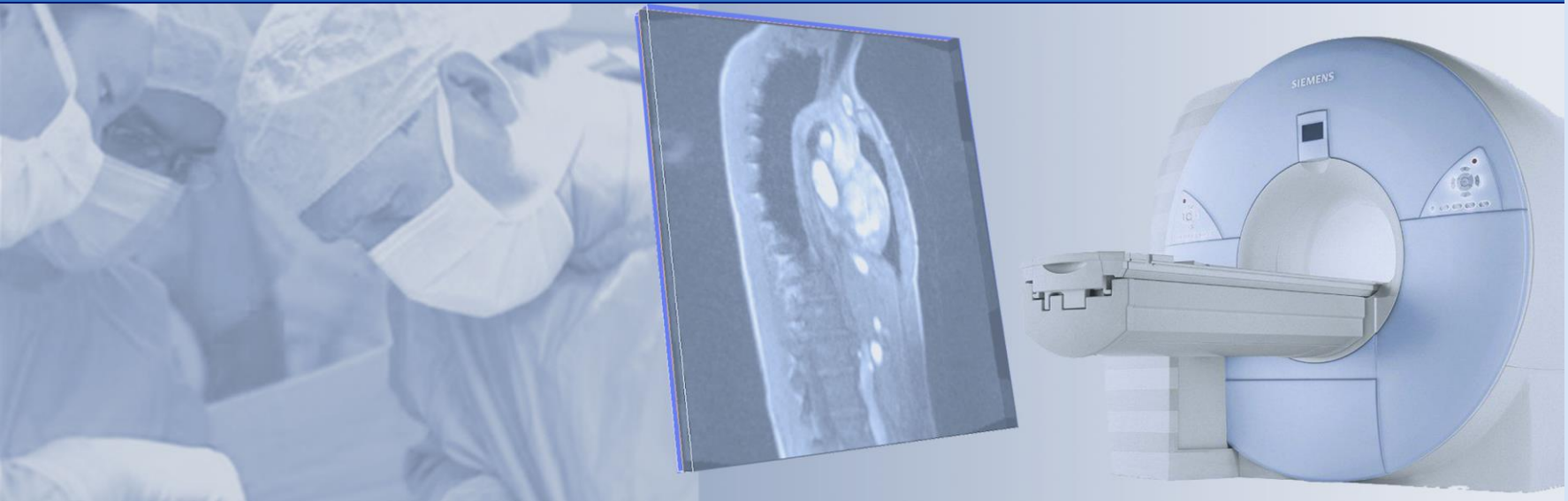


# Computer- and robot-assisted Surgery



NATIONALES CENTRUM  
FÜR TUMORERKRANKUNGEN  
PARTNERSTANDORT DRESDEN  
UNIVERSITÄTS KREBSCENTRUM UCC

getragen von:

Deutsches Krebsforschungszentrum  
Universitätsklinikum Carl Gustav Carus Dresden  
Medizinische Fakultät Carl Gustav Carus, TU Dresden  
Helmholtz-Zentrum Dresden-Rossendorf

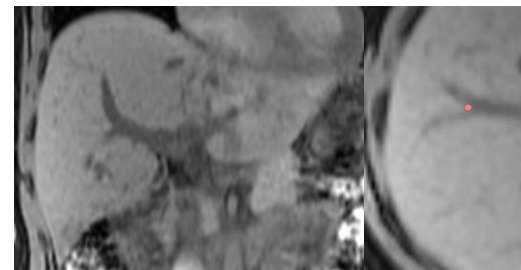
## Lecture 13 Robotics

# Master Thesis Topic: Analysis of a Human in-vivo Liver Deformation Dataset for Non-Rigid Registration

Supervisor: Bianca Güttner (bianca.guettner@nct-dresden.de)

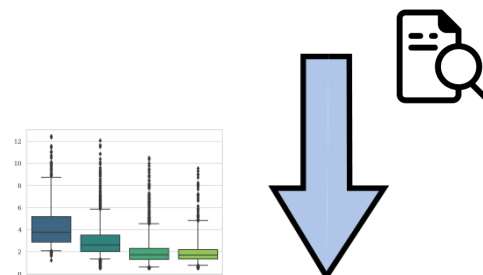
## Clinical context

- Real-world data for evaluating preoperative-intraoperative landmark registration is sparse → collected a dataset (annotation ongoing)
- Idea: Evaluate quality and share the dataset to support non-rigid registration research



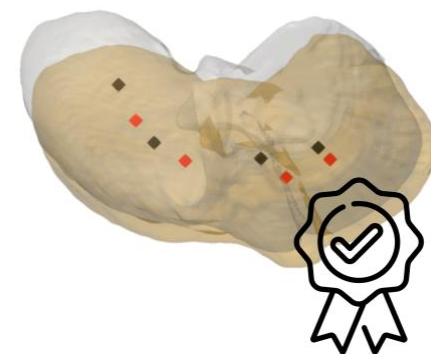
## Tasks

- Meta-analysis of dataset quality reporting in the literature
- Derivation of quality criteria for registration datasets
- Application to the collected dataset
- Discussion of implications for the intended downstream task



## Skills & Tools

- Strong analytical skills, attention to detail
- Python (scripting, data handling, environment setup, version control)
- VTK, SimpleITK, pandas



# Research Assistant Position or Research Project: Designing an Experimental Test Bench for Synthetic Tissue Deformation and Cuts

Supervisor: Bianca Güttner ([bianca.guettner@nct-dresden.de](mailto:bianca.guettner@nct-dresden.de))

## Clinical context

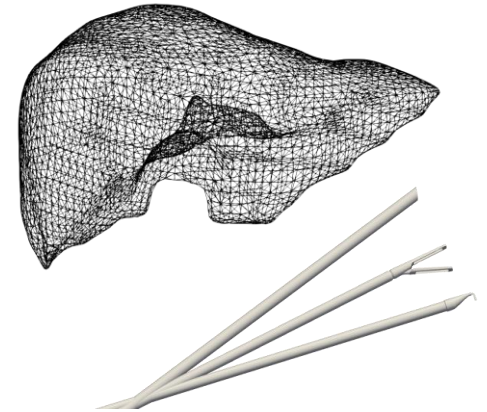
- Simulated data (tissue deformation) for training surgical navigation systems is being extended by manipulations
- To Do: Validation through experiments on a test bed including precisely defined movements and cuts

## Tasks

- Conceptualization, construction and evaluation of a validation setup → actuators, sensors, deformation assessment
- Development of data collection and storage protocols → FAIR principles

## Skills & Tools

- Python, C++ (scripting, environment setup, version control)
- Interest in hardware elements (sensors, actuators) and their specifications
- Strong analytical skills, attention to detail
- Robot Operating System (ROS), microcontrollers



# Research Assistant Position: Advancing Simulation Methods: Tissue Manipulation and Remeshing

Supervisor: Bianca Güttner ([bianca.guettner@nct-dresden.de](mailto:bianca.guettner@nct-dresden.de))

## Clinical context

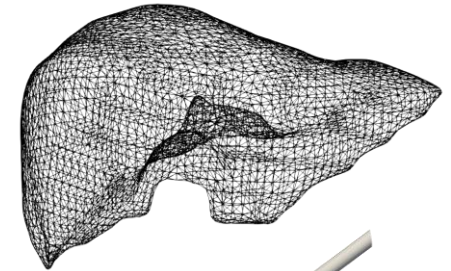
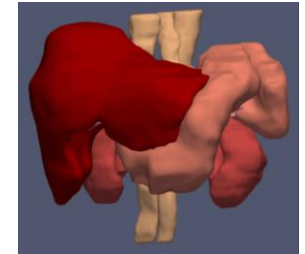
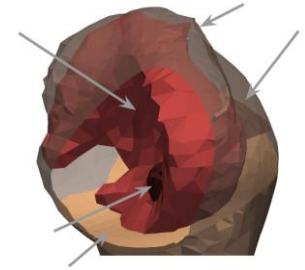
- Simulated data (tissue deformation) for training surgical navigation systems lacks manipulations → limited use
- Mitigation: Incorporate cuts into simulations

## Tasks

- Familiarization with the in-house data generation pipeline
- Implementation of cut simulations (with and without known path)
- Implementation of communication between an external mesher and the simulation, incl. adaptation of the simulation to mesh changes between timesteps (matrix updates)

## Skills & Tools

- Python, C++, Simulation Open Framework Architecture (SOFA)
- Quickly adapting to new frameworks, interfaces, and concepts
- Interest in FEM simulations and basic soft tissue mechanics



# Research Assistant Position: Developing a Synthetic Data Generation Pipeline for Surgical Navigation

Supervisor: Bianca Güttner ([bianca.guettner@nct-dresden.de](mailto:bianca.guettner@nct-dresden.de))

## Clinical context

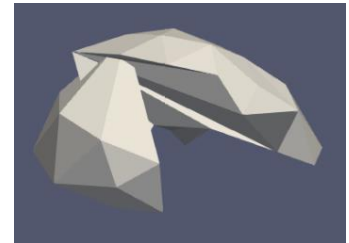
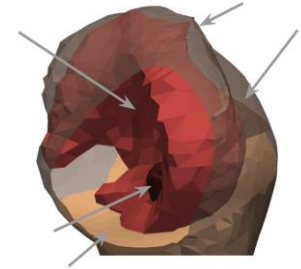
- Data for training surgical navigation algorithms is sparse → generate synthetic data of tissue deformation
- Contribution: Process large number of samples with automated data generation pipeline

## Tasks

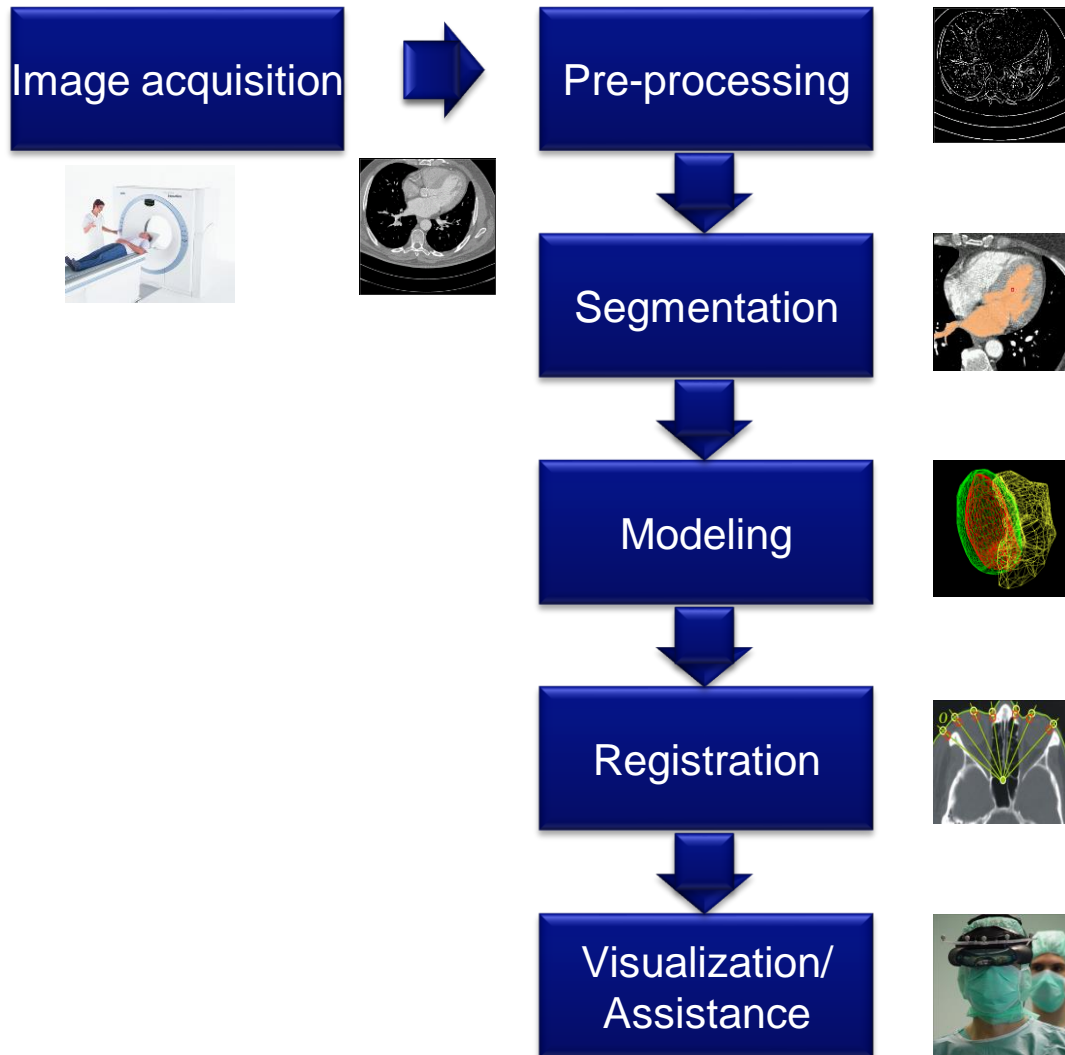
- Integration of methods into pipeline functionality, method development
- Failure case analysis and mitigation
- Preprocessing of real intraoperative data for validation
- Literature research on datasets and algorithms

## Skills & Tools

- Python (scripting, environment setup, version control)
- Quickly adapting to new frameworks, interfaces, and concepts
- Literature survey skills
- Visualization Toolkit (VTK), SimpleITK, video processing



# Process chain computer-assisted surgery





# Overview of the lecture

- Robotics
  - General definition
  - Components of a robotic system
  - Modelling a robotic system
    - Forward and inverse kinematics
  - Path Planning
  - History surgical robots

# What is a robot?

- Term: Robota, Slavic for “forced labor”
  - Coined by Karel Capek in 1920
- Context industry (VDI-guideline 2860, 1990)
  - A robot is a freely programmable, multi-functional manipulator with at least 3 independent axes that can move materials, parts, tools or devices along programmed, variable paths to perform a task.
- Context science (Christaller et al. 2001)
  - Robots are sensor-motoric machines for expanding human ability to act. They consist of mechatronic components, sensors and computer-based control functions. The complexity of a robot differs significantly from other machines in the greater number of degrees of freedom and the variety and scope of its behavior.



