top
                               BRA
   l_malloc1_top:
                                        l_malloc1_bot
27
                               BRA
28
                               ADDI
                                       $1 1
29
                               EXCH
                                       $2 $1
30
                               SUB
                                       $17 $8
                               XOR
                                        $17 $4
31
   l_malloc1:
                               SWAPBR $2
32
33
                               NEG
                                       $2
34
                               EXCH
                                       $2 $1
                               ADDI
                                        \$1 -1
35
                               XOR
                                       $17 $4
36
37
                               ADD
                                       $17 $8
38
                               EXCH
                                       $19 $17
39
                               XOR
                                       $18 $19
```

```
40
                                EXCH
                                         $19 $17
41
                                XOR
                                         $13 $9
42
                                SUB
                                         $13 $7
43
                                BGEZ
   cmp_top_1:
                                         13 \text{ cmp\_bot\_2}
                                XORI
44
                                         $14 1
45
                                BGEZ
                                         $13 cmp_top_1
   cmp\_bot\_2:
46
                                XOR
                                         $10 $14
47
                                BGEZ
   cmp_bot_2i:
                                         13 \text{ cmp-top-1-i}
48
                                XORI
                                         $14 1
49
   cmp_top_1i:
                                BGEZ
                                         13 \text{ cmp-bot-}2_i
                                ADD
50
                                         $13 $7
                                         $13 $9
51
                                XOR
52
                                BEQ
   l_o_test:
                                         $10 $0 l_o_test_false
                                XORI
53
                                         $10 1
                                ADDI
                                         $8 1
54
55
                                EXCH
                                         $19 $17
56
                                XOR
                                         $18 $19
                                EXCH
                                         $19 $17
57
                                RL
58
                                         $9 1
                                         $10 $1
                                EXCH
59
                                ADDI
                                         $1 -1
60
                                EXCH
                                         $11 $1
61
62
                                ADDI
                                         $1 -1
                                EXCH
                                         $12 $1
63
                                ADDI
64
                                         $1 -1
                                EXCH
                                         $14 $1
65
                                ADDI
                                         $1 -1
66
                                EXCH
                                         $16 $1
67
68
                                ADDI
                                         $1 -1
                                         $17 $1
69
                                EXCH
                                ADDI
                                         \$1 -1
70
                                EXCH
                                         $18 $1
71
                                ADDI
                                         $1 -1
72
73
                                EXCH
                                         $20 $1
74
                                ADDI
                                         $1 -1
75
                                EXCH
                                         $21 $1
76
                                ADDI
                                         $1 -1
                                EXCH
                                         $22 $1
77
                                ADDI
78
                                         $1 -1
79
                                EXCH
                                         $23 $1
                                         $1 -1
                                ADDI
80
                                BRA
                                         l_malloc1
81
82
                                ADDI
                                         $1 1
                                EXCH
                                         $23 $1
83
84
                                ADDI
                                         $1 1
```

```
85
                                EXCH
                                        $22 $1
86
                                ADDI
                                        $1 1
87
                                EXCH
                                        $21 $1
                                ADDI
                                        $1 1
88
                                EXCH
                                        $20 $1
89
90
                                ADDI
                                        $1 1
                                EXCH
                                        $18 $1
91
92
                                ADDI
                                        $1 1
93
                                EXCH
                                        $17 $1
94
                                ADDI
                                        $1 1
                                EXCH
                                        $16 $1
95
                                ADDI
                                        $1 1
96
                                EXCH
                                        $14 $1
97
                                ADDI
                                        $1 1
98
                                EXCH
                                        $12 $1
99
100
                                ADDI
                                        $1 1
                                EXCH
