



Computational Methods

Final Project: AGB-WD

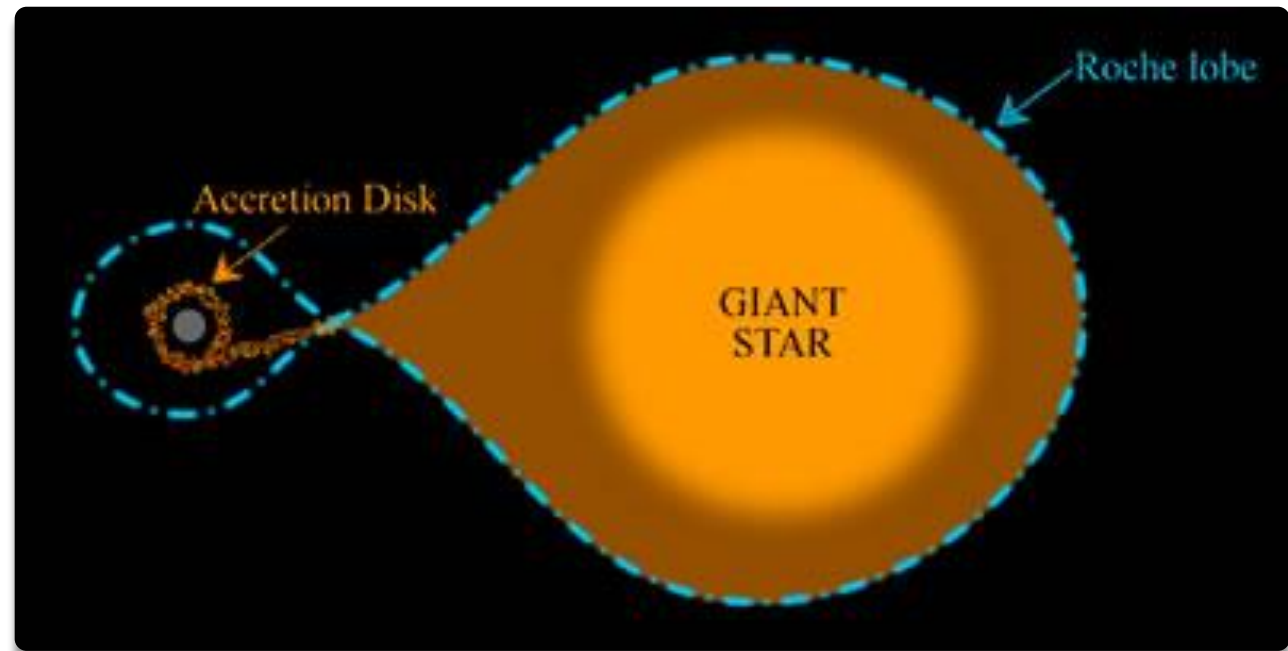
Binary Mass Transfer

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GITHUB LINK: [HTTPS://GITHUB.COM/ZRD7527/ASTP720.GIT](https://github.com/ZRD7527/ASTP720.GIT)

Background

- ▶ If 2 stars are in a binary orbit, mass can be transferred between them
- ▶ Mass is transferred when one star (or both) fill their “Roche Lobe”
- ▶ The “Roche Lobe” is an area surrounding a star where material is gravitationally bound to that star (ref. 1)



User Inputs

- ▶ My code is interactive!
- ▶ It requires a lot of inputs and gives warnings if the inputs are outside of normal physical values

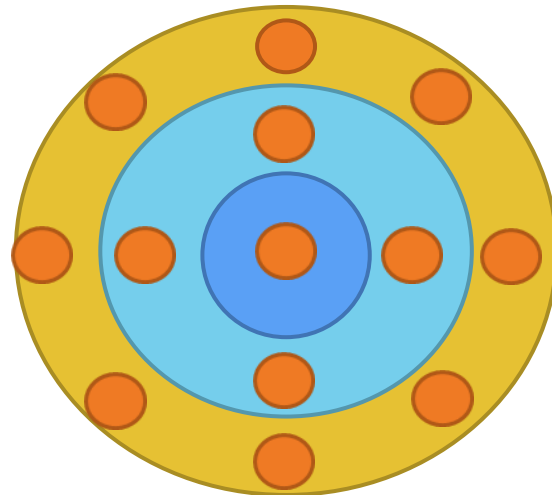
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main()
```

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```

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Mass of red giant star (solar masses): 150
Mass must be between 0.1 and 100 solar masses!
Mass of red giant star (solar masses): 18
Mass of white dwarf star (solar masses): 4
Mass must be between 0.4 and 1.44 solar masses!
Mass of white dwarf star (solar masses): 0.9
Initial rotational velocity of AGB star (km/s): 15
Initial rotational velocity of WD star (km/s): 50
Binary separation (AU): 0.01
```

