

Performance

Elliott Johnson



O1 General 12

Performance legislation

- Performance class A aeroplane: > 9 Pax or 5700 kg and all multi-engined jet aeroplane
- Performance class B aeroplane: Propeller aircraft with max pax seating ≤ 9 and mtom ≤ 5700kg
- Max cruise thrust does not exist
- Gross performance = calculated performance with no safety factor
- net take off flight path = actual flight path of the aeroplane reduced by a safety margin

↳ based on number of engines

General performance theory

Speeds

Jets

- V_{HD} = min thrust required

↳ V_x = best angle of climb = best endurance
= holding = min glide angle

- V_y = best rate of climb = best range

Prop

- V_x = max endurance
- V_{HD} (at most efficient altitude for power unit)

↳ V_y = max range

- Higher fuel flow at altitude because of reducing power output

No engine

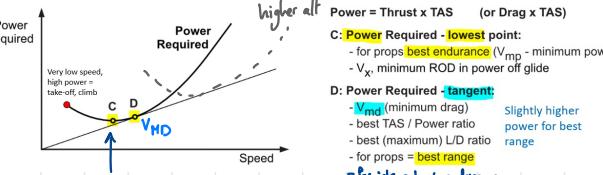
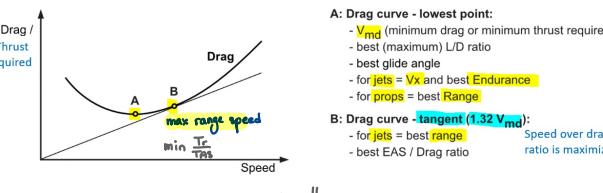
- Max endurance = V_{HD}

- Max range = V_{HD}

$$\text{Rate of Climb} = \text{climb gradient} \cdot \text{TAS} [\%]$$

$$\text{climb gradient} [\%] = \frac{(\text{Thrust} - \text{Drag})}{\text{weight}} \cdot 100$$

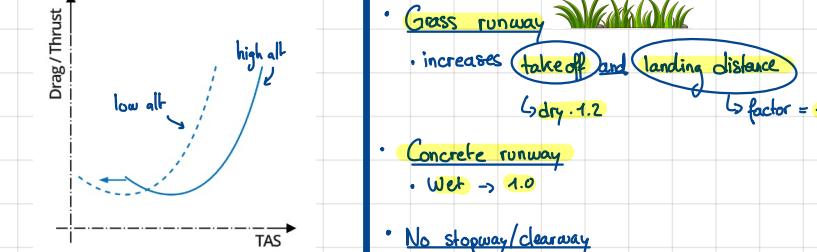
↳ change in height / horiz. air distance



Descent at constant IAS

↳ descent gradient is constant, constant drag = constant gradient

→ ROD decreases because density increases (which would increase IAS)
So we pull up a bit and reduce ROD



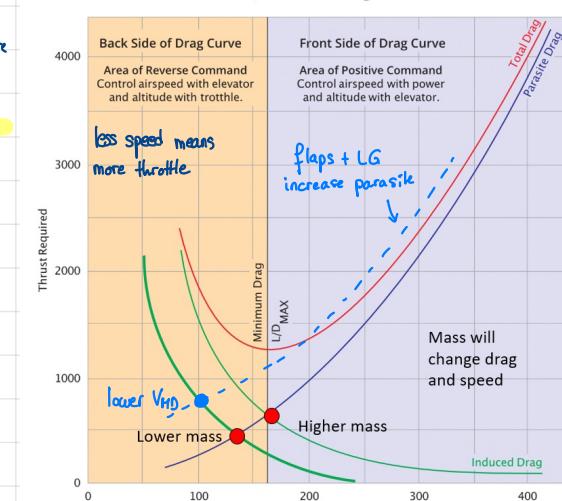
High vs low mass

↳ C-172 at given AOA, same H-distance
Boeing 747 greater V-speed and forward speed

High mass → V_x and V_y are increased
→ speed for best angle of descent increases
→ for given AOA ⇒ increase in airspeed and power

