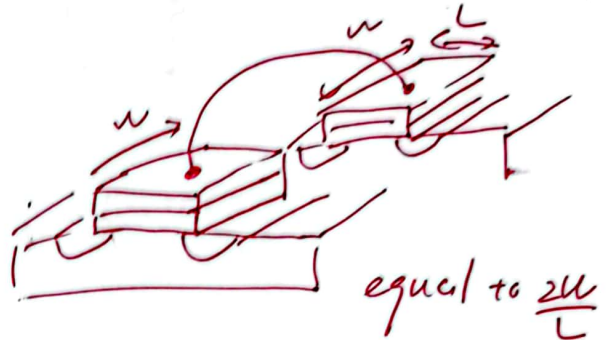


in three dimension



derive in math:

$$I_1 = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$I_2 = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$I = I_1 + I_2 = \frac{1}{2} \mu_n C_{ox} \frac{2W}{L} (V_{GS} - V_{TH})^2$$

$g_m$ :

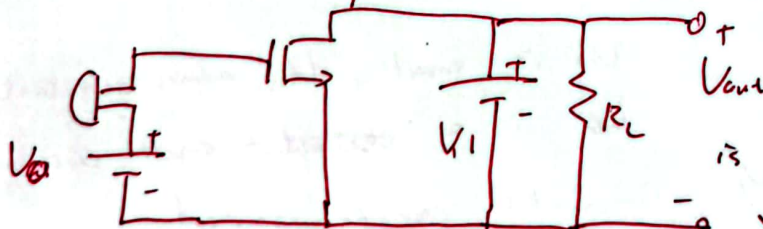
$$g_{m1} = \frac{2I_1}{V_{GS} - V_{TH}} \quad g_{m2} = \frac{2I_2}{V_{GS} - V_{TH}}$$

$$g_m = \frac{2(I_1 + I_2)}{V_{GS} - V_{TH}} = \frac{4I_1}{V_{GS} - V_{TH}} = 2g_{m1}$$

Let's build an amplifier:

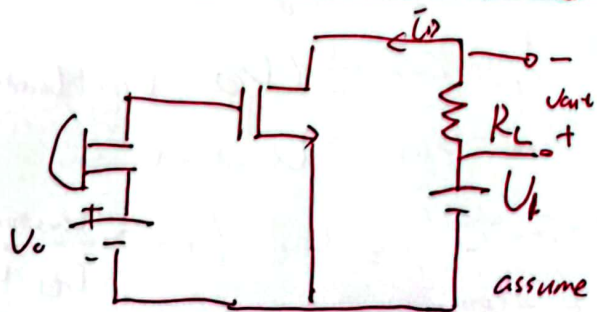
Last day we didn't consider  $V_{DS}$ .

Actually we must keep it in Sat.



is it true?

X the  $V_{out}$  is always  $V_1$



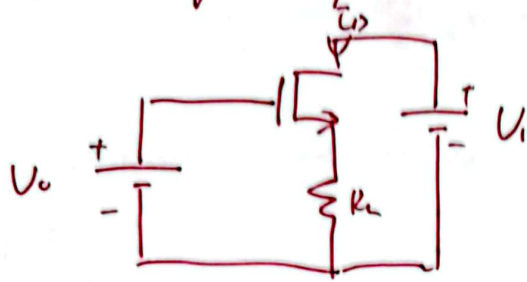
assume  $V_D = 0.9V$ ,  $V_{TH} = 0.5V$ .

$\therefore V_{DS} \geq V_D - V_{TH} = 0.4V$ .

assume  $\mu_n C_{ox}$ ; let  $I_{min} = 1mA$ ,  $R_L = 1k\Omega$

$\therefore V_1 \geq I_{min} \cdot R_L + V_{DS} = 1.4V$ .

## Large - signal Operation



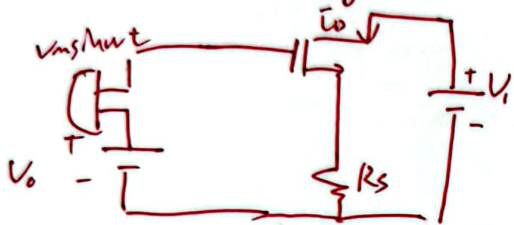
$$V_O = V_{GS} + I_D \times R_L$$

$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

$$\Rightarrow V_{GS} = \sqrt{\frac{2 I_D}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH}$$

$$\therefore V_O = \sqrt{\frac{2 I_D}{\mu_n C_{ox} \frac{W}{L}}} + V_{TH} + I_D R_L$$

Let's add a signal



$$V_O + v_{msmwt} = V_{GS} + I_D R_S$$

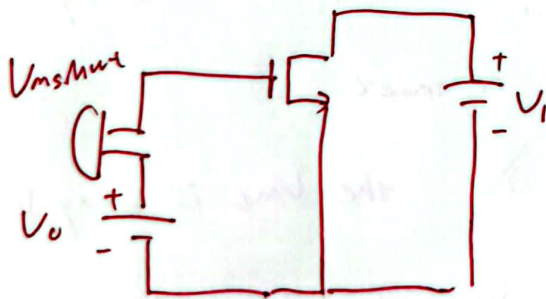
$$= \sqrt{\frac{2 I_D}{\mu_n C_{ox} \frac{W}{L}}} + I_D R_S + V_{TH}$$

Large-signal operation (if  $V_m$  is not "small")



