Assembly Language and Microcomputer Interface

Chapter 1 – Introduction to the Microprocessor and Computer

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Introduction

- Overview of Intel microprocessors
- Discussion of history of computers
- Function of the microprocessor
- Computer data formats
- Terms and jargon (computer)

1-1 A HISTORICAL BACKGROUND

- Once programmable machines developed, programs and programming languages began to appear.
- As early practice of rewiring circuits proved too cumbersome, computer languages began to appear in order to control the computer.
- The first, machine language, was constructed of ones and zeros using binary codes.
 - stored in the computer memory system as groups of instructions called a program

- More efficient than rewiring a machine to program it.
 - still time-consuming to develop a program due to sheer number of program codes required
- Mathematician John von Neumann first modern person to develop a system to accept instructions and store them in memory.
- Computers are often called von Neumann machines in his honor.

- Once systems such as UNIVAC became available in early 1950s, assembly language was used to simplify entering binary code.
- Assembler allows programmer to use mnemonic codes...
 - such as ADD for addition
- In place of a binary number.
 - such as 0100 0111
- Assembly language an aid to programming.

- 1957 Grace Hopper developed first high-level programming language called FLOWMATIC.
- In same year, IBM developed FORTRAN(FORmula TRANslator) for its systems.
 - Allowed programmers to develop programs that used formulas to solve mathematical problems.
- First successful, widespread programming language for business applications was COBOL (COmputer Business Oriented Language).



Grace Hopper (1906-1992)



first bug (1947)

The Microprocessor Age

- World's first microprocessor the Intel 4004.
- A 4-bit microprocessor-programmable controller on a chip.
- Addressed 4096, 4-bit-wide memory locations.
 - a bit is a binary digit with a value of one or zero
 - 4-bit-wide memory location often called a nibble
- The 4004 instruction set contained 45 instructions.

- Fabricated with then-current state-of-the-art P-channel MOSFET technology.
- Executed instructions at 50 KIPs (kiloinstructions per second).
 - slow compared to 100,000 instructions per second by 30-ton ENIAC computer in 1946
- Difference was that 4004 weighed less than an ounce.
- 4-bit microprocessor debuted in early game systems and small control systems.
 - early shuffleboard game produced by Bailey

The Modern Microprocessor

- The IA-32 (Intel Architecture 32) family was preceded by 16-bit processors, the 8086 and 8088.
- In 1978 Intel released the 8086; a year or so later, it released the 8088.
- The 8086 has 16-bit registers and a 16-bit external data bus, with 20-bit addressing giving a 1-MByte address space.
- The 8088 is similar to the 8086 except it has an 8-bit external data bus.
- Popularity of Intel ensured in 1981 when IBM chose the 8088 in its personal computer.

16-bit Processors and Segmentation (1978)

00000 → Code

Data

Stack

Data

stack

FFFFF →

Data

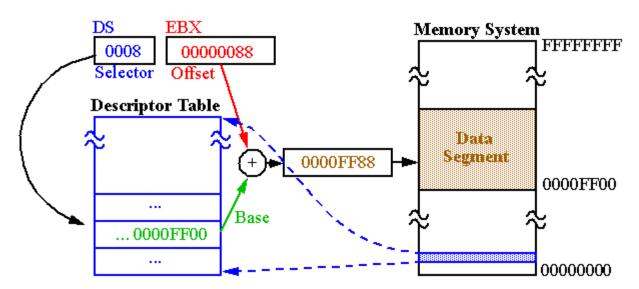
Extra

Memory Segmentation

- The 8086/8088 introduced segmentation to the IA-32 architecture. With segmentation, a 16-bit segment register contains a pointer to a memory segment of up to 64 KBytes.
- Using four segment registers at a time, 8086/8088 processors are able to address up to 256 KBytes without switching between segments.

The Intel 286 Processor (1982)

- The Intel 286 processor introduced protected mode operation into the IA-32 architecture.
- Protected mode uses the segment register content as selectors or pointers into descriptor tables.



Protected Mode Memory Addressing

The Intel 286 Processor (1982)

- Descriptors provide 24-bit base addresses
 with a physical memory size of up to 16
 MBytes, support for virtual memory
 management on a segment swapping basis,
 and a number of protection mechanisms.
- Protection mechanisms include:
 - Segment limit checking
 - Read-only and execute-only segment options
 - Four privilege levels

The Intel 386 Processor (1985)

- The Intel 386 processor was the first 32-bit processor in the IA-32 architecture family. It introduced 32-bit registers for use both to hold operands and for addressing.
- The lower half of each 32-bit Intel 386 register retains the properties of the 16-bit registers of earlier generations, permitting backward compatibility.

The Intel 386 Processor (1985)

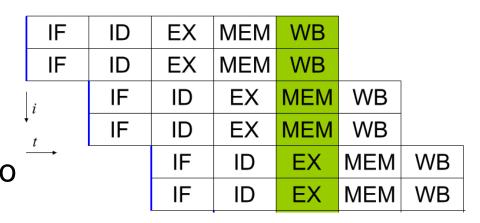
- The processor also provides a virtual-8086 mode that allows for even greater efficiency when executing programs created for 8086/8088 processors.
- The 386 was the first processor in the Intel family to include parallel stages (pipelining) in its execution cycle.
- In addition, the 386 processor has support for paging with a fixed 4-KByte page size providing a method for virtual memory management.