Fuel consumption $\propto T$ (temperature)
at Mach = constant because $M = \frac{\text{TAS}}{\text{LSS}}$

C_L (lift coefficient) is independent of altitude



Climb

$$T = \sin(y)W + D$$

$$L = W \cos(y)$$

$$\frac{L}{W} = \frac{1}{\cos(y)}$$

$$\frac{T}{W} = \frac{D}{L} \sin(y) = \sin(y)$$

$$\gamma = \tan^{-1}(\frac{T-D}{W})$$

Descent

$$T + \sin(y)W = D$$

$$L = \cos(y)W$$

$$T = D - W \sin(y)$$

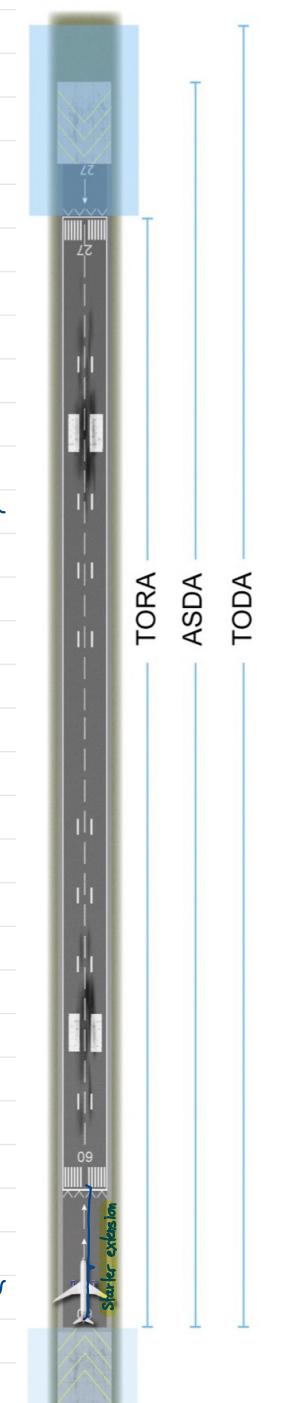
$$n = \frac{1}{\cos(\text{bank angle})}$$

Small angles $\cos(y) \approx 1 + \dots$

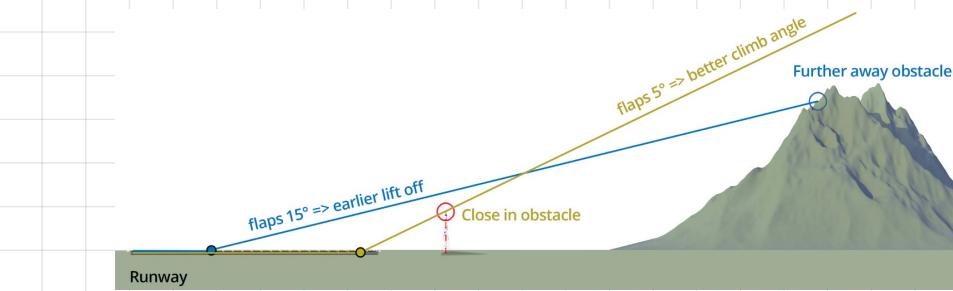
$$\frac{T}{W} - \frac{D}{L} = \sin(y)$$

climb gradient

$$n = \frac{1}{\cos(\text{bank angle})}$$



TODR



- Specific Range (SR) = still air distance / unit of fuel

Level flight, range and endurance

Specific fuel consumption (SFC)

- For jet: Fuel flow / unit thrust
- For piston: Fuel flow / unit of power

Specific endurance: 1/fuel flow

$$\text{NH}/\text{unit mass fuel}$$

- Specific range = TAS / Fuel flow (best at high altitude and low temperature)

- Minimum Fuel Flow (FF): Speed for max endurance (V_{MD} for jets)

- If temp increases → specific range decreases (as performance decrease)

