Lab 4: Dimensionality Reduction

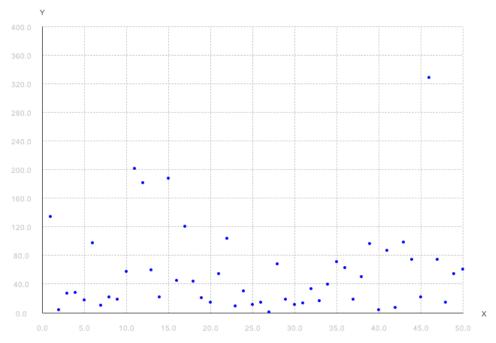
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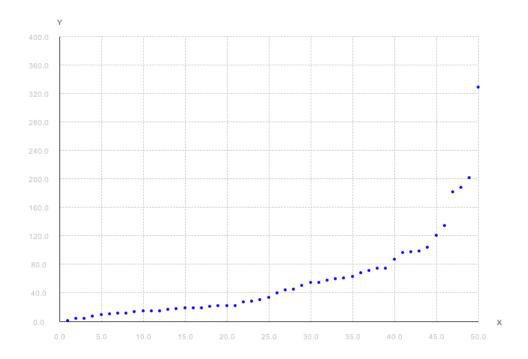
1 Faces

1.1 Dimensionality of the Dataset

- 1. There are 5000 faces and 50 measurements.
- 2. See the *variance-dimension* plot as below:



- 3. I perfer to describe the face with 7 variable parts: hat color, hair length, hair color, eye size, face color, mouth shape, eye color.
- 4. I sorted the variances and get the plot:



5.

1.2 Principal Component Analysis

See file CoActorPrediction.java to view my implementation of the classes.

And I computer MyOwnScorning with:

$$\frac{N(u,v)^2 \times \sqrt{|N(u)-N(v)|}}{N(u)+N(v)}$$

In which N(i) stands for neibour number of i, and N(i, j) stands for common neibour number of i and j.

And Here's accuracy of the 3 link prediction strategies:

Name	Accuracy	Improvement
PreferentialAttachment	2.096%	3.19x
CommonNeighbors	5.114%	7.79x
MyOwnScoring	5.388%	8.21x

2 Random Walks

1. Setting N=10000 and node u as initial seed, the average of a Facebook user is 48.6725, which still has a difference with the reference answer. The problem I think, is the algorithm itself, and maybe node u is in a small component of the network, and maybe the dataset itself changes.

2. I changed walk strategy in my algorithm: every time I walk across 3 people instead of one (i.e. I walk to the node's neighbor's neighbor's neighbor instead of its neighbor), and there's also a repeat judgment in my code. After changing, the estimated age becomes 50.675, which is more close to the reference answer.

2.1 Bizarre Social Networks

1. Setting N = 10000 and using different beginning node, we get average age as below:

Beginning Node	Average Age	Age of Beginning Node
u	50.1445	13
V	55.5635	39
W	64.1295	89

we can see much difference between each other. And we can also find that with younger beginning node we get smaller average age and with older beginning node we get larger average age. Maybe it's the *Herding* property. The friends are seems so familiar.

2. The same strategy as above, now get the answers:

Beginning Node	Average Age	Age of Beginning Node
u	58.721	13
V	58.2856	39
W	57.4979	89

The answeres now become more similar:)

Finally, I use my strategy(this time, walk across 6 people every time) on the *Directions*, get answers:

Beginning Node	Average Age	Age of Beginning Node
u	49.5636	23
V	49.4373	22
W	49.4054	39

So, my estimate of the average age of Directions's users is 49.5.