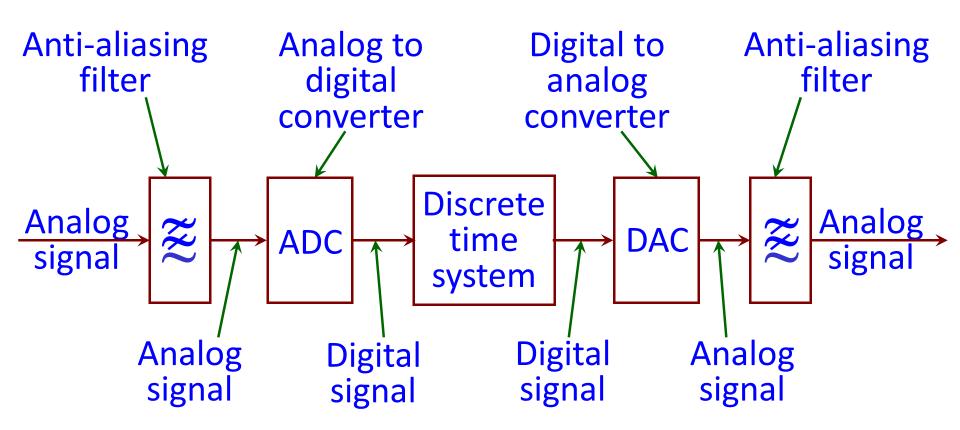
# Week 4 Signal Processing Systems

### **Typical DSP Systems**



# Where Does the Signal Come From?

# Where Does the Signal Come From?

☐ A sensor acquires a physical parameter and converts it into a signal suitable for processing

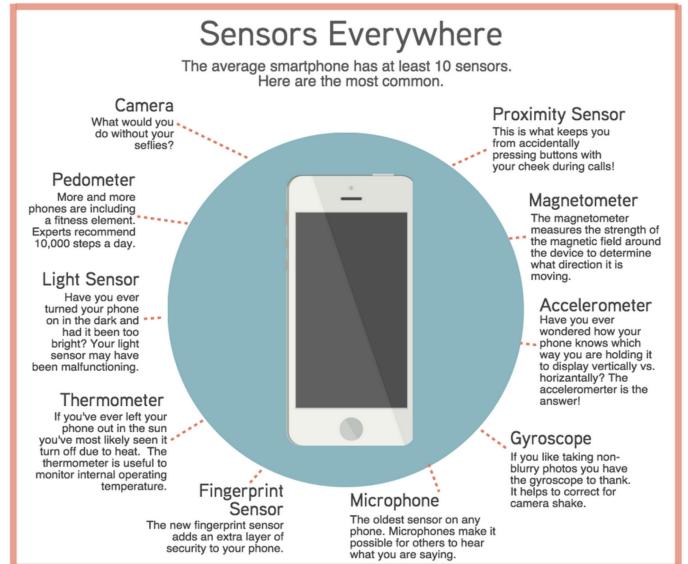


# Where Does the Signal Come From?

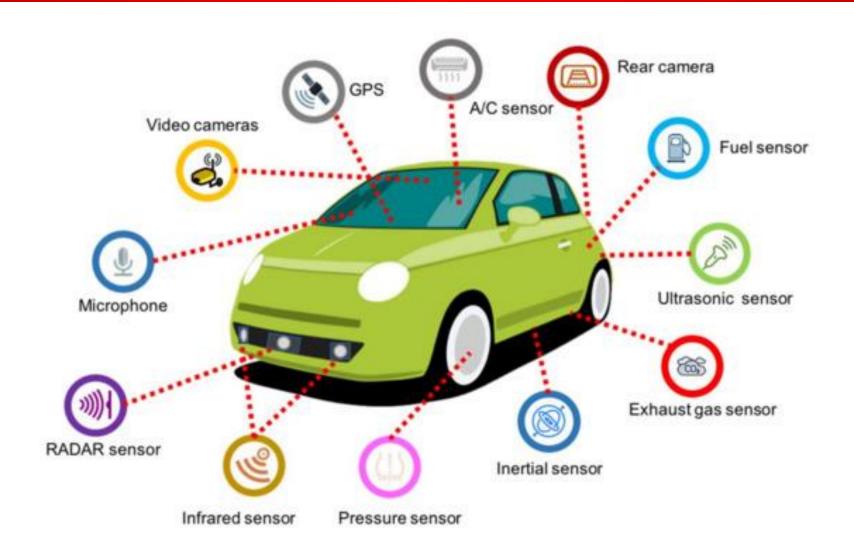
- Sensors
  - **≻**Temperature Sensor
  - ► Light Sensor
  - **Accelerometer**
  - ➤ Magnetic Field Sensor
  - ➤ Ultrasonic Sensor
  - >Photogate
  - ➤ CO2 Gas Sensor