- For propeller airplane → max endurance is at low altitudes

- Endurance is always independent of wind and flown at V_{MP}

- Fuel consumption is proportional to mass

↳ lighter aircraft ⇒ optimum altitude gets higher

→ Drag and IAS decrease
(we can go slower to maintain flight level)

- Jet aircraft cruise at 85% to 90% of their max RPM

Propeller

- if increase Power from max endurance
→ range will first increase then decrease (too much power required)

→ Endurance will decrease

- Max achievable IAS/TAS decrease steadily with altitude (less power available)

Climbing

- V_x (max angle) is achieved with minimum thrust required speed (bottom of drag chart)

- V_x and V_y increase with TAS with altitude

- Max ROC speed increases with increasing mass

memo: higher mass, all speed increase

- Gradient is always higher than climb angle (different units)

- Max ratio btw thrust available and thrust required during climb → V_x (max angle)

Engine failure

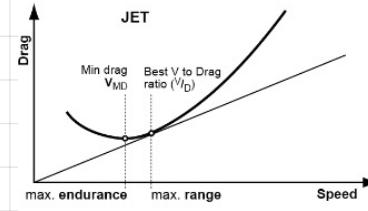
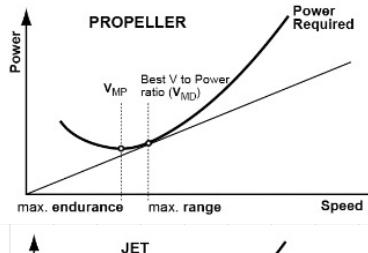
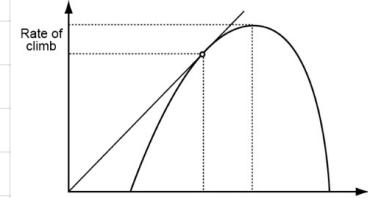
- $V_x \rightarrow V_{xse}$ $V_{yse} \leftarrow V_y$ (sex, yes!)

- SFC increases

- Thrust available reduce by 50%

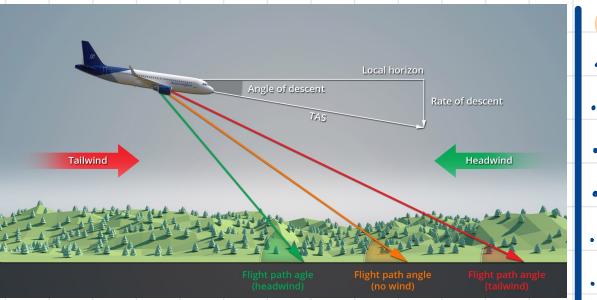
- Excess thrust reduce by more than 50% (assymetric thrust + additional drag)

- Aft CG → increases max range and absolute ceiling



Descending

- If headwind, reduce angle of descent and maintain CAS



02 CS-23/Applicable Operational Requirements Performance Class B - Theory 6

Airworthiness requirements

Speed definitions

- V_{SO} = stalling in landing configuration (flaps down)
- V_{REF} = Speed in landing config. at descent through landing screen height (50 ft)

Limitations on speeds

- V_R
- $\geq 1.05 V_{HC}$
- $\geq 1.1 V_{SI}$
- $\geq V_{S1}$ for single engine
- V_{REF} (barrier speed)
- $1.3 V_{SO}$ class B
- $1.2 V_{S1}$ class A

Effect of engine failure

- Total drag increase because of rudder deflection
- Best is: left quartering wind, right engine failure

High Altitude takeoff

- V_1 decreases (you need to make decision quicker)

- Max bank angle after takeoff for Performance Class B is:
 - 0° below 50ft or half-wingspan (whichever higher)
 - 25° above 50ft

- Landing distances should be multiplied by 1.15 when wet runway

Take-off and landing

- Screen height 50ft → ends at 1500ft

Landing distance

- $0.7 \cdot LDA = LDR$

Runway slope

- Increase by 5% for each 1% of downslope

Correction factor to headwind and tailwinds

- Not more than 50% of headwind
- Not less than 150% of tailwind

- Fixed-pitch prop → accelerates during takeoff → blade AOA decreases and thrust decreases
- Constant speed prop → accelerates during takeoff → thrust increase and then decreases