# Robotics

- Interdisciplinary branch of engineering and science
- Includes among others
  - mechanical engineering
  - electronic engineering
  - information engineering
- Deals with the design, construction, operation, and use of robots, as well as computer systems for their control, sensory feedback, and information processing.

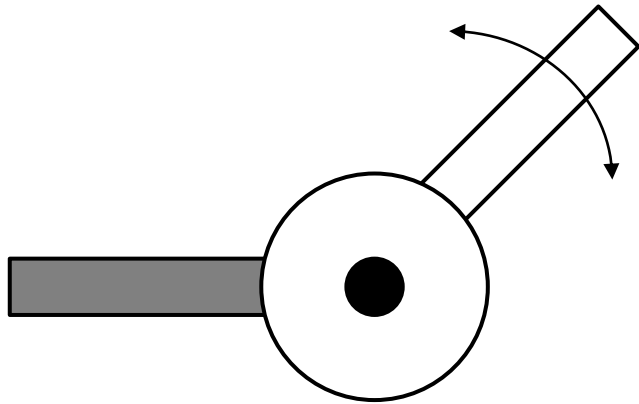
# Examples



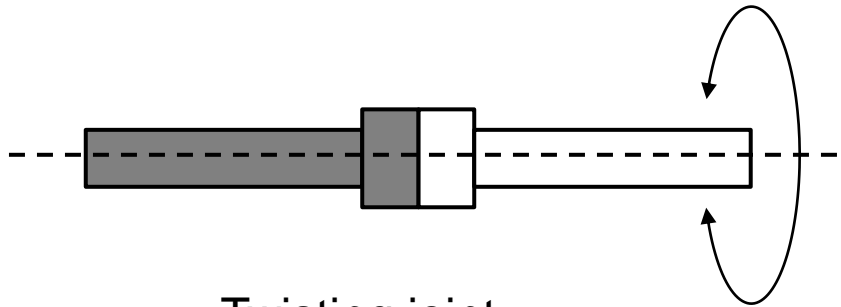
# Components of a robotic system

- Mechanical components
  - **Joint types**
  - **Workspace**
  - Wheel configurations
- Drive system
  - Fluid drive (e.g. hydraulic)
  - Muscular drive
  - Electric drive
- Gear drive
- Sensors
  - Internal sensors (Encoders, speedometer, temperature, forces, ...)
  - External sensors (Cameras, microphone, laser, ultrasound, ...)

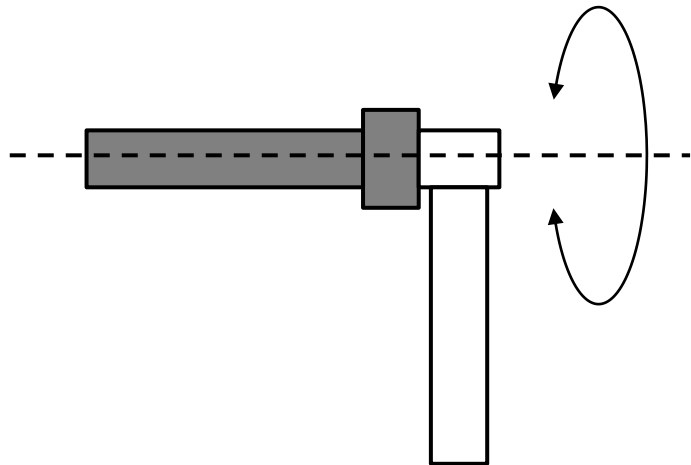
# Components of a robotic system: Joint types



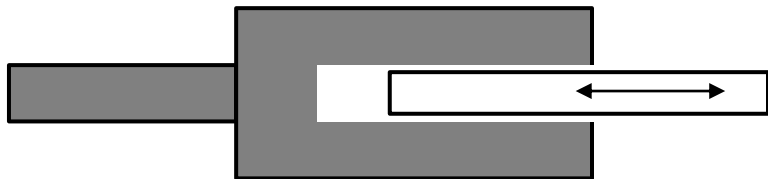
Rotational joint



Twisting joint



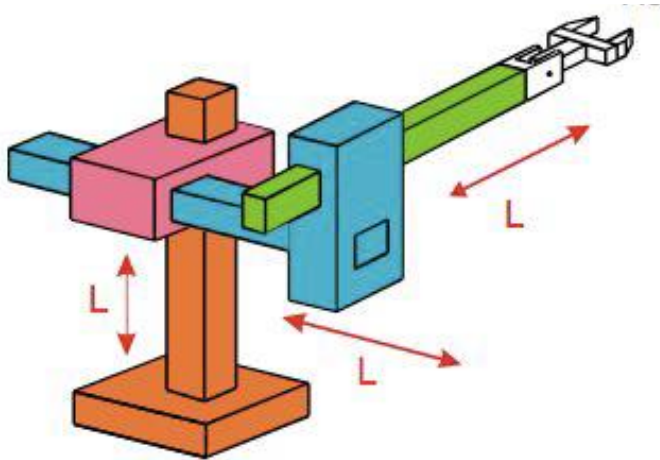
Revolving joint



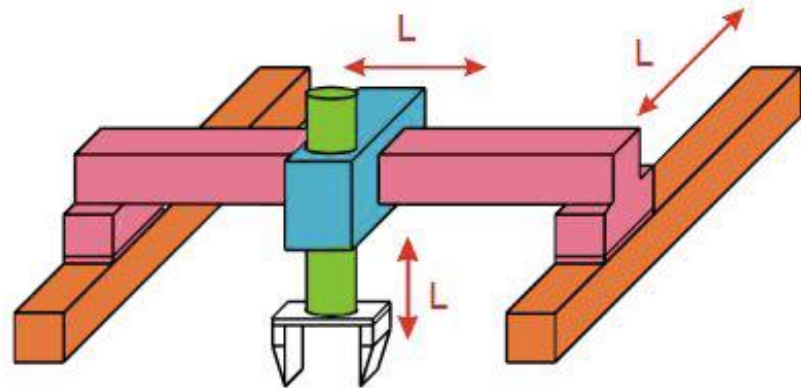
Linear joint

# Components of a robotic system: Workspace

- The points in 3D space that can be reached with the end effector
- The basic form of the workspace results when collisions between robot arms and the angle range boundaries of the joints are not considered



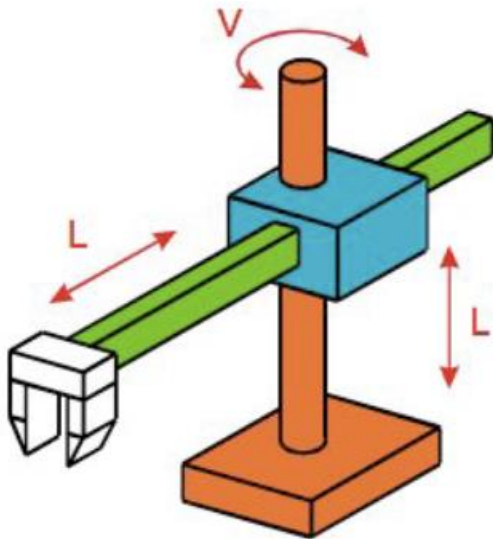
Workspace: Cuboid



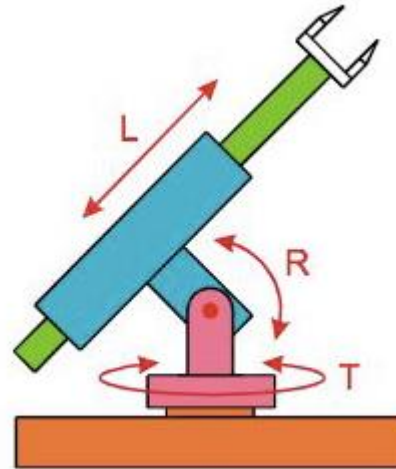
Workspace: Cuboid

# Components of a robotic system: Workspace

- The points in 3D space that can be reached with the end effector
- The basic form of the workspace results when collisions between robot arms and the angle range boundaries of the joints are not considered



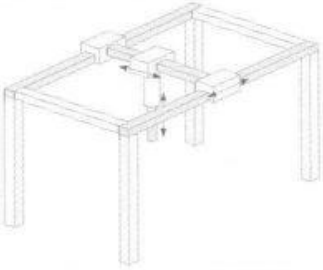
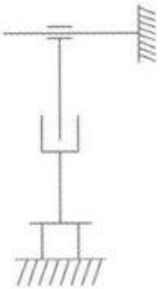
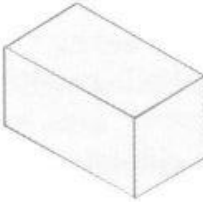
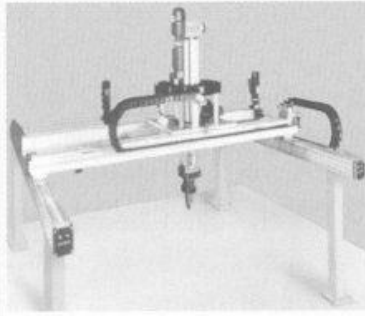
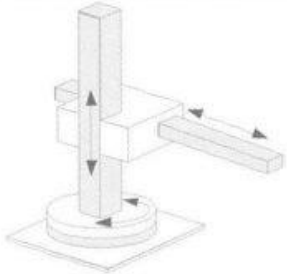
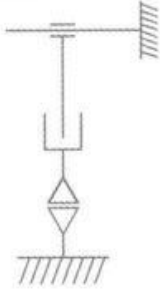


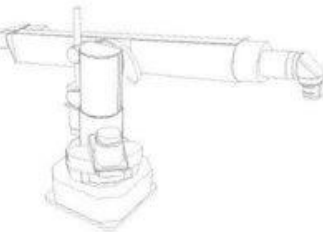
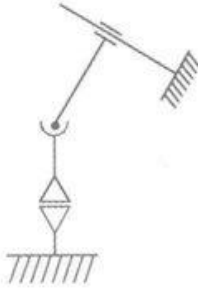
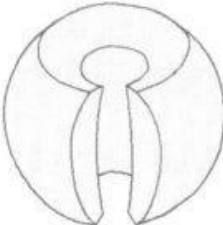
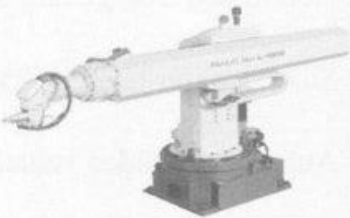
Workspace: Hollow cylinder



Workspace: Hollow sphere



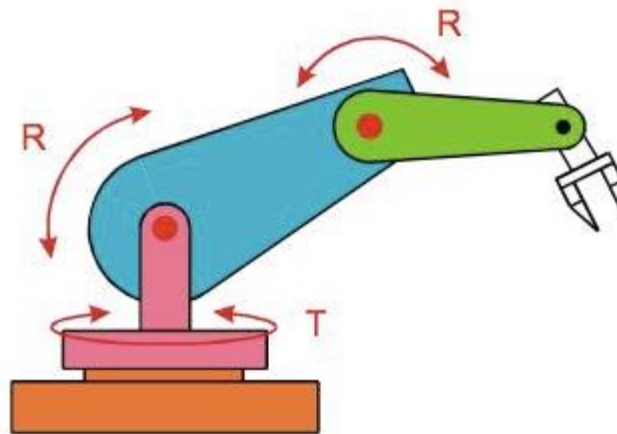
# Components of a robotic system: Workspace

| Robot   | Axes  |  | Examples  |
|---|---|--|---|
| Principle   | Kinematic Structure   | Workspace  | Photo   |
| <br>Cartesian Robot    |    |    |    |
| <br>Cylindrical Robot |   |   |   |
| <br>Spherical Robot  |  |  |  |



## Workspace

What shape does the workspace of this robot have?



