

# Introduction to Computer Graphics

AMES101, Lingqi Yan, UC Santa Barbara

## Lecture 21: Animation



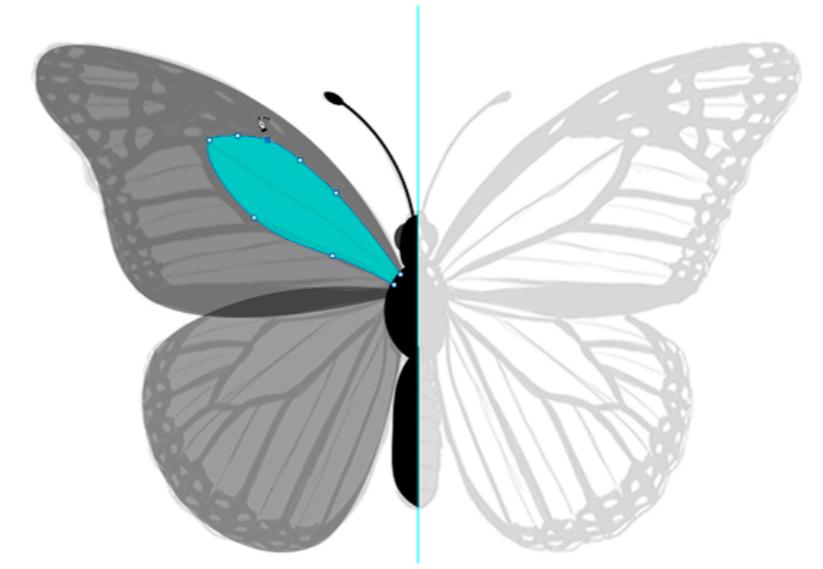
# Announcements

- Homework 7: 95 submissions so far
- Final project ideas: 18 submissions so far (expected more)
- My personal bad habit
  - Misuse of conjunctions
  - “OK”, “so”, etc. in English
  - “这个”, “然后”, etc. in Chinese
  - Can't really control when I'm thinking,  
but will try my best to avoid them

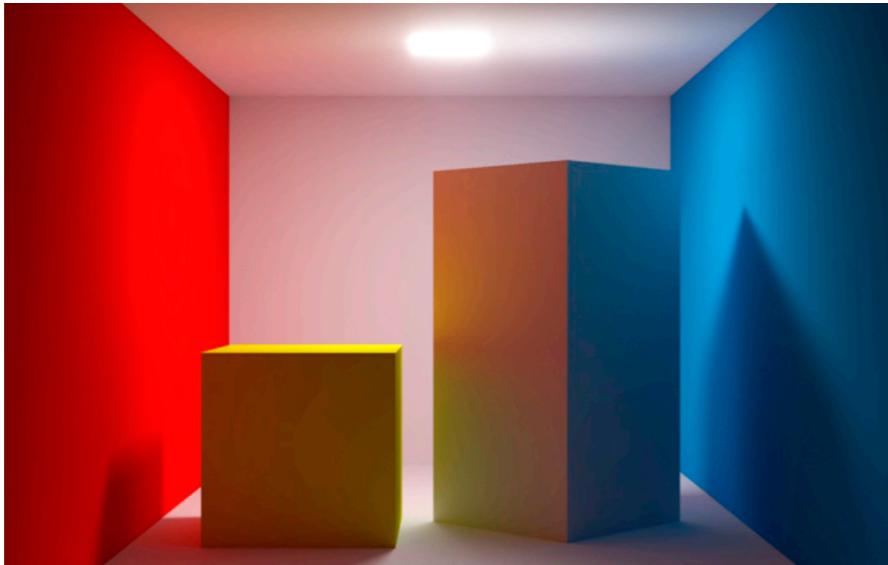
# Course Roadmap



Rasterization



Geometry



Light Transport



Animation / simulation

# Today

## Introduction to Computer Animation

- History
- Keyframe animation
- Physical simulation
- Kinematics
- Rigging

# Animation

“Bring things to life”

- Communication tool
- Aesthetic issues often dominate technical issues

An extension of modeling

- Represent scene models as a function of time

Output: sequence of images that when viewed sequentially provide a sense of motion

- Film: 24 frames per second
- Video (in general): 30 fps
- Virtual reality: 90 fps

# Historical Points in Animation

(slides courtesy of Prof. Keenan Crane @ CMU)

# First Animation



(Shahr-e Sukteh, Iran 3200 BCE)

# History of Animation

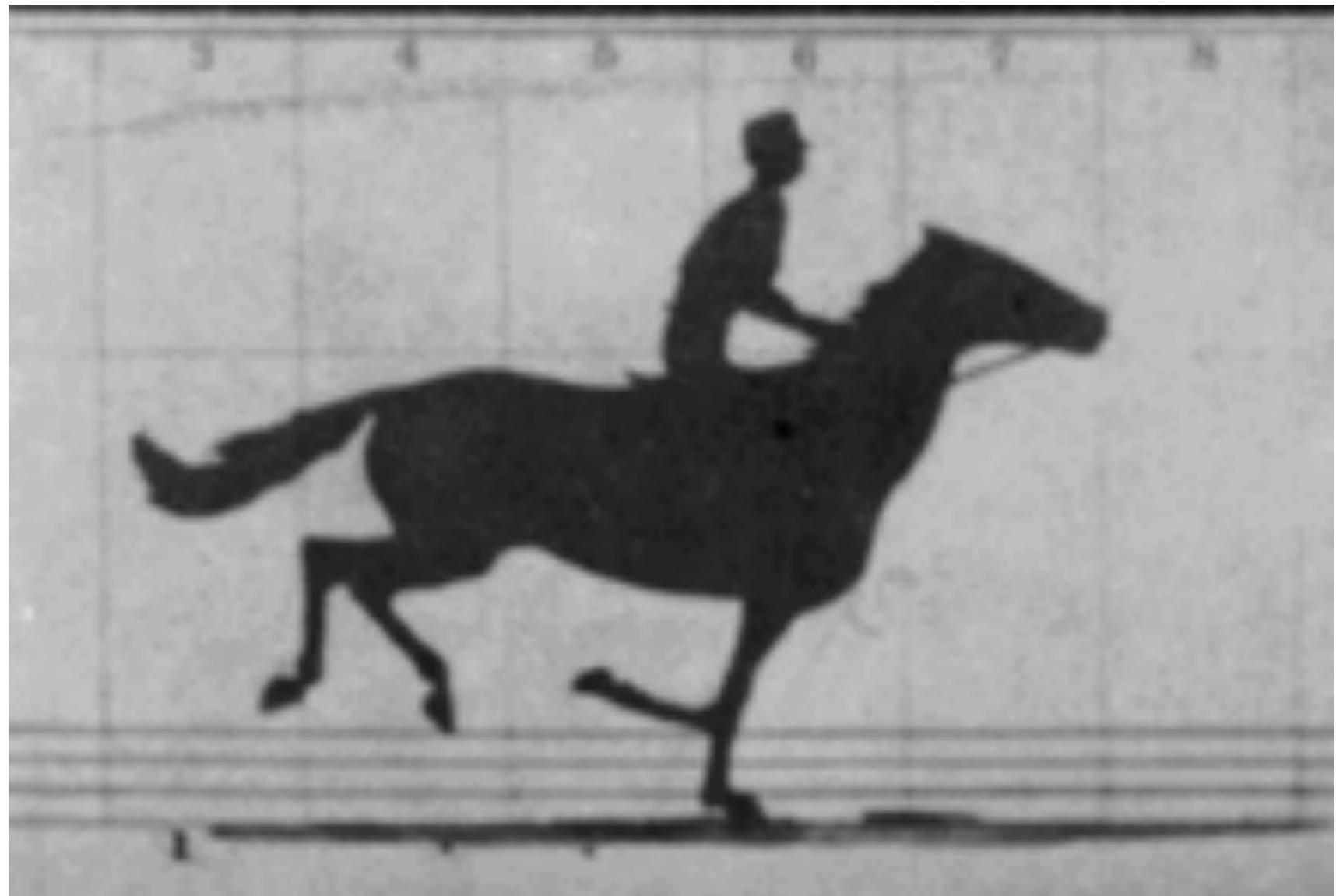


(Phenakistoscope, 1831)

# First Film

Originally used as scientific tool rather than for entertainment

Critical technology that accelerated development of animation



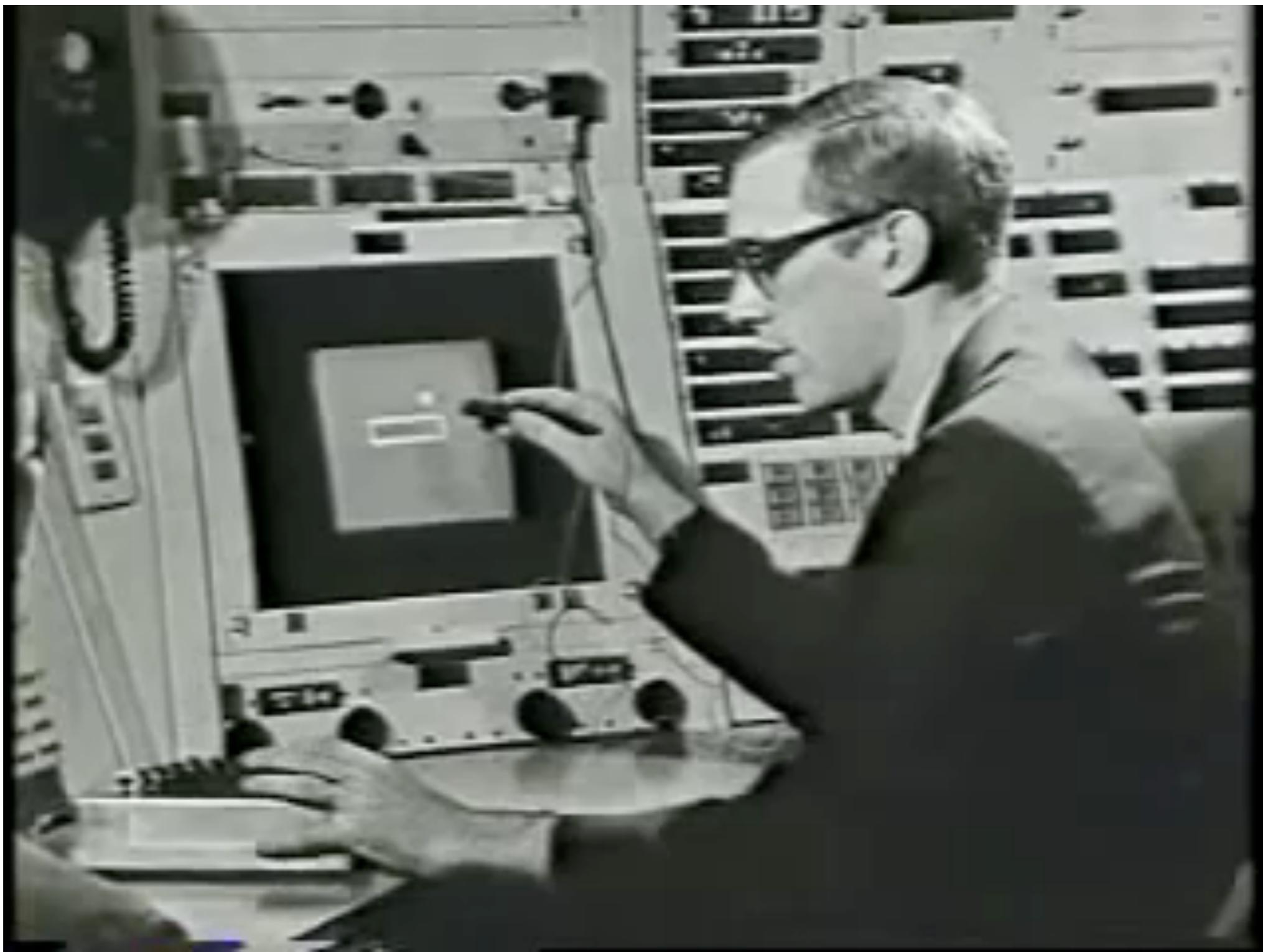
Edward Muybridge, "Sallie Gardner" (1878)

# First Hand-Drawn Feature-Length (>40 mins) Animation



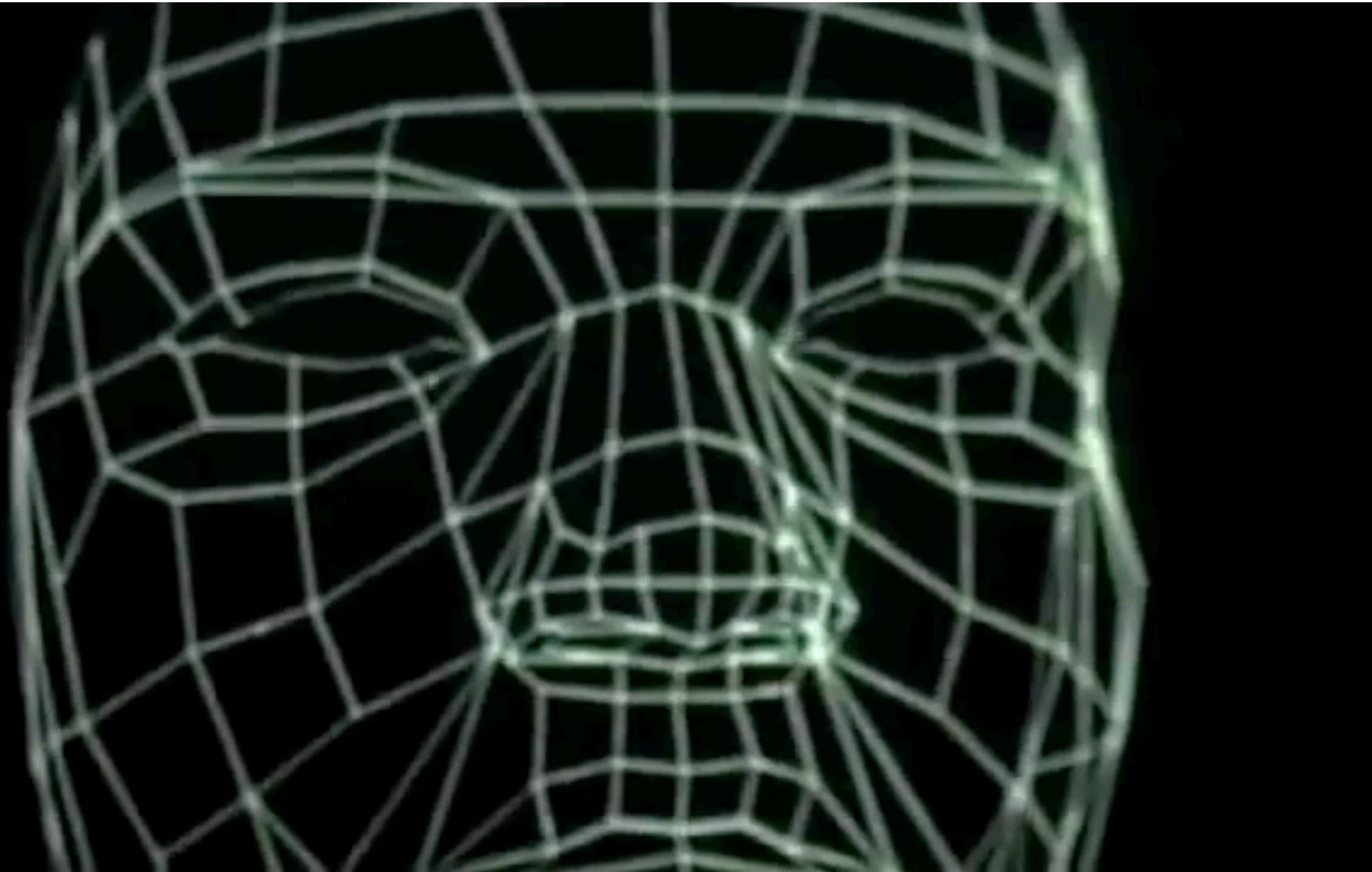
Disney, "Snow White and the Seven Dwarfs" (1937)

# First Digital-Computer-Generated Animation



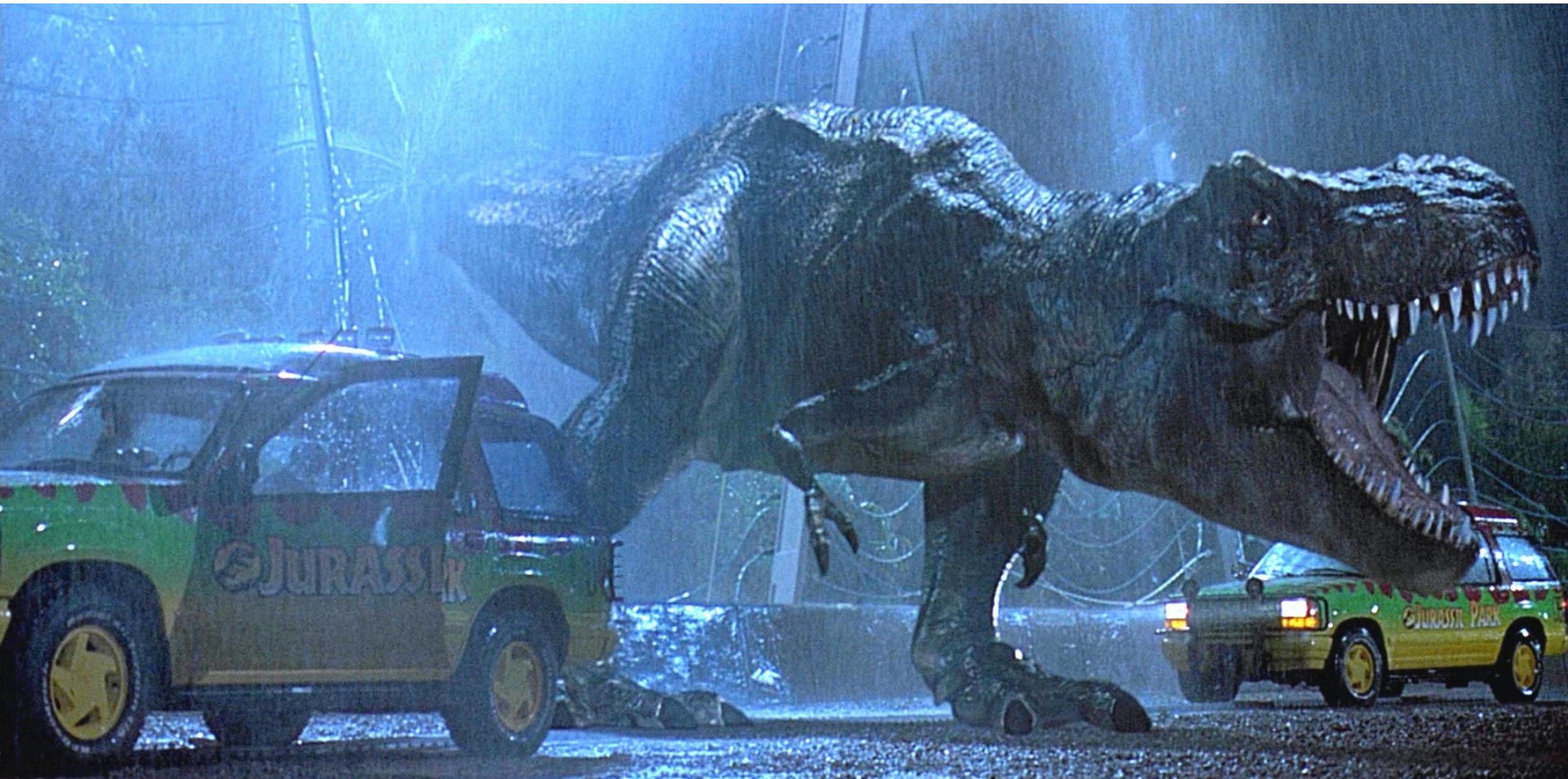
Ivan Sutherland, "Sketchpad" (1963) – Light pen, vector display

