

课后练习18

$$W(i, j) = Q(i) + \sum_{l=i+1}^j Q(l) + P(l)$$

$$C(i, j) = \min_{i < k < j} \{C(i, k-1) + C(k, j)\} + W(i, j)$$

$$P(1 : 4) = (3, 3, 1, 1)$$

$$Q(0 : 4) = (1, 3, 2, 1, 1)$$

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$$j-i=1, \quad 0 \leq i < 4$$

$$W(0,1)=Q(0)+Q(1)+P(1)=1+3+3=7$$

$$C(0,1)=0+7=7$$

$$R(0,1)=k=1$$

$$W(1,2)=Q(1)+Q(2)+P(2)=3+2+3=8$$

$$C(1,2)=0+8=8$$

$$R(1,2)=k=2$$

$$W(2,3)=Q(2)+Q(3)+P(3)=2+1+1=4$$

$$C(2,3)=4$$

$$R(2,3)=k=3$$

$$W(3,4)=Q(3)+Q(4)+P(4)=1+1+1=3$$

$$C(3,4)=3$$

$$R(3,4)=k=4$$

∅

$$j-i=2 \quad 0 \leq i < 3$$

$$W(0,2)=Q(0)+Q(1)+P(1)+Q(2)+P(2)=1+3+3+2+3=12$$

$$C(0,2)=\min(8, 7)+W(0,2)=19$$

$$R(0,2)=2$$

$$W(1,3)=3+2+3+1+1=10$$

$$C(1,3)=\min(C(1,1)+C(2,3), C(1,2)+C(3,3))+W(1,3)=14$$

$$R(1,3)=2$$

$$W(2,4)=2+1+1+1+1=6$$

$$C(2,4)=\min(C(2,2)+C(3,4), C(2,3)+C(4,4))+W(2,4)=9$$

$$R(2,4)=3$$

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$$j-i=3 \quad 0 \leq i < 2$$

$$W(0,3)=1+3+2+1+3+3+1=14$$

$$C(0,3)=\min(C_{00}+C_{13}, C_{01}+C_{23}, C_{02}+C_{33})+W_{03}=\min(14, 7+4, 19)+14=25$$

$$R(0,3)=2$$

$$W(1,4)=3+2+1+1+3+1+1=12$$

$$C(1,4)=\min(C_{11}+C_{24}, C_{12}+C_{34}, C_{13}+C_{44})+W_{14}=\min(9, 11, 14)+12=21$$

$$R(1,4)=2$$

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$$j-i=4$$

$$W(0,4)=1+7+8=16$$

$$C(0,4)=\min(C_{00}+C_{14}, C_{01}+C_{24}, C_{02}+C_{34}, C_{03}+C_{44})+W_{04}=\min(21, 16, 22, 25)+16=32$$

$$R(0,4)=2$$

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$$T(0,4)=2 \rightarrow T(0,1), T(2,4)$$

$$T(0,1)=1 \rightarrow T(0,0), T(1,1)$$

$$T(2,4)=3 \rightarrow T(2,2), T(3,4)$$

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              if
            /  \
          do   stop
        /  \  /  \
      E0 E1 E2 then

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/ \
E3 E4