- A: Cube
- B: Rectangle
- C: Hollow cylinder
- D: Hollow sphere

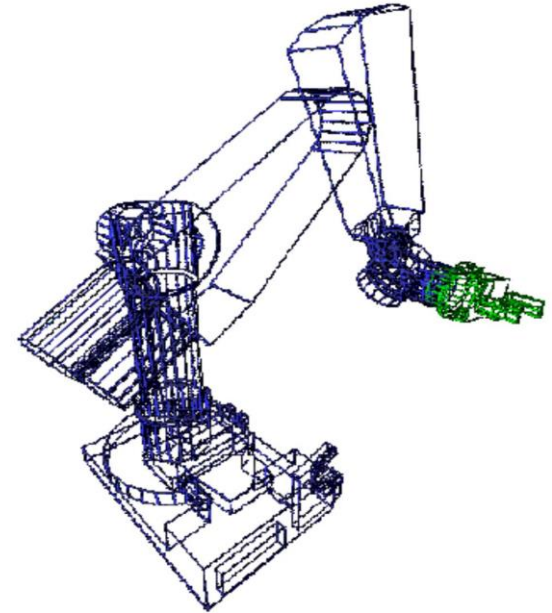
# Modelling robotic systems

- Geometric model
  - Describing the shape of the robot
  - For measuring distances and collision detection
  - Basis for calculation of movements
  - Basis for determining forces and momentum
- Kinematic model
  - Kinematics: branch of mechanics that geometrically and analytically describes motion of a system
  - Describes the relationship between the space of joint angles and the space of end effector poses
- Dynamic model
  - Analyses of the movement of a body as a result of forces and momentum
  - Describes the relationship between forces, momentum and movements in a mechanical multi-body system

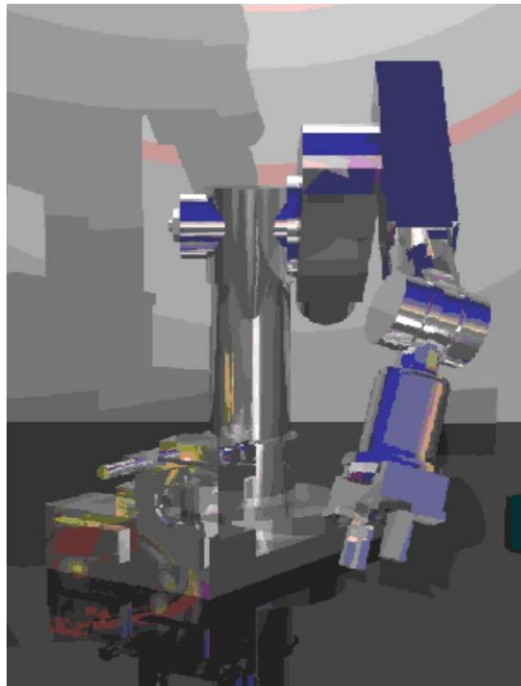
# Modelling robotic systems: Geometric model

## Classification

- By space
  - 2D model
  - 2.5D model
  - 3D model
- By geometric primitive
  - Wire frame model
  - Surface model
  - Volume model



Wire frame model

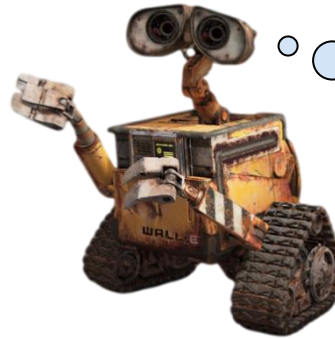


Volume model

# Modelling robotic systems: Kinematic model

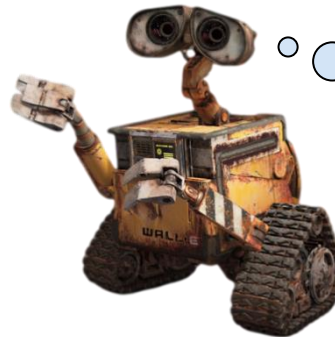
## Two main problems

- Forward kinematics
  - Determining position of end effector from the joint angles of the robot



Where is  
my hand?

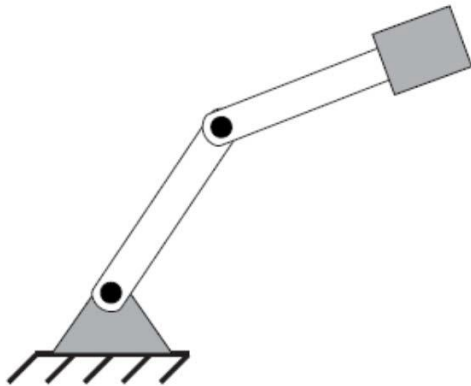
- Inverse kinematics
  - Determining joint angles for a specific position of the end effector



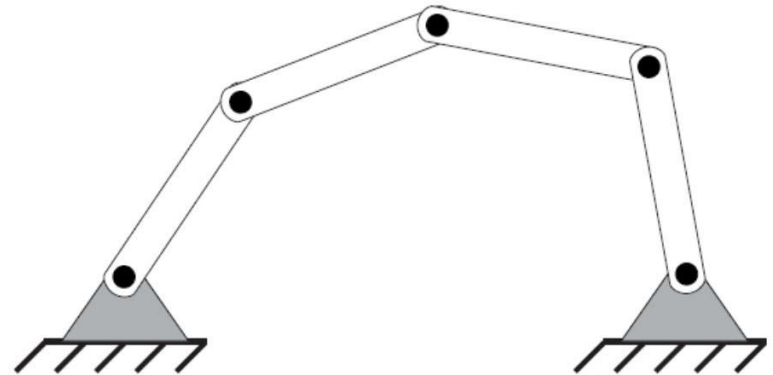
How do I  
get my hand  
to point b?

# Kinematic model: Kinematic chain

- Definition: A kinematic chain is formed by multiple bodies that are kinematically connected via a joint, e.g. a robot arm
- Types



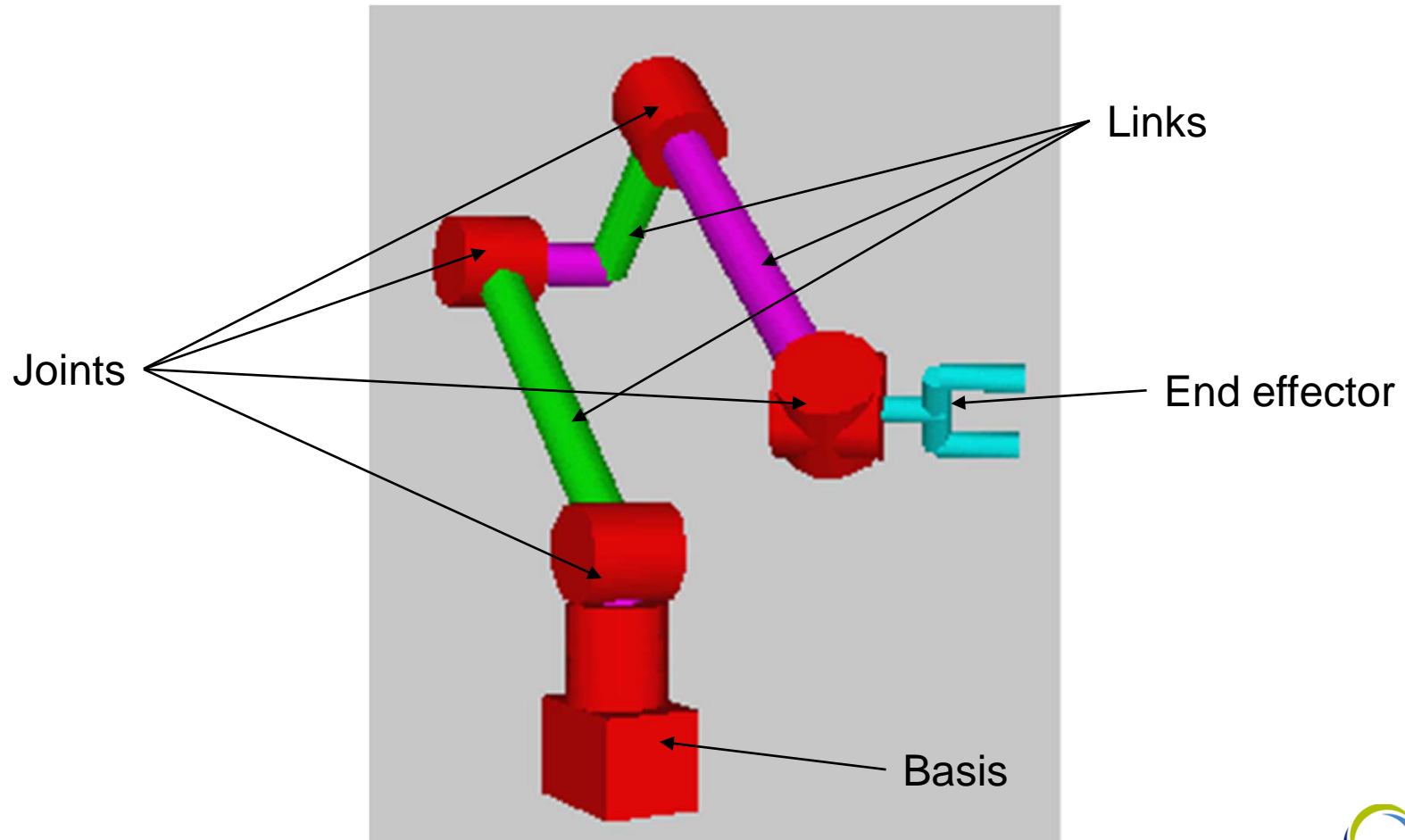
Open kinematic chain



Closed kinematic chain

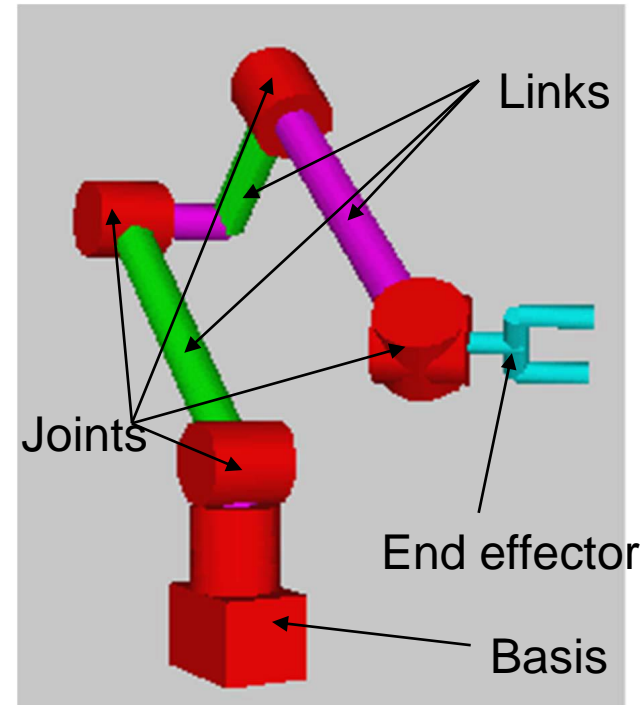
# Kinematic model: Kinematic chain

- Elements of a kinematic chain



# Kinematic model: Kinematic chain

- Convention
  - Each link is a rigid body
  - Each link is connected to the next via a joint (rotational or translational)
  - Each joint only has one degree of freedom (rotational or translational)
- Kinematic parameters = Joint & link parameters