# Early Computer Animation



Ed Catmull & Frederick Parke, "Computer Animated Faces" (1972)

# Digital Dinosaurs!



Jurassic Park (1993)

# First CG Feature-Length Film



Pixar, "Toy Story" (1995)

# Computer Animation - 10 years ago



Sony Pictures Animation, "Cloudy With a Chance of Meatballs" (2009)

# Computer Animation - last year



Walt Disney Animation Studios, "Frozen 2" (2019)

# Keyframe Animation

# Keyframe Animation

**Keyframes**



**"Tweens"**

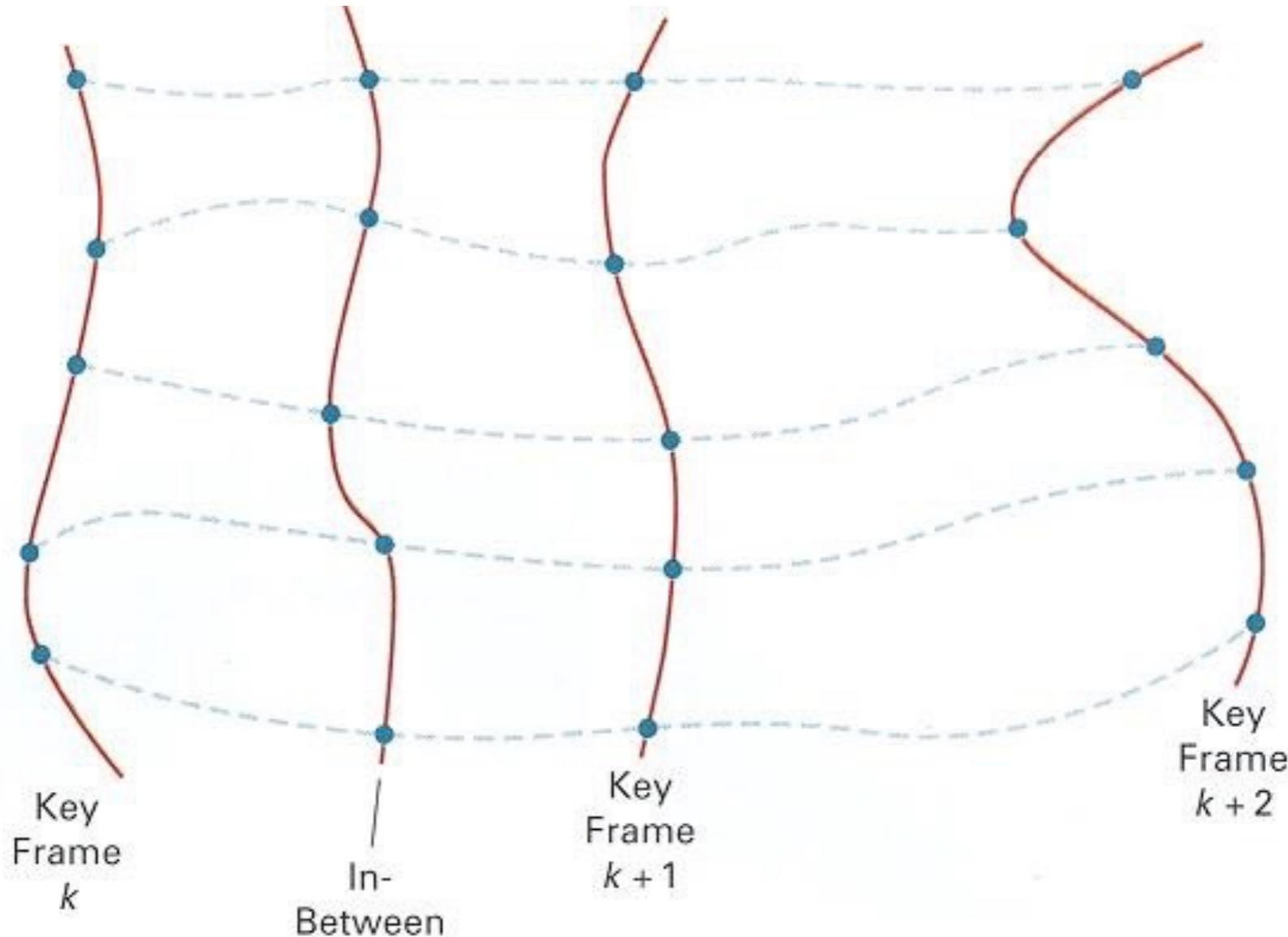


Animator (e.g. lead animator) creates keyframes

Assistant (person or computer) creates in-between frames ("tweening")

# Keyframe Interpolation

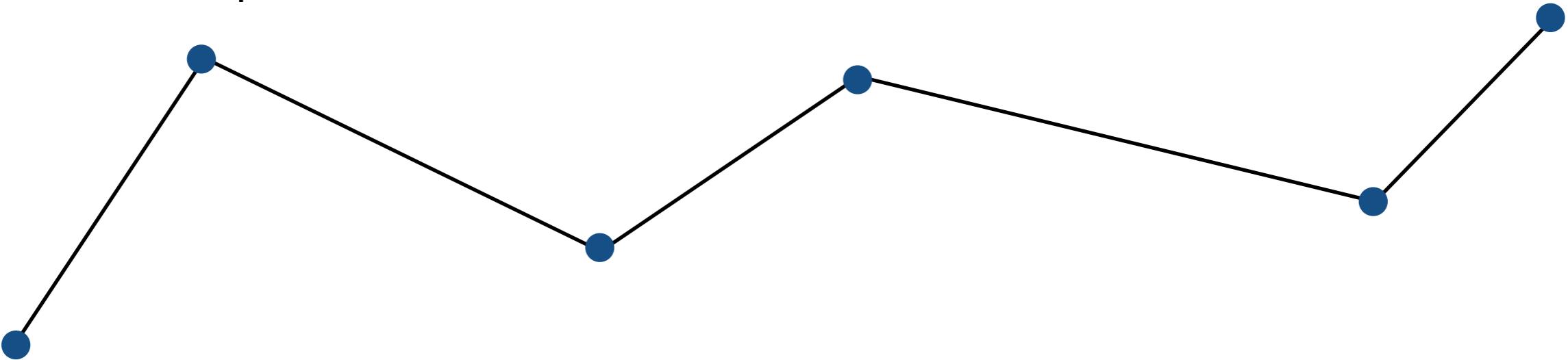
Think of each frame as a vector of parameter values



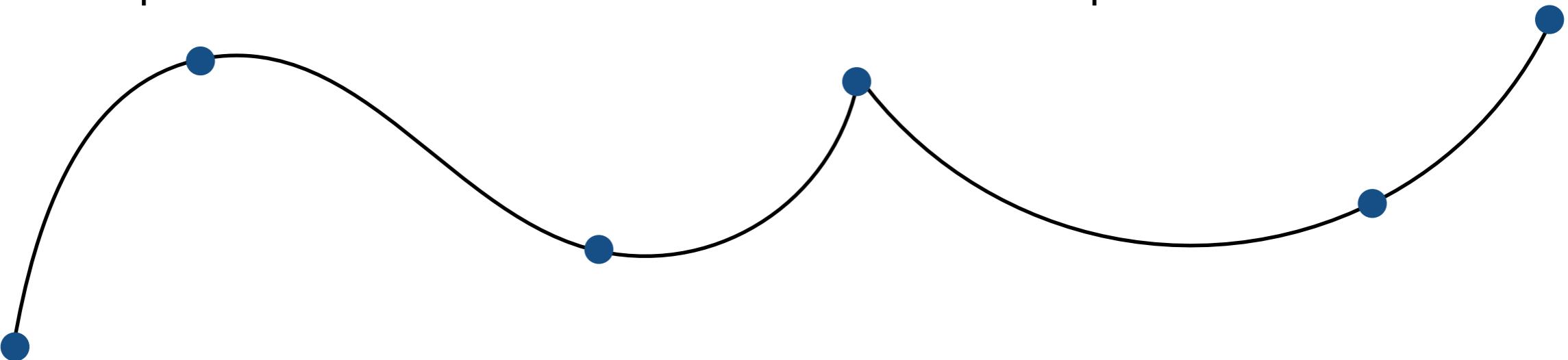
Hearn, Baker and Carithers, Figure 16.11

# Keyframe Interpolation of Each Parameter

Linear interpolation usually not good enough



Recall splines for smooth / controllable interpolation



# Physical Simulation

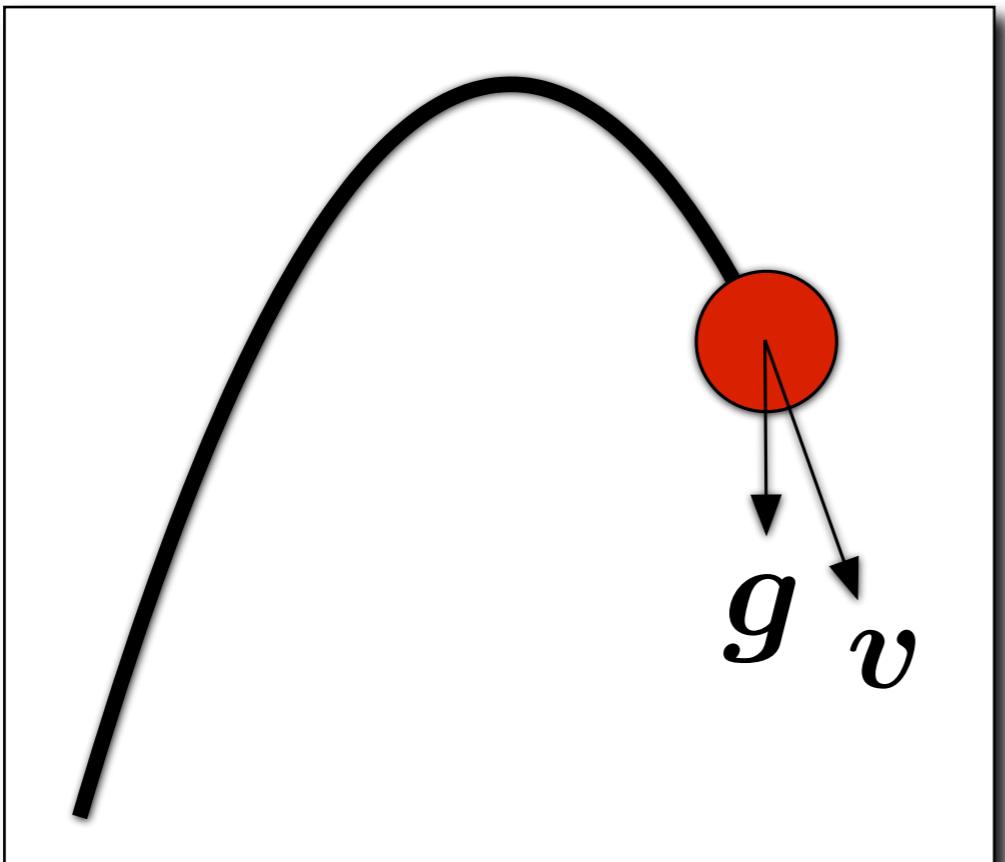
# Newton's Law

$$F = ma$$

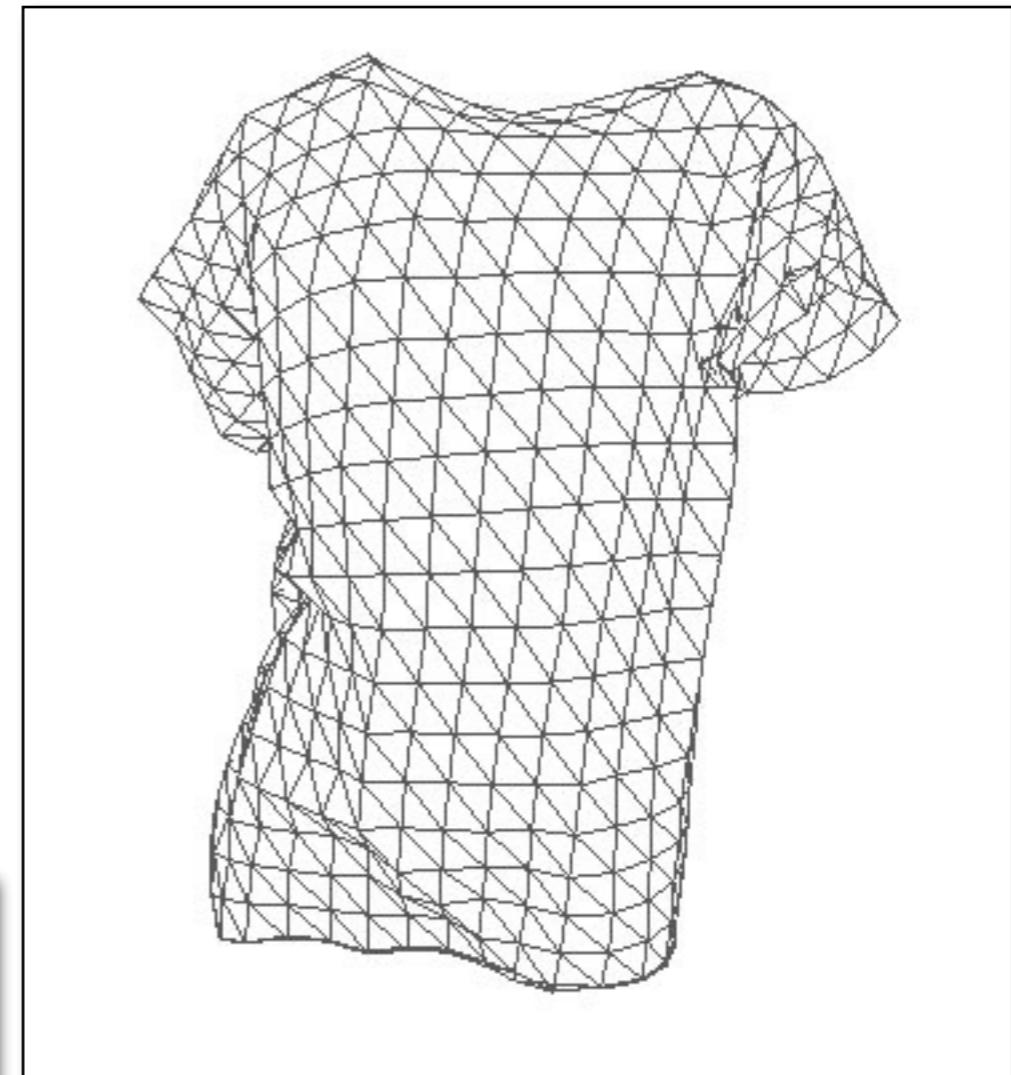
The diagram illustrates the components of Newton's second law of motion. The equation  $F = ma$  is centered. To the left of the equals sign, a vertical arrow points upwards from the word "Force" to the letter  $F$ . To the right of the equals sign, there are two vertical arrows pointing upwards: one from the word "Mass" to the letter  $m$ , and another from the word "Acceleration" to the letter  $a$ .

# Physically Based Animation

Generate motion of objects using numerical simulation



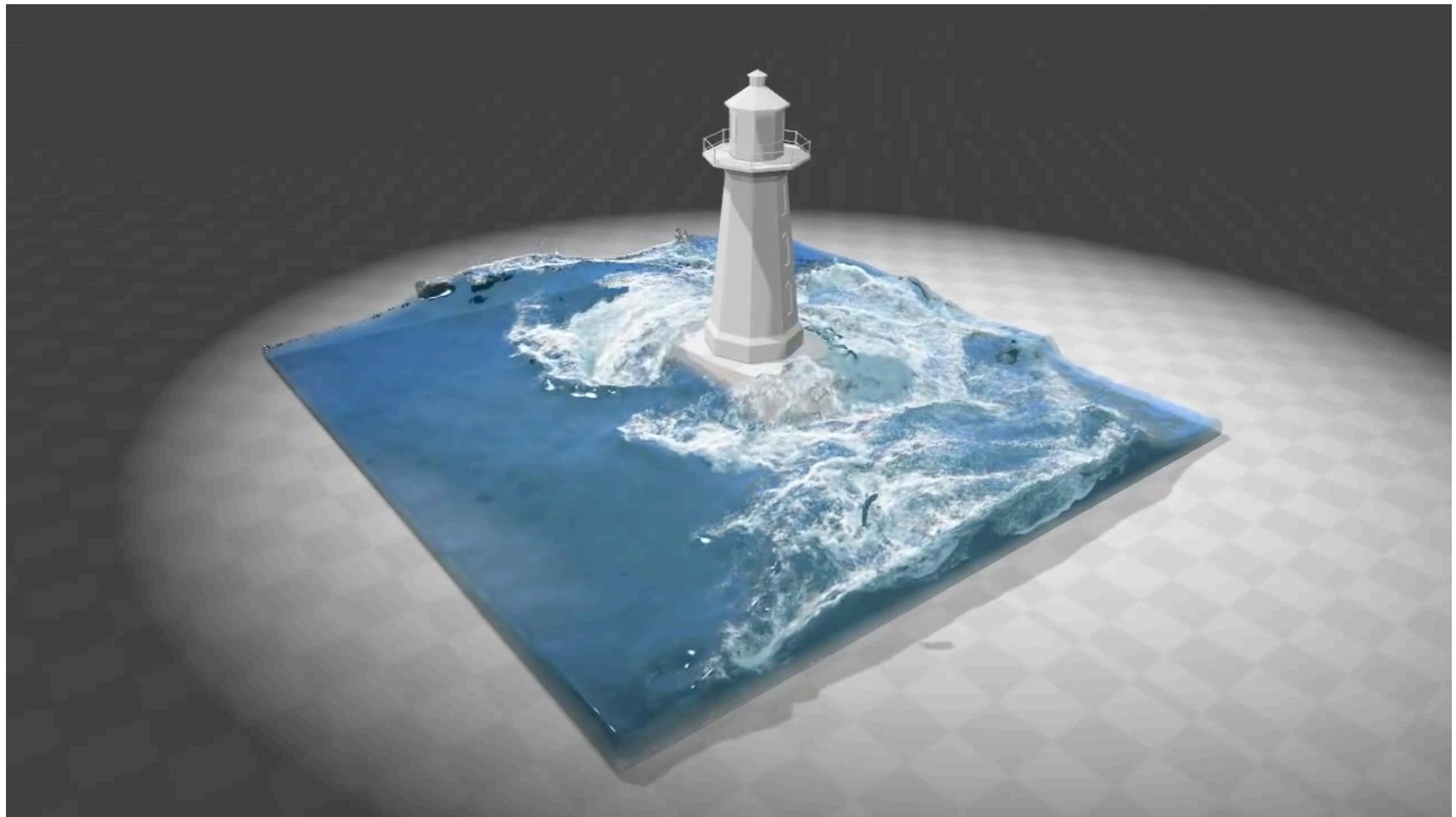
$$\mathbf{x}^{t+\Delta t} = \mathbf{x}^t + \Delta t \mathbf{v}^t + \frac{1}{2} (\Delta t)^2 \mathbf{a}^t$$