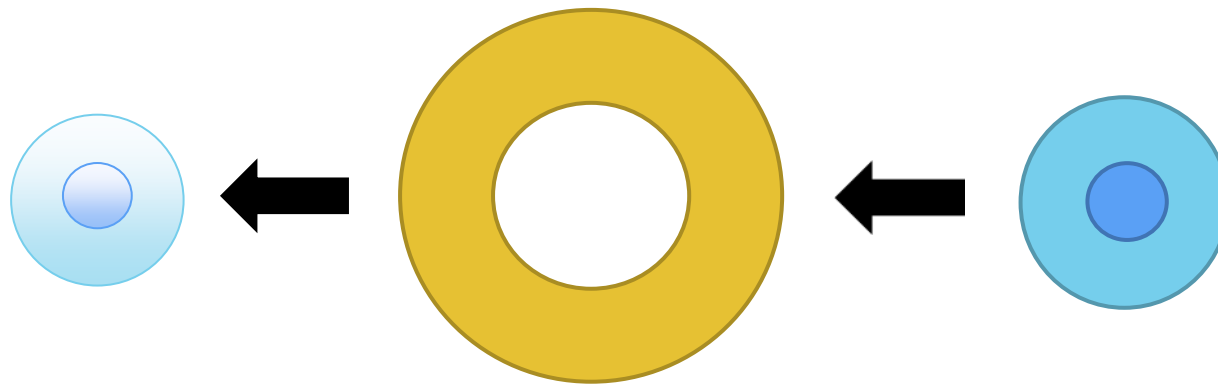
Creating an array of “Star Particles”

- ▶ A variable called resolution is used to build up the star (integrating dm)
- ▶ A resolution of 0.01 corresponds to each “star particle” having a mass of 0.01 solar masses
- ▶ My code builds the star with these by adding shells containing many particles



Solving the Gravitational Potential

- ▶ Once the array is built, the potential from each star is found for shells of the giant star
- ▶ Any outer shells with a greater potential from the white dwarf star are transferred



Exchange of Mass and Angular Momentum

- ▶ The total transferred mass is added to the white dwarf star
- ▶ The transferred angular momentum is used to find the new rotational velocity of each star

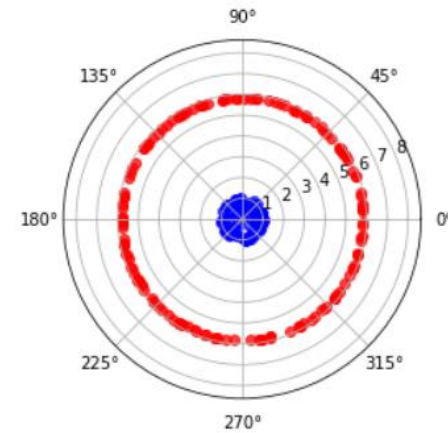
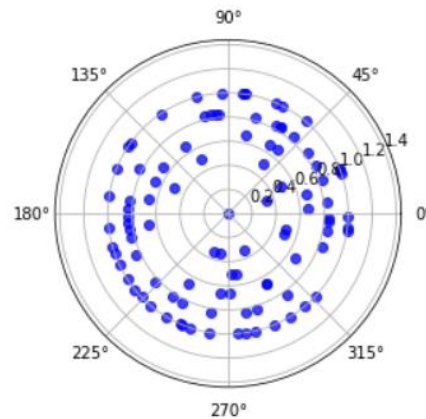
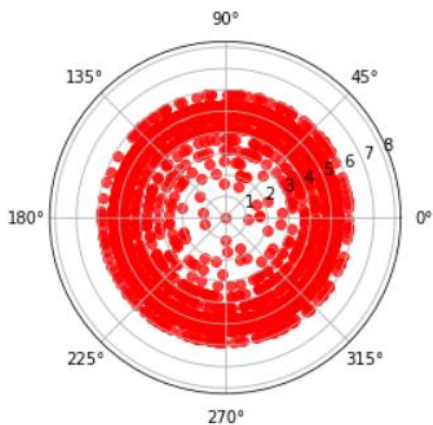
Mass transferred from AGB star to white dwarf: 7.79 Solar Masses

AGB star rotational velocity after mass transfer: 6.8854166666665435 (km/s)