                                        $11 $1
101
102
                                ADDI
                                        $1 1
                                EXCH
                                        $10 $1
103
104
                                RR
                                        $9 1
105
                                ADDI
                                        \$8 -1
                                XORI
                                        $10 1
106
107
    l_o_assert_true:
                                BRA
                                        l_oassert
    l_o_test_false:
                                BRA
                                        l_otest
108
109
                                BEQ
                                        $18 $0 cmp_bot_6
    cmp\_top\_5:
110
                                XORI
                                        $20 1
                                        18 \ cmp\_top_5
111
    cmp\_bot\_6:
                                BEQ
112
                                        $11 $20
                                XOR
113
                                BEQ
                                        $18 $0 cmp_top_5_i
    cmp_bot_6_i:
114
                                XORI
                                        $20 1
                                        18 \ 0 \ cmp_bot_6_i
115
    cmp_top_5_i:
                                BEQ
116
    l_i_{test}:
                                        BEQ
                                XORI
                                        $11 1
117
                                        $6 $18
118
                                ADD
119
                                SUB
                                        $18 $6
120
                                EXCH
                                        $12 $6
121
                                EXCH
                                        $12 $17
122
                                XOR
                                        $12 $6
123
                                XORI
                                        $11 1
124
    l_i_assert_true:
                                BRA
                                        l_i_assert
125
    l_i_test_false:
                                BRA
                                        l_i_{test}
126
                                ADDI
                                        $8 1
127
                                RL
                                        $9 1
                                        $10 $1
128
                                EXCH
129
                                ADDI
                                        $1 -1
```

1		
130	EXCH	\$11 \$1
131	ADDI	\$1 -1
132	EXCH	\$12 \$1
133	ADDI	\$1 -1
134	EXCH	\$14 \$1
135	ADDI	\$1 -1
136	EXCH	\$16 \$1
137	ADDI	\$1 -1
138	EXCH	\$17 \$1
139	ADDI	\$1 -1
140	EXCH	\$18 \$1
141	ADDI	\$1 -1
142	EXCH	\$20 \$1
143	ADDI	\$1 -1
144	EXCH	\$21 \$1
145		
	ADDI	\$1 -1
146	EXCH	\$22 \$1
147	ADDI	\$1 -1
148	EXCH	\$23 \$1
149	ADDI	\$1 -1
150	BRA	$l_malloc1$
151	ADDI	\$1 1
152	EXCH	\$23 \$1
		\$1 1
153	ADDI	
154	EXCH	\$22 \$1
155	ADDI	\$1 1
156	EXCH	\$21 \$1
157	ADDI	\$1 1
158	EXCH	\$20 \$1
159	ADDI	\$1 1
160	EXCH	\$18 \$1
161	ADDI	\$1 1
162	EXCH	\$17 \$1
163	ADDI	\$1 1
164	EXCH	\$16 \$1
165	ADDI	\$1 1
166	EXCH	\$14 \$1
167	ADDI	\$1 1
168	EXCH	\$12 \$1
169	ADDI	\$1 1
170	EXCH	\$11 \$1
171	ADDI	\$1 1
172	EXCH	\$10 \$1
173	RR	\$9 1
174	ADDI	\$8 -1
ı		l.

```
175
                                 XOR
                                          $12 $6
176
                                 EXCH
                                          $12 $17
177
                                 ADD
                                          $6 $9
                                 BNE
                                          $11 $0 l_i_assert_true
178
    l_i_assert:
                                          $12 $17
179
                                 EXCH
180
                                 SUB
                                          $6 $9
                                          $6 $12 cmp_bot_8
181
    cmp\_top\_7:
                                 BEQ
182
                                 XORI
                                          $21 1
183
                                 BEQ
                                          $6 $12 cmp_top_7
    cmp_bot_8:
184
    cmp_top_9:
                                 BNE
                                          $12 $0 cmp_bot_10
                                          $22 1
185
                                 XORI
                                          $12 $0 cmp_top_9
186
                                 BNE
    cmp_bot_10:
187
                                 ORX
                                          $23 $21 $22
                                 XOR
                                          $11 $23
188
189
                                          $23 $21 $22
                                 ORX
190
    cmp_bot_10_i:
                                 BNE
                                          $12 $0 cmp_top_9_i
                                          $22 1
191
                                 XORI
192
    cmp_top_9_i:
                                 BNE
                                          $12 $0 cmp_bot_10_i
                                          $6 $12 cmp_top_7_i
193
    cmp_bot_8_i:
                                 BEQ
194
                                 XORI
                                          $21 1
195
                                          $6 $12 \text{ cmp\_bot\_8\_i}
                                 BEQ
    cmp_top_7_i:
196
                                 ADD
                                          $6 $9
197
                                 EXCH
                                          $12 $17
                                 BNE
                                          $10 $0 l_o_assert_true
198
    l_o_assert:
199
                                 XOR
                                          $15 $9
200
                                 SUB
                                          $15 $7
201
    cmp\_top\_3:
                                 BGEZ
                                          15 \text{ cmp\_bot\_4}
                                 XORI
202
                                          $16 1
203
                                 BGEZ
                                          $15 \text{ cmp-top-3}
    cmp\_bot\_4:
204
                                 XOR
                                          $10 $16
                                          15 \text{ cmp-top-3-i}
205
    cmp_bot_4i:
