# O PyTorch

## 交叉熵

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#### Why not MSE?

Label	predict	correct
3	[0.3, 0.3, 0.4]	yes
2	[0.3, 0.4, 0.3]	yes
1	[0.1, 0.2, 0.7]	no



Label	predict	correct
3	[0.1, 0.2, 0.7]	yes
2	[0.1, 0.7, 0.2]	yes
1	[0.3, 0.4, 0.3]	no



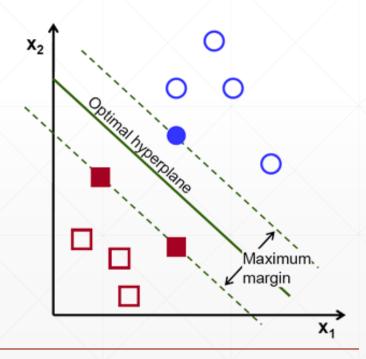
#### Loss for classification

MSE

Cross Entropy Loss

Hinge Loss
 SVM

$$\sum_i max(0,1-y_i*h_ heta(x_i))$$

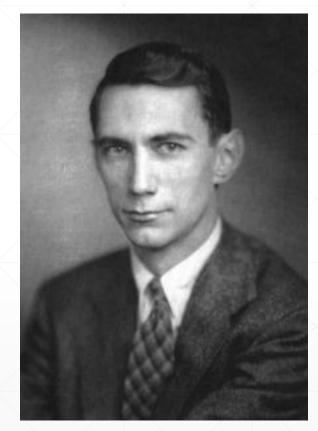


#### **Entropy**

- Uncertainty
- measure of surprise

higher entropy: higher uncertainty.

$$Entropy = -\sum_{i} P(i) \log P(i)$$



Claude Shannon

#### Lottery

```
In [2]: a=torch.full([4],1/4.)
tensor([0.2500, 0.2500, 0.2500, 0.2500])
In [4]: a*torch.log2(a)
Out[4]: tensor([-0.5000, -0.5000, -0.5000, -0.5000])
In [6]: -(a*torch.log2(a)).sum()
Out[6]: tensor(2.)
In [7]: a=torch.tensor([0.1,0.1,0.1,0.7])
In [8]: -(a*torch.log2(a)).sum()
Out[8]: tensor(1.3568)
In [15]: a=torch.tensor([0.001,0.001,0.001,0.999])
In [16]: -(a*torch.log2(a)).sum()
Out[16]: tensor(0.0313)
```



#### **Cross Entropy**

$$H(p,q) = -\sum p(x)\log q(x)$$

$$H(p,q) = H(p) + D_{\mathrm{KL}}(p|q).$$

- P=Q
  - cross Entropy = Entropy

- for one-hot encoding,
  - entropy =  $1\log 1=0$



#### **Binary Classification**

$$\begin{split} H(P,Q) &= -P(cat)\log Q(cat) - (1-P(cat))\log(1-Q(cat)) \\ P(dog) &= (1-P(cat)) \\ H(P,Q) &= -\sum_{i=(cat,dog)} P(i)\log Q(i) \\ &= -P(cat)\log Q(cat) - P(dog)\log Q(dog) \\ -(y\log(p) + (1-y)\log(1-p)) \end{split}$$

#### for example











$$P_1 = [1 \quad 0 \quad 0 \quad 0 \quad 0]$$

$$Q_1 = \begin{bmatrix} 0.4 & 0.3 & 0.05 & 0.05 & 0.2 \end{bmatrix}$$

$$H(P_1, Q_1) = -\sum_i P_1(i) \log Q_1(i)$$

$$= -(1\log 0.4 + 0\log 0.3 + 0\log 0.05 + 0\log 0.05 + 0\log 0.2)$$

$$=-\log 0.4$$

$$\approx 0.916$$

$$Q_1 = [0.98 \quad 0.01 \quad 0 \quad 0 \quad 0.01]$$

$$H(P_1, Q_1) = -\sum_{i} P_1(i) \log Q_1(i)$$

$$= -(1\log 0.98 + 0\log 0.01 + 0\log 0 + 0\log 0 + 0\log 0.01)$$

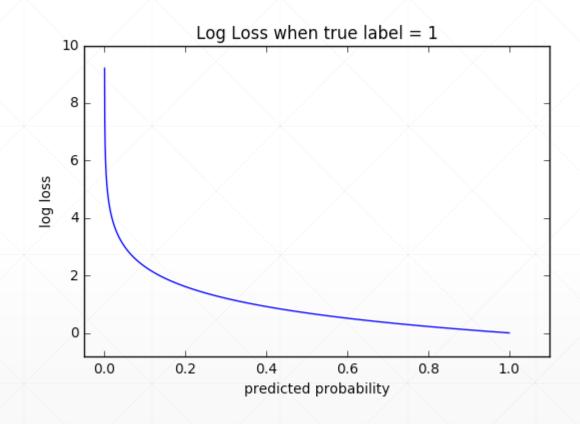
$$= -\log 0.98$$

$$\approx 0.02$$

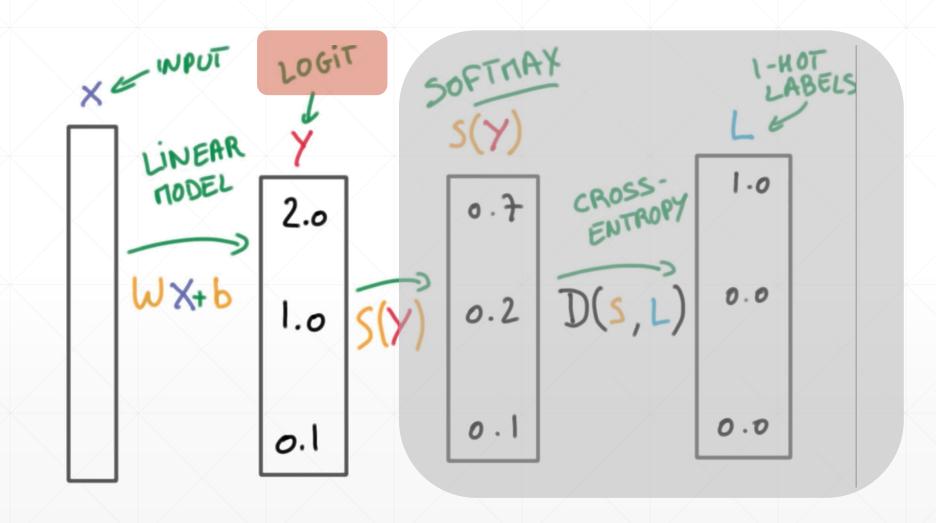
#### why not use MSE

- sigmoid + MSE
  - gradient vanish
- converge slower

- But, sometimes
  - e.g. meta-learning



#### **Therefore**



#### **Numerical Stability**

```
In [17]: x=torch.randn(1,784)
In [18]: w=torch.randn(10,784)
In [19]: logits=x@w.t()
Out[20]: torch.Size([1, 10])
In [34]: pred=F.softmax(logits, dim=1)
Out[37]: torch.Size([1, 10])
In [40]: pred_log=torch.log(pred)
In [41]: F.cross_entropy(logits,torch.tensor([3]))
Out[41]: tensor(82.4905)
In [42]: F.nll_loss(pred_log, torch.tensor([3]))
Out[42]: tensor(82.4905)
```

## 下一课时

实战多分类问题

### Thank You.