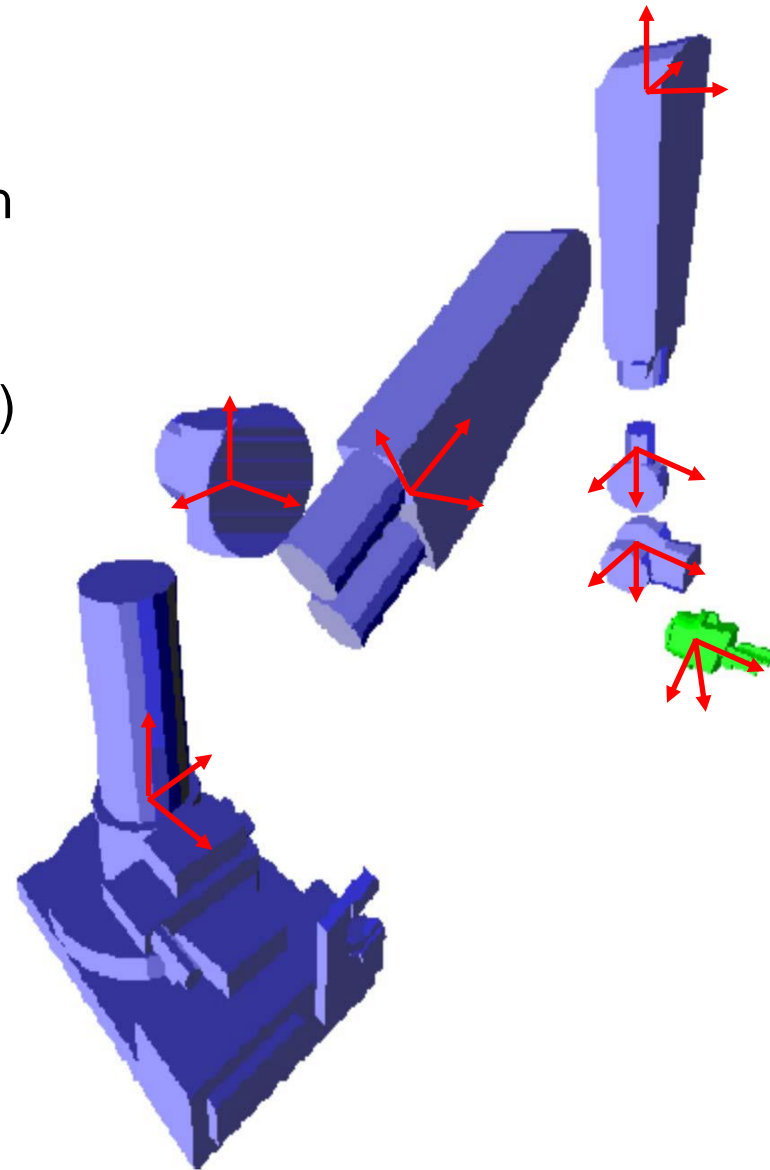




# Kinematic model: Kinematic chain

## Description of a kinematic chain

- Requires the pose of each link in relation to a basis coordinate system
- Each link has a fixed local coordinate system (Object coordinate system, OCS)
  - Robot basis  $OCS_{Basis}$
  - Link 1  $OCS_{Link1}$
  - Link 2  $OCS_{Link2}$
  - ...
  - Link 6  $OCS_{Link6}$
- Origin of each OCS lies in the joint that moves the current link
- Each link requires a transformation from the OCS into the reference CS
- Transformation via, e.g., homogenous matrices



# Kinematic model: Kinematic chain

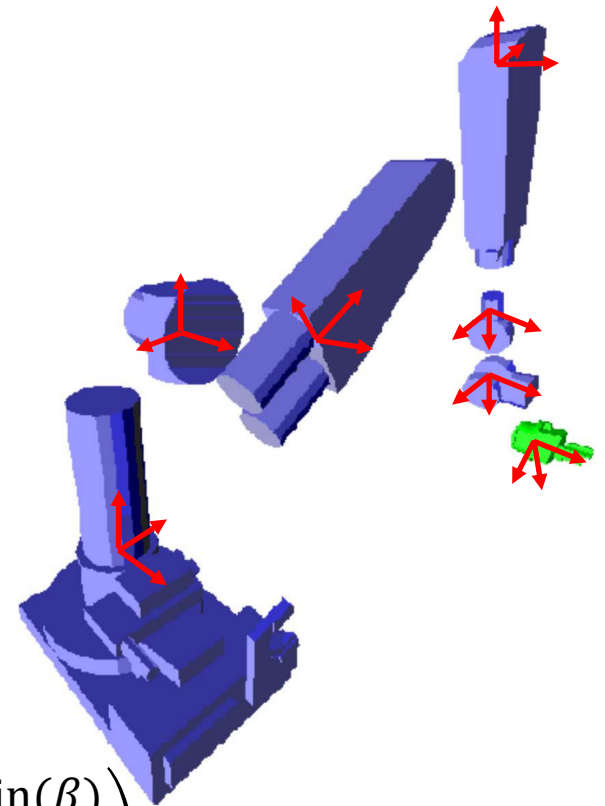
- For each link, a transformation matrix to the reference coordinate system is required:
  - 3 rotational parameters
  - 3 translation parameters
  - $\Rightarrow$  6 parameters per link
- E.g. via
  - Rotation matrix  $R$

$$R = R_z(\gamma)R_y(\beta)R_x(\alpha)$$

$$R_x(\alpha) = \begin{pmatrix} 1 & 0 & 0 \\ 0 & \cos(\alpha) & -\sin(\alpha) \\ 0 & \sin(\alpha) & \cos(\alpha) \end{pmatrix} \quad R_y(\beta) = \begin{pmatrix} \cos(\beta) & 0 & \sin(\beta) \\ 0 & 1 & 0 \\ -\sin(\beta) & 0 & \cos(\beta) \end{pmatrix}$$

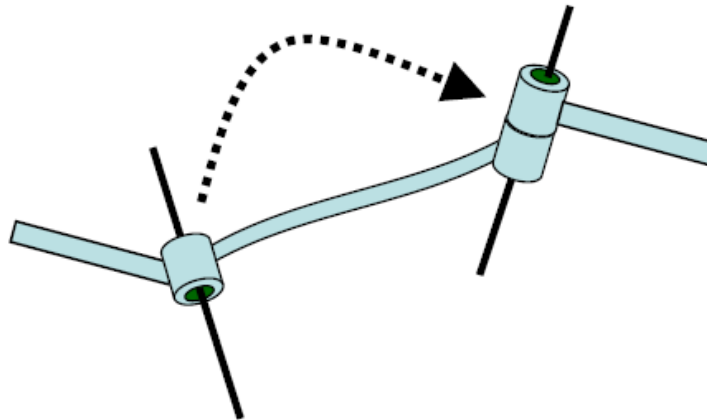
$$R_z(\gamma) = \begin{pmatrix} \cos(\gamma) & -\sin(\gamma) & 0 \\ \sin(\gamma) & \cos(\gamma) & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Translation vector  $t$   $t = \begin{pmatrix} t_x \\ t_y \\ t_z \end{pmatrix}$



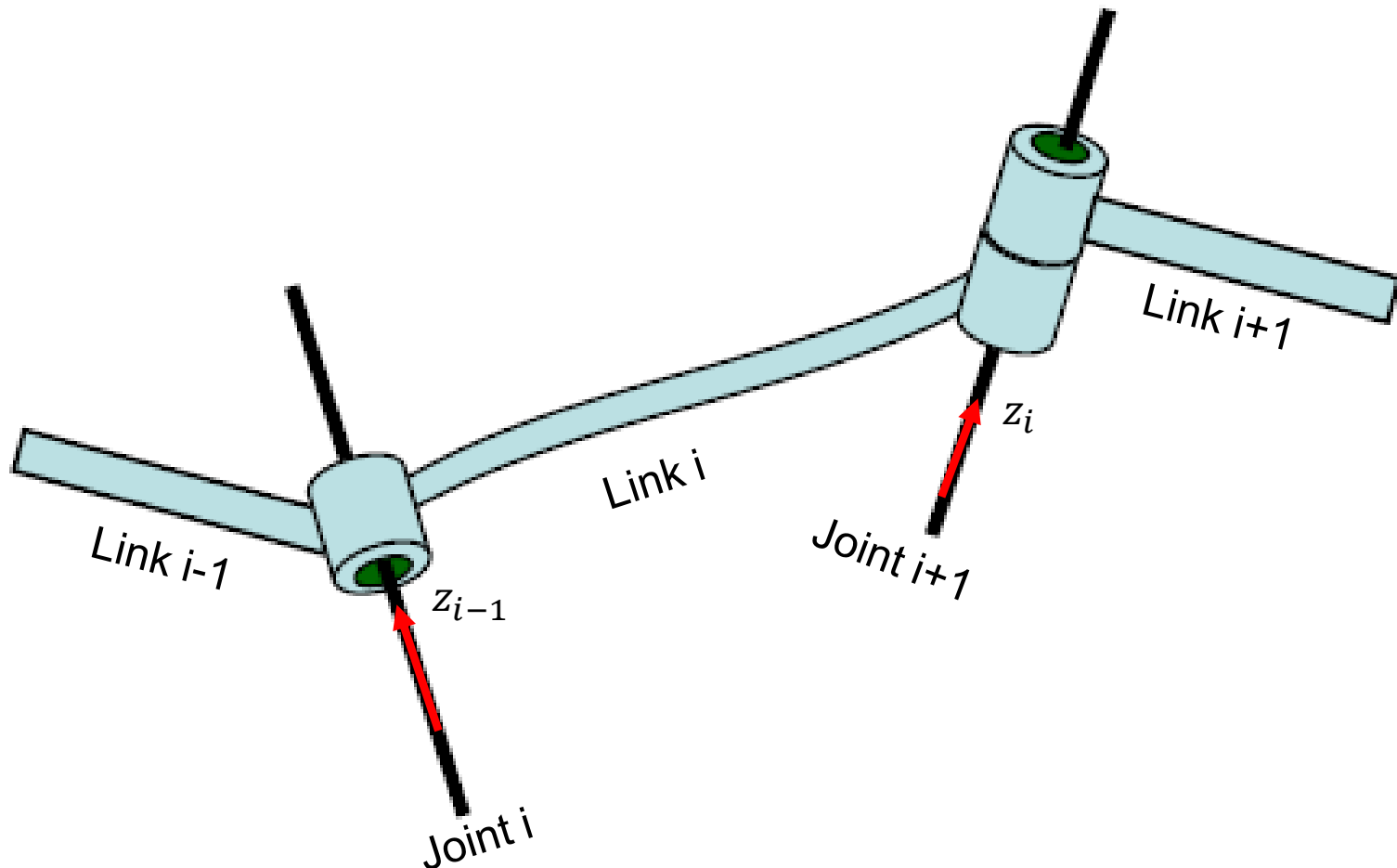
# Kinematic model: Denavit-Hartenberg convention

- Goal: reduction of parameters for describing a link with a joint
- Properties: Systemically describes the relationship (translation and rotation) between **neighboring** joints
- Reduces the number of parameters from 6 to 4