# Example: Cloth Simulation



# Example: Fluids



Macklin and Müller, Position Based Fluids

# Mass Spring System: Example of Modeling a Dynamic System

# Example: Mass Spring Rope

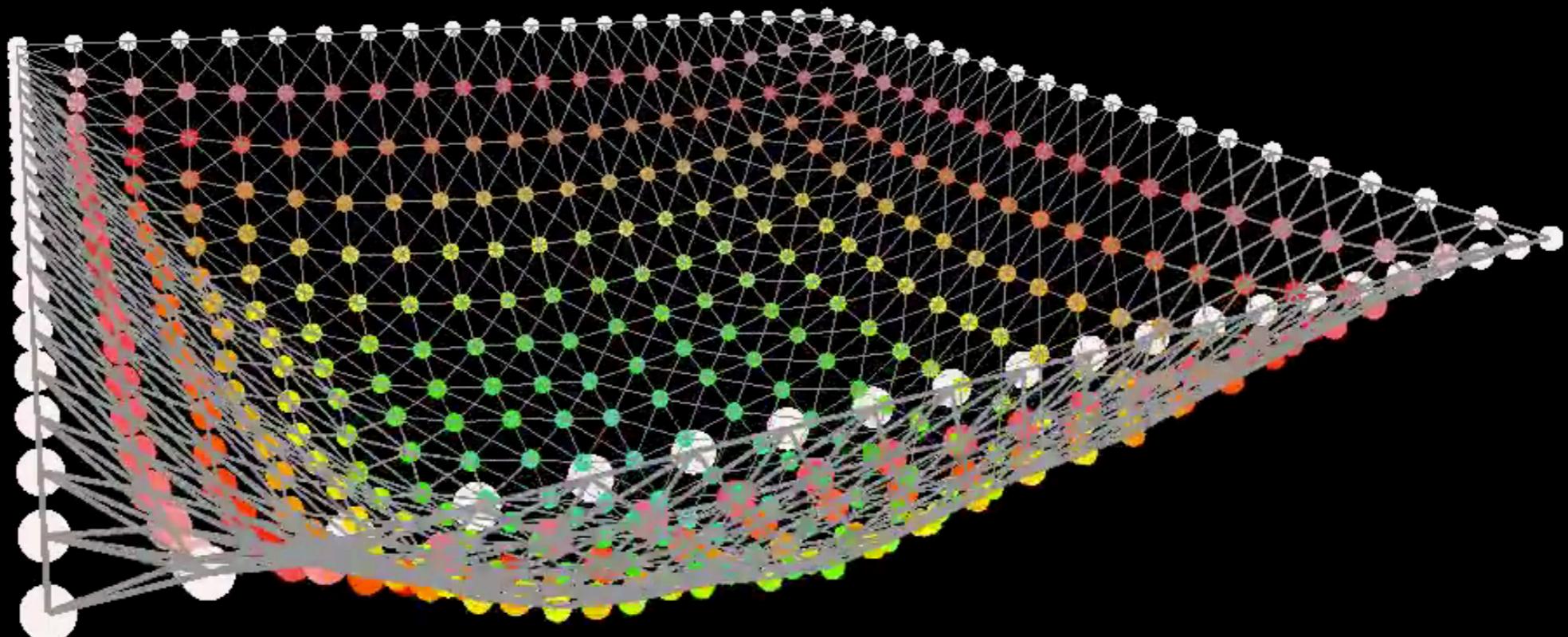


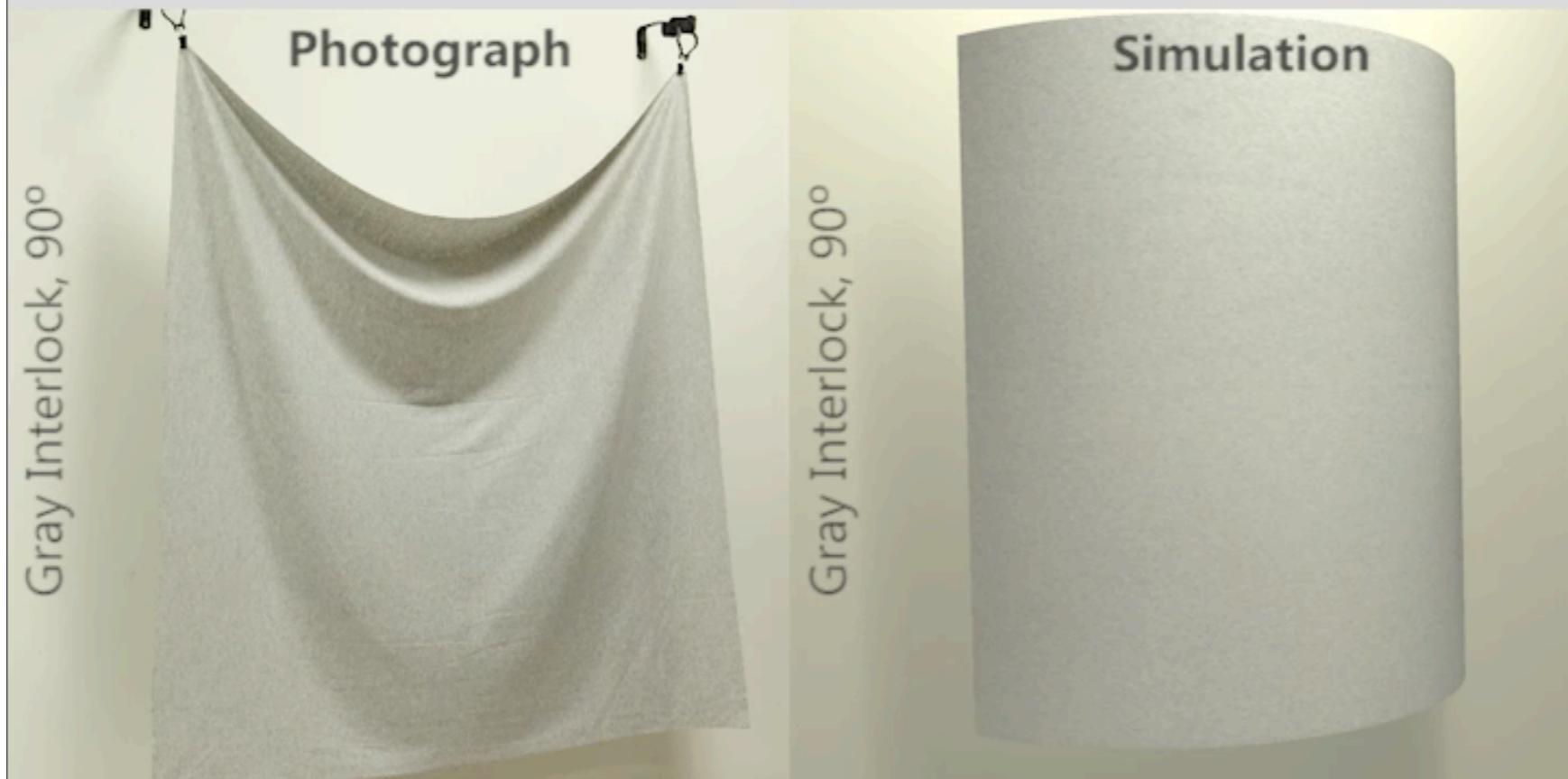
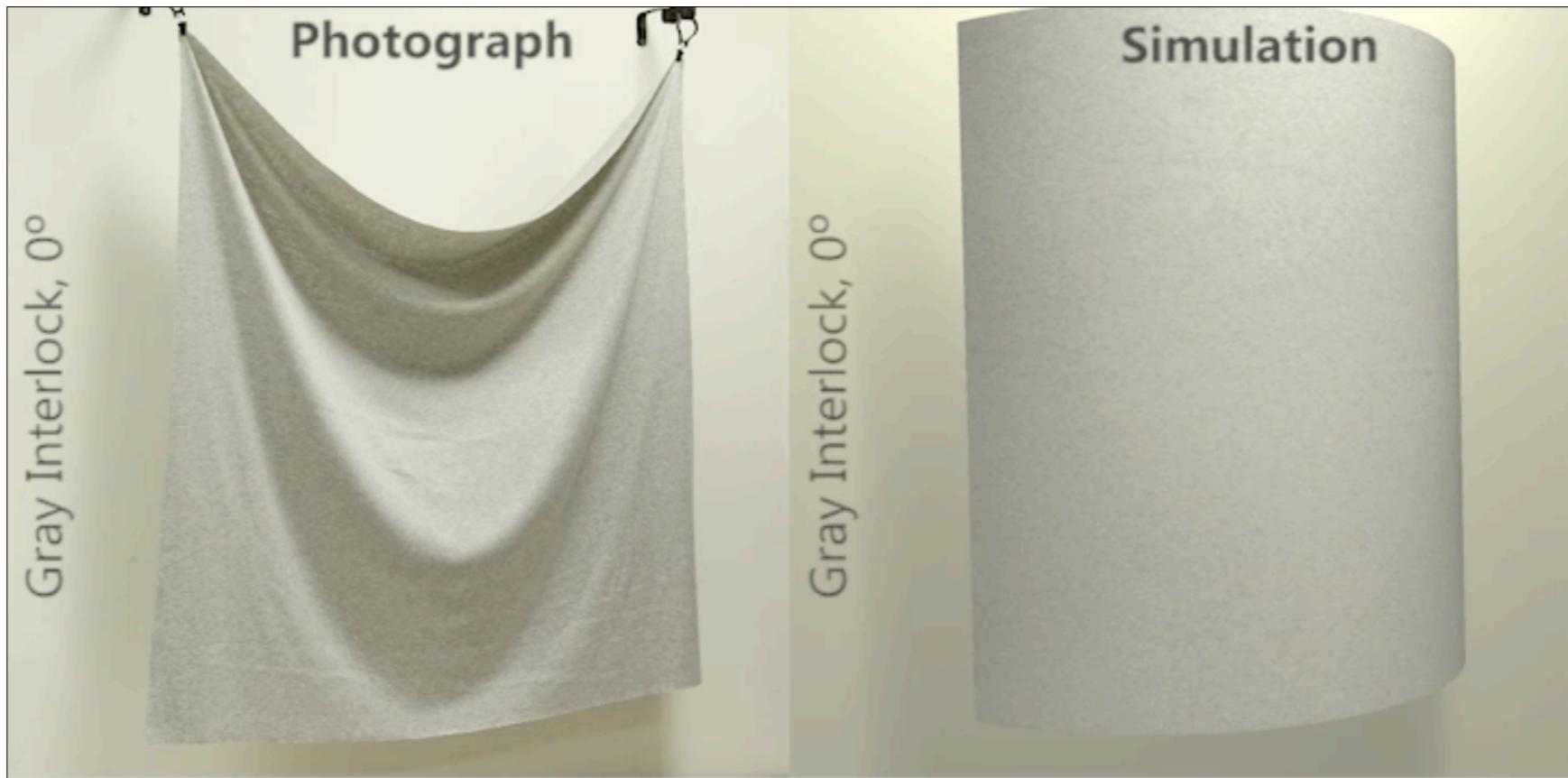
<https://youtu.be/Co8enp8CH34>

# Example: Hair



# Example: Mass Spring Mesh





Huamin Wang, Ravi Ramamoorthi, and James F. O'Brien. "Data-Driven Elastic Models for Cloth: Modeling and Measurement". *ACM Transactions on Graphics*, 30(4):71:1–11, July 2011. Proceedings of ACM SIGGRAPH 2011, Vancouver, BC Canada.

# A Simple Spring

Idealized spring



$$f_{a \rightarrow b} = k_s(b - a)$$

$$f_{b \rightarrow a} = -f_{a \rightarrow b}$$

Force pulls points together

Strength proportional to displacement (Hooke's Law)

$k_s$  is a spring coefficient: stiffness

Problem: this spring wants to have zero length

# Non-Zero Length Spring

Spring with non-zero rest length



$$f_{a \rightarrow b} = k_s \frac{b - a}{\|b - a\|} (\|b - a\| - l)$$

Rest length

Problem: oscillates forever

# Dot Notation for Derivatives

If  $\mathbf{x}$  is a vector for the position of a point of interest, we will use dot notation for velocity and acceleration:

$$\mathbf{x}$$

$$\dot{\mathbf{x}} = \mathbf{v}$$

$$\ddot{\mathbf{x}} = \mathbf{a}$$

# Introducing Energy Loss

Simple motion damping

$$\frac{f}{\dot{b}} \quad f = -k_d \dot{b}$$

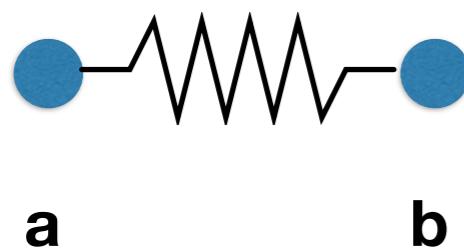
- Behaves like viscous drag on motion
- Slows down motion in the direction of velocity
- $k_d$  is a damping coefficient

Problem: slows down *all* motion

- Want a rusty spring's oscillations to slow down, but should it also fall to the ground more slowly?

# Internal Damping for Spring

Damp only the internal, spring-driven motion



a                  b

$$f_b = -k_d \frac{b - a}{\|b - a\|} (\dot{b} - \dot{a}) \cdot \frac{b - a}{\|b - a\|}$$

Relative velocity of b,  
assuming a is static (vector)

Damping force  
applied on b

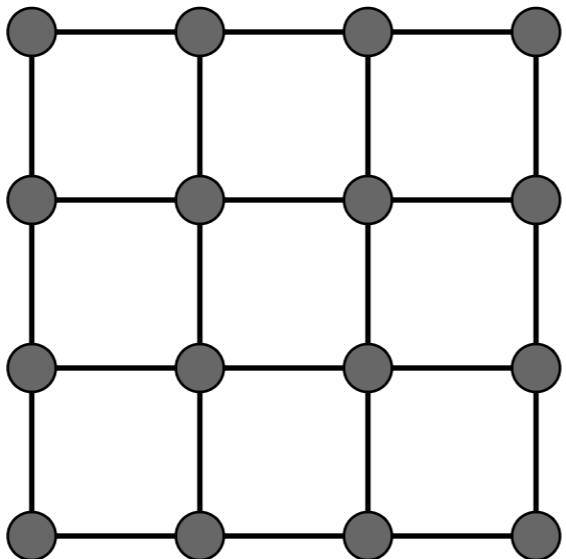
Direction from  
a to b

**Relative velocity projected to  
the direction from a to b (scalar)**

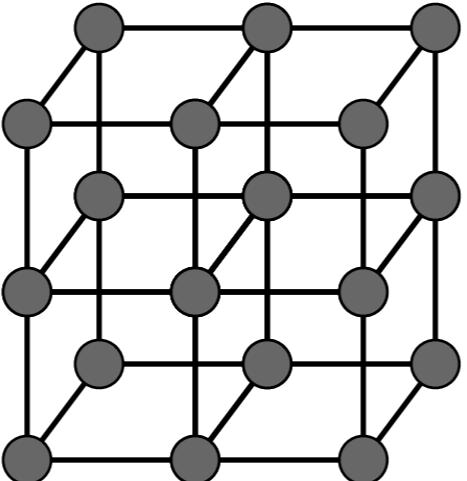
- Viscous drag only on change in spring length
  - Won't slow group motion for the spring system (e.g. global translation or rotation of the group)
- Note: This is only one specific type of damping