The Intel 486 Processor (1989)

- The 486 processor added more parallel execution capability by expanding the 386 processor's instruction decode and execution units into five pipelined stages.
- In addition, the 486 added:
 - An 8-KByte on-chip first-level cache that increased the percent of instructions that could execute at the scalar rate of one per clock
 - An integrated x87 FPU (floating point unit)

The Intel Pentium Processor (1993)

 Pentium processor added a second execution pipeline to achieve superscalar performance (two pipelines, known as u and v, execute two instructions per clock).



superscalar

- The first-level cache doubled, with 8 KBytes devoted to code and another 8 KBytes devoted to data.
- The data cache uses the MESI protocol to support more efficient write-back cache in addition to the previous used write-through cache.
- Branch prediction with an on-chip branch table was added to increase performance in looping constructs.

The P6 Family of Processors (1995-1999)

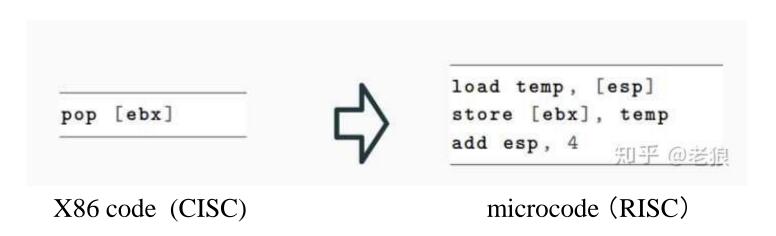
- The Pentium Pro processor is three-way superscalar.
- The Pentium II processor added MMX technology to the P6 family processors along with new packaging and several hardware enhancements.
- The **Pentium III** processor introduced the Streaming SIMD Extensions (SSE) to the IA-32 architecture. SSE extensions expand MMX technology by providing a new set of 128-bit registers and the ability to perform SIMD operations on packed single-precision floating-point values.

The Pentium 4 Processor Family (2000-2006)

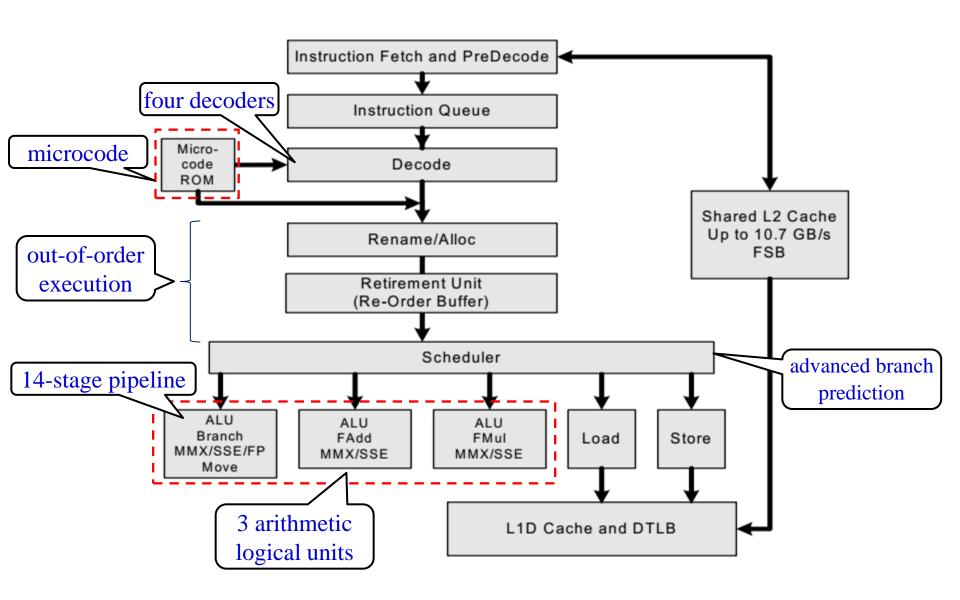
- The Intel Pentium 4 processor is based on NetBurst microarchitecture and introduced:
 - Streaming SIMD Extensions 2 (SSE2)
 - Intel 64 architecture
 - Hyper-Threading Technology
 - Intel Virtualization Technology (Intel VT)
- The Intel Pentium Processor Extreme Edition (2005) introduced dual-core technology. The processor supports SSE, SSE2, SSE3, Hyper-Threading Technology, and Intel 64 architecture.

More Information on Specific Advances

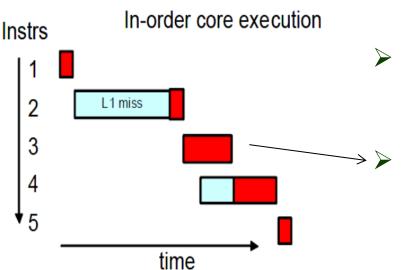
- Starting with Pentium Pro, Intel redesigned it's microprocessors and used internal RISC core under the CISC instructions.
- Since Pentium Pro, all CISC instructions are divided into microcode and then executed by the RISC core.



Intel Core Microarchitecture



Out-of-order Execution (1/2)



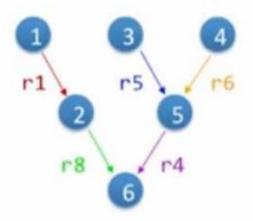
- On usual in-order execution, next instruction waits until the previous one finishes.
- ➤ Instruction 2 has a big delay due to an L1 miss, and next instructions wait until instruction 2 finishes.
- Pipeline exploits instruction level parallelism. However, only independent subsequent instructions can be executed in parallel. Whereas subsequent instructions are often dependent.
- So the utilization of the second pipe is often low.
- Execute instructions based on the "data flow" graph, rather than program order.