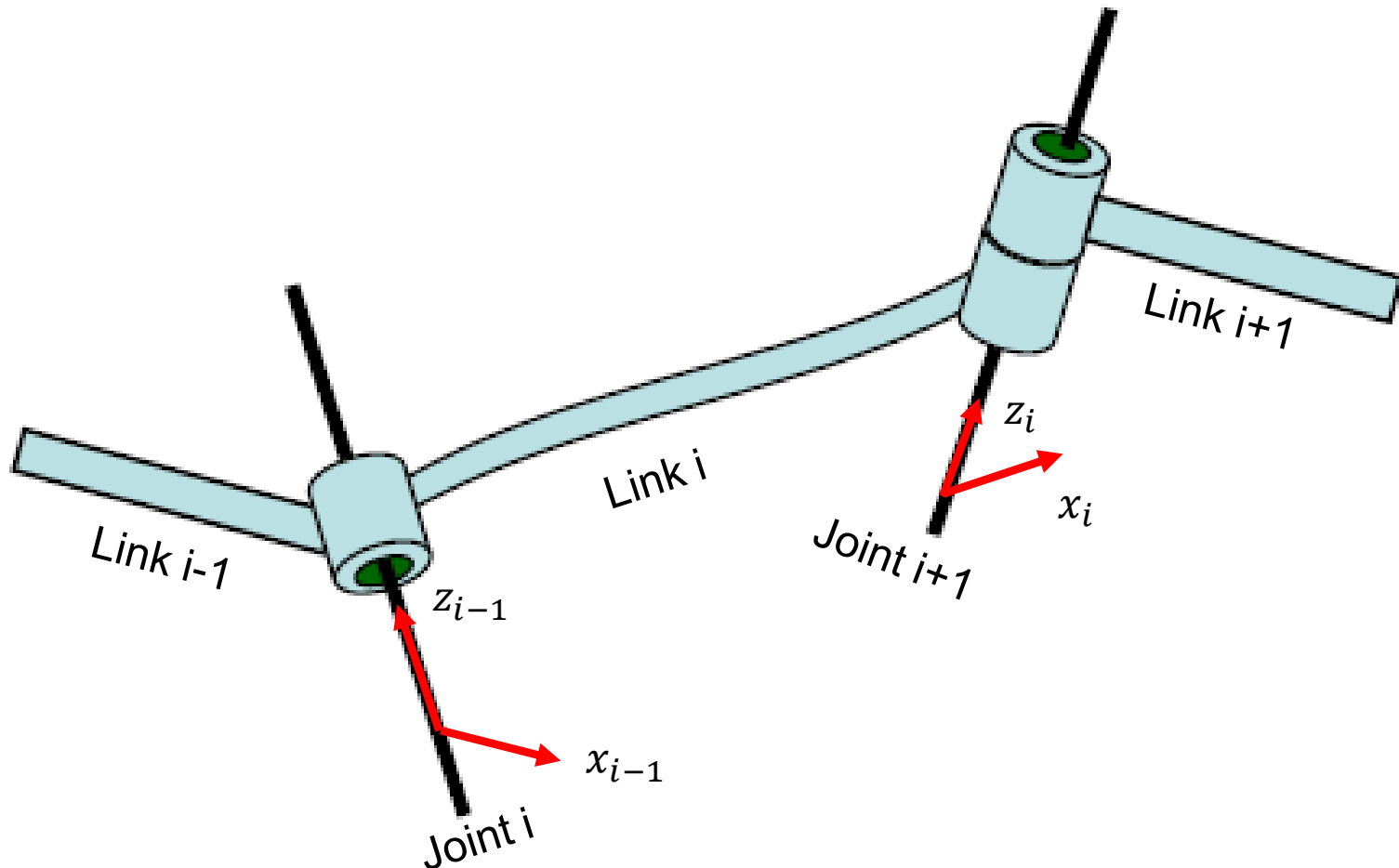
# Kinematic model: Denavit-Hartenberg convention

- Axis  $z_{i-1}$  is in the direction of the joint axis



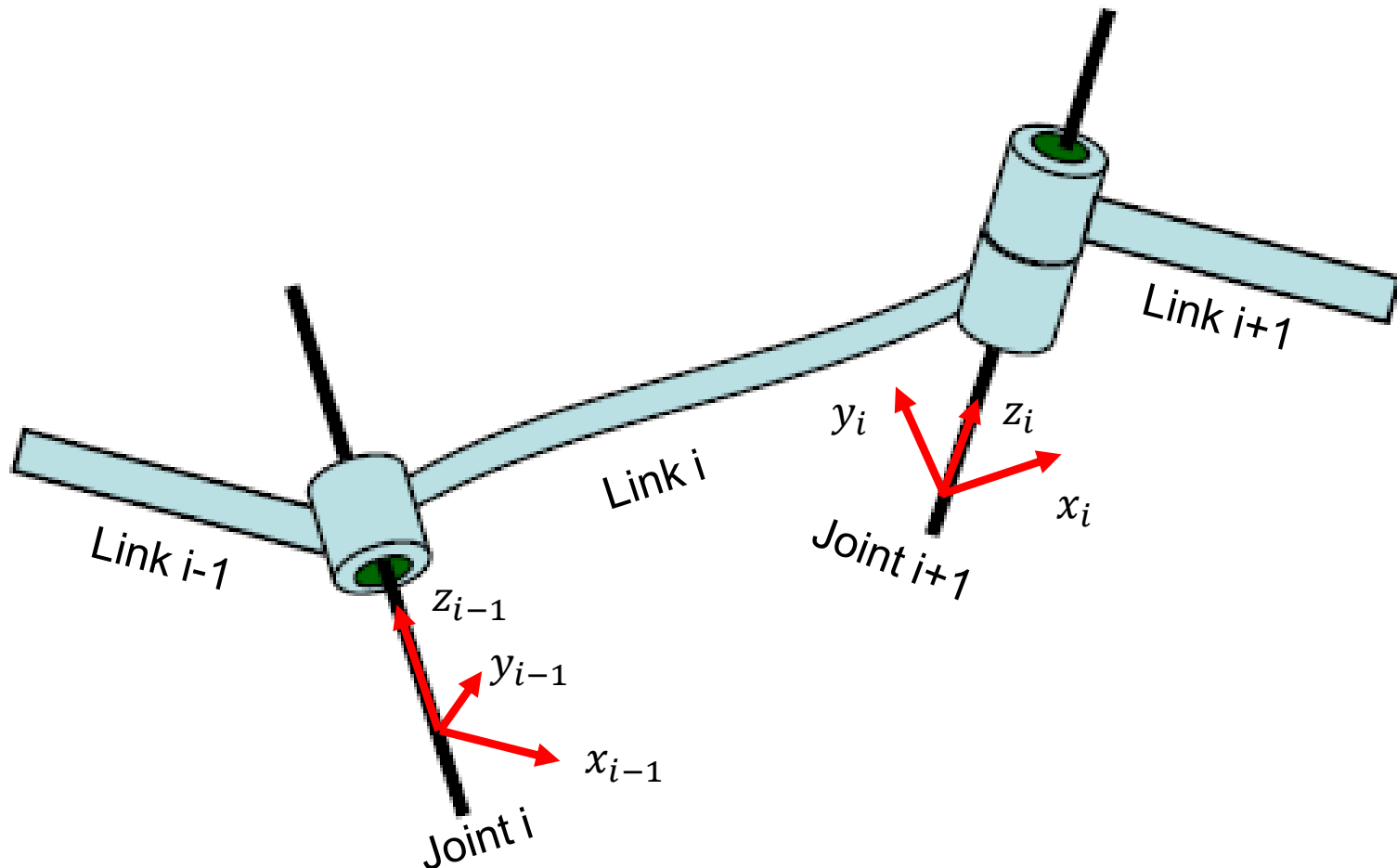
# Kinematic model: Denavit-Hartenberg convention

- Axis  $x_i$  is orthogonal to  $z_i$  and  $z_{i-1}$ :  $x_i = z_i \times z_{i-1}$ 
  - i.e.  $x_i$  is orthogonal to rotation axis and points along the link



# Kinematic model: Denavit-Hartenberg convention

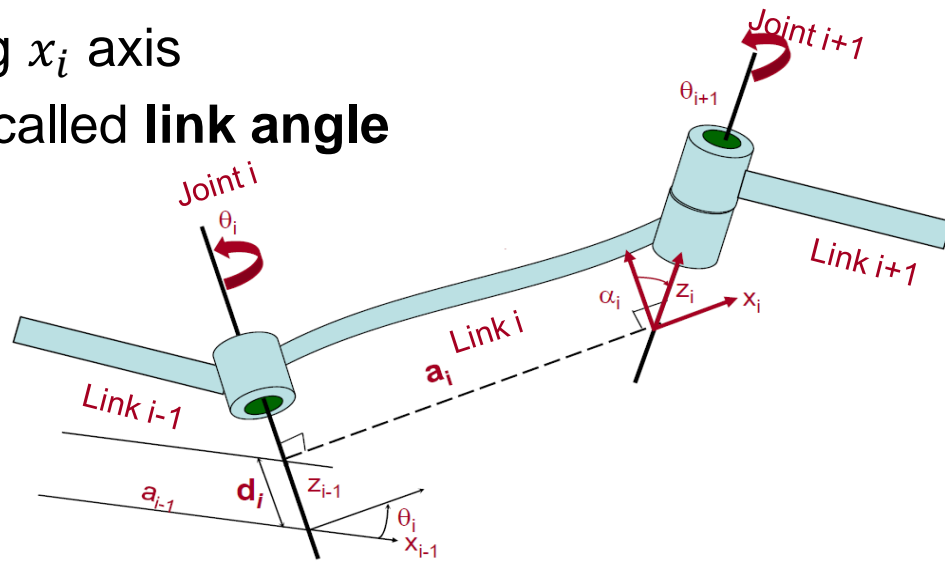
- Axis  $y_i$  is orthogonal to  $x_i$  and  $z_i$ :  $y_i = x_i \times z_i$  (right-handed coordinate system)



# Kinematic model: Denavit-Hartenberg convention

## Parameters of the link

- Each link is connected via 2 neighboring joints  $i$  and  $i+1$
- Let  $g_i$  and  $g_{i+1}$  be the axes of the joints (skewed to one another)
- Shared normal (base point distance) with the shortest distance is called **link length**  $a_i$
- Basis point of  $a_i$  with axis  $g_{i+1}$  is origin of the CS  $(x_i, y_i, z_i)$ 
  - $x_i$  axis: extension  $a_i$  to joint  $i+1$
  - $z_i$  axis: is in direction of  $g_{i+1}$  axis
  - $y_i$  axis: completed according to right-hand rule
- Link length  $a_i$  is translation along  $x_i$  axis
- Angle  $\alpha_i$  between  $z_{i-1}$  and  $z_i$  is called **link angle**

