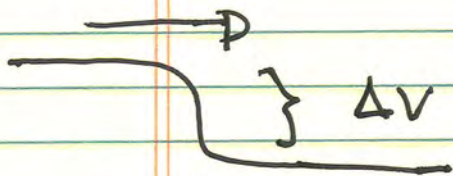


Supplement: Gas Dynamic Shocks Lecture III

a) Scale

Consider Burgers Eqn.

$$\partial_t V + v \partial_x V - \nu \partial_x^2 V = 0$$



for shock width

$$\frac{\Delta V}{W} \frac{\Delta V}{W} \sim \nu \frac{\Delta V}{W^2}$$

$$W \sim \nu / \Delta V$$

dissipation
sets shock
thickness

for $\nu \sim l_{mf} c_s$

$$\Delta V \sim c_s$$

$$W \sim l_{mf}$$

characteristic
thickness of
shock layer.

6.2 Entropy Production

In gas-dynamics

- initially ideal dynamics

- entropy constant

but 

pulse steepens and shocks

- sharp gradients produced in shock

- \Rightarrow couple to diffusive dissipation

- \Rightarrow drive collisional transport

- \Rightarrow produce entropy.

N.B. :- Entropy production required in shock

- sets arrow of time

- to calculate:

→ factor #

$$\frac{dS}{dt} = () \left(-\Gamma_x \nabla X \right) \rightarrow$$

$\nabla X \rightarrow$ thermodynamic force

$\Gamma_x \rightarrow$ flux

i.e. $\Gamma_x = -D_x \nabla X$

$$dS/dt \sim () D_x (\nabla X)^2$$

↓
entropy production rate density

then, for Burgers shock:

$$dS/dt \sim \nu (\partial_x v)^2$$

$$\sim \nu \frac{(\Delta v)^2}{w^2} \sim \nu (\Delta v)^2 \frac{(\Delta v)^2}{v^2}$$

$$\sim (\Delta v)^4 / \nu$$

but, total entropy production ~~is~~
 is integrated over shock thickness

$$\int dx \frac{dS}{dt} \sim \frac{dS}{dt} \sim W \frac{dS}{dt}$$

$$\sim \frac{v}{\Delta v} \frac{v}{v^2} (\Delta v)^2 (\Delta v)^2$$

$$\sim (\Delta v)^3$$

so total entropy production:

$$dS/dt \sim (\Delta v)^3$$

- independent of v !

- entropy / heating produced by collisions but total dS/dt independent of v .