WD star rotational velocity after mass transfer: 58.13858776796397 (km/s)

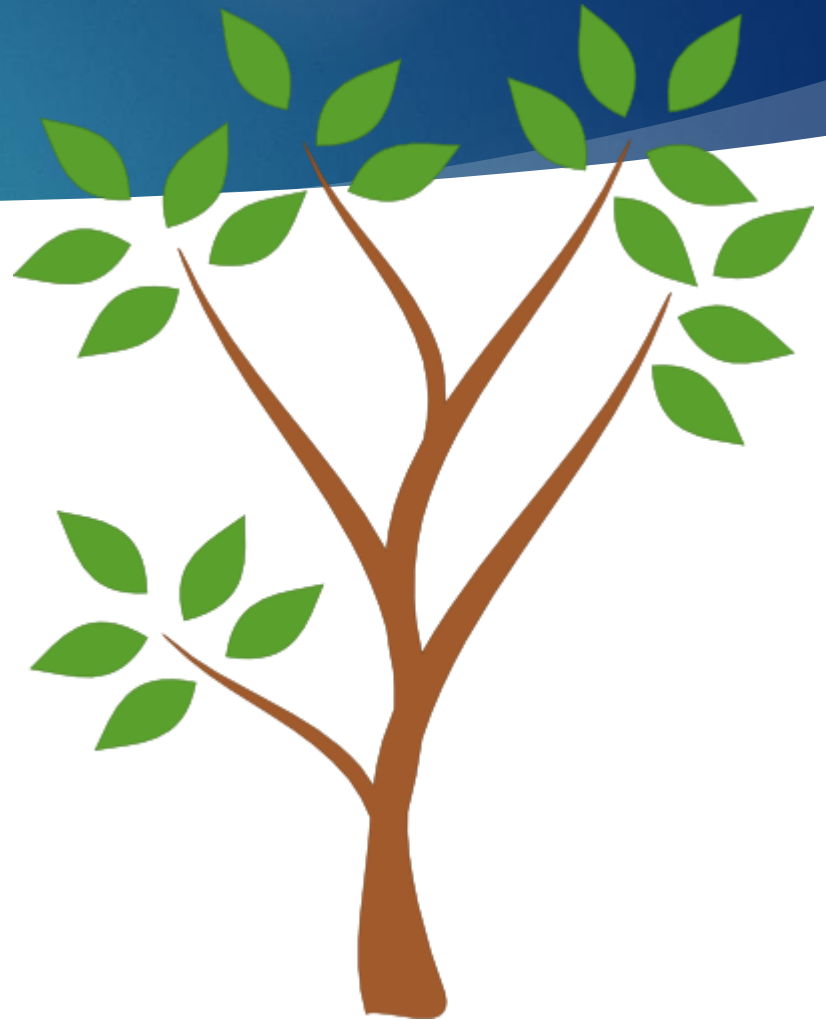
Simulation

- For my simulation I used the radial dimension of each star particle to project the stars onto 2D polar coordinates
- The red giant star is shown in red and the white dwarf in blue
- The last plot shows the outer layers of the AGB star that are transferred to the white dwarf



Future Updates: Algorithm

- ▶ My code would benefit greatly from a tree structure
- ▶ The star particle cluster is currently just a clunky 2D array
- ▶ A tree containing branches for each shell of the star and a leaf for each particle would be much more efficient than an array.



Future Updates: Accuracy and Simulation

- ▶ The system only has 1 time step; having intermediate time steps would increase accuracy
- ▶ My code does not consider orbital velocity or change in orbital separation
- ▶ The mass transfer is lossless
- ▶ Entire shells are removed for the mass transfer
- ▶ The simulation is not 3D



Questions?

References

- ▶ Paczynski, B. (1971). "Evolutionary Processes in Close Binary Systems". Annual Review of Astronomy and Astrophysics. **9**: 183–208.
Bibcode:1971ARA&A...9..183P. doi:10.1146/annurev.aa.09.090171.001151.
- ▶ Hayashi, C. Evolution of stars of small mass in the pre-main sequence stages. Prog. Theor. Phys. (1963)
- ▶ Karttunen, H. Fundamental Astronomy. Springer-Verlag Berlin Heidelberg (2007)
- ▶ Keeton, K.: Principles of Astrophysics. Springer New York Heidelberg Dordrecht London, New York (2014)
- ▶ Nakano, T.: Pre-main Sequence Evolution and the Hydrogen-Burning Minimum Mass. 50 Years of Brown Dwarfs, Astrophysics and Space Science Library Volume 401 (2014)