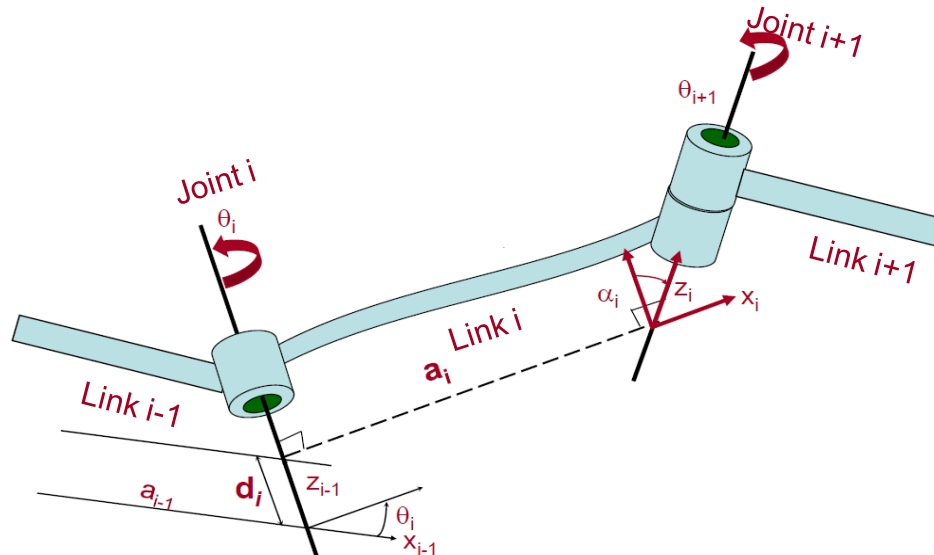




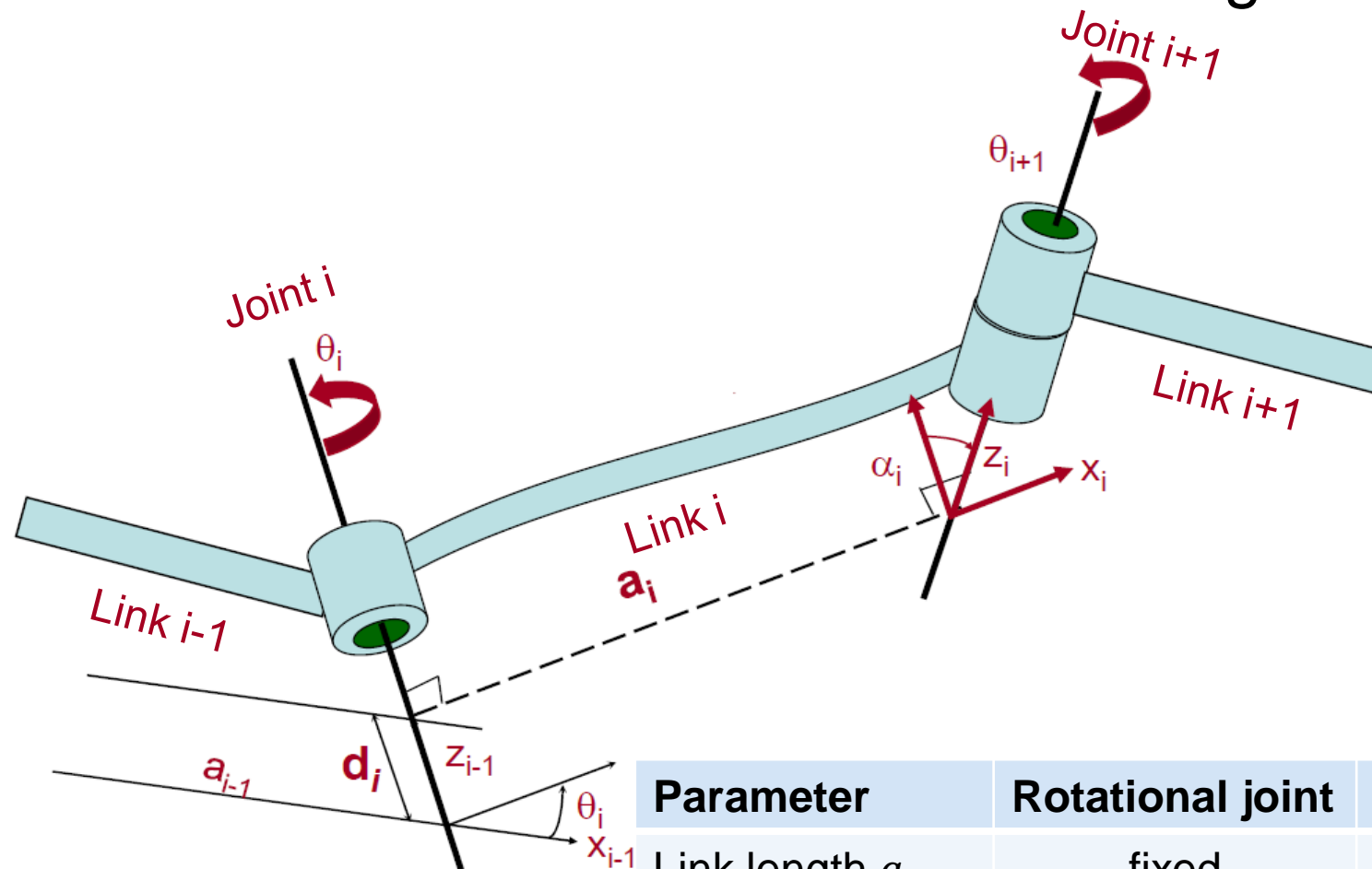
# Kinematic model: Denavit-Hartenberg convention

## Parameters of the joint

- Distance from origin  $i$  to origin  $i-1$  along  $z_{i-1}$  is called **joint distance  $d_i$**
- $d_i$  is translation along  $z_{i-1}$  axis so the x axes cut each other
- Rotation of link  $i$  around joint  $i$  with **joint angle  $\theta_i$**  makes  $x_{i-1}$  and  $x_i$  parallel to one another



# Kinematic model: Denavit-Hartenberg convention



| Parameter              | Rotational joint | Translational joint |
|------------------------|------------------|---------------------|
| Link length $a_i$      | fixed            | fixed               |
| Link angle $\alpha_i$  | fixed            | fixed               |
| Joint distance $d_i$   | fixed            | variable            |
| Joint angle $\theta_i$ | variable         | fixed               |

# Kinematic model: Denavit-Hartenberg convention

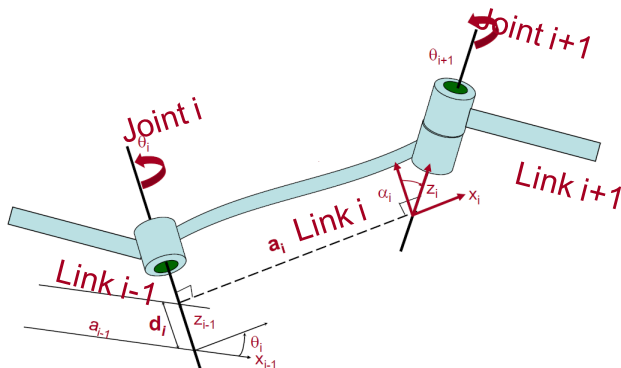
## Transformation from $OCS_i$ to $OCS_{i-1}$

1. A rotation of  $\theta_i$  around  $z_{i-1}$  axis, so  $x_{i-1}$  axis is parallel to  $x_i$  axis

$$R_{z_{i-1}}(\theta_i) = \begin{bmatrix} \cos \theta_i & -\sin \theta_i & 0 & 0 \\ \sin \theta_i & \cos \theta_i & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

2. A translation of  $d_i$  along  $z_{i-1}$  axis, so  $z_{i-1}$  axis and  $x_i$  axis cut each other

$$T_{z_{i-1}}(d_i) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & d_i \\ 0 & 0 & 0 & 1 \end{bmatrix}$$



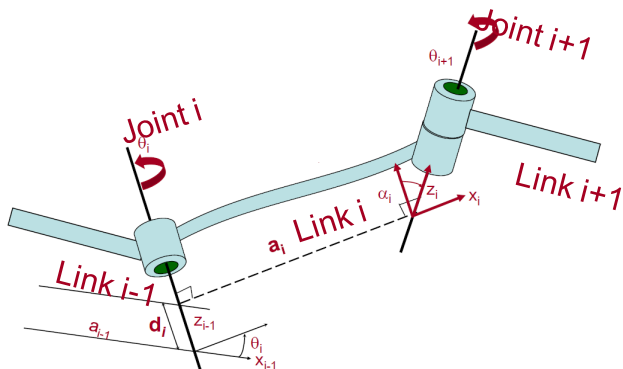
# Kinematic model: Denavit-Hartenberg convention

## Transformation from $OCS_i$ to $OCS_{i-1}$

3. A translation of  $a_i$  along  $x_i$  axis so the origins of the coordinate systems match

$$T_{x_i}(a_i) = \begin{bmatrix} 1 & 0 & 0 & a_i \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

4. A rotation of  $\alpha_i$  along  $x_i$  axis, so  $z_{i-1}$  axis and  $z_i$  axis match



$$R_{x_i}(\alpha_i) = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \alpha_i & -\sin \alpha_i & 0 \\ 0 & \sin \alpha_i & \cos \alpha_i & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

# Kinematic model: Denavit-Hartenberg convention

Transformation from  $\text{OCS}_i$  to  $\text{OCS}_{i-1}$

$$A_{i-1,i} = R_{z_{i-1}}(\theta_i) \cdot T_{z_{i-1}}(d_i) \cdot T_{x_i}(a_i) \cdot R_{x_i}(\alpha_i)$$

**Forward kinematic:**

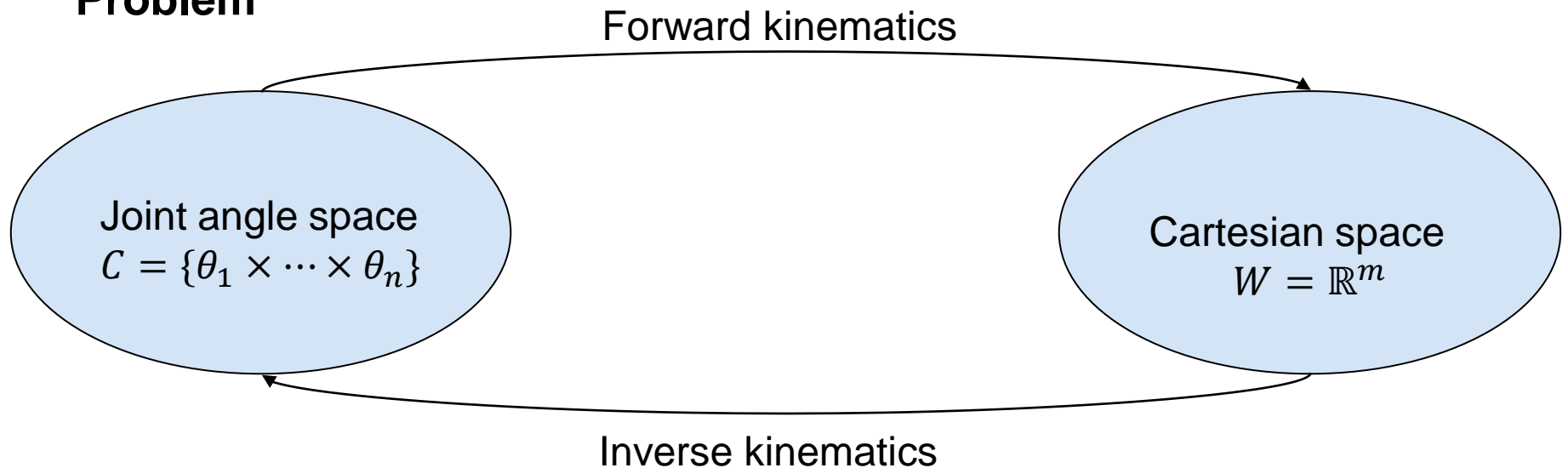
Transformation from  $\text{OCS}_{\text{basis}}$  ( $i=0$ ) to  $\text{OCS}_{\text{end effector}}$  ( $i=n$ )

$$A_{0,n}(\theta) = A_{0,1}(\theta_1) \cdot A_{1,2}(\theta_2) \cdot \cdots \cdot A_{n-1,n}(\theta_n) = \prod_{i=1}^n A_{i-1,i}(\theta_i)$$

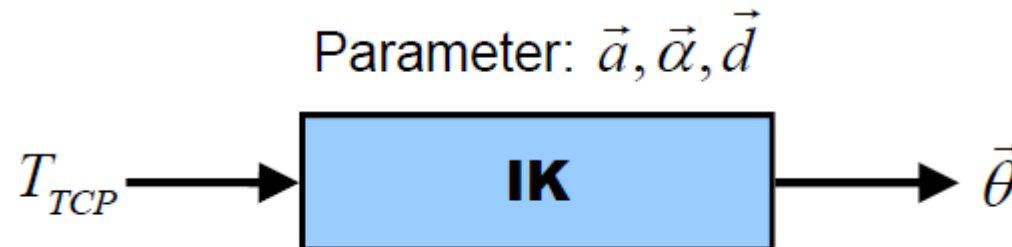
$\theta_i$ : Variable joint parameter (joint angle)

# Kinematic model: Inverse kinematics

## Problem



n: DOF movement, i.e. number of joints  
m: DOF



# Kinematic model: Inverse kinematics

## Approach

- Pose of end effector ( $T_{TCP}$ ) is given
- Kinematic model

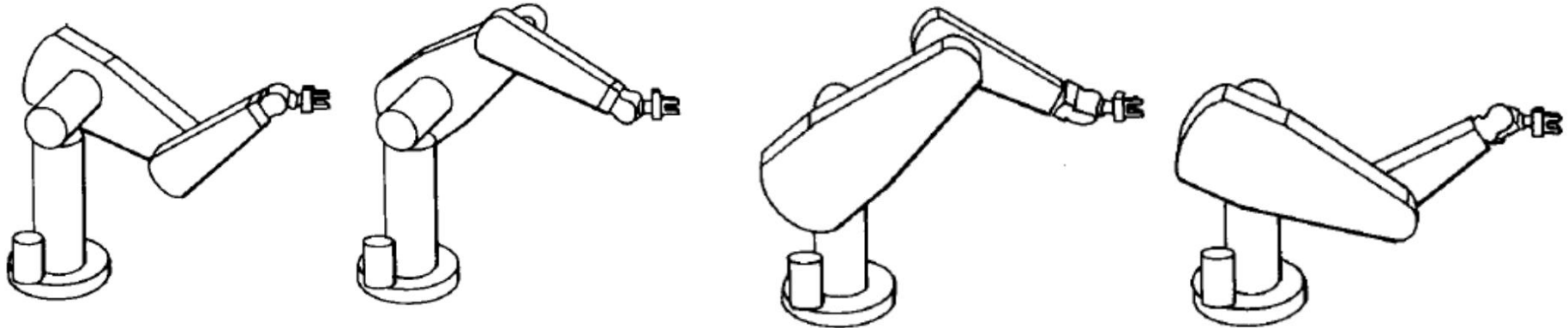
$$T_{TCP} = A_{0,n}(\theta) = \prod_{i=1}^n A_{i-1,i}(\theta_i)$$

