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We can easily have:

$$\overline{AB}(A + B) = (\bar{A} + \bar{B})(A + B) = A\bar{B} + \bar{A}B = A \oplus B$$

So from the logic diagram we can have:

$$S_0 = C_0 \oplus (\overline{A_0 B_0}(A_0 + B_0)) = C_0 \oplus A_0 \oplus B_0$$

Also

$$C_0 = \overline{\overline{A_0 + B_0} + (\overline{A_0 B_0})\bar{C}_0} = A_0 B_0 + (A_0 + B_0)C_0$$

So it is a full adder.

3-51

1001 1100

1's complement: 0110 0011

2's complement: 0110 0100

1001 1101

1's complement: 0110 0010

2's complement: 0110 0011

1010 1000

1's complement: 0101 0111

2's complement: 0101 1000

0000 0000

1's complement: 1111 1111

2's complement: 0000 0000

1000 0000

1's complement: 0111 1111

2's complement: 1000 0000

3-52

(a)

$$\begin{aligned} & 11010 - 10001 \\ &= 11010 + 01111 \\ &= 01001 \end{aligned}$$

(b)

$$\begin{aligned} & 11110 - 1110 \\ &= 11110 - 01110 \\ &= 11110 + 10010 \\ &= 10000 \end{aligned}$$

(c)

$$\begin{aligned} & 1111\ 110 - 1111\ 110 \\ &= 0000\ 000 \end{aligned}$$

(d)

$$\begin{aligned} & 1010\ 01 - 101 \\ &= 1010\ 01 - 0001\ 01 \\ &= 1010\ 01 + 1110\ 11 \\ &= 1001\ 00 \end{aligned}$$

3-59

Starting from the the highest digit, compare the digits of A and B one by one.

Or we can consider an extension of A and B, with 2's complement we can apply subtraction of two signed numbers.

For the first method:

$$\begin{aligned} X &= \overline{A_3}B_3 + (A_3B_3 + \overline{A_3}\overline{B_3})\overline{A_2}B_2 \\ &\quad + (A_3B_3 + \overline{A_3}\overline{B_3})(A_2B_2 + \overline{A_2}\overline{B_2})\overline{A_1}B_1 \\ &\quad + (A_3B_3 + \overline{A_3}\overline{B_3})(A_2B_2 + \overline{A_2}\overline{B_2})(A_1B_1 + \overline{A_1}\overline{B_1})\overline{A_0}B_0 \end{aligned}$$