TODA 1.15

TORA 1.25

ASDA 1.3

- Declared safe area $\leq 90m$

- Obstacle accountability area = area beyond TODA where obstacles considered T-O perf

Climb, cruise and descent

- Speed for max rate of climb \uparrow with \uparrow mass (all speed increase with mass increase)
- Brake horsepower \downarrow with \downarrow air density
- Fuel consumption \uparrow after VMP (speed best endurance)
- With \uparrow altitude, drag stay constant but TAS \uparrow
- $\boxed{\text{Net gradient} = \text{gross gradient} + 0.5\%}$
- Climb rate of at least 300 ft/min with all engine operating at maximum continuous power
- Min all engine climb gradient = 4%
- V_y between holding speed and V_{HBE}

Example

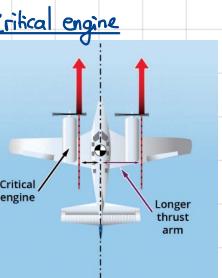
net = 11.5%.

$$\frac{9000 \text{ ft}}{11.5\%} = \frac{9000 \text{ ft}}{0.115} = 78,100 \text{ ft}$$

$$\frac{NAM}{TAS} = \frac{NM}{GS}$$

$$12.4 \quad 168$$

$$2500 \text{ ft} \quad 168 \text{ ft}$$



03 CS-23/Applicable Operational Requirements Performance Class B -

Use of Aeroplane Performance Data for Single and Multi-engine Aeroplane

Use of aeroplane performance data

Takeoff

Field length requirements

- No stopway or clearway → balanced field
 - when multiplied by 1.25 must not exceed TORA
- Stopway or clearway available
 - when multiplied by 1.3 must not exceed ASDA
 - when multiplied by 1.15 must not exceed TODA

Grass

- Dry = 1.2
- Wet = 1.3
- 1% uplope = 5% = 1.05
- No factorization for downslope

Climb

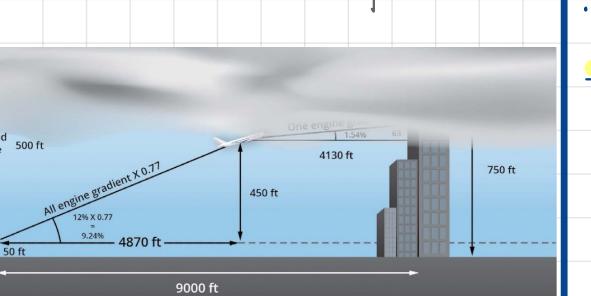
- Start calculation at screen height of 50ft

- Below cloud base, take all engine operative multiplied by 0.77

- At cloud base, OEI climb gradient

- min climb gradient = 4%.

→ after balked landing = 2.5%.



Example

$$\begin{array}{rcl} \text{TORA} & = & 4500 \text{ ft} \\ & & \text{wet grass, no stopway, } \\ & & \text{upslope } 5\% \\ & = & 1.3 \cdot 1.25 \cdot 1.05 \end{array}$$

$$\begin{array}{rcl} \text{STOP} & & \text{GO} \\ \text{TORA} & 1270 & \\ \text{TODA} & 1655 & / 1.15 \quad | \quad 1439 \\ \text{ASDA} & 1485 & / 1.3 \quad | \quad 1142 \end{array}$$

Landing

- HEP must land within 70% LDA so multiply by 1.43

- Wet 1.15

- Grass 1.15

- 1% downslope = 5% = 1.05

- No factorization for uplope

Note: $TAS = IAS + \frac{IAS \cdot 2}{100} / 1000 \text{ ft}$ ⚠ If question asks for "required" or "minimum"

→ factorization is needed

04 CS-25/Applicable Operational Requirement Performance Class A - Theory

Take-off memo: mass increase = all speed increase

VS speeds

V_1

- improved climb take-off → higher V_1 and longer TODR
- using V_1 of 155 kts instead of 142 kts → reduces take-off distance → improves climb performance