- Solve for  $\theta$
- Non-linear problem



# Kinematic model: Inverse kinematics

- Unreachable pose: Outside of the arm radius of the robot
- Invalid pose: In principle reachable, but not possible due to physical boundaries
  - Construction-based restraints (workspace)
  - Collisions with obstacles in workspace
  - Collision of handled objects or end effector with obstacles or the robot itself
- Uniqueness of configurations
  - In a plane, a system with  $n \geq 3$  DOF in movement has multiple possibilities for reaching a given end effector pose
  - In 3D, the same is true for a robot with  $n \geq 6$  DOF in movement



Same end effector pose with different configurations

# Kinematic model: Inverse kinematics

## Properties inverse kinematics

- No general applicable method
- Has to be fast

## Solving

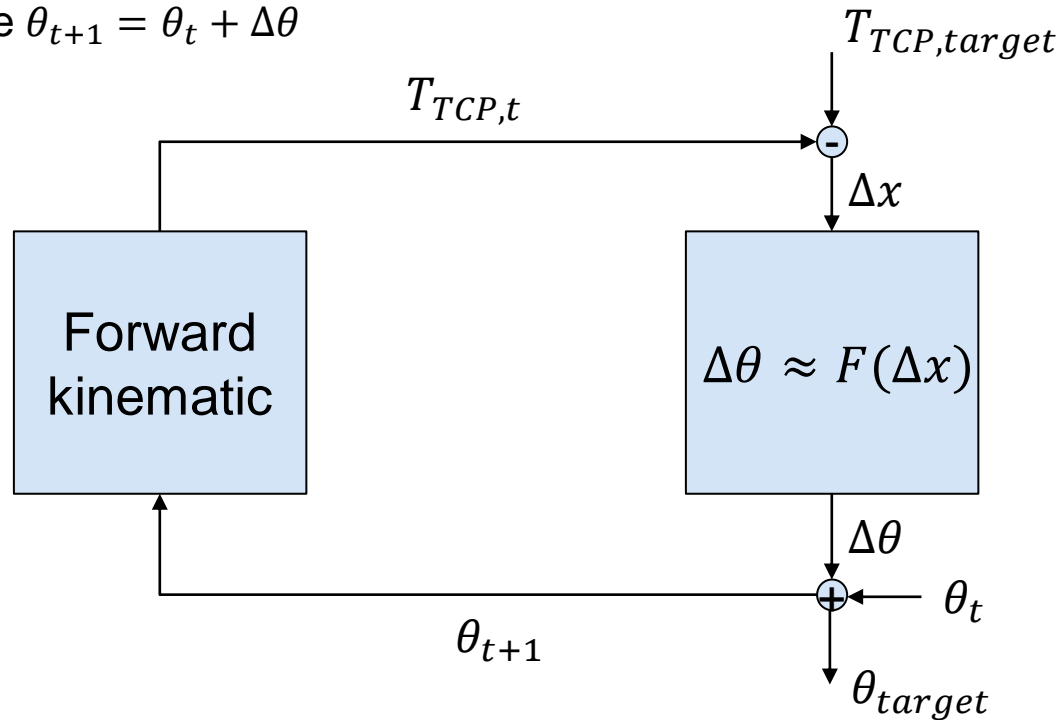
- Solution in closed form
  - Geometric methods
    - Trigonometric functions
    - Difficult to solve due to non-linear terms
  - Analytical methods
    - Solve analytically
    - 16 equations, 12 non-trivial
    - Often not enough to solve for all parameters
- **Numerical methods**

# Kinematic model: Inverse kinematics

## Numerical methods

- Iterative approach

- Compute  $T_{TCP,t}$  in iteration  $t$  from current joint angles  $\theta_t$  ( $\theta_0$ = actual position robot)
- Compute error  $\Delta x$   $T_{TCP,t}$  and  $T_{TCP,target}$
- Use approximated inverse kinematic model  $F$  to compute joint angle error  $\Delta\theta$
- Compute  $\theta_{t+1} = \theta_t + \Delta\theta$



# Kinematic model: Inverse kinematics

Numerical methods: Approach Jacobian

1. Forward kinematics as function

$$x(t) = f(\theta(t))$$

2. Derivative with respect to time

$$\frac{dx(t)}{dt} = \dot{x}(t) = J(\theta)\dot{\theta}(t)$$

3. Difference quotient

$$\Delta x \approx J(\theta)\Delta\theta$$

4. Inversion

$$\Delta\theta \approx J^{-1}(\theta)\Delta x$$

$x(t)$ : Pose end effector

$\theta(t)$ : Joint angles

$\dot{x}(t)$ : Velocity end effector

$\dot{\theta}(t)$ : Joint angle velocities

$J(\theta)$ : Jacobian matrix

$\Delta x$ : Error in end effector

$\Delta\theta$ : Error in joint angles

# Dynamic model

- Definition: Relationship between forces, momentum and motion that occur in a system
- Purpose
  - Analysis of dynamics
  - Synthesis of mechanical structures
  - Modelling of elastic structures
  - Controller design

$$Q = M(q) \cdot \ddot{q} + n(\dot{q}, q) + g(q) + R \cdot \dot{q}$$

- $Q$ : Vector of forces and momentum
- $M(q)$ : Mass inertia matrix
- $n(\dot{q}, q)$ : Vector of centrifugal and Coriolis components
- $g(q)$ : Gravitational components
- $R$ : Diagonal matrix describing friction forces
- $q$ : Angular position of the robot arm

# Dynamic model

$$Q = M(q) \cdot \ddot{q} + n(\dot{q}, q) + g(q) + R \cdot \dot{q}$$

- Forward dynamic problem
  - Given external forces and momentums as well as initial state of the robot, compute movement changes

=> Solve for  $q(t), \dot{q}(t), \ddot{q}(t)$

- Inverse dynamic problem
  - Given target movement parameters, compute required forces and momentums

=> Compute  $Q$

# Path planning

- Definition: Methods for planning collision-free movements
- Movements of the robot are seen as state changes over time relative to a stationary coordinate system
- Given:
  - $S_{start}$ : State at initial position
  - $S_{target}$ : State at end position
- Goal
  - $S_i$ : intermediate states for a smooth and continuous movement

# Path planning: Terms

- A **configuration**  $q$  describes the state of the robot
  - In Euclidean space through its pose
  - In joint angle space through the values of the joints
- The **configuration space**  $\mathcal{C}$  is the space of all possible configurations of the robot
- A **path** is a continuous map from the configuration  $q_{start}$  to configuration  $q_{target}$

$$\tau: [0,1] \rightarrow \mathcal{C}$$

$$\text{With } \tau(0) = q_{start}, \tau(1) = q_{target}$$

- A **workspace obstacle**  $H_i$  is the space taken up by an object in workspace
- **Configuration space obstacle**  $\mathcal{C}H_i$  is the set of all configurations that result into points in  $H_i$
- **Obstacle space** is the set of all configuration space obstacles

$$\mathcal{C}_{obst} = \bigcup \mathcal{C}H_i$$

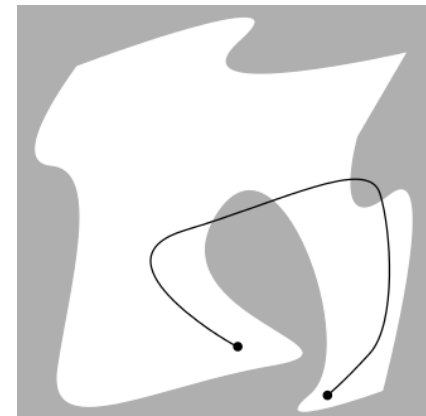
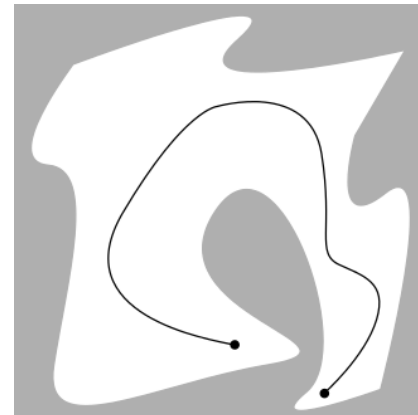


# Path planning: Terms

- **Free space** is the set of all points from  $C$  that are not in obstacle space

$$C_{free} = \{q \in C \mid q \notin C_{obst}\} = C \setminus C_{obst}$$

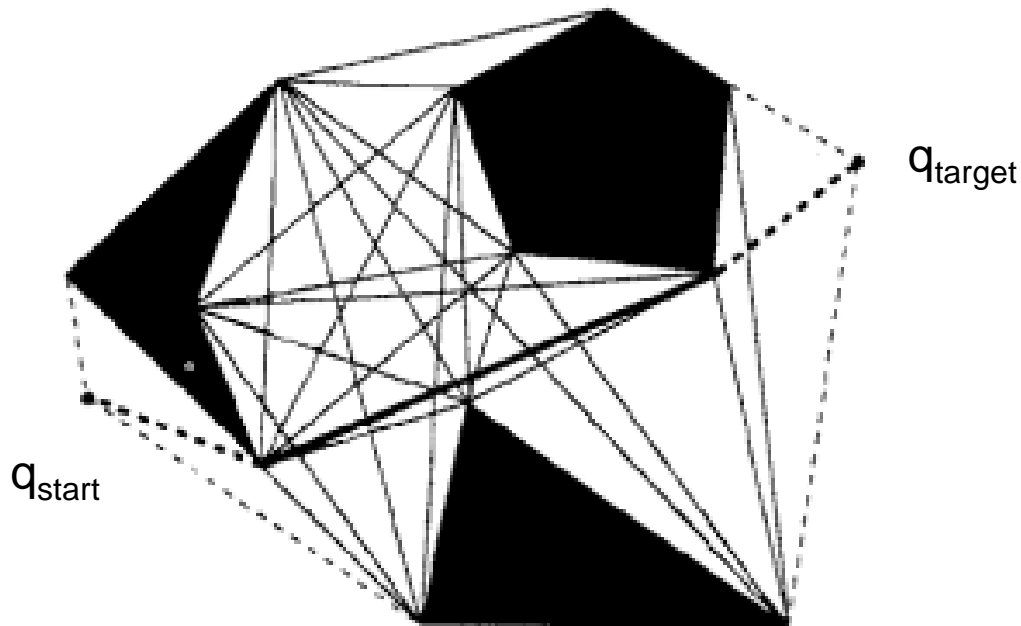
- Cost of computing free space:  $O(m^n)$ 
  - With  $n$ : Movement DOF of the robot (number of joints)  
     $m$ : Number of obstacles
  - Costly for complex ( $n > 3$ ) systems  $\Rightarrow$  Approximate free space
    - Voronoi diagrams
    - Visibility graphs
    - Quad- or Octtrees
    - Rapidly-exploring Random Trees