# Structures from Springs

Sheets



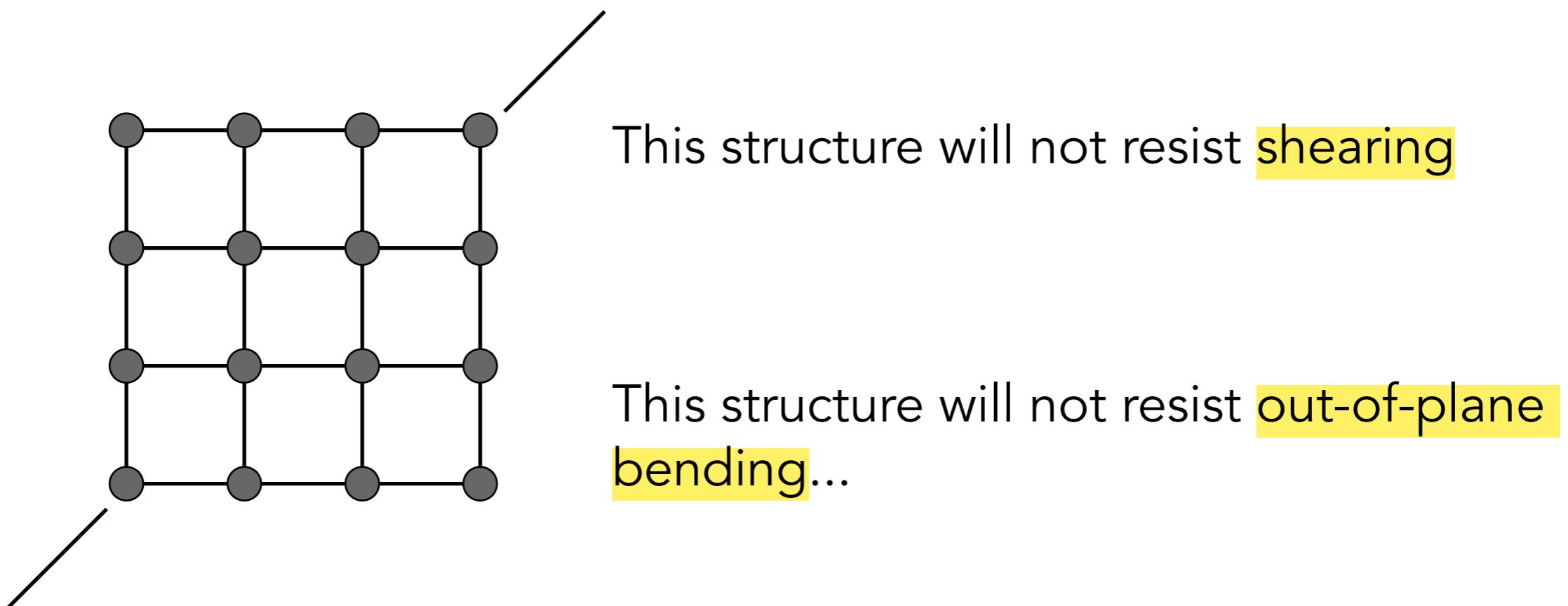
Blocks



Others

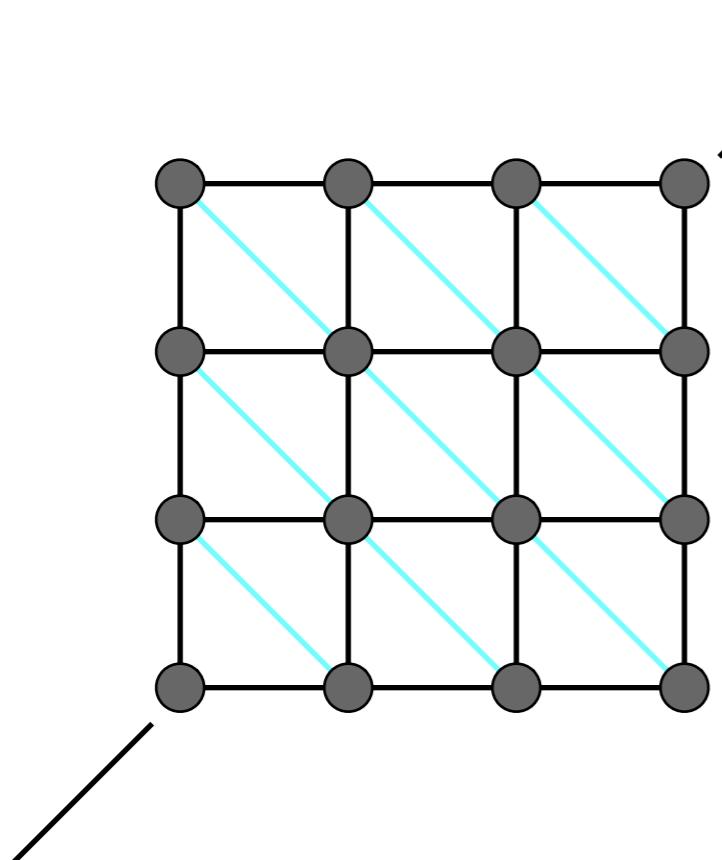
# Structures from Springs

Behavior is determined by structure linkages



# Structures from Springs

# Behavior is determined by structure linkages

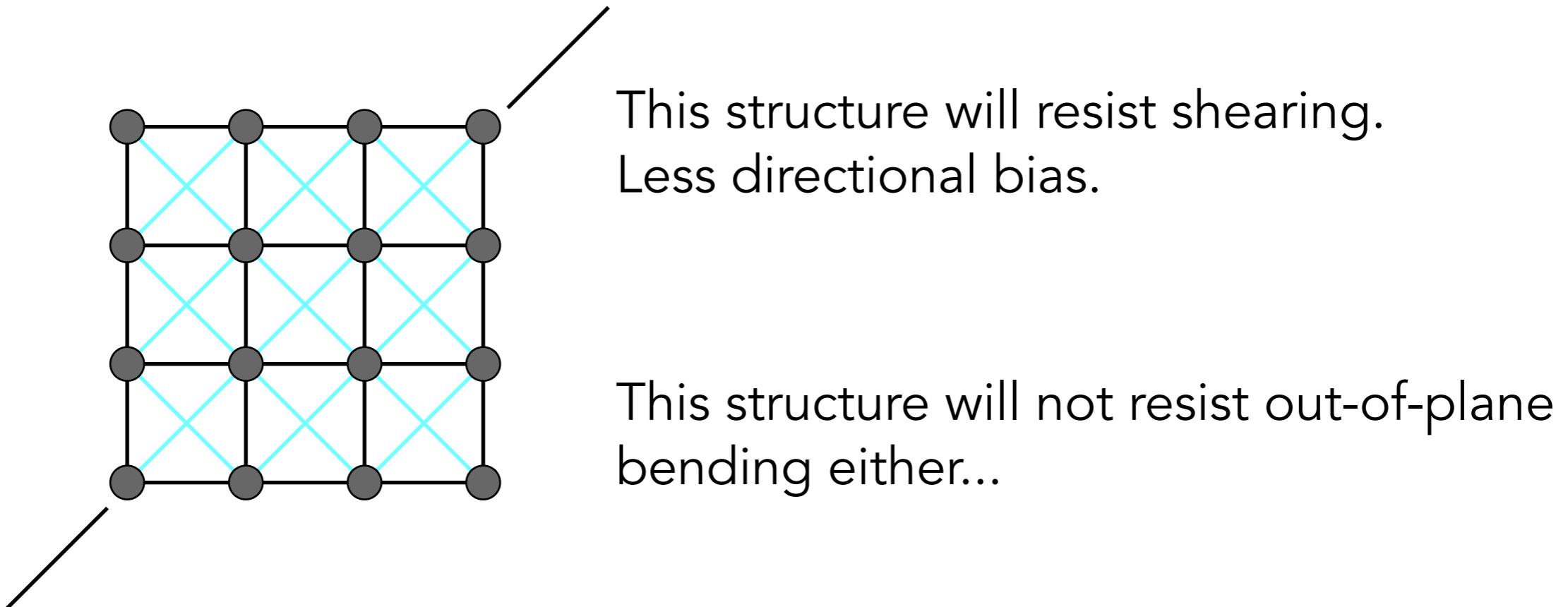


This structure will resist shearing  
but has anisotropic bias

This structure will not resist out-of-plane bending either...

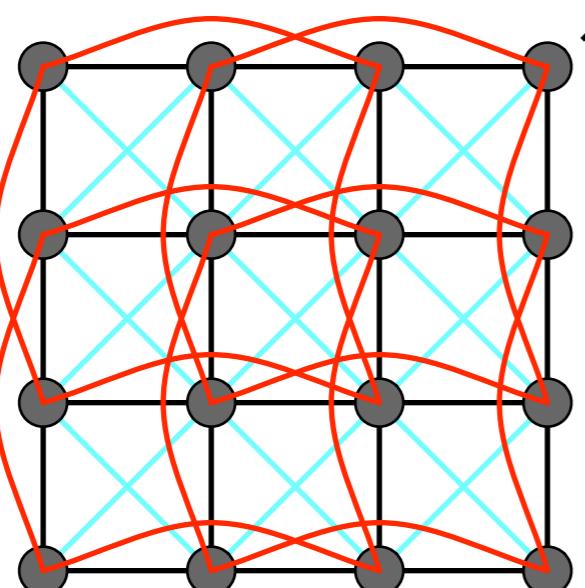
# Structures from Springs

Behavior is determined by structure linkages



# Structures from Springs

They behave like what they are (obviously!)



This structure will resist shearing.  
Less directional bias.

This structure will resist out-of-plane bending  
Red springs should be much weaker

# Example: Mass Spring Dress + Character



Aside: FEM (Finite Element Method) Instead of Springs



# Particle Systems

# Particle Systems

Model dynamical systems as collections of large numbers of particles

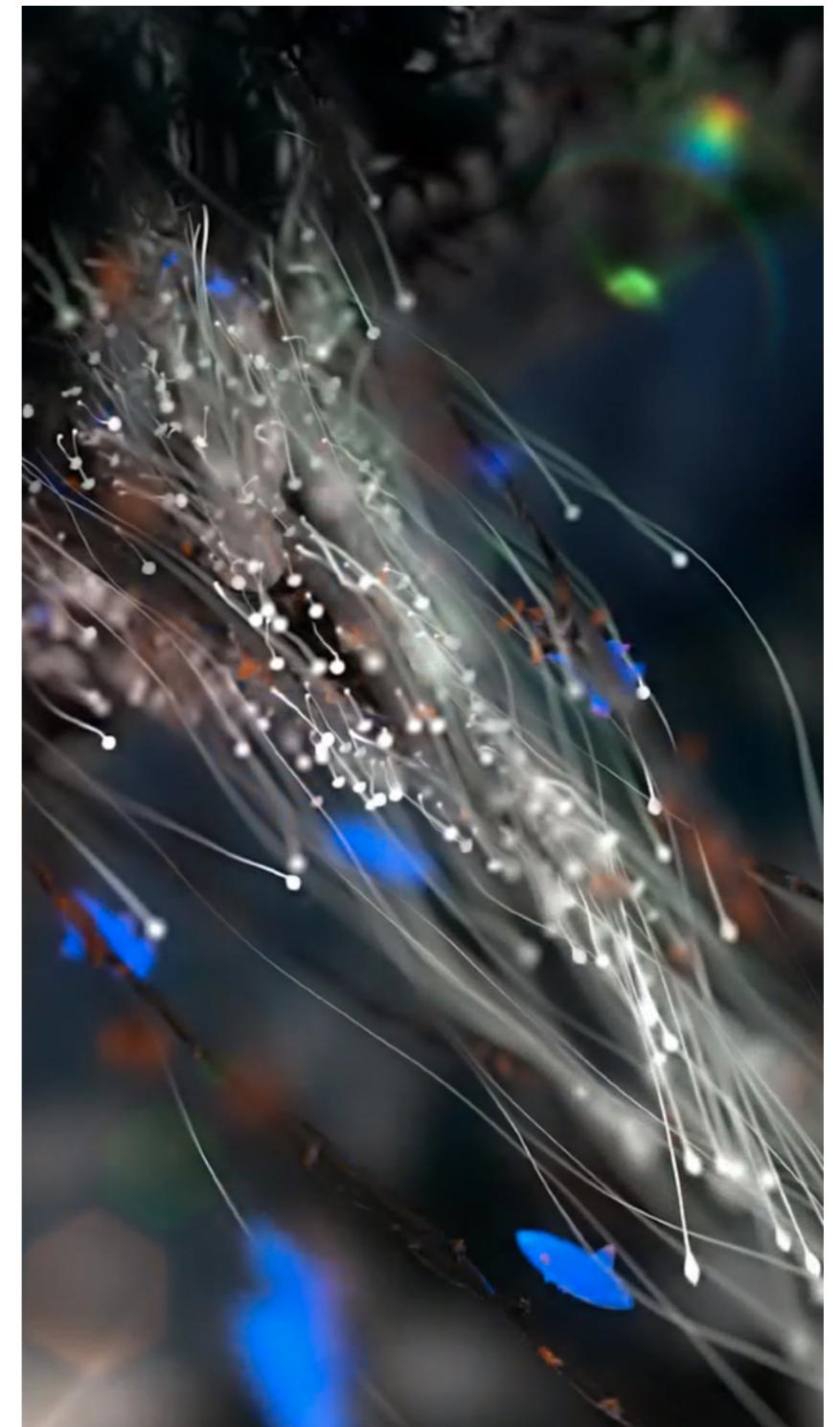
Each particle's motion is defined by a set of physical (or non-physical) forces

Popular technique in graphics and games

- Easy to understand, implement
- Scalable: fewer particles for speed, more for higher complexity

Challenges

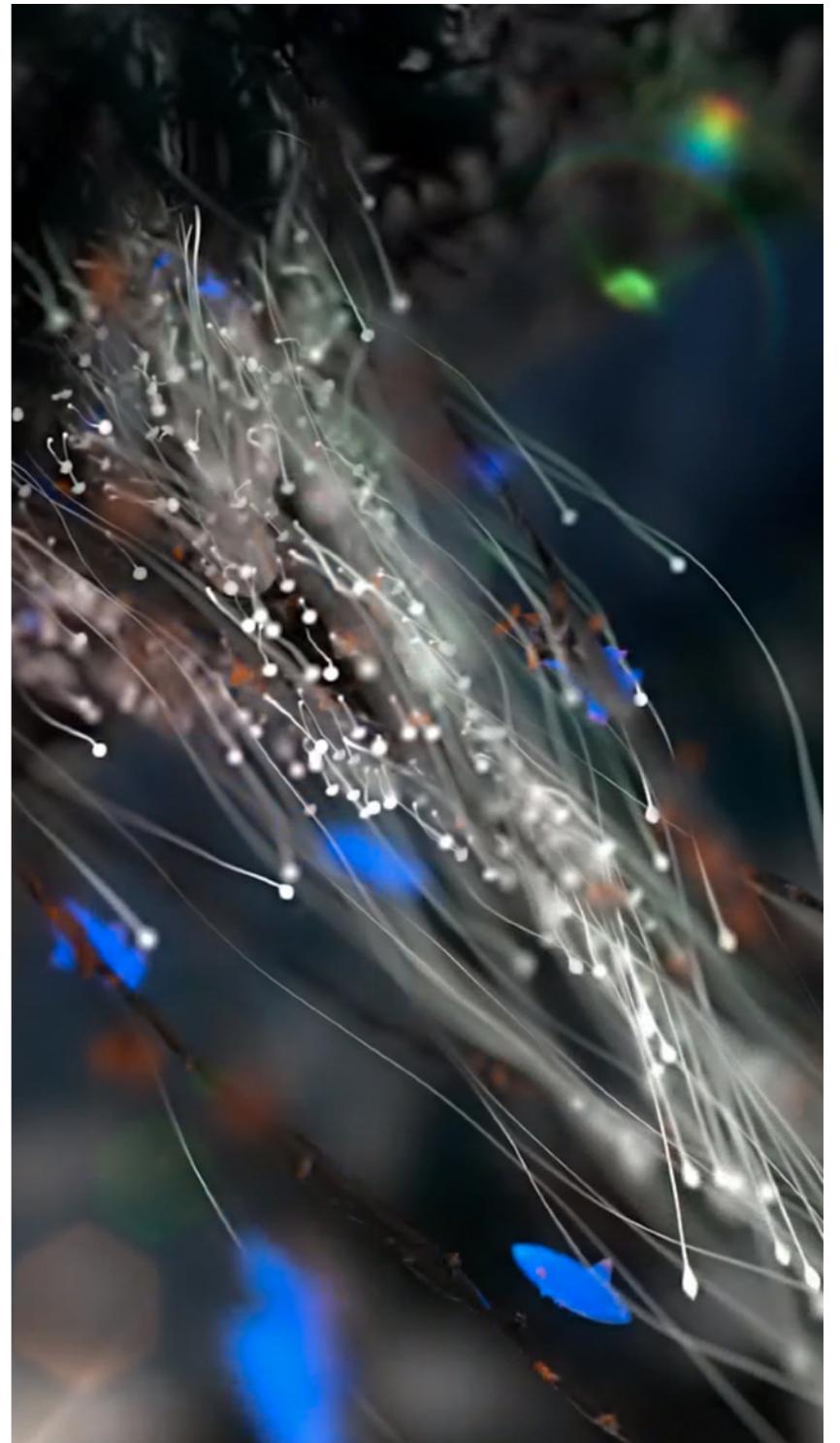
- May need many particles (e.g. fluids)
- May need acceleration structures (e.g. to find nearest particles for interactions)



# Particle System Animations

For each frame in animation

- [If needed] Create new particles
- Calculate forces on each particle
- Update each particle's position and velocity
- [If needed] Remove dead particles
- Render particles



# Particle System Forces

Attraction and repulsion forces

- Gravity, electromagnetism, ...
- Springs, propulsion, ...

Damping forces

- Friction, air drag, viscosity, ...

Collisions

- Walls, containers, fixed objects, ...
- Dynamic objects, character body parts, ...

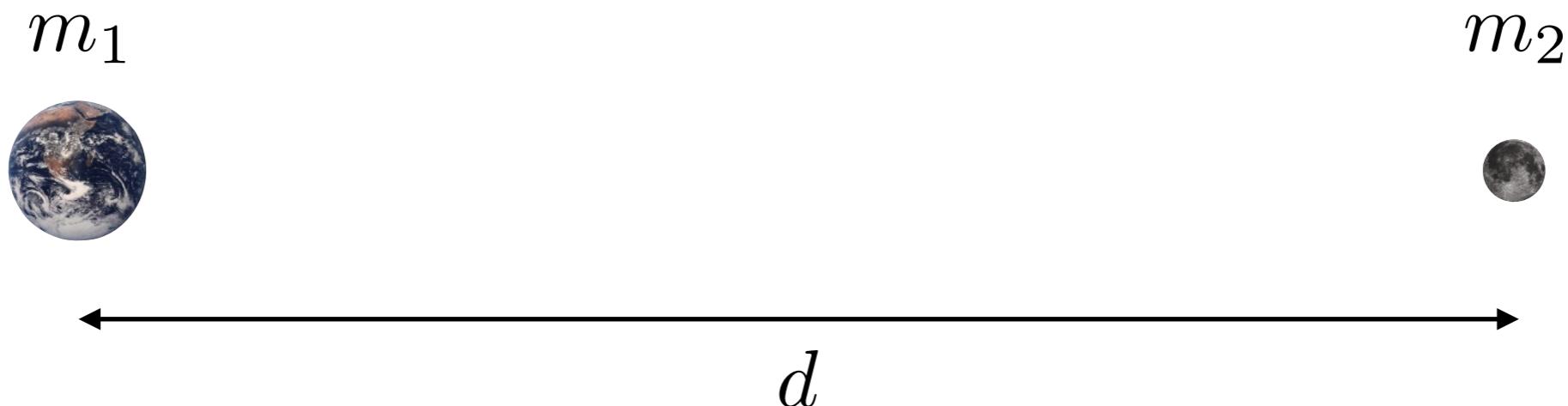
# Gravitational Attraction

Newton's universal law of gravitation

- Gravitational pull between particles

$$F_g = G \frac{m_1 m_2}{d^2}$$

$$G = 6.67428 \times 10^{-11} \text{ Nm}^2\text{kg}^{-2}$$

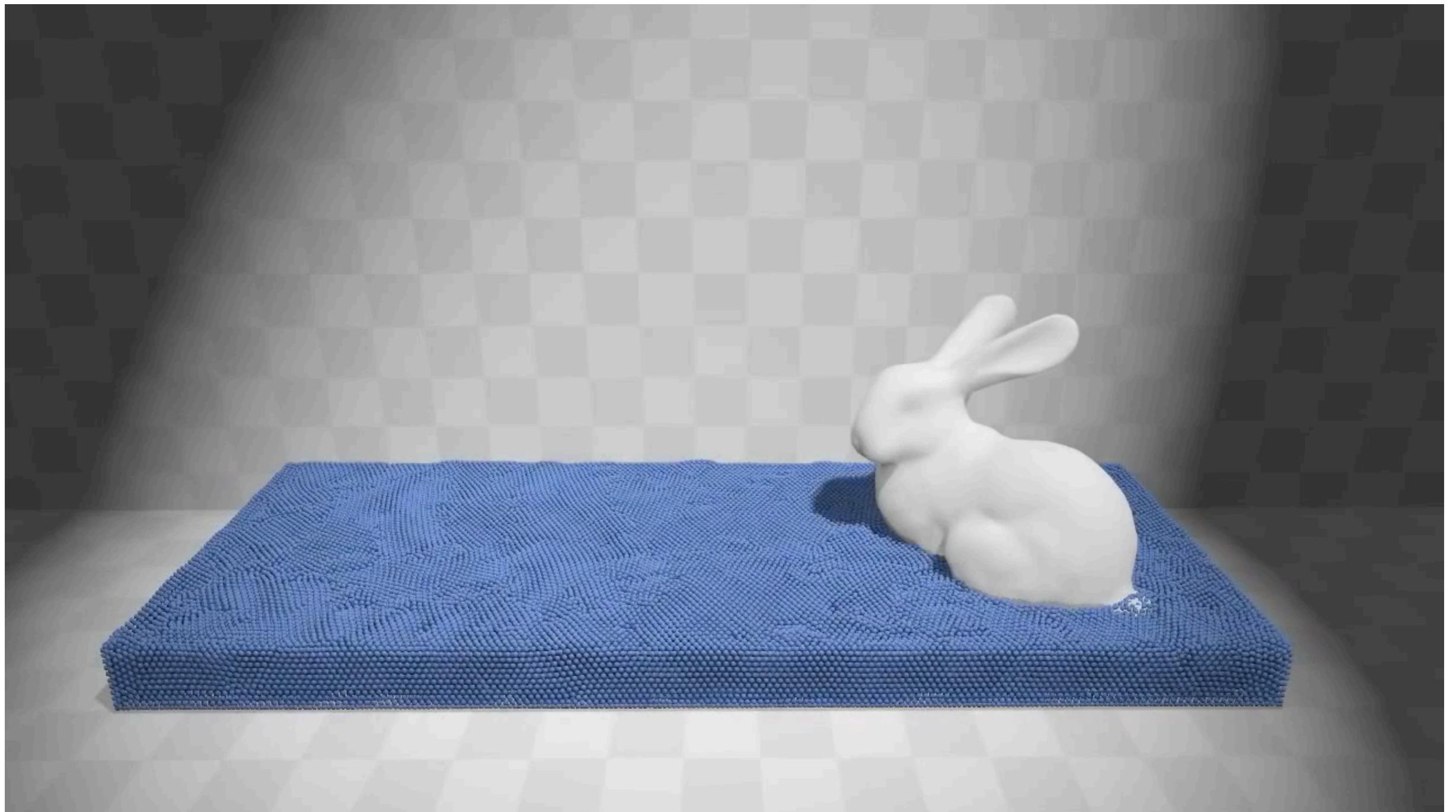


# Example: Galaxy Simulation



Disk galaxy simulation, NASA Goddard

# Example: Particle-Based Fluids



Macklin and Müller, Position Based Fluids

# Simulated Flocking as an ODE

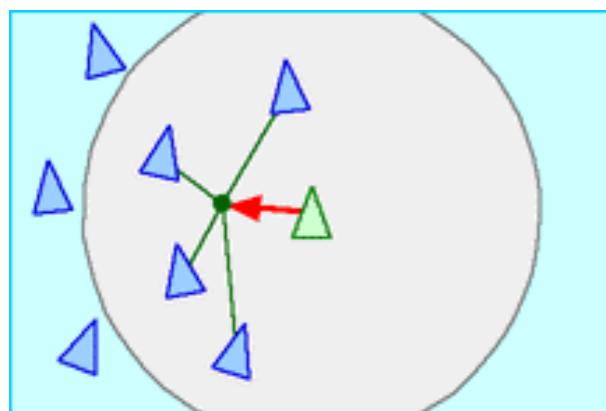
Model each bird as a particle

Subject to very simple forces:

