Toy Models of Superposition Replication and Findings

Abstract

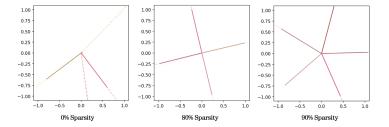
Toy Models of Superpostion[1] is a groundbreaking paper published by researchers affilated with Anthropic and Harvard University in 2022. By investigating small models with under 100 neurons, the paper demonstrates that neural networks can represent more features than they have demensions. Additionally, they use these so called "toy models" to understand the relationship between how neural networks are trained and how they represent the data internally. This paper was able to the finding from this paper and make new observations about "toy models" and how they behave under different training circumstances.

1 Introduction

The original paper motivates the idea of superpostion with the following graphic:



The basic idea is this: if you think of each feature as being represented inside a nueral network as a direction, you can graph these directions and observe them. In the graphic above, the researchers studied a model with two neurons and five inputs. Recreating this model showed the same results when sparsity was varied. A replication of the original graphic can be found below and the code used to generate it can be found here.



Although this example only has two neurons (meaning it can be graphed in 2D), in future sections we will see how similar approachs scale nicely to models with more neurons. As far as I understand, it is still unclear weather the ideas dicussed in the original paper can be scaled to help understand and identify bias in much larger models such as GTP-4, Claude 2, or Gemini.

2 Background and Motivation

In this section of Toy Models of Superpostion[1], the authors provide context and define terms. In this paper, I make a few additional comments about some of the key ideas and terms the authors discuss.

(1) Defining Features: The original paper Toy Models of Superpostion defines features broadly as "properties of the input which a sufficiently large neural network will reliably dedicate a neuron to representing." The authors do however describe this definition as "slightly circular" and note that they are not "overly attached to it." I find the definition especially problematic because a network that is small or has unconventional archetecture may represent a feature that a larger network or a network with a more typical archetecture may represent. These representations are clearly still features, but are not treated as so under the original definition.

As a result, I propose an alternative definition: features are aspects of the input that a neural network represents accuratly with a higher propability than a randomly initialized network. In other words, features are parts of the input that a model determines to be important enough to represent internally.

- (2) Role of linear functions in Neural Networks: The original authors of Toy Models of Superpostion strongly emphasize the role of linear functions in neural networks. They claim that "Linear representations are the natural format for neural networks to represent information in!" Although this is clearly mostly true, I dont think there is sufficient evidence to justify the confidence of the authors in the original paper. Nonlinearities are also clearly doing lots of useful computation and it seems just as important to study their role in how a neural network represents features from layer to layer. The nonlinearity at each layer of a neural network may be just as important as the linear transformation in understanding how a model makes decisions.
- (3) **Defining Superposition:** The original paper has a fantastic and simple defination for Superposition: "Roughly, the idea of superposition is that neural networks 'want to represent more features than they have neurons', so they exploit a property of high-dimensional spaces to simulate a model with many more neurons." This is the definition I will used throughout this paper.

3 Demonstrating Superposition

References

[1] Nelson Elhage, Tristan Hume, Catherine Olsson, Nicholas Schiefer, Tom Henighan, Shauna Kravec, Zac Hatfield-Dodds, Robert Lasenby, Dawn Drain, Carol Chen, Roger Grosse, Sam McCandlish, Jared Kaplan, Dario Amodei, Martin Wattenberg, and Christopher Olah. Toy models of superposition, 2022.