                                 BGEZ
206
                                 XORI
                                          $16 1
                                 BGEZ
                                          15 \text{ cmp-bot-}4_{-i}
207
    cmp\_top\_3\_i:
208
                                 ADD
                                          $15 $7
209
                                 XOR
                                          $15 $9
210
    l_malloc1_bot:
                                 BRA
                                          l_malloc1_top
211
    l_main_0_top:
                                 BRA
                                          l_main_0_bot
212
                                 ADDI
                                         $1 1
                                          $2 $1
213
                                 EXCH
214
                                 EXCH
                                          $3 $1
215
                                 ADDI
                                          $1 -1
216
                                 SWAPBR $2
    l_main_0:
217
                                 NEG
                                          $2
218
                                 ADDI
                                          $1 1
                                          $3 $1
219
                                 EXCH
```

```
220
                                 EXCH
                                          $2 $1
221
                                 ADDI
                                          \$1 -1
222
                                 ADD
                                          $6 $3
223
                                 ADDI
                                          $6 3
224
                                 EXCH
                                          $7 $6
225
                                 ADDI
                                          $6 -3
226
                                 SUB
                                          $6 $3
227
                                 XORI
                                          $8 100
228
                                 ADD
                                          $7 $8
229
                                 XORI
                                          $8 100
                                          $6 $3
230
                                 ADD
                                 ADDI
231
                                          $6 3
232
                                 EXCH
                                          $7 $6
                                 ADDI
                                          $6 -3
233
234
                                 SUB
                                          $6 $3
235
                                 XORI
                                          $6 1
                                          $6 $0 assert_13
236
    entry_11:
                                 BEQ
237
                                 ADD
                                          $7 $3
238
                                          $7 2
                                 ADDI
                                          $8 $7
239
                                 EXCH
240
                                 ADDI
                                          $7 -2
                                          $7 $3
241
                                 SUB
                                          88 \ 0 \ cmp\_bot\_16
242
    cmp\_top\_15:
                                 BNE
243
                                 XORI
                                          $9 1
244
                                 BNE
                                          $8 $0 cmp_top_15
    cmp_bot_16:
245
                                          $9 $0 f_bot_18
    f_{top_{1}7}:
                                 BEQ
246
                                 XORI
                                          $10 1
247
                                 BEQ
                                          $9 $0 f_top_17
    f_bot_18:
248
                                 XOR
                                          $6 $10
249
                                 BEQ
                                          $9 $0 f_top_17_i
    f_bot_18_i:
250
                                          $10 1
                                 XORI
251
                                 BEQ
    f_{top_{1}7_{i}}:
                                          $9 $0 f_bot_18_i
                                 BNE
252
                                          $8 $0 cmp_top_15_i
    cmp_bot_16_i:
253
                                 XORI
                                          $9 1
                                          88 \ \text{mp_bot_16_i}
254
    cmp_top_15_i:
                                 BNE
255
                                 ADD
                                          $7 $3
256
                                 ADDI
                                          $7 2
257
                                 EXCH
                                          $8 $7
258
                                 ADDI
                                          \$7 -2
259
                                 SUB
                                          $7 $3
                                          $7 $3
260
                                 ADD
                                 ADDI
                                          $7 2
261
262
                                 EXCH
                                          $8 $7
263
                                 ADDI
                                          \$7 -2
                                 SUB
                                          $7 $3
264
```

```
265
                                 ADD
                                         $9 $3
266
                                 ADDI
                                         $9 3
267
                                 EXCH
                                         $10 $9
                                 ADDI
                                         $9 -3
268
269
                                         $9 $3
                                 SUB
270
                                 BNE
                                         $8 $10 cmp_bot_20
    cmp\_top\_19:
271
                                 XORI
                                         $11 1
272
                                 BNE
                                         $8 $10 cmp_top_19
    cmp_bot_20:
273
                                 BEQ
                                         $11 $0 f_bot_22
    f_{top_21}:
274
                                 XORI
                                         $12 1