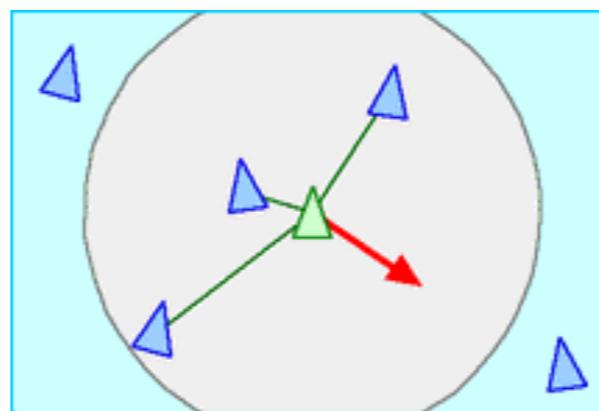
- attraction to center of neighbors
- repulsion from individual neighbors
- alignment toward average trajectory of neighbors

Simulate evolution of large particle system numerically

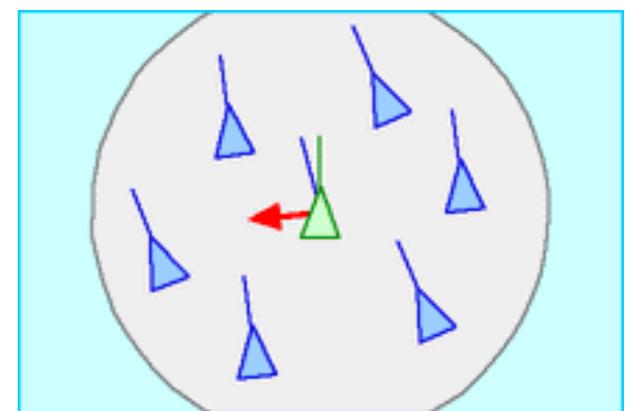
Emergent complex behavior (also seen in fish, bees, ...)



**attraction**



**repulsion**

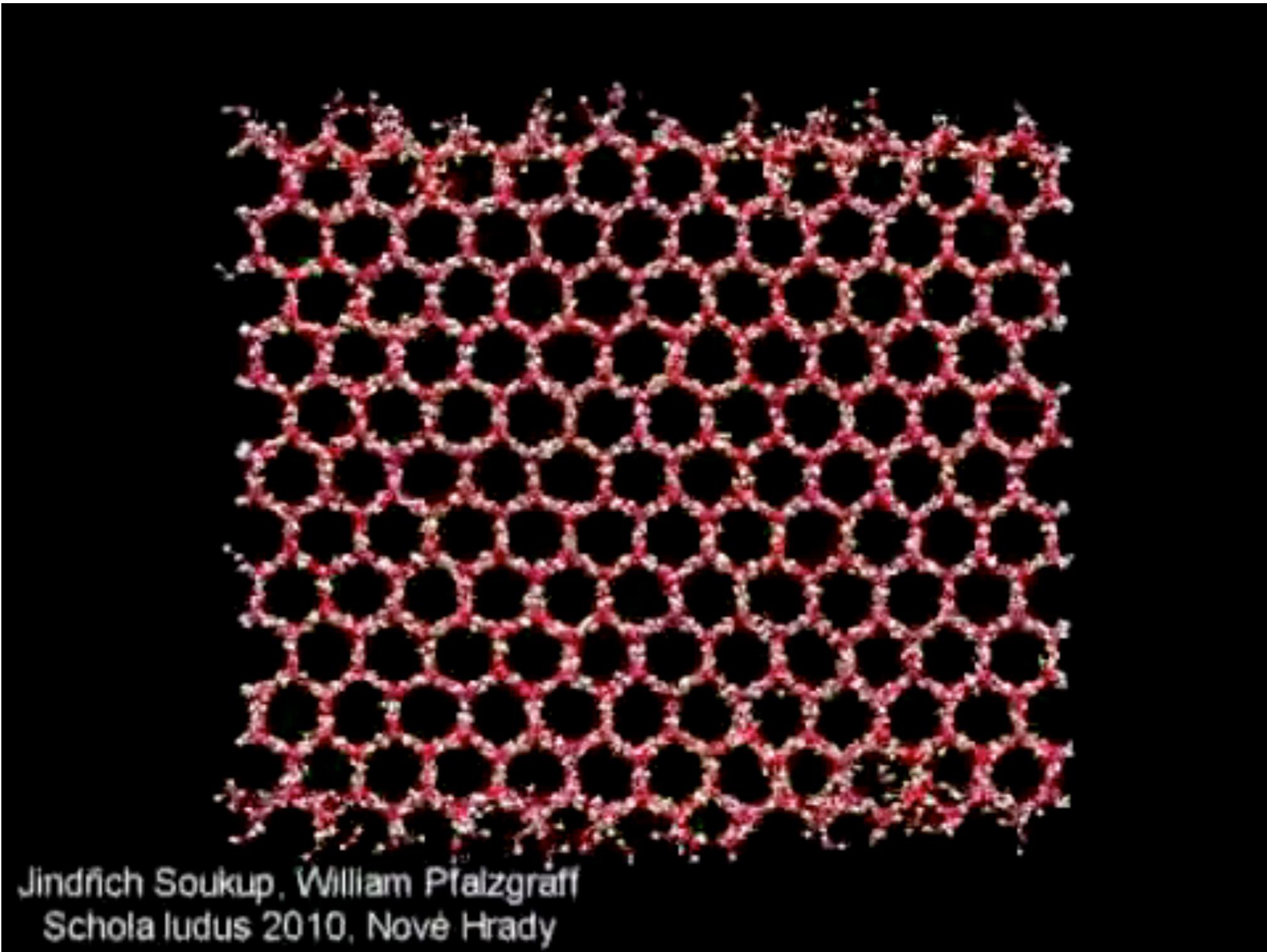


**alignment**

Credit: Craig Reynolds (see <http://www.red3d.com/cwr/boids/>)

Slide credit: Keenan Crane

# Example: Molecular Dynamics



(model of melting ice crystal)

# Example: Crowds + “Rock” Dynamics



# Forward Kinematics

(Slides by Prof. James O'Brien)

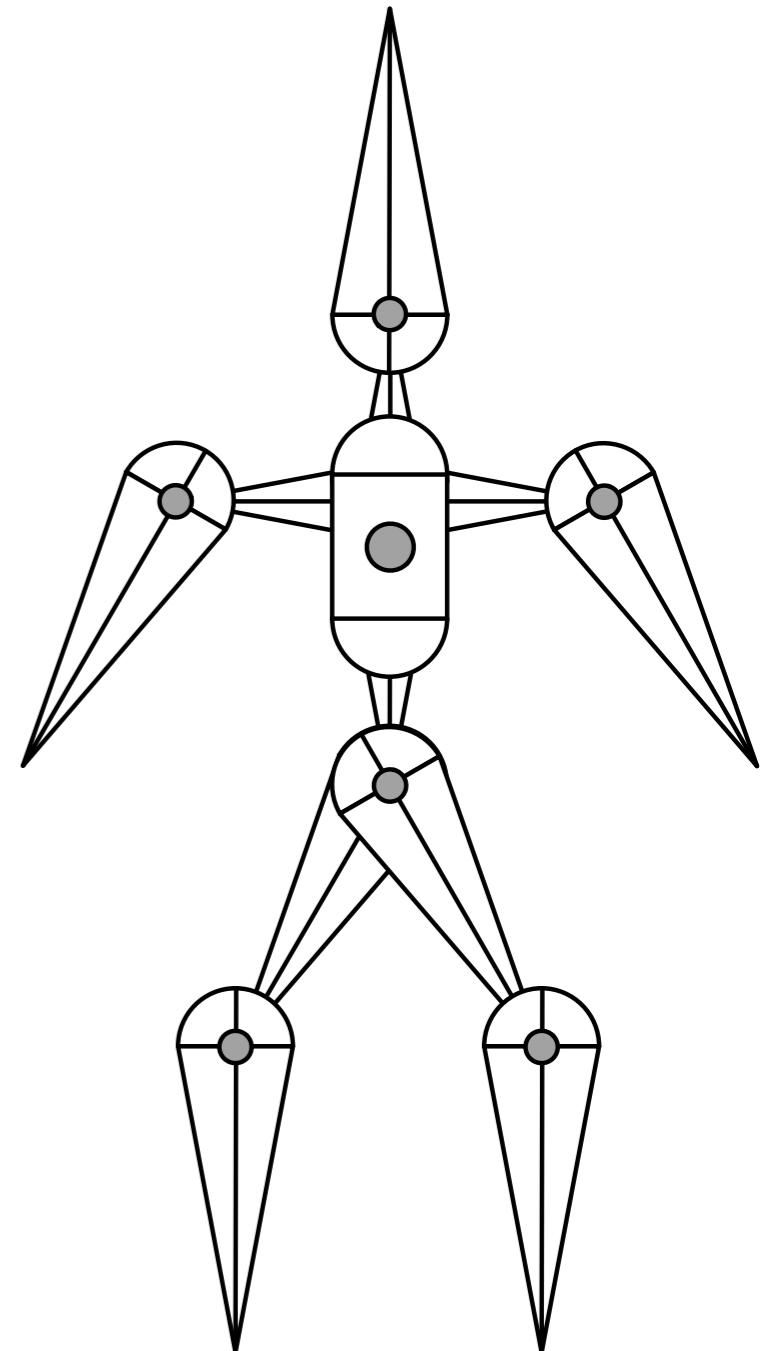
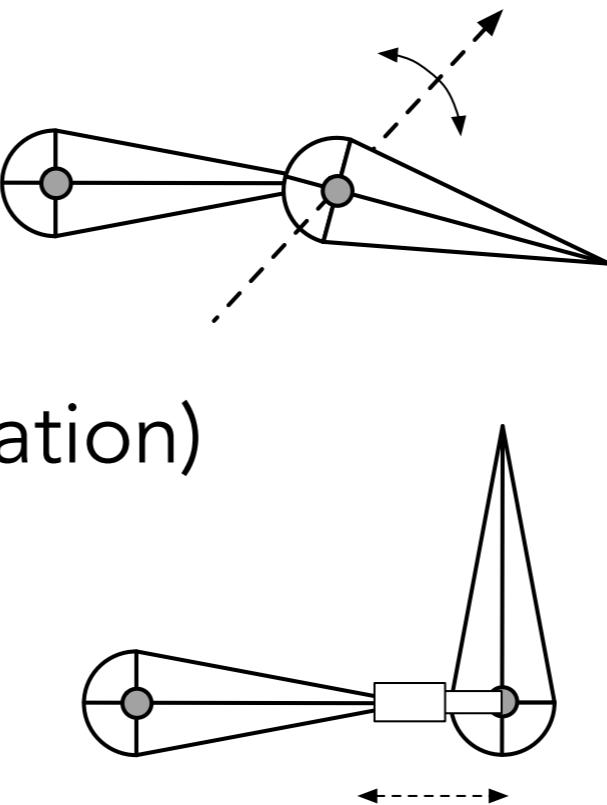
# Forward Kinematics

## Articulated skeleton

- Topology (what's connected to what)
- Geometric relations from joints
- Tree structure (in absence of loops)

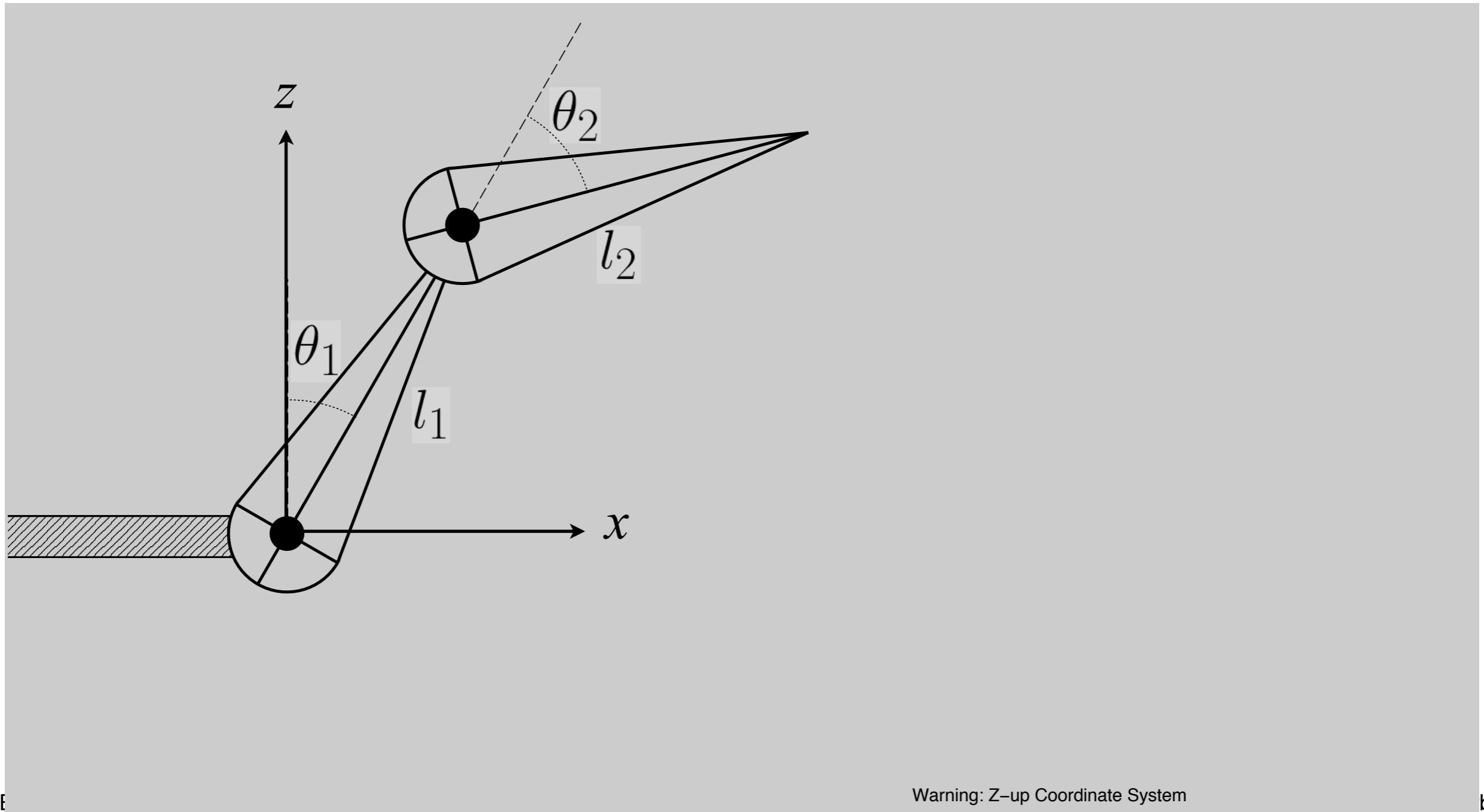
## Joint types

- Pin (1D rotation)
- Ball (2D rotation)
- Prismatic joint (translation)



