

## Total Factor Productivity (TFP) Shocks

## Preference Shocks

## TFP in COBB-DOUGLAS PRODUCTION FUNCTION

$$\text{output}_t = A_t f(k_t, n_t) = A_t k_t^\alpha n_t^{1-\alpha}$$

Cobb-Douglas form useful for illustrating effects of TFP shocks

Unexpected change (i.e., a shock) in  $A_t$ 

$$\frac{\partial \text{output}_t}{\partial A_t} = \frac{\partial (A_t k_t^\alpha n_t^{1-\alpha})}{\partial A_t} = k_t^\alpha n_t^{1-\alpha} = A_t^{-1} k_t^\alpha n_t^{1-\alpha}$$

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## demand for labor

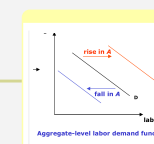
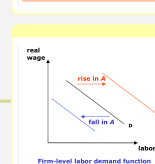
## TFP SHOCKS AND LABOR DEMAND

$$w_t = A_t (1-\alpha) k_t^\alpha n_t^{1-\alpha} (= mpn_t)$$

Because exponent number, can move

$$w_t = A_t (1-\alpha) \left( \frac{k_t}{n_t} \right)^{\frac{1}{1-\alpha}}$$

FOR GIVEN  $r_t$  and  $w_t$ , rise (fall) in  $A_t$  raises (lowers)  $n_t$



IMPLICATION: TFP shocks shift the labor demand curve

## demand for capital

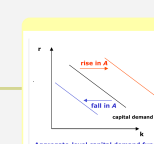
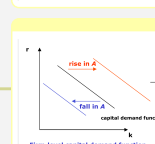
## TFP SHOCKS AND CAPITAL/INVESTMENT DEMAND

$$r_t = A_t \alpha k_t^{\alpha-1} n_t^{1-\alpha} (= mpk_t)$$

Because exponent number, can move

$$r_t = A_t \alpha \left( \frac{n_t}{k_t} \right)^{1-\alpha}$$

FOR GIVEN  $r_t$  and  $w_t$ , rise (fall) in  $A_t$  raises (lowers)  $k_t$



IMPLICATION: TFP shocks shift the capital demand (and hence investment demand) —implies  $\dot{n}_t > 0$ ,  $\dot{k}_t > 0$

## PREFERENCE SHOCKS

## using consumption-leisure framework

Utility function (modified from Chapter 2):  $u(c, l)$

- consumption
- leisure
- preferences change, utility  $u$  is  $\theta$
- Chapter 2: same utility on consuming  $u = 1$

Mechanics of  $\theta$

- Make each unit of  $c$  more (high  $\theta$ ) desirable...
- ...or less (low  $\theta$ ) desirable

Interpretation of  $\theta$

- "Culture" events that alter individuals' preferences
- "Political" events that alter individuals' preferences
- Any other events that alter individuals' preferences

## MRS between consumption and leisure

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c}$$

But now need Chain rule of calculus to compute  $\partial u / \partial \theta$

- Because first argument of  $u$  is now the (variable)  $\theta$ , not simply  $c$

Chain rule:  $\partial u / \partial \theta = u_1(B_C, l) \cdot B$

→ MRS between consumption and leisure

$\theta$  affects MRS in "two" ways

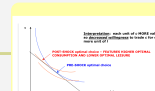
$$\frac{\partial MRS_{c,l}}{\partial \theta} = \frac{\partial}{\partial \theta} \left( \frac{u_1(B_C, l)}{u_2(B_C, l)} \right) = \frac{u_{11}(B_C, l) \cdot B + u_{12}(B_C, l)}{u_2(B_C, l)^2}$$

## PREFERENCE SHOCKS AND INDIFFERENCE MAPS

POSITIVE SHOCK TO  $\theta$ 

$$MRS_{c,l} = \frac{\partial u / \partial l}{\partial u / \partial c} = \frac{u_1(B_C, l)}{u_2(B_C, l)}$$

Since  $\theta$  is a parameter of the utility function, it affects the MRS at any point in  $(c, l)$  space.

IF  $\theta$  RISES

Rise in  $\theta$  rotates all indifference curves (i.e., rotates MRS at any point in  $(c, l)$  space).

Interpretation: each unit of  $c$  more valuable, so decrease willingness to trade a for one more unit of  $l$



Fall in  $\theta$  rotates all indifference curves (i.e., rotates MRS at any point in  $(c, l)$  space).

Interpretation: each unit of  $c$  less valuable, so increase willingness to trade a for one more unit of  $l$

Superimpose a budget line: optimal choice of  $c$  and  $l$  clearly affected by shock to  $\theta$ 

## PREVIEW OF BUSINESS CYCLE THEORY



## Supply shocks: TFP shocks, others

## Demand shocks: preference shocks, monetary policy shocks, others

Shocks now focus on changes over time in:

- technology: technological shock, energy and climate
- preferences: preference shocks, monetary policy shocks
- supply: supply shocks, supply shocks