Out-of-order Execution (2/2)

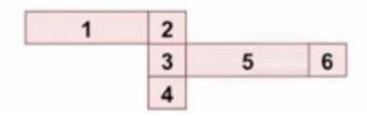
Example:

- (1) $r1 \leftarrow r4 / r7$
- (2) $r8 \leftarrow r1 + r2$
- (3) $r5 \leftarrow r5 + 1$
- (4) $r6 \leftarrow r6 r3$
- (5) $r4 \leftarrow load [r5 + r6]$
- (6) r7 ← r8 * r4

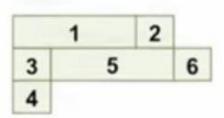
Data Flow Graph



In-order execution

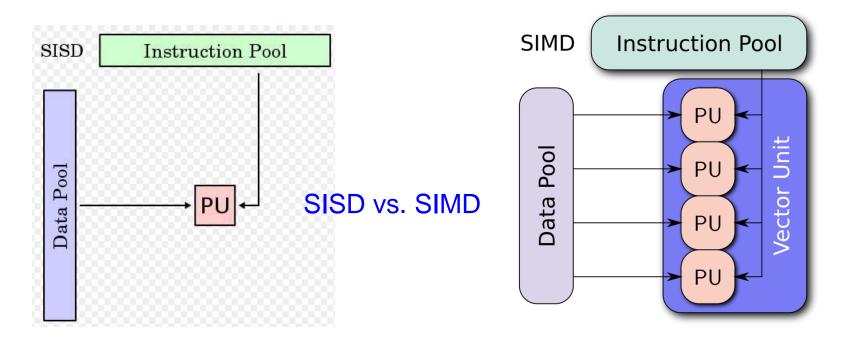


Out-of-order execution



three-way superscalar

SIMD Instructions (1/3)



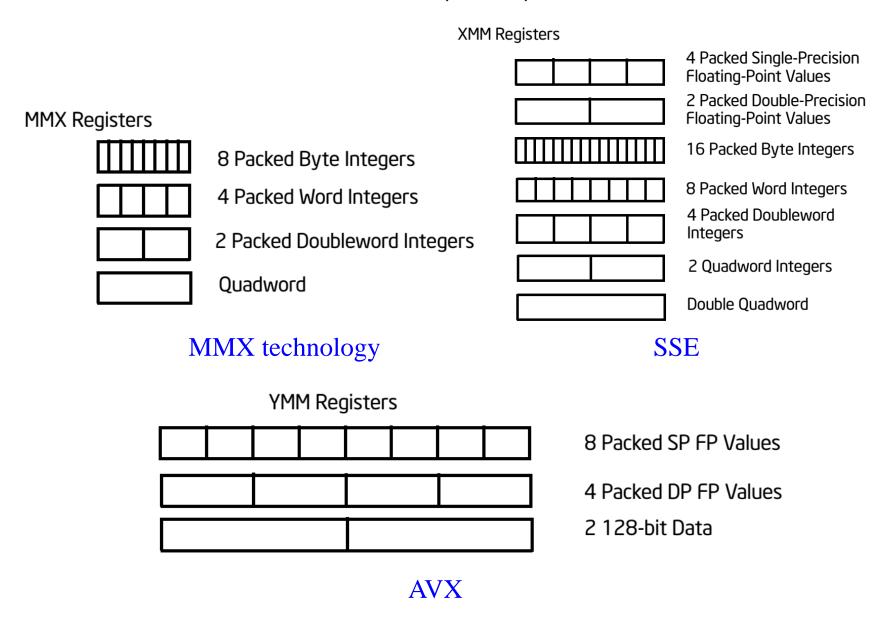
 Compared with SISD, a SIMD computing element performs the same operation on multiple data items simultaneously. Typical SIMD operations include basic arithmetic (addition, subtraction, multiplication, and division), shifts, compares, and data conversions.

SIMD Instructions (2/3)

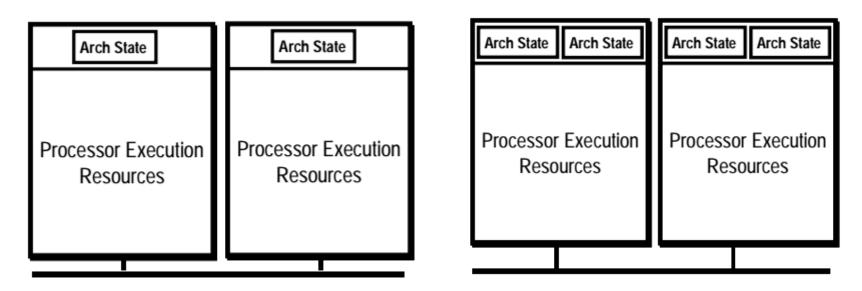


 Since MMX technology in the Pentium II, six extensions (SSE, SSE2,SSE3, SSSE3,SSE4 and AVX) have been introduced into the Intel 64 and IA-32 architectures to perform SIMD operations.

SIMD Instructions (3/3)



Hyper-Threading Technology (1/3)



Processors without HT

Processors with HT

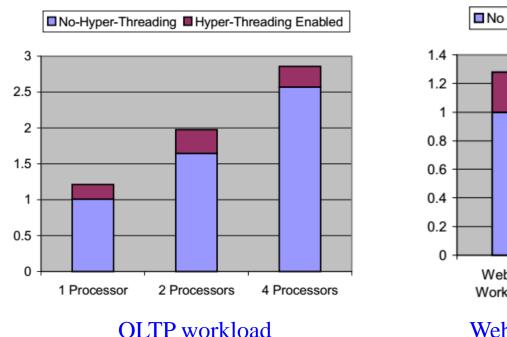
- HT technology provides hardware multi-threading capability with a single physical package by using shared execution resources in a processor core.
- An IA-32 processor that supports HT technology consists of two or more logical processors, each of which has its own IA-32 architectural state.