- $V_1 < V_{HBE}$ (max breaking energy)

V_2

- $> V_1 \text{ and } 105\% V_{MCA}$

V_2

- take-off climb/safety speed at 30ft

- higher V_2 → improved climb capability

- $V_2 > 110\% V_{MCA}$

- Flaps reduce V_2 because V_2 is safety speed and flaps increase safety

- Speed to keep until 400ft

- Screen height class A take-off = 35ft

↳ lowered to 15ft if wet for OEI TODR

- All engine at Take-off Run (TOR) apply factor of 1.15

Accelerated-Stop Distances

- FSD = distance to engine failure + 2 sec at V_1 + distance full stop

- Breaking assumed to start at V_1

No Clearway, no stopway

- balanced field length gives the minimum required field length in the event of engine failure

- Single V_1 speed

- OEI take-off distance and rejected take-off distance to full stop are equal

Clearway, no stopway

- Lower V_1 (because no stopway, need to take off decision sooner)

- Can take higher mass

Slope, no clearway

- Higher V_1 (you have a lot of time to stop)

Climb segments

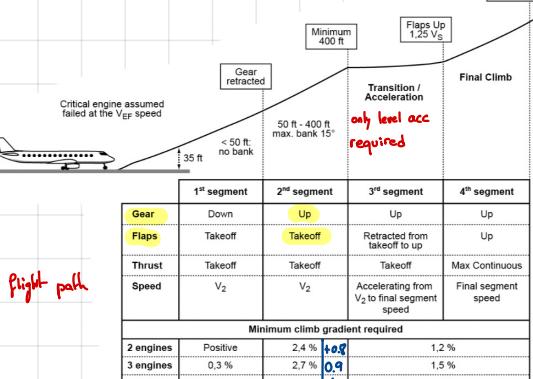
- Specification only for failure of critical engine

2nd Segment

- max $15^\circ/25^\circ$ bank between 200-400ft
 - $25^\circ/30^\circ$ bank > 400ft
 - ↳ if approved
 - ↳ obstacle clearance because soft of net flight path

3rd Segment

- max acceleration height depends on max time T-O thrust



Performance Limited Take-Off Mass (PLToM)

- Take-off mass subject to departure aerodrome limitation

$V_1 \leq V_{mbc}$ (max breaking)

$V_{HC} \rightarrow \text{min control speed OEI}$
↳ lower at higher temperature (deceler engine, less thrust)

V_{LOF} lift off speed

↳ max tyre speed

V_{MCG} and $V_1 < V_R$

↑ Minimum control ground

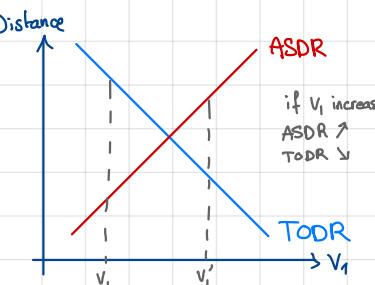
$\sqrt{V_{min}}$: minimum take-off speed

• 1.13 V_{SR} for turbojets and 2-3 engine turboprop

• 1.08 V_{SR} 4-engine or more

• 1.1 V_{ACA}

• V_{FTO} (final take-off speed) $> 1.18 V_{SR}$



Question about TODR
highest between $\begin{cases} \text{TOD OEI} \\ \text{TOD AEO} \cdot 1.15 \end{cases}$

Reduced or Derated Take-off

- Max assumed temperature is $+55^{\circ}\text{C}$
- Derated take-off thrust can be applied when TOTL is limited by ASDA
- Reduced / Flex
 - can select TOGA
 - max 25% reduction
- Derate
 - can't select TOGA (because you calculate lower V_{100})
 - allowed on wet/contaminated RWY
 - Derate thrust to decrease V_{100} (available on contaminated runways)

Obstacle limited Take-off

- If change of track $< 15^{\circ}$
 - $\downarrow 300\text{ m}$ if sufficient navigational accuracy

- Take-off flight path = actual take off distance with no safety margins included