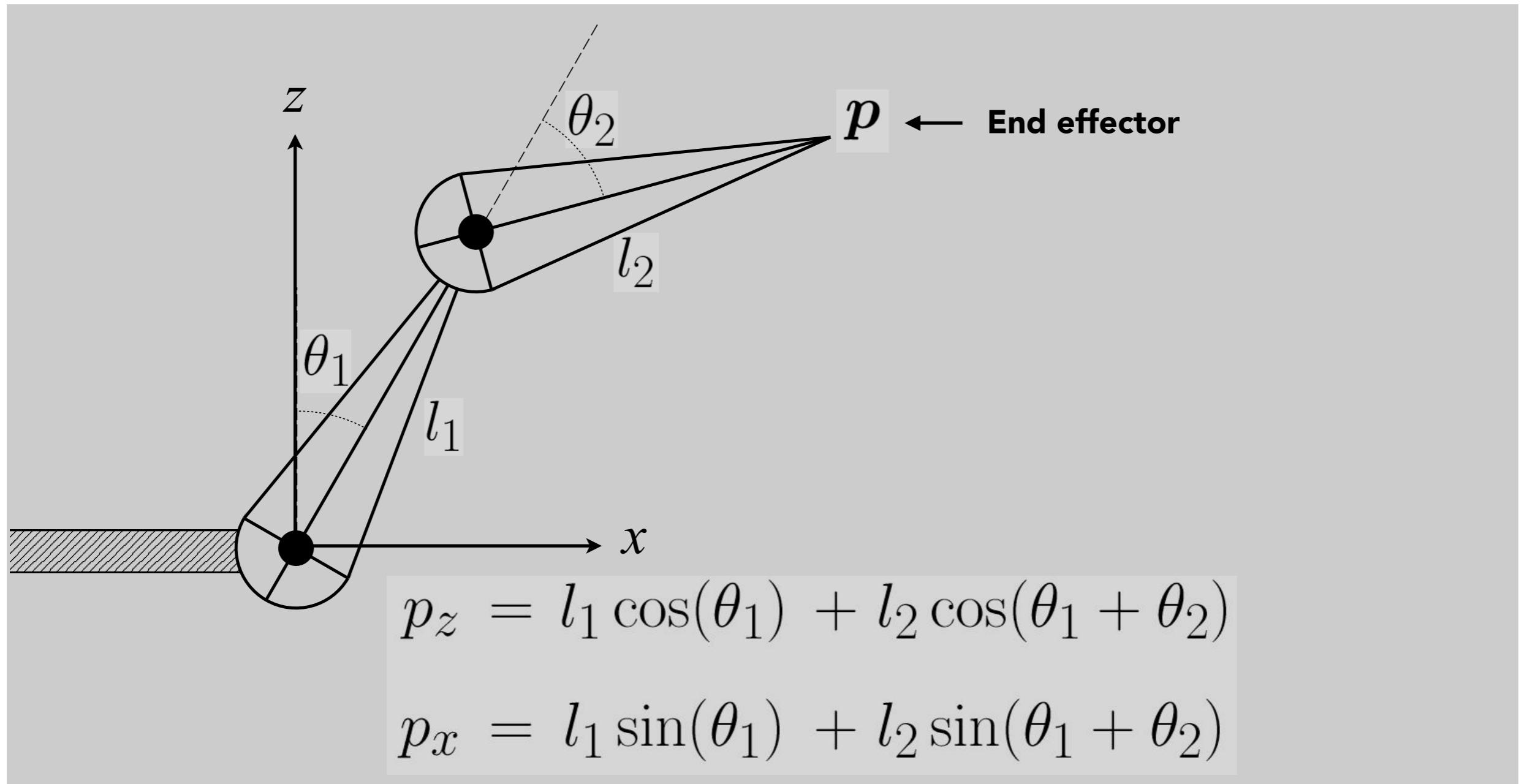
# Forward Kinematics

Example: simple two segment arm in 2D



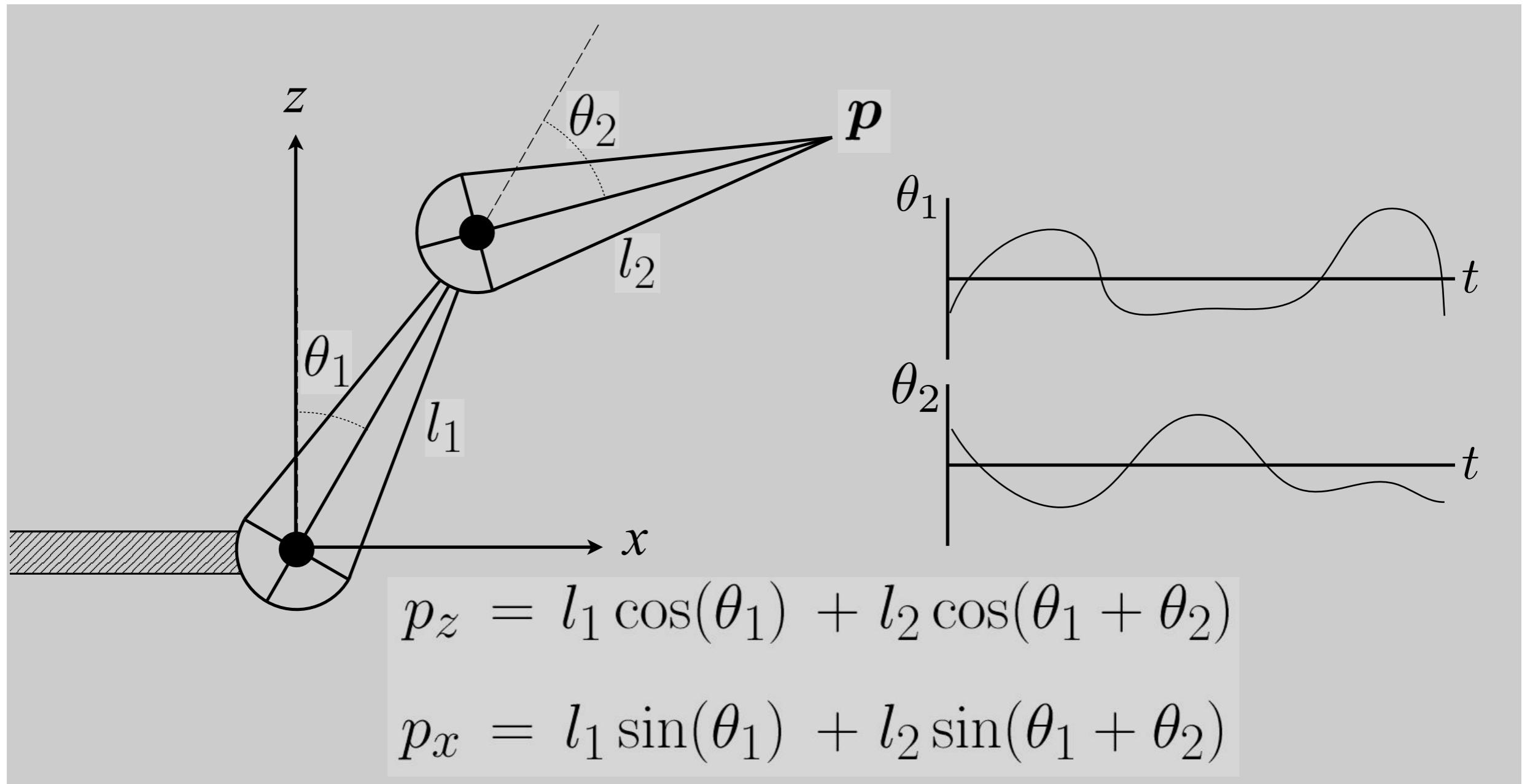
# Forward Kinematics

Animator provides angles, and computer determines position  $p$  of end-effector

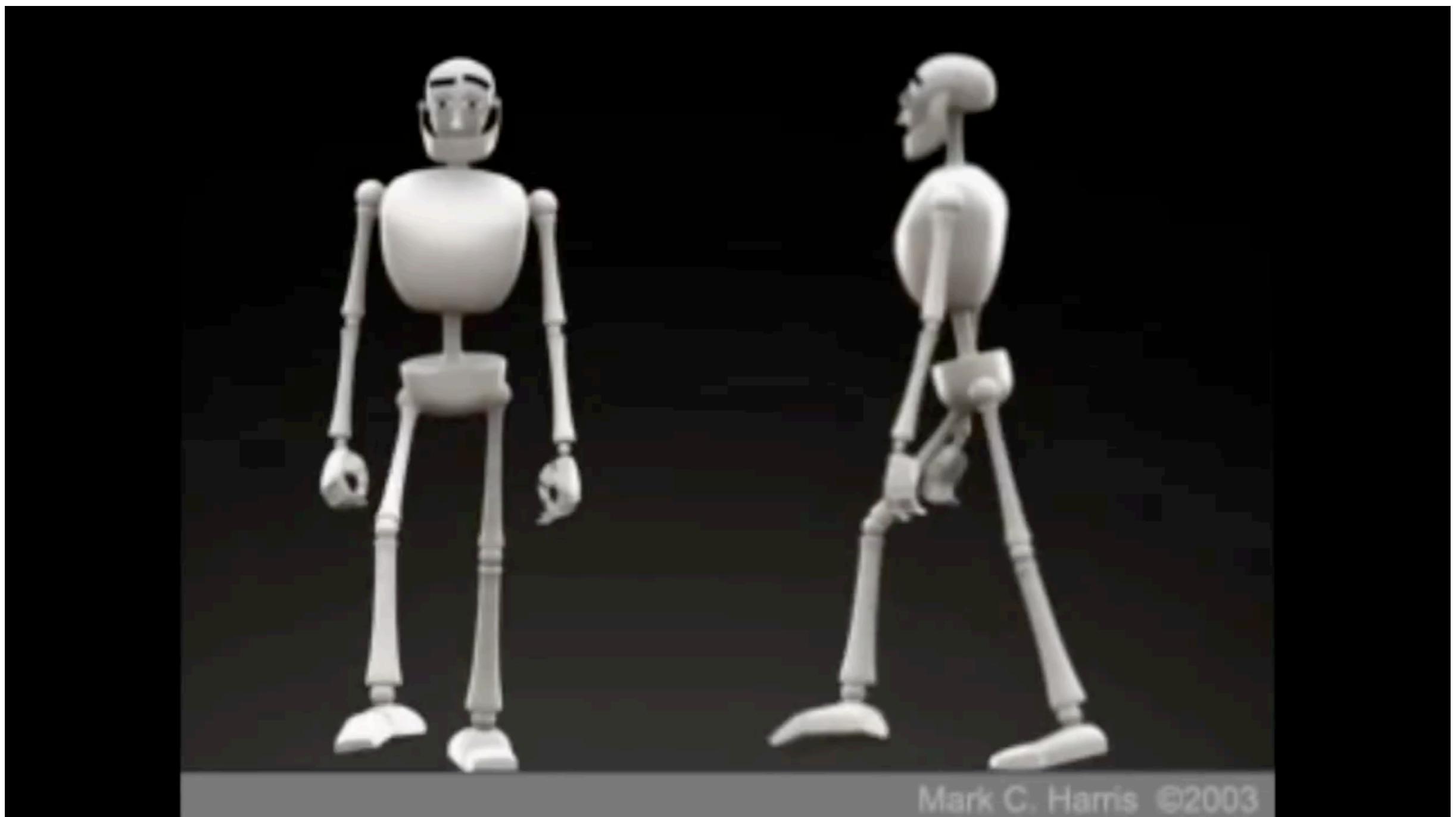


# Forward Kinematics

Animation is described as angle parameter values as a function of time



# Example Walk Cycle



Mark C. Harris ©2003

# Kinematics Pros and Cons

## Strengths

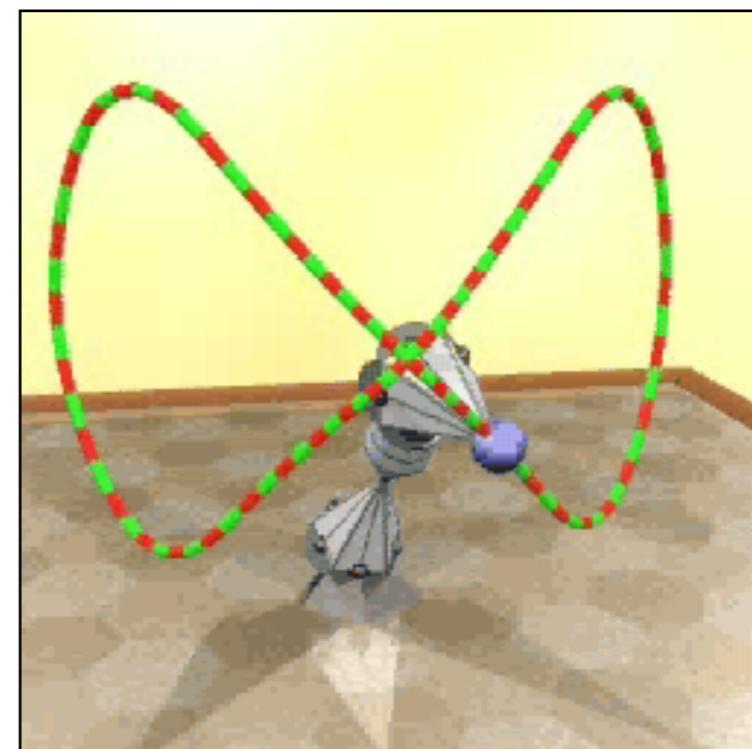
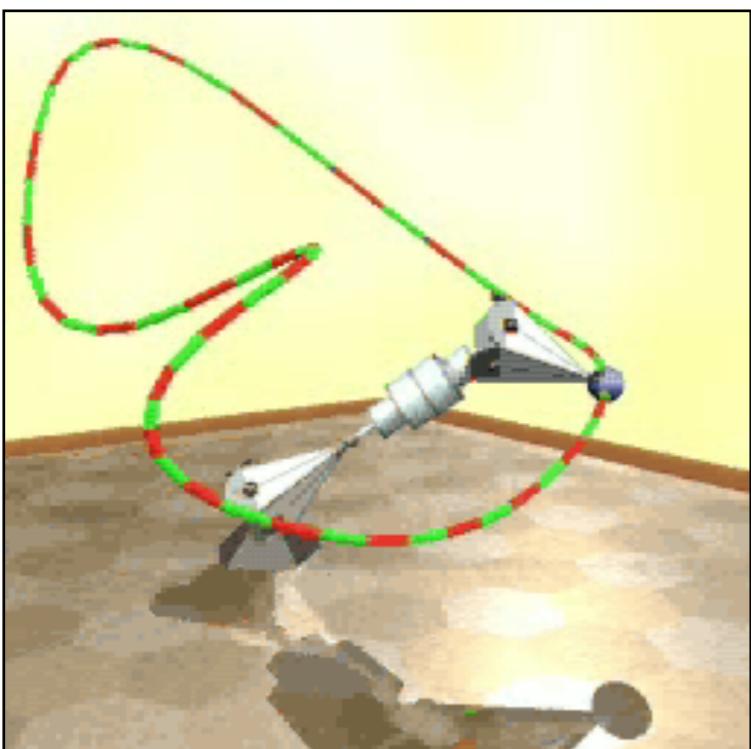
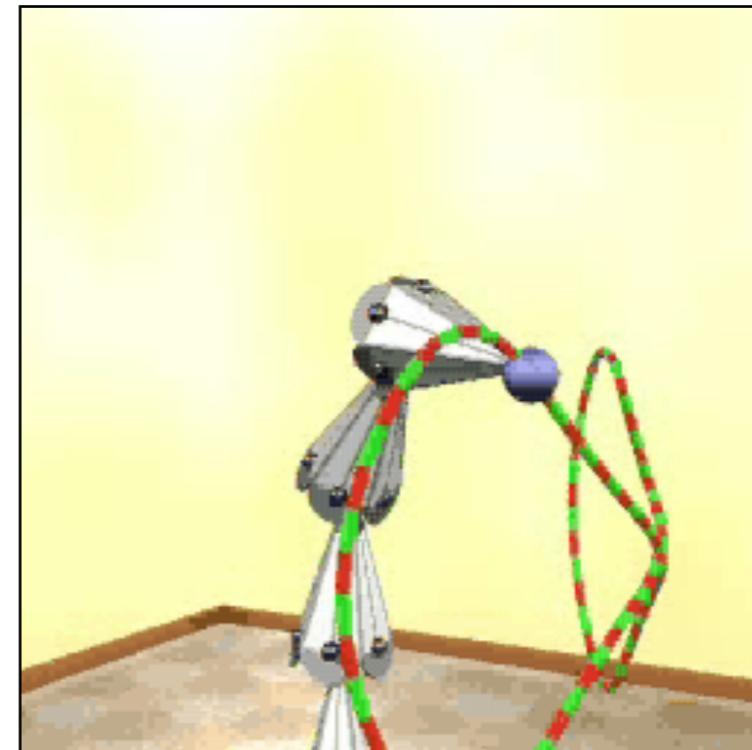
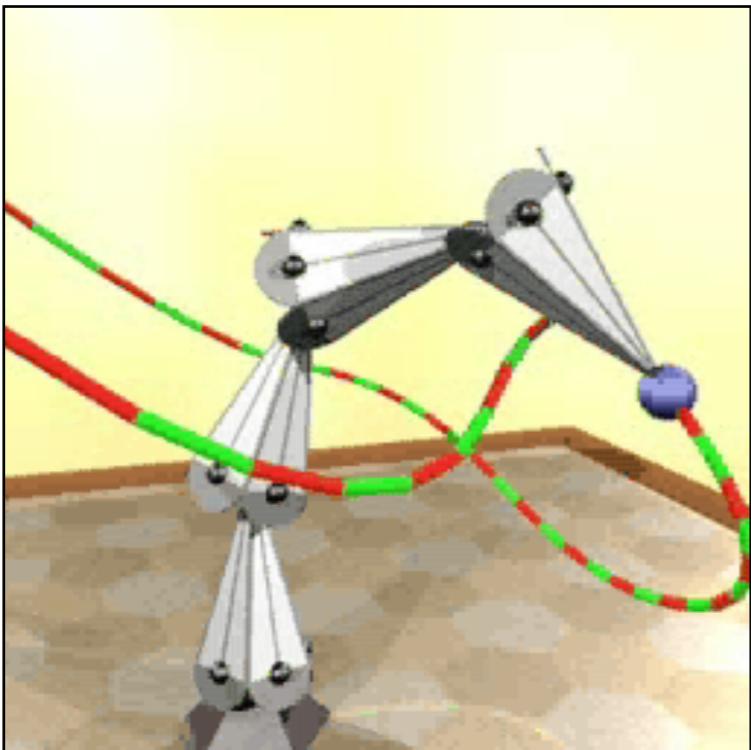
- Direct control is convenient
- Implementation is straightforward