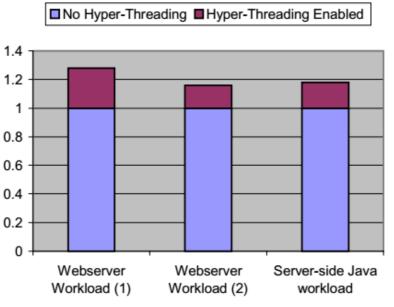
Hyper-Threading Technology (2/3)

- The architecture state consists of registers including the general-purpose registers, the control registers, the advanced programmable interrupt controller (APIC) registers, and some machine state registers.
- Logical processors share nearly all other resources on the physical processor, such as caches, execution units, branch predictors, control logic, and buses.
- Three goals of HT technology:
 - To minimize the die area cost of implementing HT technology.
 - When one logical processor is stalled the other could continue.
 - To run at the same speed with HT technology as without this capability when only one software thread is active.

Hyper-Threading Technology (3/3)

 Three goals were achieved through efficient logical processor selection algorithms and the partitioning and recombining algorithms of many key resources with less than 5% of the total die area to obtain up to 30% gain.





Web server benchmark performance

Hyper-Threading Technology Architecture and Microarchitecture. Intel Technology Journal, 2002.

Multi-Core Technology

Logical Proces sor	Logical Proces sor	Logical Proces sor	Logical Proces sor	Logical Proces sor	Logical Proces sor	Logical Proces sor	Logical Proces sor
L1 and L2		L1 and L2		L1 and L2		L1 and L2	
Execution Engine		Execution Engine		Execution Engine		Execution Engine	
Third Level Cache							
QuickPath Interconnect (QPI) Interface, Integrated Memory Controller							
		QPI			IMC		R3

Intel Core i7 Processor (quad-core + Hyper-Threading)

 Multi-core technology enhances hardware multi-threading capability by providing two or more execution cores in a physical package.

Intel 64 Architecture

- Intel 64 architecture increases the linear address space for software to 64 bits and supports physical address space up to 52 bits.
- The technology also introduces a new operating mode referred to as IA-32e mode.
- IA-32e mode operates in one of two sub-modes
 - Compatibility mode enables a 64-bit operating system to run most legacy 32-bit software unmodified.
 - 64-bit mode enables a 64-bit operating system to run applications written to access 64-bit address space.

1-3 NUMBER SYSTEMS

- Use of a microprocessor requires working knowledge of numbering systems.
 - binary, decimal, and hexadecimal
- This section provides a background for these numbering systems.
- Conversions are described.
 - decimal and binary
 - decimal and hexadecimal
 - binary and hexadecimal

Converting Binary to Decimal

- To convert to decimal, use decimal arithmetic to form Σ (digit \times respective power of 2).
- **Example:** Convert 11010_2 to N_{10} :

$$110102 =>
1 * 24 = 16
+ 1 * 23 = 8
+ 0 * 22 = 0
+ 1 * 21 = 2
+ 0 * 20 = 0
2610$$

Converting Decimal to Binary

- To convert from one base to another:
 - 1) Convert the Integer Part
 - 2) Convert the Fraction Part
 - 3) Join the two results with a radix point

Conversion Details

To Convert the Integral Part:

Repeatedly divide the number by the new radix and save the remainders. The digits for the new radix are the remainders in *reverse order* of their computation. If the new radix is > 10, then convert all remainders > 10 to digits A, B, ...

To Convert the Fractional Part:

Repeatedly multiply the fraction by the new radix and save the integer digits that result. The digits for the new radix are the integer digits in *order* of their computation. If the new radix is > 10, then convert all integers > 10 to digits A, B, ...

Example: Convert 725₁₀ To Base 2

```
2 7 2 5 <u>remainder</u>
2 3 6 2......1
  2 9 0......1
  2 4 5.....0
  (725)_{10} = (10 \ 1101 \ 0101)_{2}
```

Example: Convert 0.678₁₀ To Base 2

$$\begin{array}{c} (0.678)_{10} = (0.1010 \ 1101 \ 1001)_2 \\ \hline & overflow \\ 2 \times 0.678 \dots = 1.356 \\ 2 \times 0.356 \dots = 0.712 \\ 2 \times 0.712 \dots = 1.424 \\ 2 \times 0.424 \dots = 0.848 \\ 2 \times 0.848 \dots = 1.696 \\ 2 \times 0.696 \dots = 1.392 \\ 2 \times 0.392 \dots = 0.784 \\ 2 \times 0.784 \dots = 1.568 \\ 2 \times 0.568 \dots = 1.136 \\ 2 \times 0.136 \dots = 0.272 \\ 2 \times 0.272 \dots = 0.544 \\ 2 \times 0.544 \dots = 1.088 \\ \end{array}$$

Example: Convert 46.6875₁₀ To Base 2

Convert 46 to Base 2

$$46_{10} = 101110_2$$

- **Convert 0.6875 to Base 2** $0.6875_{10} = 0.1011_2$
- Join the results together with the radix point:

$$46.6875_{10} = 101110.1011_2$$

Octal (Hexadecimal) to Binary and Back

- Octal (Hexadecimal) to Binary:
 - Restate the octal (hexadecimal) as three (four) binary digits starting at the radix point and going both ways.
- Binary to Octal (Hexadecimal):
 - Group the binary digits into three (four) bit groups starting at the radix point and going both ways, padding with zeros as needed in the fractional part.
 - Convert each group of three bits to an octal (hexadecimal) digit.