275
    f_bot_22:
                                 BEQ
                                         $11 $0 f_top_21
276
                                         $6 $12
                                 XOR
277
    f_bot_22_i:
                                         11 \ f_t op_2 1_i
                                 BEQ
278
                                 XORI
                                         $12 1
279
                                         $11 $0 f_bot_22_i
    f_{top_{2}1_{i}}:
                                 BEQ
280
    cmp_bot_20_i:
                                 BNE
                                         88 10 cmp_top_19_i
281
                                 XORI
                                         $11 1
282
                                 BNE
                                         $8 $10 cmp_bot_20_i
    cmp_top_19_i:
283
                                         $9 $3
                                 ADD
                                         $9 3
284
                                 ADDI
285
                                 EXCH
                                         $10 $9
                                         $9 -3
286
                                 ADDI
287
                                 SUB
                                         $9 $3
288
                                         $7 $3
                                 ADD
                                         $7 2
289
                                 ADDI
290
                                 EXCH
                                         $8 $7
                                 ADDI
                                         \$7 -2
291
292
                                         $7 $3
                                 SUB
293
    test_12:
                                 BNE
                                         $6 $0 exit_14
294
                                 ADD
                                         $7 $3
295
                                 ADDI
                                         $7 2
296
                                 EXCH
                                         $8 $7
                                 ADDI
                                         \$7 -2
297
298
                                 SUB
                                         $7 $3
299
                                 XORI
                                         $9 1
300
                                 ADD
                                         $8 $9
301
                                 XORI
                                         $9 1
                                         $7 $3
302
                                 ADD
                                         $7 2
303
                                 ADDI
304
                                 EXCH
                                         $8 $7
305
                                 ADDI
                                         \$7 -2
306
                                 SUB
                                         $7 $3
307
    assert_13:
                                 BRA
                                         entry_11
308
    exit_14:
                                 BRA
                                         test_12
309
                                 XORI
                                         $6 1
```

```
310
                                          $6 $3
                                  ADD
311
                                  ADDI
                                          $6 2
312
                                  EXCH
                                          $7 $6
                                  ADDI
313
                                          $6 -2
314
                                  SUB
                                          $6 $3
                                          $8 $3
315
                                  ADD
316
                                  ADDI
                                          $8 3
317
                                  EXCH
                                          $9 $8
318
                                  ADDI
                                          \$8 -3
                                  SUB
                                          $8 $3
319
                                  SUB
                                          $7 $9
320
321
                                  ADD
                                          $8 $3
322
                                  ADDI
                                          $8 3
323
                                  EXCH
                                          $9 $8
324
                                  ADDI
                                          \$8 -3
325
                                  SUB
                                          $8 $3
326
                                  ADD
                                          $6 $3
327
                                  ADDI
                                          $6 2
328
                                  EXCH
                                          $7 $6
                                  ADDI
                                          $6 -2
329
330
                                  SUB
                                          $6 $3
                                          $6 $3
331
                                  ADD
332
                                  ADDI
                                          $6 3
333
                                  EXCH
                                          $7 $6
                                  ADDI
334
                                          $6 -3
335
                                  SUB
                                          $6 $3
                                  XORI
336
                                          $8 100
                                  SUB
                                          $7 $8
337
338
                                  XORI
                                          $8 100
339
                                  ADD
                                          $6 $3
340
                                  ADDI
                                          $6 3
341
                                  EXCH
                                          $7 $6
342
                                  ADDI
                                          $6 -3
343
                                  SUB
                                          $6 $3
344
    l_main_0_bot:
                                  BRA
                                          l_main_0_top
345
    start:
                                  BRA
                                          top
346
                                  START