#### **Sensors In a Smart Phone**

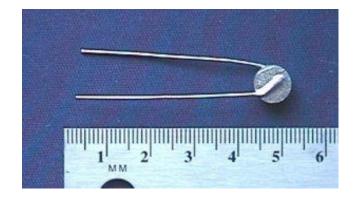


#### Sensors In a Car



#### **Temperature Sensor**

# thermal resistor "thermistor"

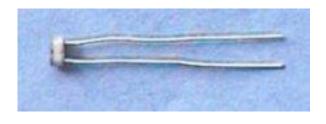




resistance changes with temperature

# **Light Sensor**

#### photo-resistor





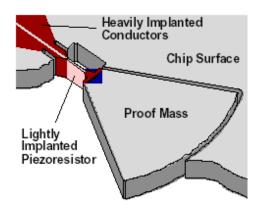
resistance changes with light intensity

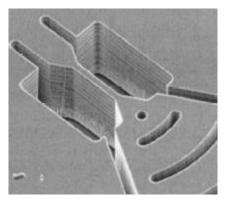
### **Physical Principles**

- ☐ Ampere's Law
  - A current carrying conductor in a magnetic field experiences a force (e.g. galvanometer)
- ☐ Faraday's Law of Induction
  - A coil resist a change in magnetic field by generating an opposing voltage/current (e.g. transformer)
- ☐ Photoconductive Effect
  - When light strikes certain semiconductor materials, the resistance of the material decreases (e.g. photoresistor)

# **Different Sensing Techniques**

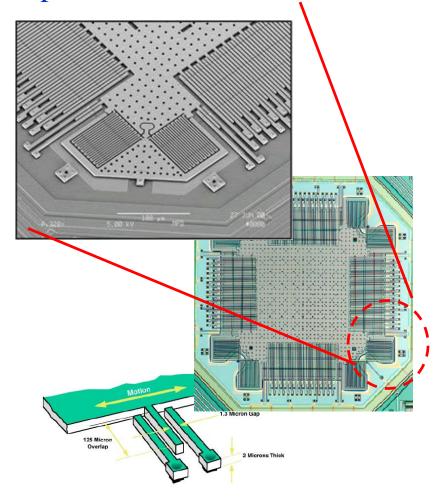
#### Piezoresistive MEMS accelerometer

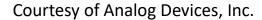




Courtesy of JP Lynch, U Mich.

#### Capacitive MEMS accelerometer







# **Sensor Signal Conditioning**

- ☐ Manipulation of an analog signal in such a way that it meets the requirements of the next stage for further processing
  - **Amplification**
  - **Limiting**
  - **Linearization**
  - >Anti-aliasing filtering
  - >...

**EE111 Electric Circuits** 



# From Analog to Digital

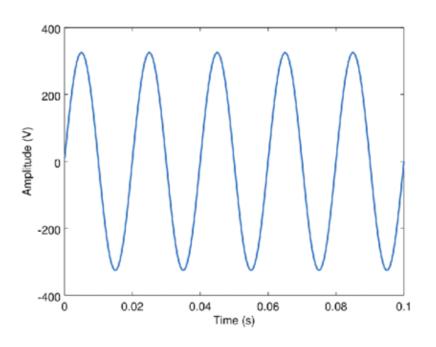
# The World is Analog

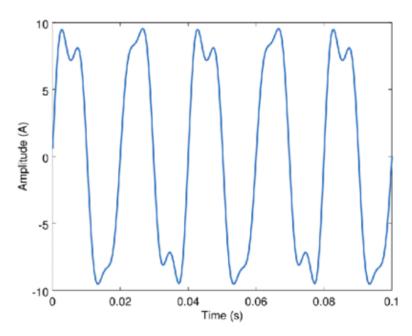
#### ☐ All the sensed signal is analog



# The World is Analog

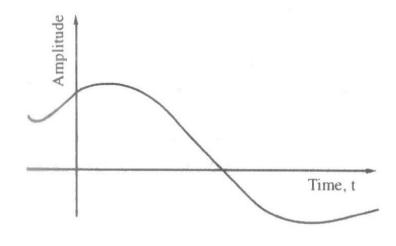
#### □ Common sensor output: voltage and current