Octal (Hexadecimal) to Binary and Back

Example:

$$(67.731)_8 = (110\ 111\ .111\ 011\ 001)_2$$

 $(312.64)_8 = (011\ 001\ 010\ .110\ 1)_2$
 $(11\ 111\ 101\ .010\ 011\ 11)_2 = (375.236)_8$
 $(10\ 110.11)_2 = (26.6)_8$
 $(3AB4.1)_{16} = (0011\ 1010\ 1011\ 0100\ .0001)_2$
 $(21A.5)_{16} = (0010\ 0001\ 1010\ .0101)_2$
 $(1001101.01101)_2 = (0100\ 1101.\ 0110\ 1000\)_2 = (4D.68)_{16}$
 $(110\ 0101.101)_2 = (65.A)_{16}$

Octal to Hexadecimal via Binary

- Convert octal to binary.
- Use groups of <u>four bits</u> and convert as above to hexadecimal digits.
- Example: Octal to Binary to Hexadecimal

6 3 5 . 1 7 7 ₈

Restate: 110|011|101.001|111|111₂

Regroup: 1|1001|1101 . 0011|1111|1(000)₂

Convert: 1 9 D . 3 F 8_{16}

Why do these conversions work?

Complements

- At times, data are stored in complement form to represent negative numbers.
- Two systems used to represent negative data:
 - radix
 - radix 1 complement (earliest)

Complements

- Two complements:
 - Radix Complement
 - r's complement for radix r
 - 2's complement in binary
 - Defined as $r^n N$
 - Diminished Radix Complement of N
 - (r-1)'s complement for radix r
 - 1's complement for radix 2
 - Defined as $(r^n 1) N$
- Subtraction is done by adding the complement of the subtrahend
- If the result is negative, takes its 2's complement

Binary 1's Complement(反码)

- For r = 2, $N = 01110011_2$, n = 8 (8 digits): $(r^n 1) = 256 1 = 255_{10}$ or 11111111_2
- The 1's complement of 01110011₂ is then: 11111111
 - 01110011 10001100
- Since the 2^n-1 factor consists of all 1's and since 1-0=1 and 1-1=0, the one's complement is obtained by complementing each individual bit (bitwise NOT).

Binary 2's Complement(补码)

• For r = 2, $N = 01110011_2$, n = 8 (8 digits), we have:

$$(\mathbf{r}^{\mathbf{n}}) = 256_{10} \text{ or } 100000000_2$$

The 2's complement of 01110011 is then:

100000000

- $-\frac{01110011}{10001101}$
- Note the result is the 1's complement plus
 1, a fact that can be used in designing hardware

Signed Integers

The leftmost bit represents the sign in machine number

Binary Code

Machine number

Example: $+1011 \rightarrow$

sign number value 0 ()

 $-1011 \rightarrow$

sign

number value

Signed Integer Representations

- Signed-Magnitude here the n 1 digits are interpreted as a positive magnitude.
- •Signed-Complement here the digits are interpreted as the rest of the complement of the number. There are two possibilities here:
 - Signed 1's Complement
 - Uses 1's Complement Arithmetic
 - Signed 2's Complement
 - Uses 2's Complement Arithmetic

Signed Integer Representation Example

$$r = 2, n = 3$$

$$S2C(X) = -w_{n-1} \cdot 2^{n-1} + \sum_{i=0}^{n-2} w_i \cdot 2^{i}$$

Number	Sign - Mag.	1's Comp.	2's Comp.
+3	011	011	011
+2	010	010	010
+1	001	001	001
+0	000	000	000
-0	100	111	
-1	101	110	111
-2	110	101	110
-3	111	100	101
-4	<u> </u>		100

1-4 COMPUTER DATA FORMATS

- Successful programming requires a precise understanding of data formats.
- Commonly, data appear as ASCII, Unicode, BCD, signed and unsigned integers, and floating-point numbers (real numbers).
- Other forms are available but are not commonly found.

ASCII and Unicode Data

- ASCII (American Standard Code for Information Interchange) data represent alphanumeric characters in computer memory.
- Standard ASCII code is a 7-bit code.
 - eighth and most significant bit used to hold parity
- If used with a printer, most significant bits are
 0 for alphanumeric printing; 1 for graphics.
- In PC, an extended ASCII character set is selected by placing 1 in the leftmost bit.

- Extended ASCII characters store:
 - some foreign letters and punctuation
 - Greek & mathematical characters
 - box-drawing & other special characters
- Extended characters can vary from one printer to another.
- ASCII control characters perform control functions in a computer system.
 - clear screen, backspace, line feed, etc.
- Enter control codes through the keyboard.
 - hold the Control key while typing a letter

- Many Windows-based applications use the Unicode system to store alphanumeric data.
 - stores each character as 16-bit data
- Codes 0000H–00FFH are the same as standard ASCII code.
- Remaining codes, 0100H–FFFFH, store all special characters from many character sets.
- Allows software for Windows to be used in many countries around the world.
- For complete information on Unicode, visit: http://www.unicode.org

Binary Coded Decimal (BCD)