## Weaknesses

- Animation may be inconsistent with physics
- Time consuming for artists

# Inverse Kinematics

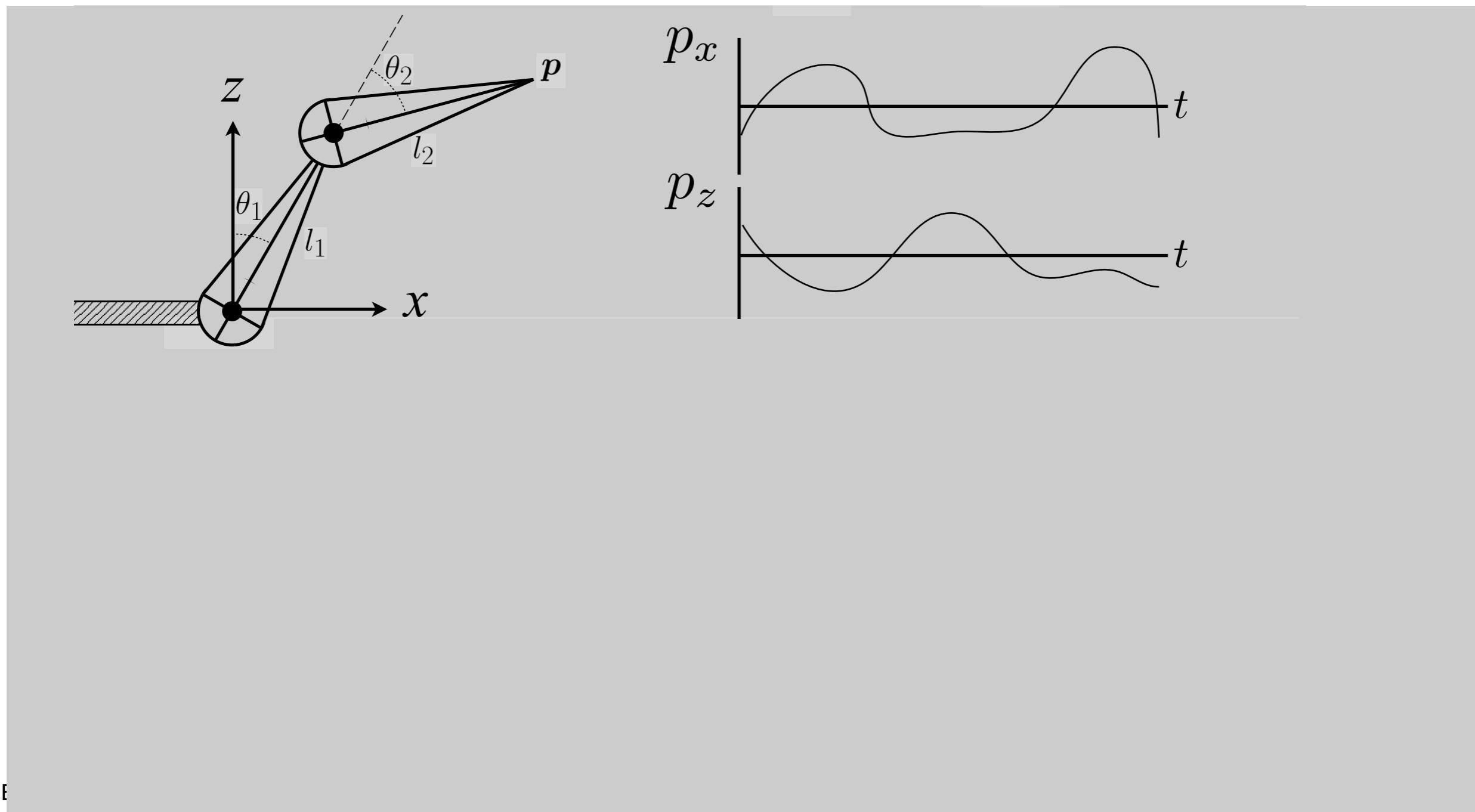
# Inverse Kinematics



Egon Pasztor

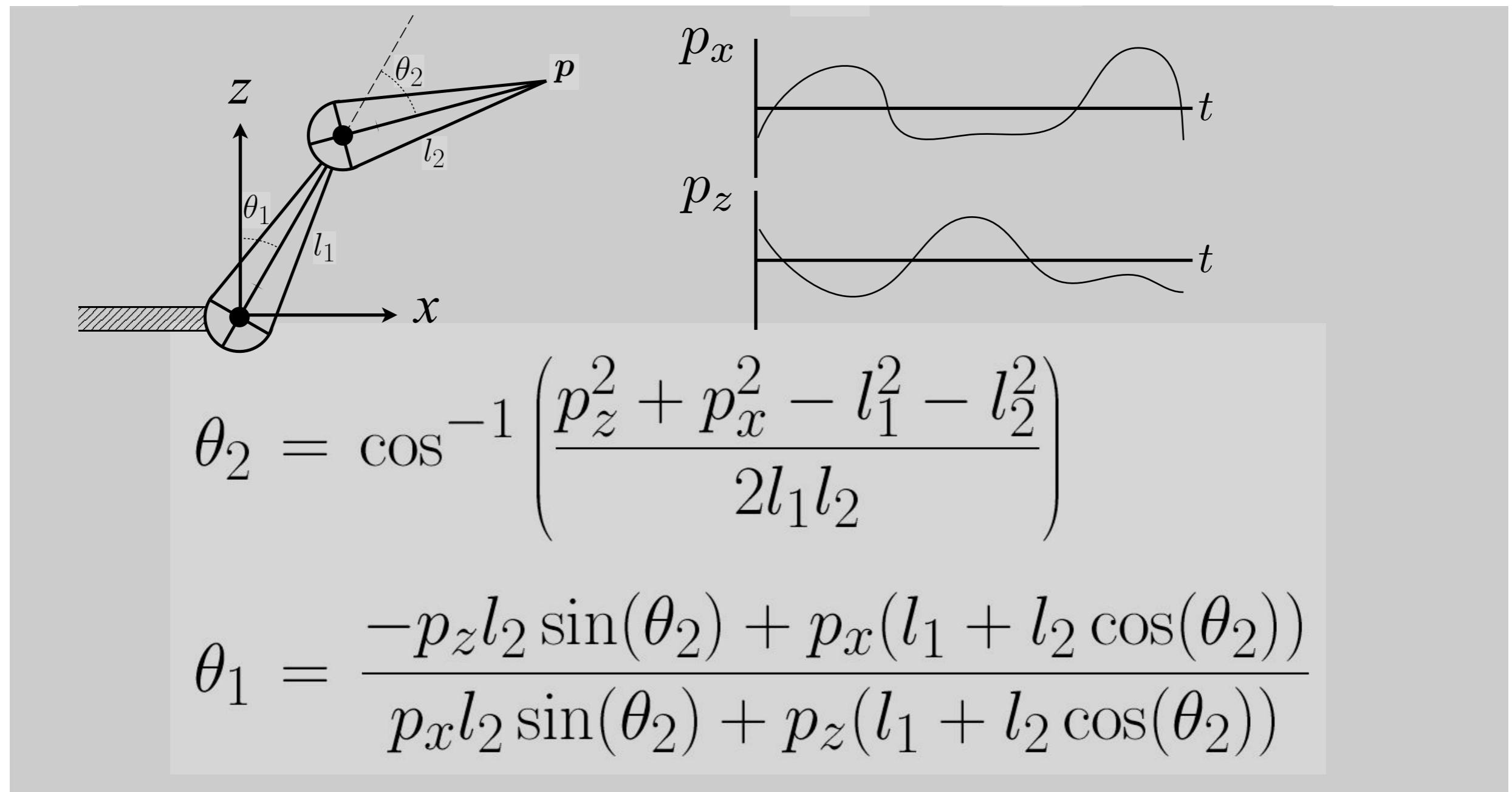
# Inverse Kinematics

Animator provides position of end-effector, and computer must determine joint angles that satisfy constraints



# Inverse Kinematics

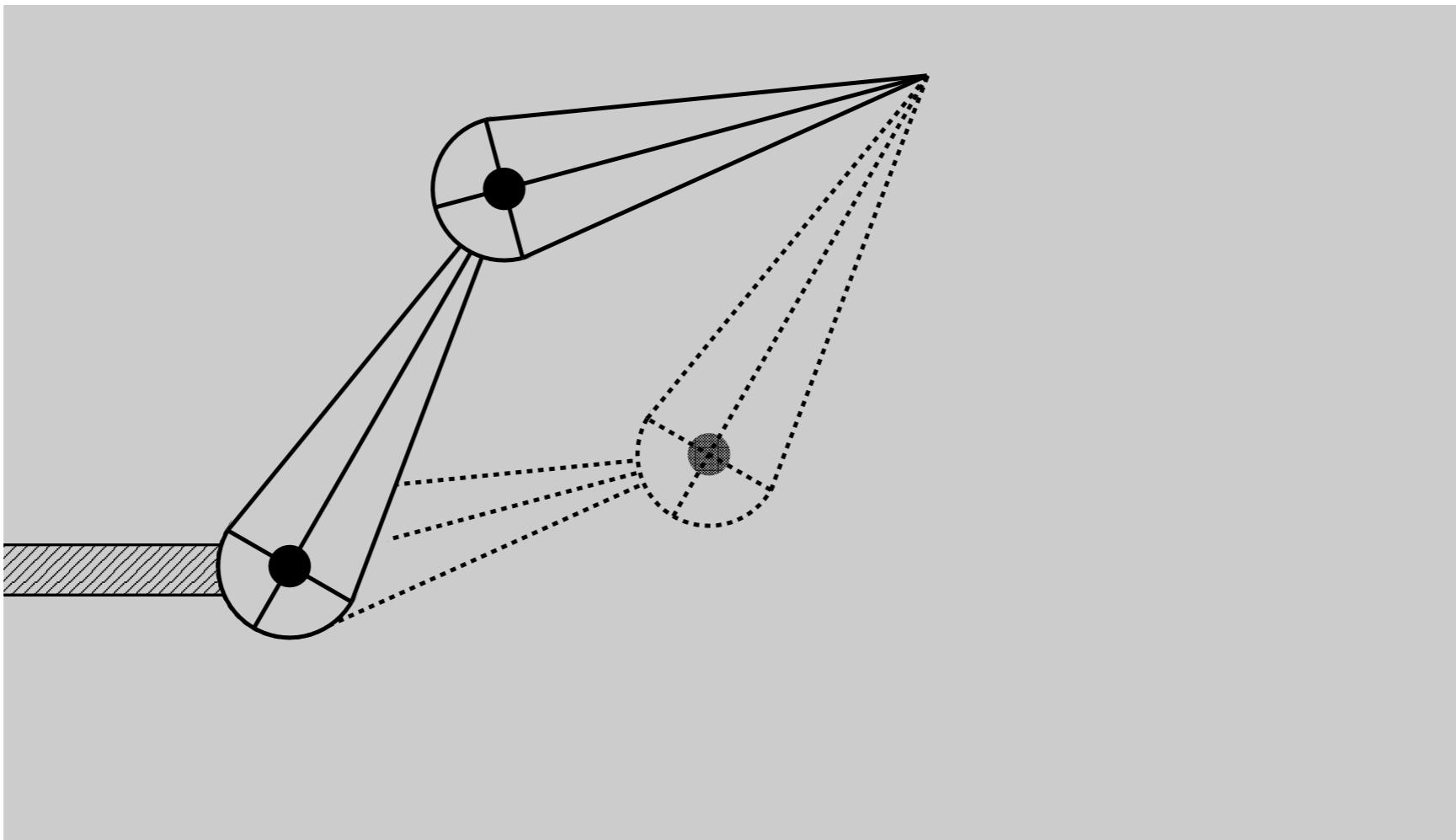
Direct inverse kinematics: for two-segment arm, can solve for parameters analytically



# Inverse Kinematics

Why is the problem hard?

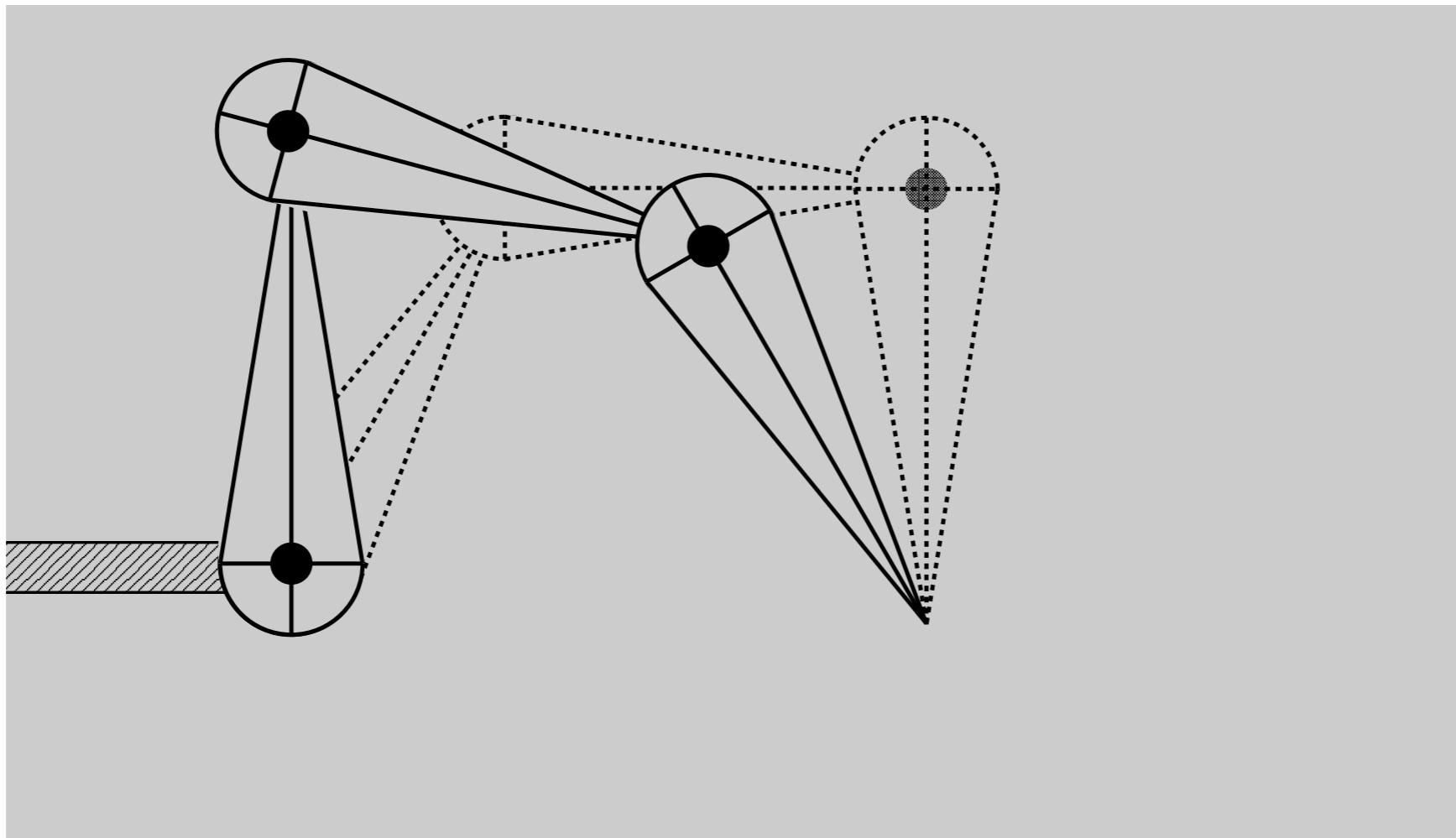
- Multiple solutions in configuration space



# Inverse Kinematics

Why is the problem hard?

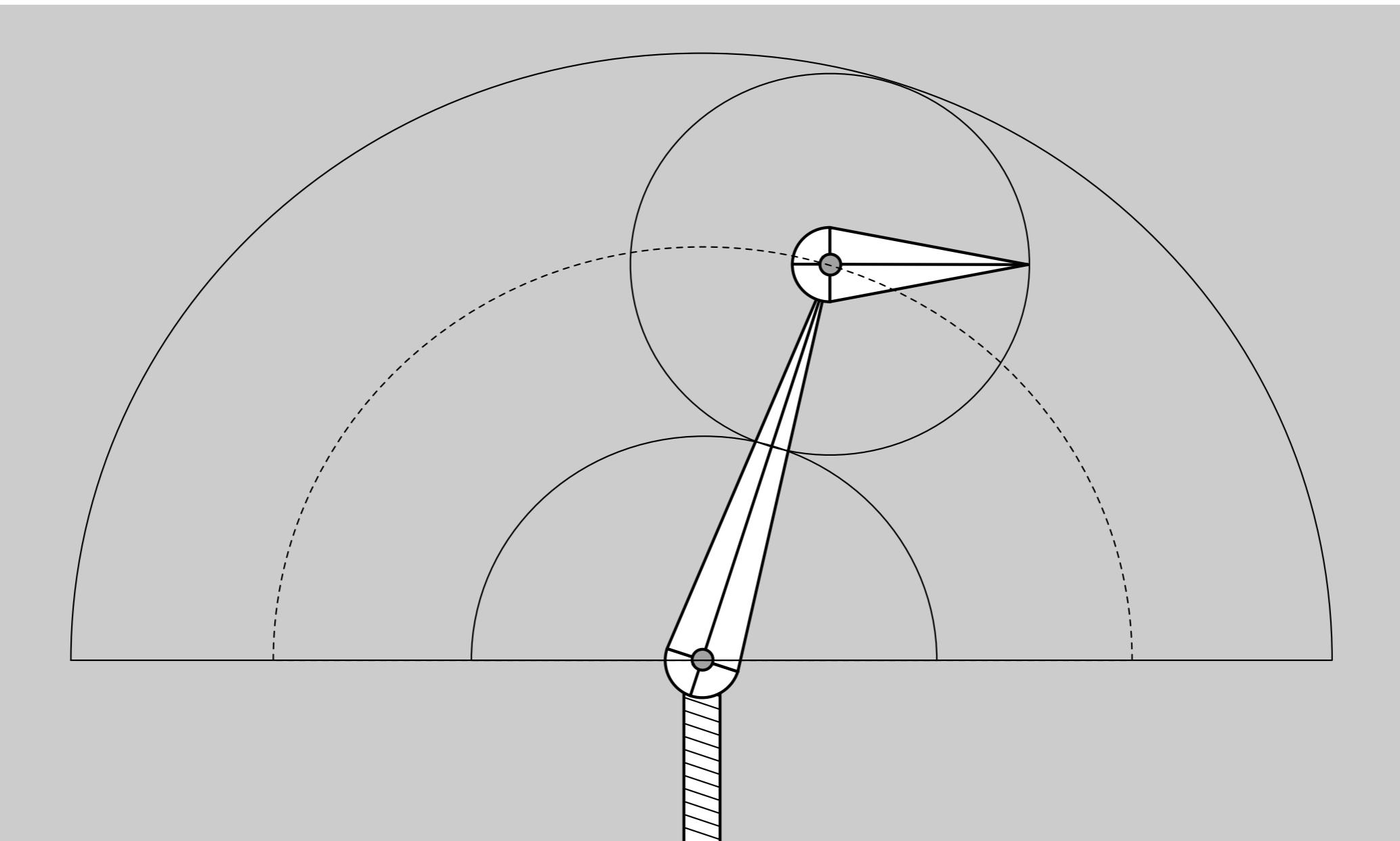
- Multiple solutions in configuration space



# Inverse Kinematics

Why is the problem hard?

- Solutions may not always exist

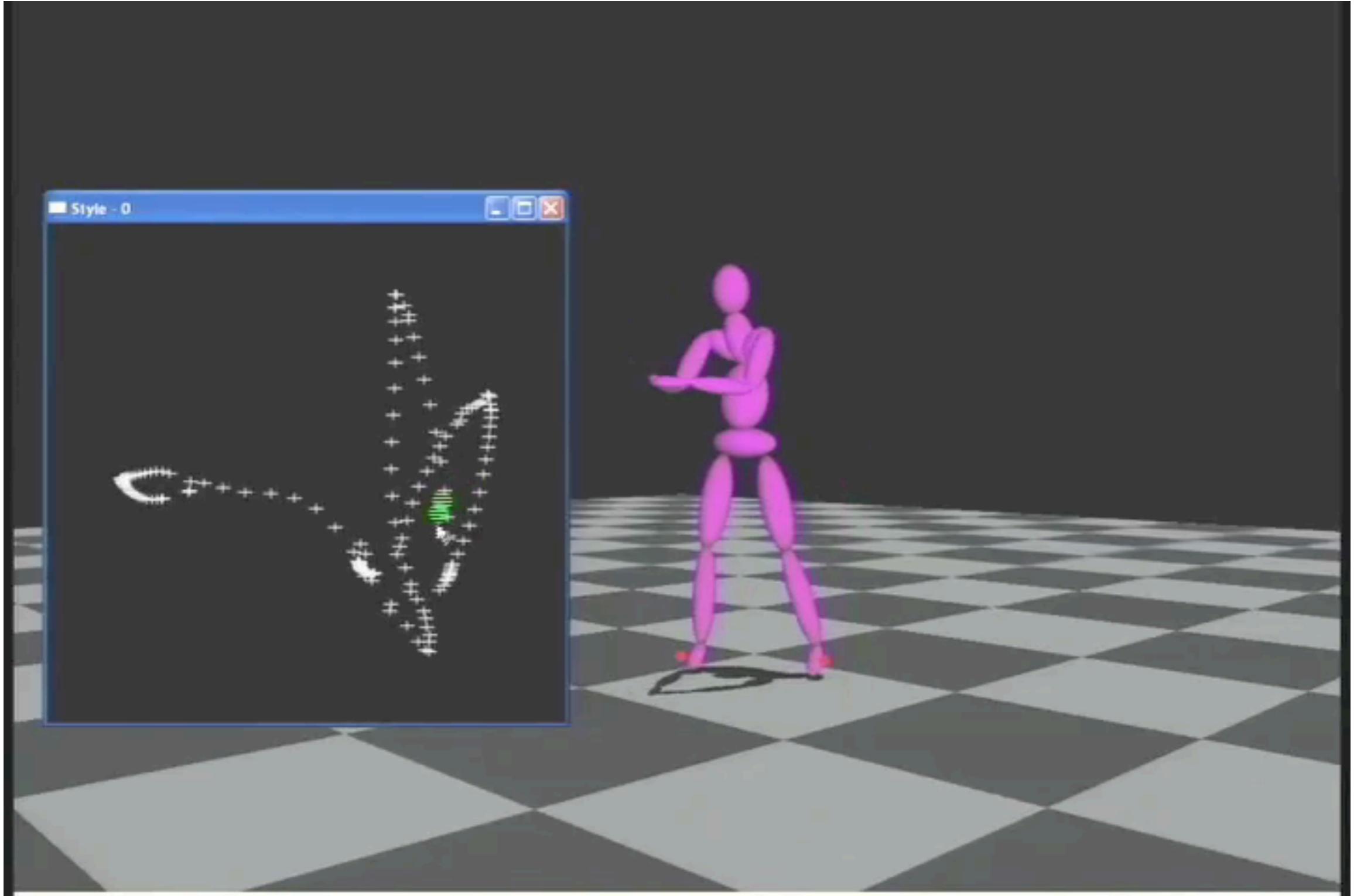


# Inverse Kinematics

Numerical solution to general N-link IK problem

- Choose an initial configuration
- Define an error metric (e.g. square of distance between goal and current position)
- Compute gradient of error as function of configuration
- Apply gradient descent (or Newton's method, or other optimization procedure)

# Style-Based IK



Grochow et al., Style Based Inverse Kinematics

# Rigging

# Rigging

Rigging is a set of higher level controls on a character that allow more rapid & intuitive modification of pose, deformations, expression, etc.