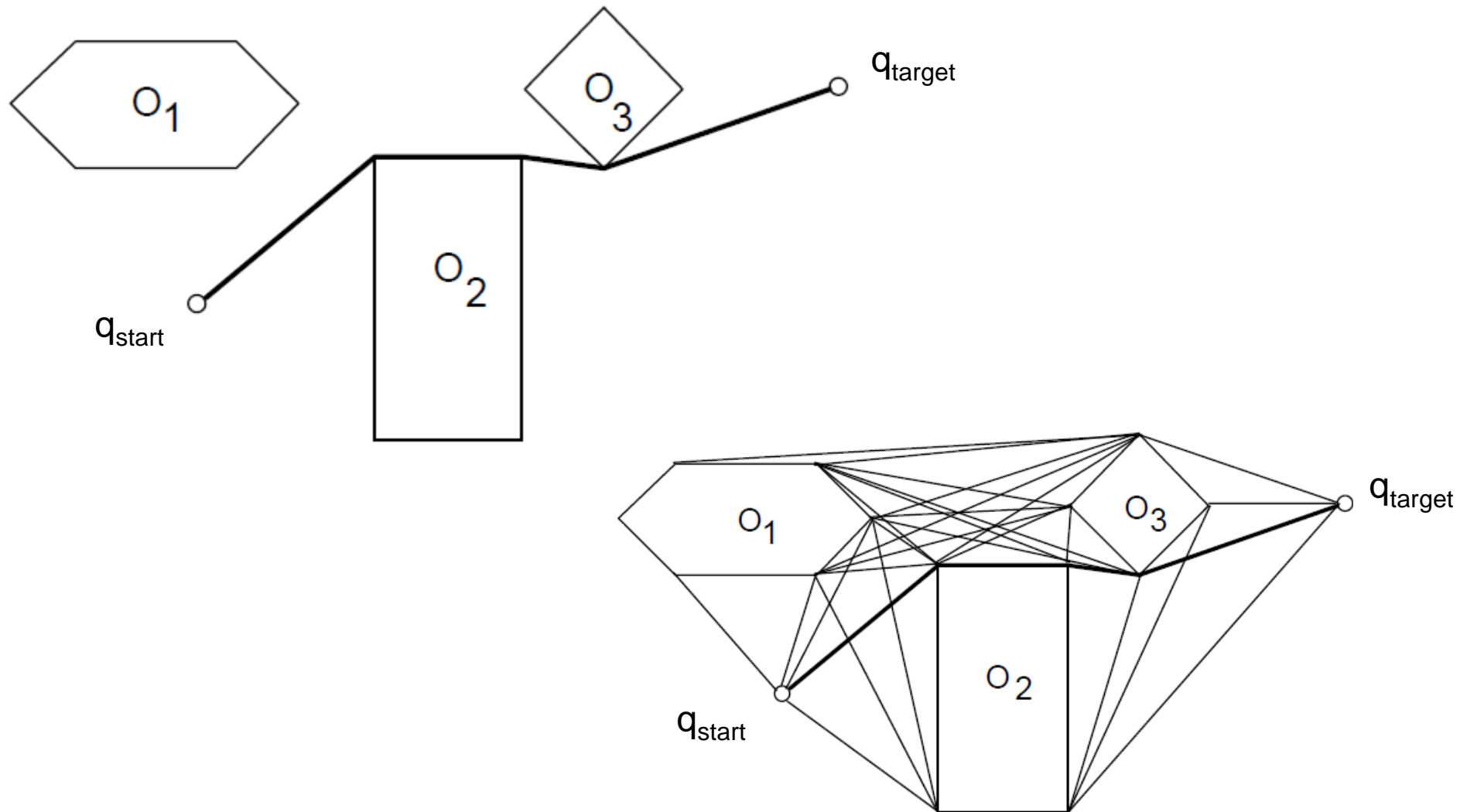
# Path planning: Visibility graph

- **Construction**

- Connect each pair of corner points on the edge of  $C_{free}$  if the line segment does not cross an obstacle
- Connect  $q_{start}$  and  $q_{target}$

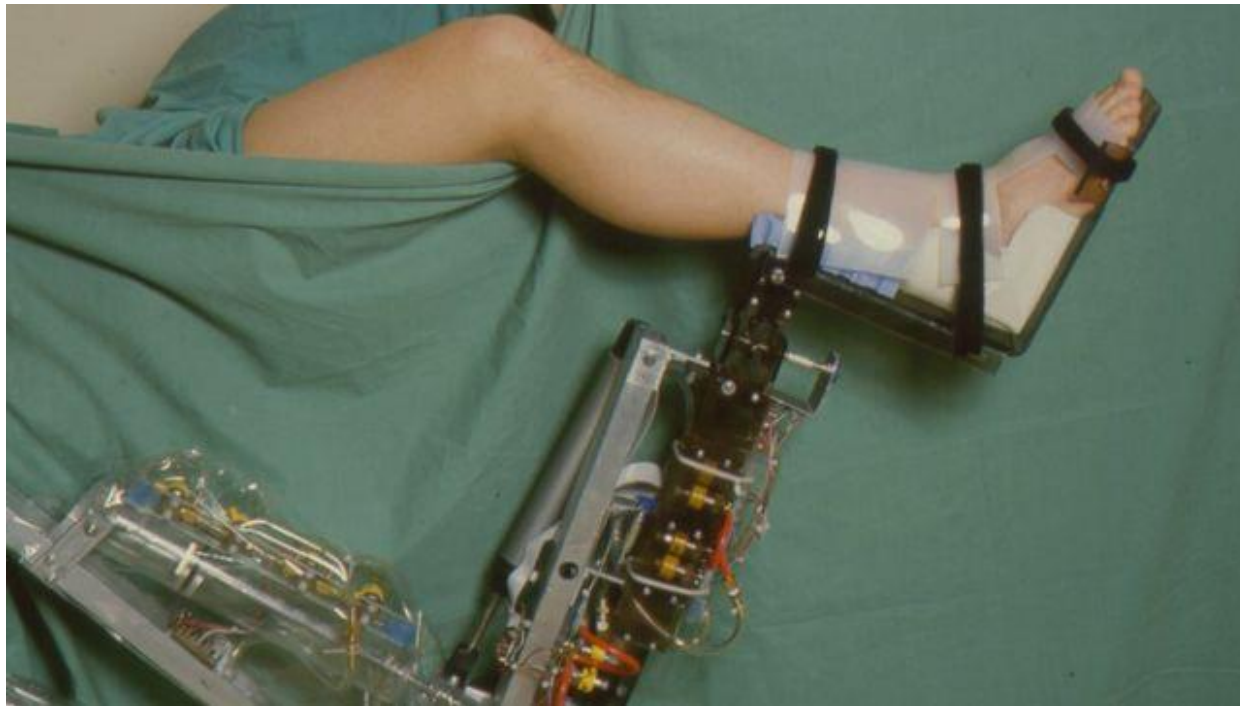


# Path planning: Visibility graph



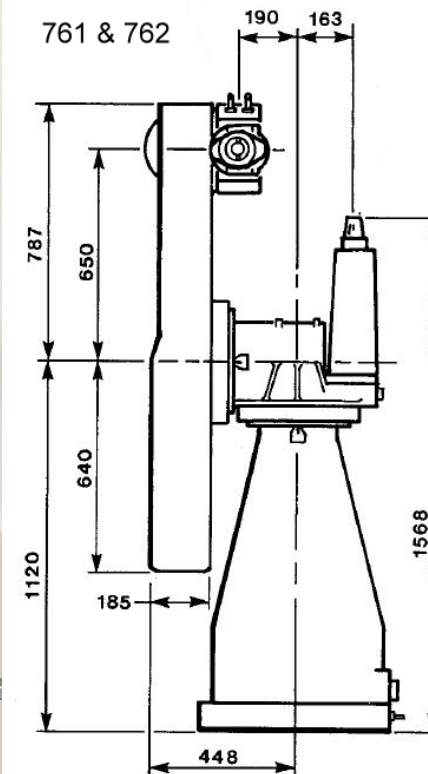
# History of surgical robots: Arthobot (1985)

- From University of British Columbia
- Assistant for orthopedic surgery
- Changes leg position via voice command



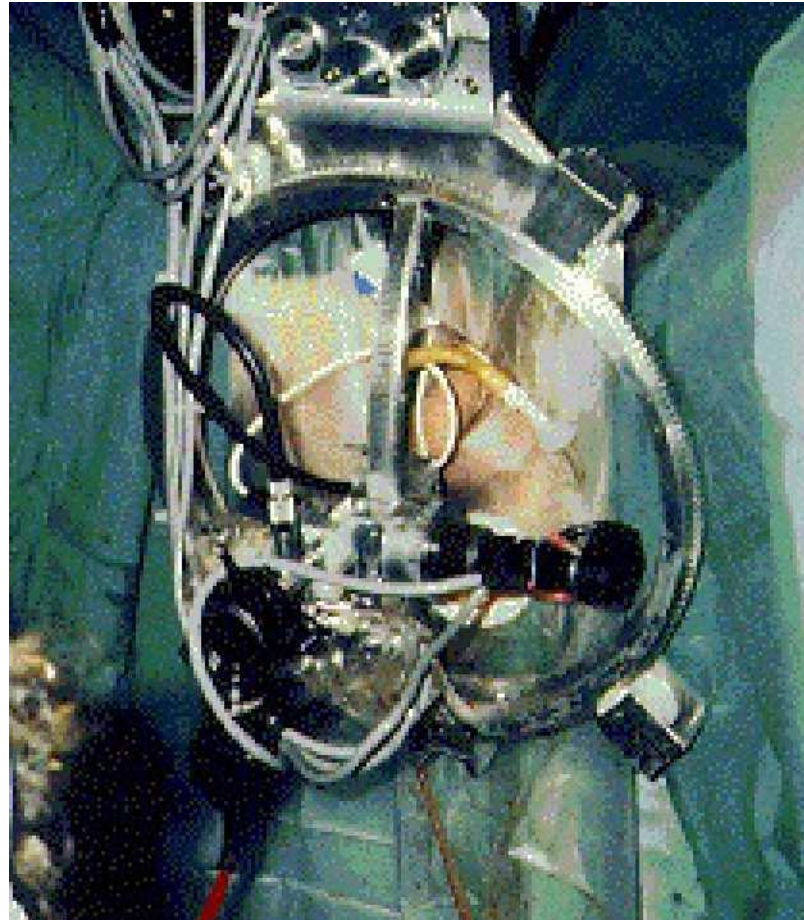
# History of surgical robots: Unimation Puma 200(1985)

- Industrial robot
- Needle orientation for brain biopsy with CT guidance



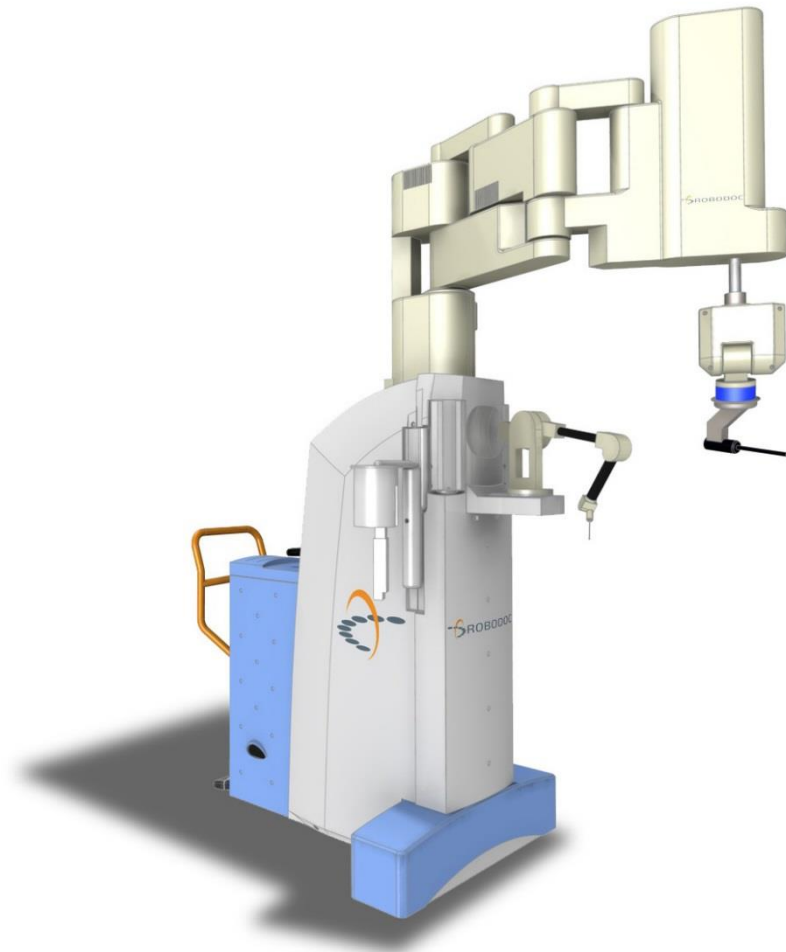
# History of surgical robots: PROBOT (late 1980s)

- Robot for prostate resection
- Surgeon can specify within the prostate to be automatically cut



# History of surgical robots: ROBODOC (1992)

- Robot for computer-guided milling of bone during hip replacement
- Needle orientation for brain biopsy with CT guidance





# History of surgical robots: AESOP (1994)

- Automated Endoscopy System
- Robot for moving endoscope
- Voice activated





# History of surgical robots: ZEUS (1998)

- Combines AESOP with two arms for holding instruments
- Tele-robot
- 3D vision



Zeus Robot Arms



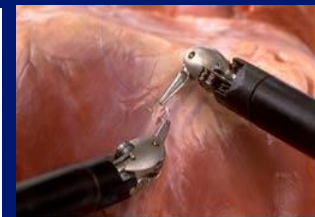
Zeus Console

# History of surgical robots: da Vinci (2000)

Konsole



Manipulator



Quelle: Intuitive Surgical

# DaVinci



# Current Systems for minimal invasive surgery

- Versius Surgical Robotic System by CMR Surgical



- Senhance Surgical System by Asensus Surgical



# Current Systems for minimal invasive surgery

- Hugo Robotic Assisted Surgery System by Medtronic