- The range of a BCD digit extends from 0000₂ to 1001₂, for 0–9 decimal. BCD can be stored in two forms.
- Stored in packed BCD form:
 - packed BCD data stored as two digits per byte;
 - used for BCD addition and subtraction in the instruction set of the microprocessor or BCD counting
- Stored in unpacked BCD form:
 - unpacked BCD data stored as one digit per byte
 - returned from a keypad or keyboard

Decimal	packed BCD	unpacked BCD				
12	0001 0010	0000 0001 0000 0010				
96	1001 0110	0000 1001 0000 0110				

- Applications requiring BCD data are point-ofsales terminals.
 - also devices that perform a minimal amount of simple arithmetic
- If a system requires complex arithmetic, BCD data are seldom used.
 - there is no simple and efficient method of performing complex BCD arithmetic

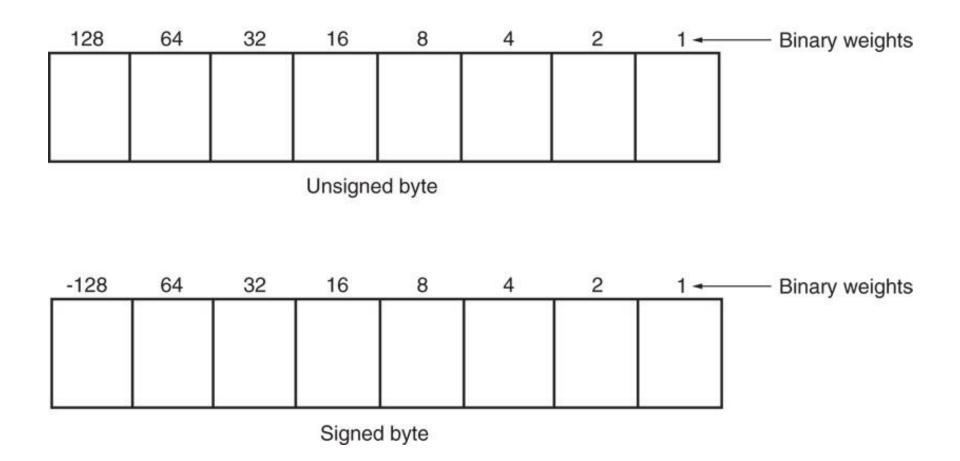
Warning: Conversion or Coding?

- Do NOT mix up conversion of a decimal number to a binary number with coding a decimal number with a BINARY CODE.
- $13_{10} = 1101_2$ (This is <u>conversion</u>)
- 13 \Leftrightarrow 0001|0011 (This is coding)

Byte-Sized Data

- Stored as unsigned and signed integers.
- Difference in these forms is the weight of the leftmost bit position.
 - value 128 for the unsigned integer
 - minus 128 for the signed integer
- In signed integer format, the leftmost bit represents the sign bit of the number.
 - also a weight of *minus* 128

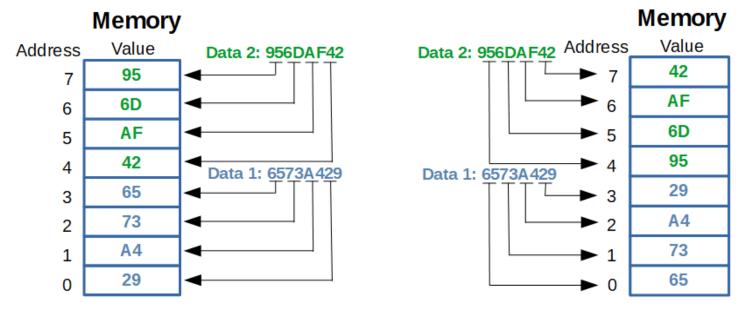
Figure 1–14 The unsigned and signed bytes illustrating the weights of each binary-bit position.



- Unsigned integers range 00H to FFH (0–255)
- Signed integers from –128 to 0 to + 127.
- Negative signed numbers represented in this way are stored in the two's complement form.
- Evaluating a signed number by using weights of each bit position is much easier than the act of two's complementing a number to find its value.
 - especially true in the world of calculators designed for programmers

Word-Sized Data

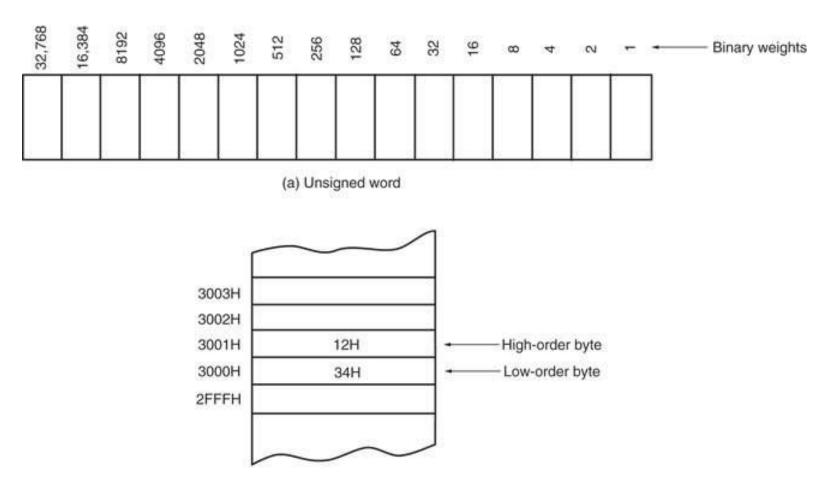
- A word (16-bits) is formed with two bytes of data. The data is stored in little-endian format:
 - The least significant byte always stored in the lowest-numbered memory location.
 - Most significant byte is stored in the highest.