Important

- Like strings on a puppet
- Captures all meaningful character changes
- Varies from character to character

Expensive to create

- Manual effort
- Requires both artistic and technical training



# Rigging Example



Courtesy Matthew Lailler via Keenan Crane

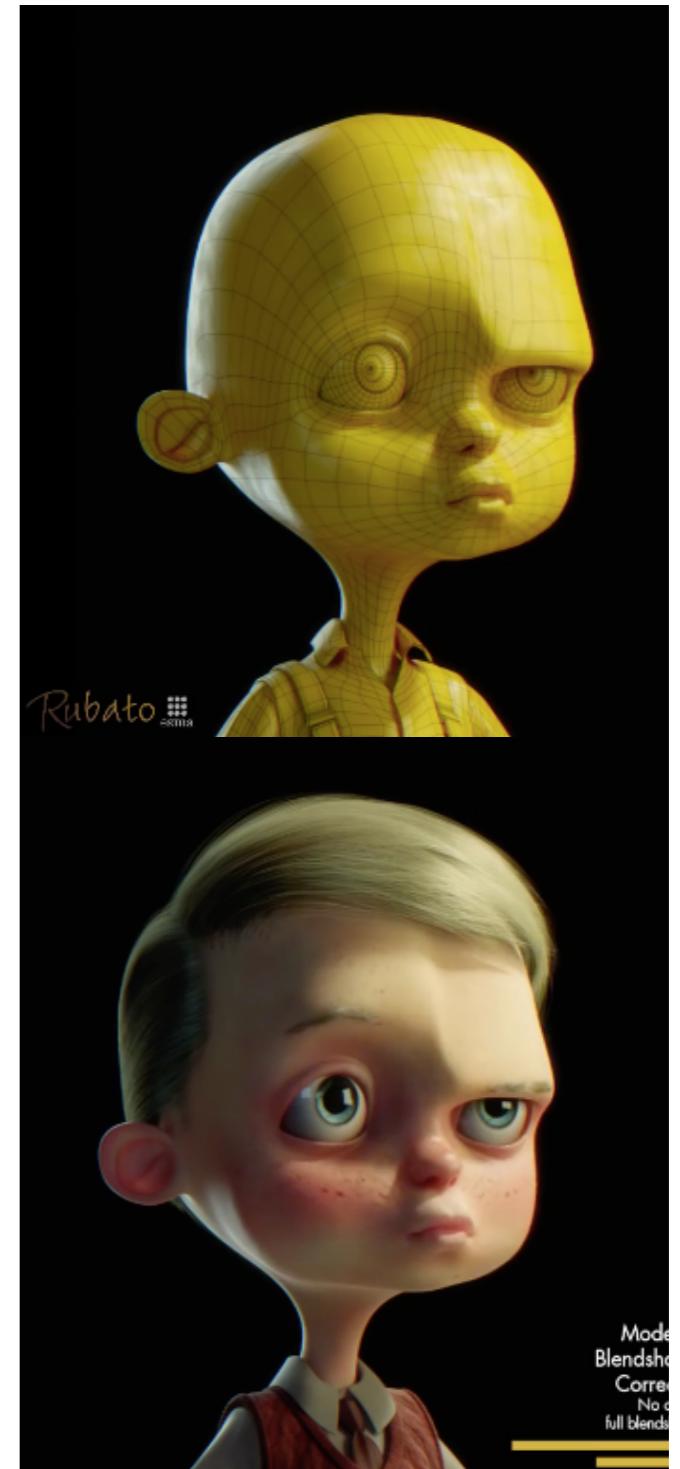
# Blend Shapes

Instead of skeleton, interpolate directly between surfaces

E.g., model a collection of facial expressions:

Simplest scheme: take linear combination of vertex positions

Spline used to control choice of weights over time



Courtesy Félix Ferrand

# Blend Shapes



Modeling  
Blendshapes  
Corrective  
No clothes  
full blendshapes

Courtesy Félix Ferrand

# Motion Capture

# Motion Capture

Data-driven approach to creating animation sequences

- Record real-world performances (e.g. person executing an activity)
- Extract pose as a function of time from the data collected



Motion capture room for ShaqFu

# Motion Capture Pros and Cons

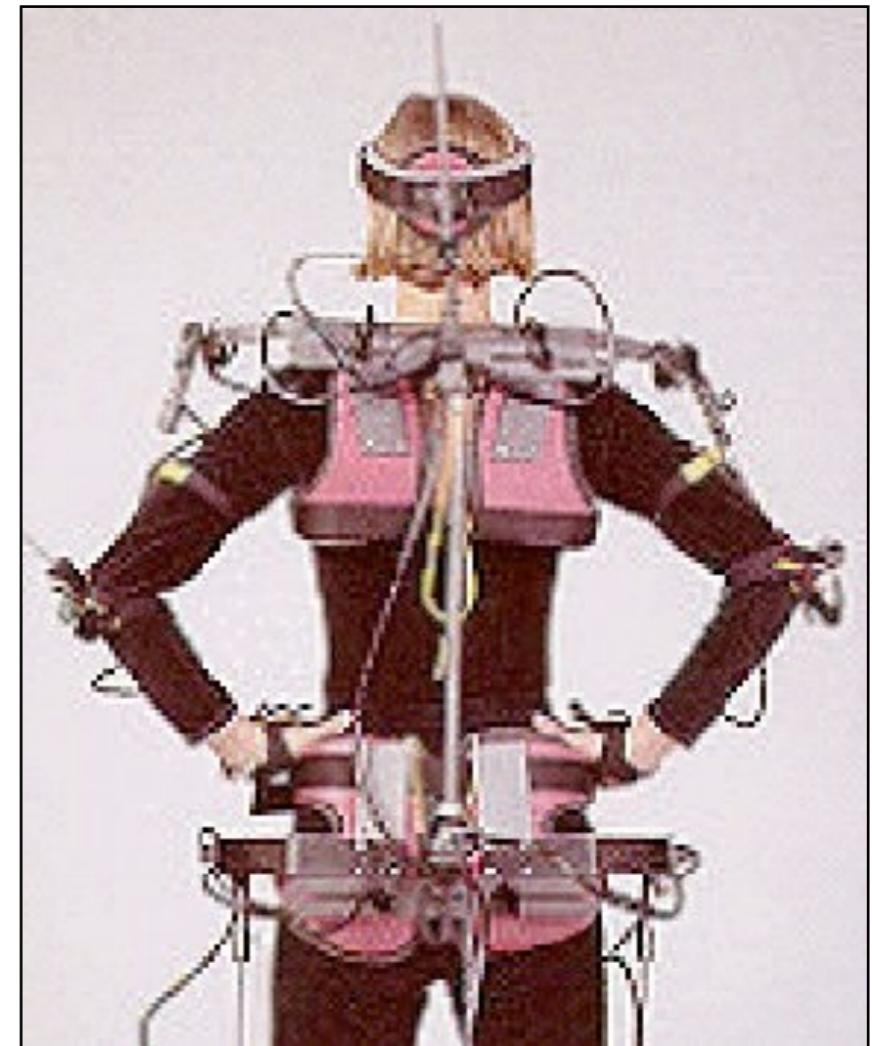
## Strengths

- Can capture large amounts of real data quickly
- Realism can be high

## Weaknesses

- Complex and costly set-ups
- Captured animation may not meet artistic needs, requiring alterations

# Motion Capture Equipment



## Optical

(More on following slides)

## Magnetic

Sense magnetic fields to infer position / orientation.  
Tethered.

## Mechanical

Measure joint angles directly.  
Restricts motion.

# Optical Motion Capture



Retroreflective markers attached to subject



IR illumination and cameras

- Markers on subject
- Positions by triangulation from multiple cameras
- 8+ cameras, 240 Hz, occlusions are difficult

Slide credit: Prof. Steve Marschner @ Cornell

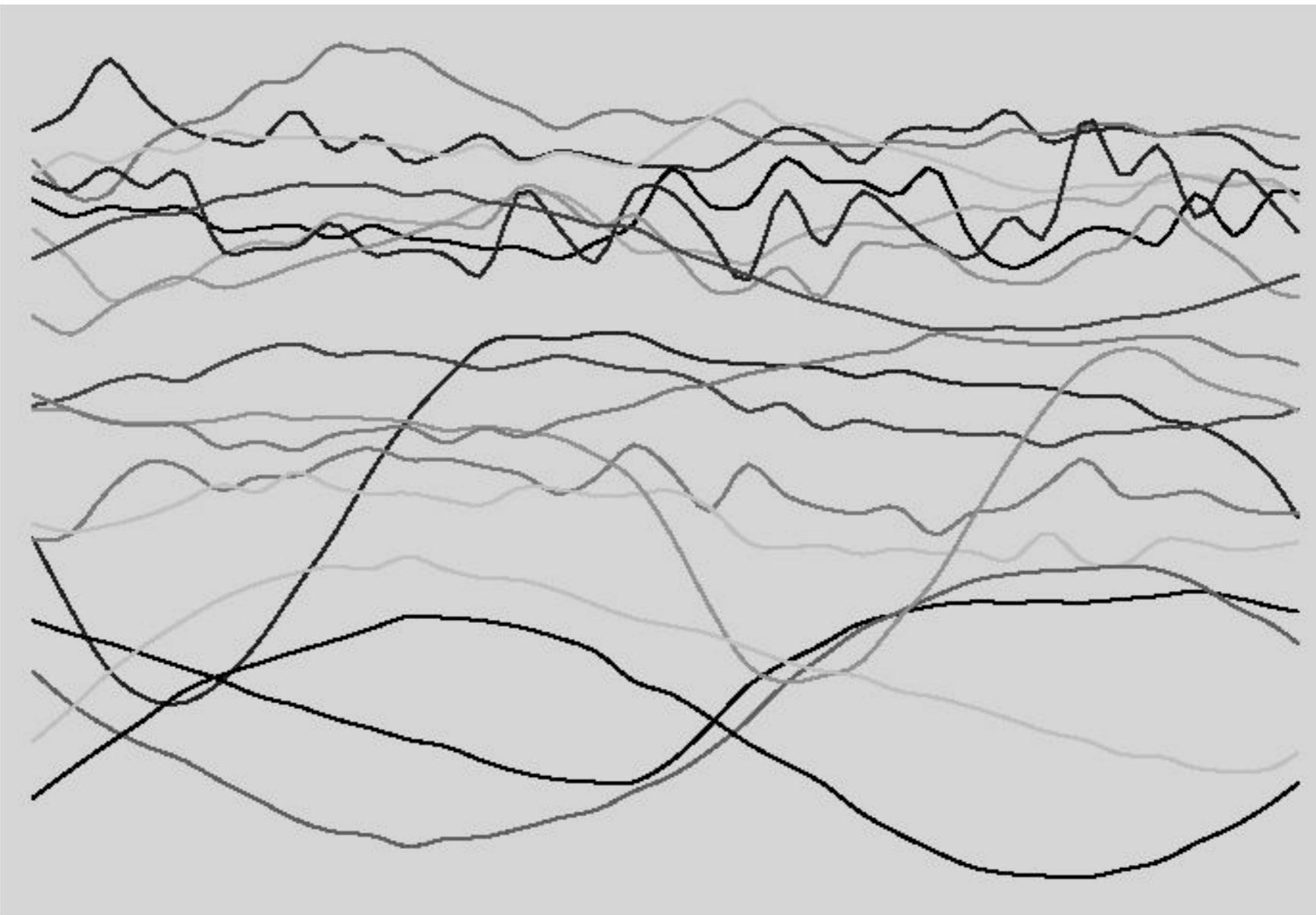
# Optical Motion Capture



Source: <http://fightland.vice.com/blog/ronda-rousey-20-the-queen-of-all-media>

Ronda Roussey in Electronic Arts' motion capture studio

# Motion Data



Subset of motion curves from captured walking motion.

From Witkin and Popovic, 1995

# Challenges of Facial Animation

Uncanny valley (恐怖谷效应)

- In robotics and graphics
- As artificial character appearance approaches human realism, our emotional response goes negative, until it achieves a sufficiently convincing level of realism in expression



Cartoon.  
Brave, Pixar



Semi-realistic. Polar Express, Warner Bros.

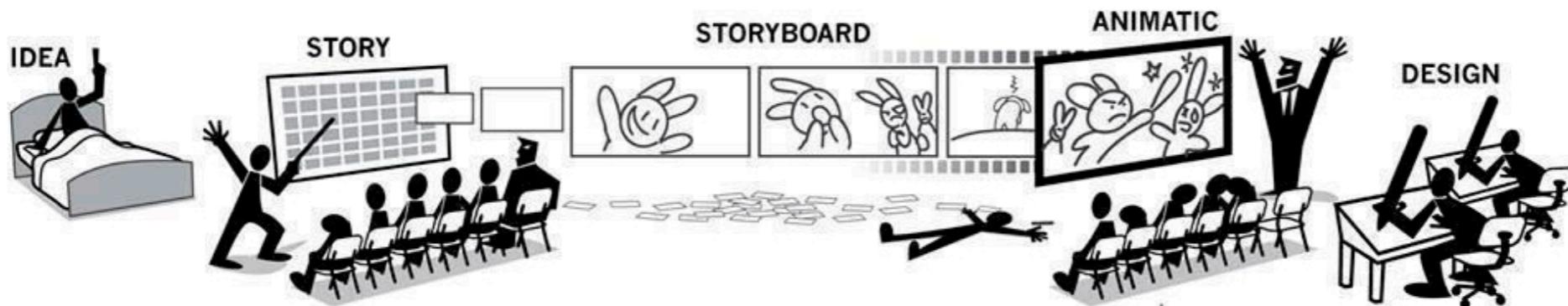
# Facial Motion Capture



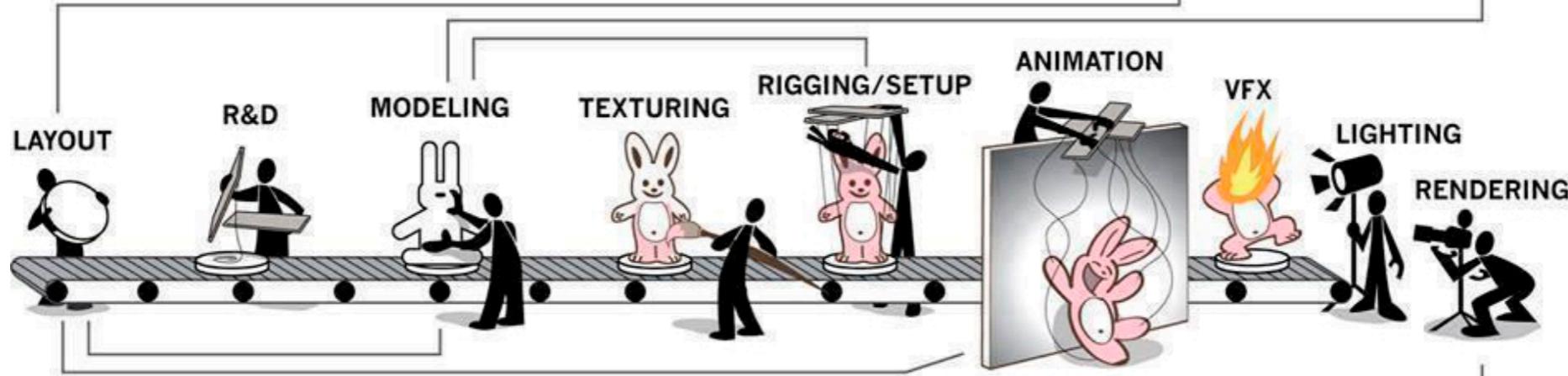
Discovery, "Avatar: Motion Capture Mirrors Emotions", <https://youtu.be/1wK1lxr-UmM>

# The Production Pipeline

## PRE-PRODUCTION



## PRODUCTION



## POST-PRODUCTION

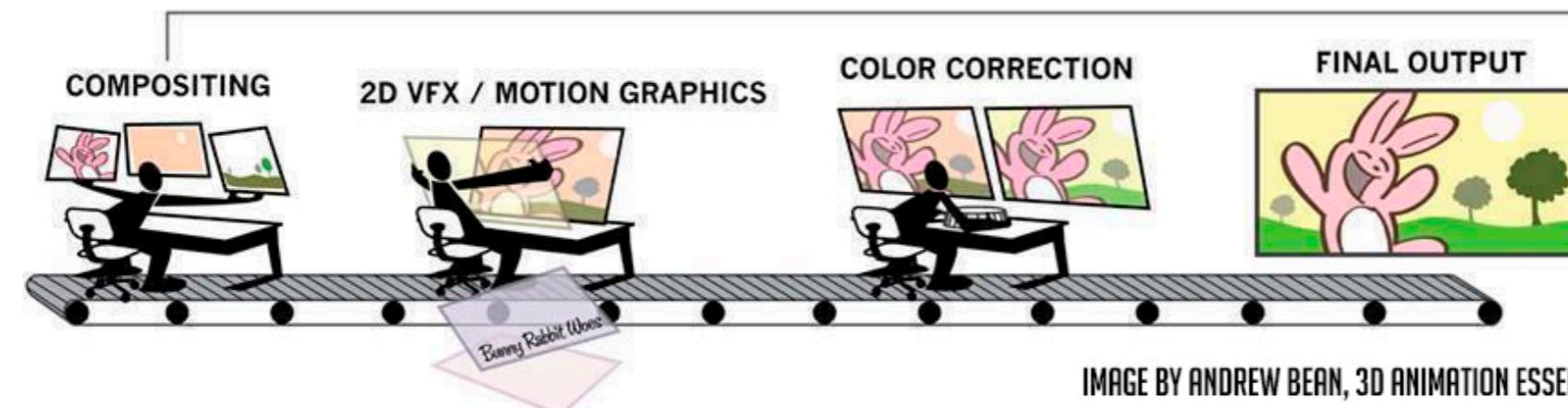


IMAGE BY ANDREW BEAN, 3D ANIMATION ESSENTIALS (2012)

# Next (Final) Lecture

Given the forces / physics / theory, how to simulate actual movements



Hint: what would he say in a fight?

Credit: JoJo's Bizarre Adventure

# Thank you!

(And thank Prof. Ren Ng for many of the slides!)