- Horizontal obstacle clearance
 - $90\text{ m} + 0.125D$
 - $60\text{ m} + 1/2 \text{ wingspan} + 0.125D$

Contaminated runways

- Drag created by slush increase then decreases (once you start hydroplaning)
- Found in Part B of the operations manual
- Derated take-off \rightarrow new minimum control speeds
- Snowball = wet snow
- Compressed snow \rightarrow TODA constant, ASD increases
- Max allowed depth of wet snow = 13 mm

(Dynamic) Hydroplaning speed (V_p) (above that speed = hydroplaning)

- Rotating = $a \cdot \sqrt{\text{tyre pressure (PSI)}}$
- Non-rotating = $7.7 \cdot \sqrt{\text{tyre pressure (PSI)}}$
- occurs for any flap setting

Dry 0% contaminated

Damp Not dry, not shiny

Wet contamination < 3mm

Contaminated > 3mm

Climb

- Max climb angle achieved at $V_x = \max \frac{C_L}{C_D}$ ratio
- Order of speed V_s, V_x, V_y
- Constant IAS = Constant drag
- Crossover altitude = at which change from constant TAS to constant Mach number

Cruise

- Long Range Cruise \rightarrow lower costs
- Maximum range cruise (MRC)
 - maximum range speed
 - $1.32 V_{100}$
- Long range cruise (LRC)
 - Smarter to fly at a 4% higher speed as you only loose 1% range
 - Slightly higher power setting \hookrightarrow best speed for economy
 - Higher cost index
 - Higher fuel flow

Step climbs

- Used to get closer to optimum altitude

Cruise altitude

- Below optimum altitude \rightarrow Mach number for LRC decreases with decreasing altitude
- ATC sometimes instructs to fly above optimum altitude \rightarrow increases with lower Mach number (Shock stall limited)

ACN < PCN

Memo: always 47F if not then GOR
• ACN may exceed PCN by 10%.

En-route one-engine-inoperative

Drift down

- net flight path vertical clearing should be 2000 ft
- To calculate drift down path you need:
 - Altitude
 - OAT
 - Mass at start of driftdown
 - Not which engine has failed as you take the worst case
- Fuel jettison taken into account when calculating obstacle clearance
- Best speed is V_{100}
 - jets: best angle of climb (V_x)
 - props: best rate of climb (V_y)

Descent

- Careful if you descend at M_{10} you might exceed V_{100} (max operating speed)
- Max endurance = speed for min power
- Continuous Descent Arrival (CDA) \rightarrow stay higher longer, operate at lower engine thrust
- Descend at $\text{Mach} = c^{te}$ \rightarrow angle of descent increase because LSS \uparrow \rightarrow TAS must \uparrow \rightarrow must pitch down.
- Descend at $\text{IAS} = c^{te}$ \rightarrow angle of descent is constant

Approach and landing

- Landing distance available (LDA)
 - 50ft (screen height) to full stop must not exceed:
 - 60% of LDA for turboprops (1.67 correction factor)
 - 70% of LDA for turboprops (1.48 correction factor)
 - if Wet 15% addition (1.92 correction factor)

Variables

- slopes are considered if $\pm 2\%$.
- $V_{REF} = 1.23 V_{S0}$
- For balked landing, must achieve climb gradient of 3.2% in landing conf. with all engines
- Required RWY length at destination = alternate (for turboprop)
- Approach climb requirements: OEI, flaps approach, gear UP
- Approach in rain you must increase speed because of deteriorated the boundary layer

04 CS-23/Applicable Operational Requirements Performance Class A

Use of Aeroplane Performance Data 6

Take-off

Climb limited chart

- Wind omitted because the climb limit performance taken relative to the air
- Kink because engine are pressure limited at lower temperature and temp limited at high temp

Drift down and stabilizing altitude

- In the Net Level-off Altitude figure, the temperature line are broken because AC OFF below 17'000ft
- Equivalent gross weight at engine failure: actual gross weight corrected for OAT higher than ISA+10°C

Landing