Little-endian format

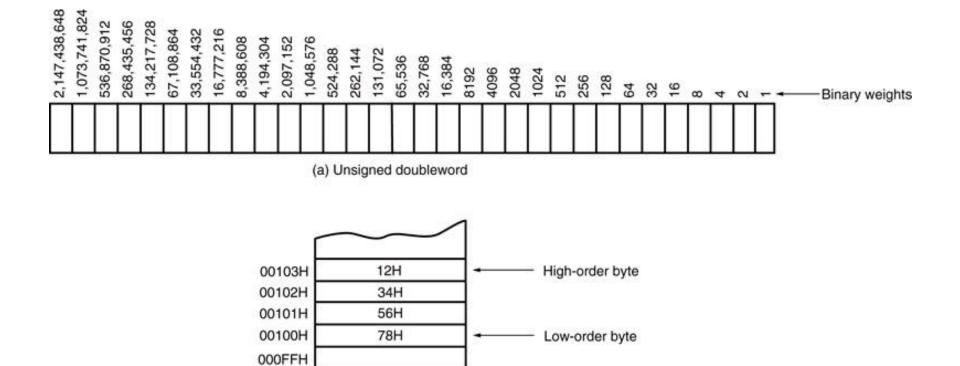
Big-endian format

Figure 1–15 The storage format for a 16-bit word in (a) a register and (b) two bytes of memory.



(b) The contents of memory location 3000H and 3001H are the word 1234H.

Figure 1–16 The storage format for a 32-bit word in (a) a register and (b) 4 bytes of memory.



(b) The contents of memory location 00100H-00103H are the doubleword 12345678H.

- Alternate method is called the big endian format.
- Numbers are stored with the lowest location containing the most significant data.
- Not used with Intel microprocessors.
- The big endian format is used with the Motorola family of microprocessors.

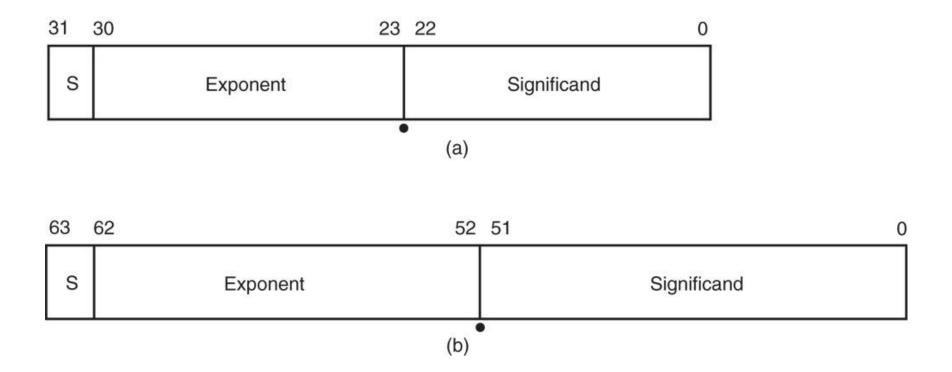
Doubleword-Sized Data

- **Doubleword-sized data** requires four bytes of memory because it is a 32-bit number.
 - appears as a product after a multiplication
 - also as a dividend before a division
- Define using the assembler directive define doubleword(s), or DD.
 - also use the DWORD directive in place of DD

Real Numbers

- Since many high-level languages use Intel microprocessors, real numbers are often encountered.
- A real, or a floating-point number contains two parts:
 - a mantissa, significand, or fraction
 - an exponent.
- A 4-byte number is called single-precision.
- The 8-byte form is called double-precision.

Figure 1–17 The floating-point numbers in (a) single-precision using a bias of 7FH and (b) double-precision using a bias of 3FFH.



- The assembler can be used to define real numbers in single- & double-precision forms:
 - use the DD directive for single-precision 32-bit numbers
 - use define quadword(s), or DQ to define 64-bit double-precision real numbers
- Optional directives are REAL4, REAL8, and REAL10.
 - for defining single-, double-, and extended precision real numbers

MASM Assembler Directive for Data Allocation

Directives	Size in bits	Data types
BYTE (DB)	8	Unsigned integer
SBYTE	8	Signed integer
WORD (DW)	16	Unsigned integer
SWORD	16	Signed integer
DWORD (DD)	32	Unsigned integer
SDWORD	32	Signed integer
FDWORD	48	Unsigned integer
QWORD (DQ)	64	Unsigned integer
TBYTE (DT)	80	Unsigned integer
REAL4	32	Single-precision FP (IEEE 754)
REAL8	64	Double-precision FP (IEEE 754)
REAL10	80	Extended FP

SIMD and Miscellaneous Data Types

 The x86 supports a variety of packed data types, which are employed to perform SIMD calculations.

Numerical Type	xmmword	ymmword	zmmword	
8-bit integer	16	32	64	
16-bit integer	8	16	32	
32-bit integer	4	8	16	
64-bit integer	2	4	8	
Single-precision floating-point	4	8	16	
Double-precision floating-point	2	4	8	

 The x86 platform also supports a number of miscellaneous data types including strings, bit fields, and bit strings.

- In the 1960's and 1970's, each line of computers supported its own range and precision for its floating point numbers, and rounded off arithmetic operations in its own peculiar way.
- IEEE 754 standard was officially adopted in 1985 based on Kahan's design model.



William Morton Kahan 1933-1989 Turing Prize

 Kahan won the ACM's Turing Award in 1989 for his work in creating IEEE 754 standard, and he has often been called "The Father of Floating Point".