347
                                  ADDI
                                          $4 393
                                  XOR
348
                                          $5 $4
349
                                  ADDI
                                          $5 10
                                  XOR
                                          $7 $5
350
351
                                  ADDI
                                          $4 10
352
                                  ADDI
                                          $4 -1
                                  EXCH
                                          $7 $4
353
354
                                  ADDI
                                          $4 1
```

```
355
                                  ADDI
                                          $4 - 10
356
                                 XOR
                                          $1 $5
357
                                  ADDI
                                          $1 2048
                                          $1 -4
358
                                  ADDI
359
                                 XOR
                                          $3 $1
                                  XORI
360
                                          $6 3
361
                                 EXCH
                                          $6 $3
362
                                  ADDI
                                          $1 -1
363
                                 EXCH
                                          $3 $1
                                  ADDI
364
                                          $1 -1
                                  BRA
365
                                          l_main_0
                                  ADDI
                                          $1 1
366
367
                                  EXCH
                                          $3 $1
                                  ADDI
                                          $3 1
368
369
                                  ADDI
                                          $3 1
370
                                 EXCH
                                          $6 $3
                                  XORI
                                          $7 1
371
372
                                 EXCH
                                          $6 $7
373
                                  XORI
                                          $7 1
                                  ADDI
374
                                          \$3 -1
375
                                  ADDI
                                          \$3 -1
                                  ADDI
                                          $3 1
376
                                  ADDI
                                          $3 2
377
378
                                  EXCH
                                          $6 $3
                                  XORI
                                          $7 2
379
                                          $6 $7
380
                                  EXCH
                                  XORI
                                          $7 2
381
                                  ADDI
                                          \$3 -2
382
383
                                  ADDI
                                          \$3 -1
384
                                  ADDI
                                          $1 1
385
                                 EXCH
                                          $6 $3
                                  XORI
386
                                          $6 3
387
                                 XOR
                                          $3 $1
                                          $1 4
388
                                  ADDI
389
                                  ADDI
                                          $1 -2048
390
                                 XOR
                                          $1 $5
391
                                  ADDI
                                          $5 -10
392
                                 XOR
                                          $5 $4
393
                                  ADDI
                                          $4 - 393
394
                                  FINISH
    finish:
```

#### 9.1.1 Malloc

# malloc

1	l_malloc_top:	BRA	l_malloc_bot
2	l_malloc:	SWAPBR	\$2
3		NEG	\$2
4		ADDI	\$9 2
5		XOR	\$8 \$0
6		ADDI	\$1 1
7		EXCH	\$6 \$1
8		ADDI	\$1 1
9		EXCH	\$7 \$1
10		EXCH	\$2 \$1
11		ADDI	\$1 -1
12		BRA	l_malloc1
13		ADDI	\$1 1
14		EXCH	\$2 \$1
15		EXCH	\$7 \$1
16		ADDI	\$1 -1
17		EXCH	\$6 \$1
18		ADDI	\$1 -1
19		XOR	\$8 \$0
20		ADDI	\$9 <b>-</b> 2
21	l_malloc_bot:	BRA	l_malloc_top

# malloc1

```
l\_malloc1\_top:
                                {\rm BRA}
                                         l_malloc1_bot
2
                                 ADDI
                                         $1 1
3
                                EXCH
                                         $2 $1
                                 SUB
                                         $17 $8
4
5
                                XOR
                                         $17 $4
6
                                SWAPBR $2
  l_malloc1:
7
                                NEG
                                         $2
8
                                ADD
                                         $15 $7
                                         $15 $9
9
                                XOR
  l_malloc1_bot:
                                BRA
                                          l\_m\,all\,o\,c\,1\_t\,o\,p
```

#### References

- [1] http://www.computinghistory.org.uk/det/32489/Kathleen-Booth/
- [2] https://www.ibm.com/support/knowledgecenter/SSLTBW\_2.1.0/com.ibm.zos.v2r1.asma400/asmr102112.htm
- [3] https://en.wikipedia.org/wiki/Von\_Neumann\_architecture
- [4] Vieri, C. J. et al. *Pendulum: A Reversible Computer Architecture*. Master's Thesis. University of California at Berkeley 1993.
- [5] Michael P. Frank. Reversibility for Efficient Computing. Ph.D Thesis. University of Florida, 1999.
- [6] Carter, P. A. PC Assembly Language. 2006
- [7] Yokoyama, T. and Glück, R. A reversible programming language and its invertible self-interpreter. ACM, 2007.
- [8] C. H. Bennet. Notes on the history of reversible computation. IBM J. Res. Dev., 32(1), 1988
- [9] https://github.com/TueHaulund/PendVM
- [10] https://plato.stanford.edu/entries/turing-machine/
- [11] J. C. Maxwell. *Theory of Heat*, 4th Ed., Longmans, Green & Co., London, 1875 (1st Ed. 1871)