$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2$$

Small - Signal Operation



$V_m$  is small,  $V_{GS}$  almost constant

$I_D$  is a ~~constant~~ small constant

$\therefore R_S$  can be ignored

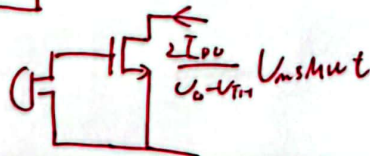
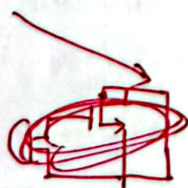
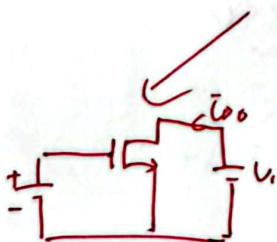
$$I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH} + v_{msmwt})^2$$

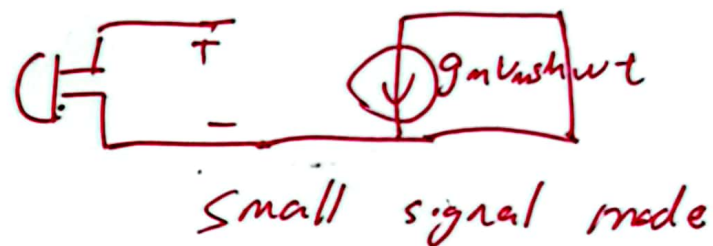
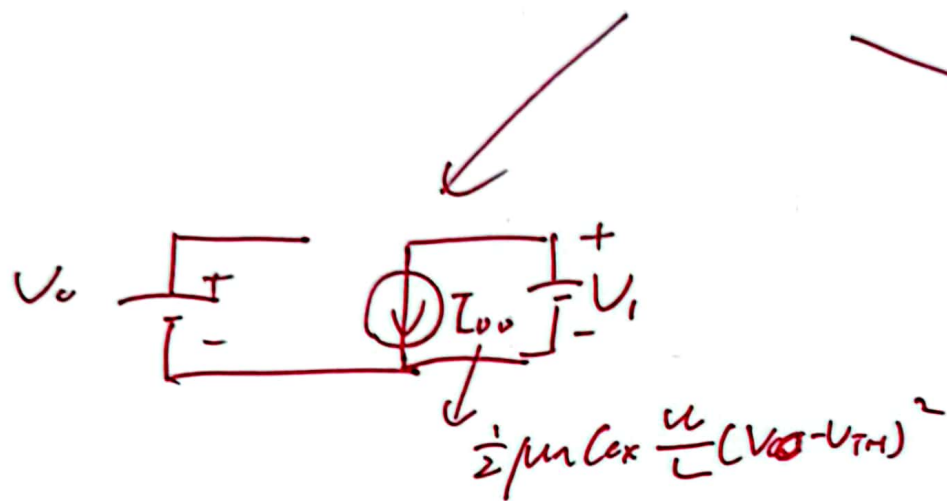
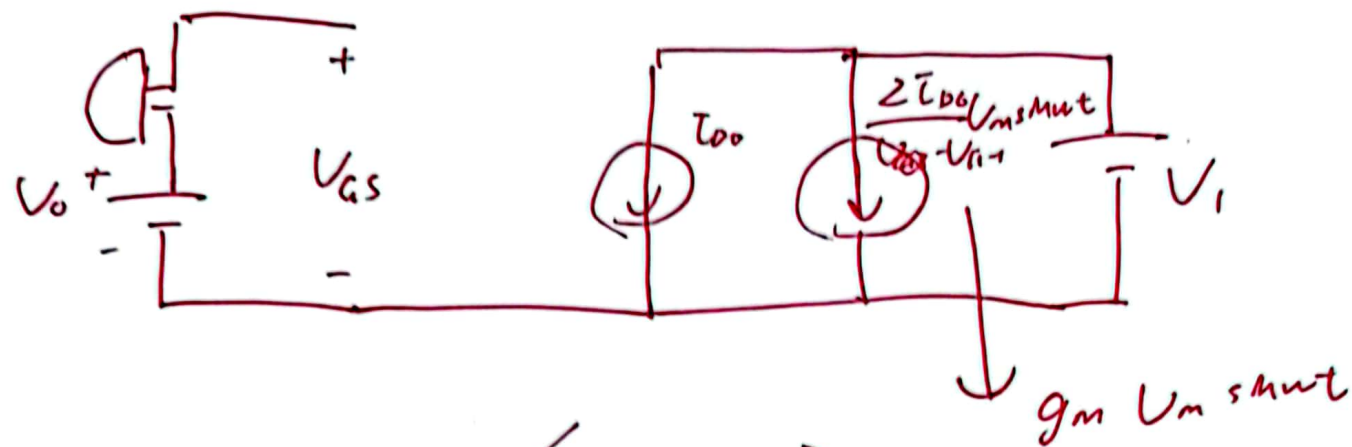
$$\therefore V_{GS} - V_{TH} \gg v_{msmwt}$$

$$(1 + \epsilon)^2 \approx 1 + 2\epsilon \Rightarrow I_D = \frac{1}{2} \mu_n C_{ox} \frac{W}{L} (V_{GS} - V_{TH})^2 \left( 1 + 2 \frac{v_{msmwt}}{V_{GS} - V_{TH}} \right)$$

$$= I_{D0} + \frac{2 I_{D0}}{V_{GS} - V_{TH}} v_{msmwt} \quad (V_{GS} \approx V_{GS})$$

Bias current      signal current





DC and  $A_{v0}$ ,  $t$ -dependent and not  $t$ -dependence  
 Large and small