From: An Interview with the Old Man of Floating-Point

- IEEE 754 uses the idea of scientific notation:
 - sign bit: 0, the number is positive; 1, the number is negative;
 - normalized fraction/mantissa
 - biased exponent: a bias is added to the actual exponent for high speed comparisons. 2^E-1 and 0 have special meanings.

$$(-1)^{ ext{sign bit}}(1 + ext{fraction}) imes 2^{ ext{exponent - bias}}$$

E.g.,

value =
$$(-1)^{0} \times (1+0.25) \times 2^{124-127} = 0.15625$$

Parameter	binary16	binary32	binary64	binary128	binary $\{k\}$ $(k \ge 128)$	
k, storage width in bits	16	32	64	128	multiple of 32	
p, precision in bits	11	24	53	113	k – round($4 \times \log_2(k)$) + 13	
emax, maximum exponent e	15	127	1023	16383	$2^{(k-p-1)}-1$	
Encoding parameters						
bias, E-e	15	127	1023	16383	emax	
sign bit	1	1	1	1	1	
w, exponent field width in bits	5	8	11	15	$round(4 \times \log_2(k)) - 13$	
t, trailing significand field width in bits	10	23	52	112	k - w - 1	
k, storage width in bits	16	32	64	128	1 + w + t	

Binary interchange format parameters

From IEEE 754-2019

Parameter	decimal32	ecimal32 decimal64		$\mathbf{decimal}\{k\} \ (k \ge 32)$			
k, storage width in bits	32	64	128	multiple of 32			
p, precision in digits	7	16	34	$9 \times k/32 - 2$			
emax	96	384	6144	$3 \times 2^{(k/16+3)}$			
Encoding parameters							
bias, E-q	101	398	6176	emax + p - 2			
sign bit	1	1	1	1			
w+5, combination field width in bits	11	13	17	k/16 + 9			
t, trailing significand field width in bits	20	50	110	15×k/16 – 10			
k, storage width in bits	32	64	128	1 + 5 + w + t			

Decimal interchange format parameters

From IEEE 754-2019

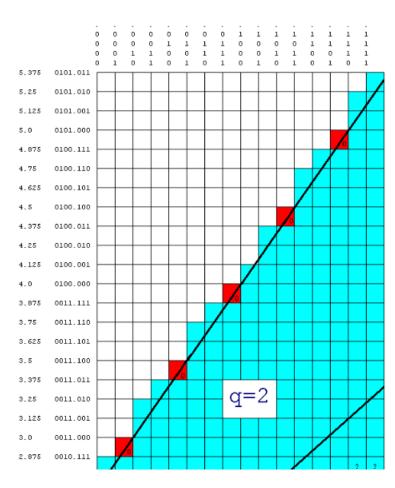
- There are some special cases:
 - Zero: sign bit = 0 and 1 for +0 and -0; biased exponent = all 0 bits; and the fraction = all 0 bits;
 - Infinity: sign bit = 0 and 1 for positive and negative infinity;
 biased exponent = all 1 bits; and the fraction = all 0 bits;
 - NaN (Not-A-Number): sign bit = 0 or 1; biased exponent = all 1 bits; and the fraction is anything but all 0 bits.

- The IEEE 754 includes five rounding modes:
 - default: roundTiesToEven
 - optional:roundTiesToAway,roundTowardPositive, roundTowardNegative,roundTowardZero

Mode / Example Value	+11.5	+12.5	-11.5	-12.5
to nearest, ties to even	+12.0	+12.0	-12.0	-12.0
to nearest, ties away from zero	+12.0	+13.0	-12.0	-13.0
toward 0	+11.0	+12.0	-11.0	-12.0
toward +∞	+12.0	+13.0	-11.0	-12.0
toward -∞	+11.0	+12.0	-12.0	-13.0

The Pentium FDIV Flaw

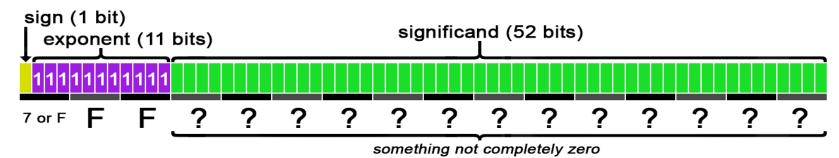
- The Pentium processor was introduced in 1993. A year later it was discovered that in certain very rare instances a division operation returned a result that was slightly incorrect.
- The Pentium uses a SRT division algorithm for floating point divisions. However, there were 5 error cells in lookup table.
- FDIV flaw cost Intel half a billion dollars.



The Pentium lookup table

NaN-Boxing Technology

In IEEE-754, 52 bit patterns that represent NaN can be encoded to carry data (e.g. 4-bit tag and 48-bit index).



NaN-Boxing technique

```
double ref;
       double set na(){
           if (!ref) {
               ref=0/0.;
               int *ci = (int *)(&ref);
               char *cr = (char *)(&ref);
markers
              ci[0]=124;
               cr[4]='a';
           return ref;
           set markers in a NaN
```

```
void read from na(double in){
    if (!isnan(in)) return ;
    char cc;
    char *cr = (char *)(&ref);
    cc = cr[4];
    int ii;
    int *ci = (int *)(&ref);
    ii = ci[0];
    printf("the integer is %d\n",ii);
    printf("the character is %c\n",cc);
```

Assignment

1-55, 58, 59, 65, 71, 75, 78, 80, 81, 82