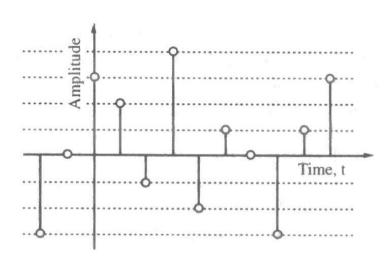


# **Analog & Digital Signal**

- □ Analog signal
  - Continuous-time signal with continuous-valued amplitude
  - ➤ Most of the natural signals are analog



- ☐ Digital signal
  - Discrete-time signal with discrete-valued amplitude
  - A digital signal is a quantized sampled-data signal



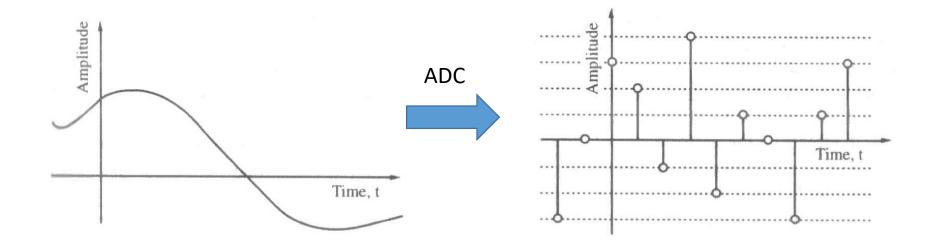
# Digital Processing Has Many Advantages

- ☐ Digital processing has many advantages
  - Refer to slides of week 1

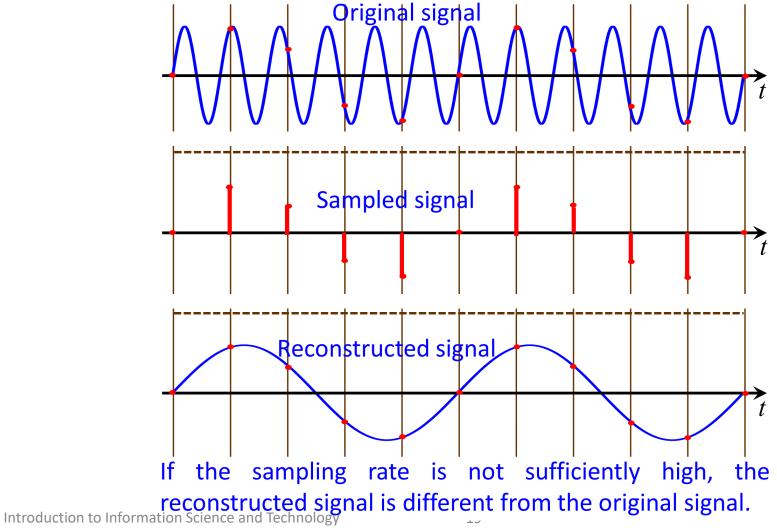




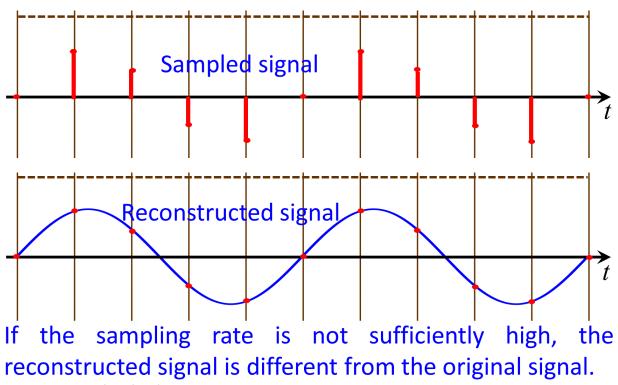
# The Bridge Between Analog and Digital



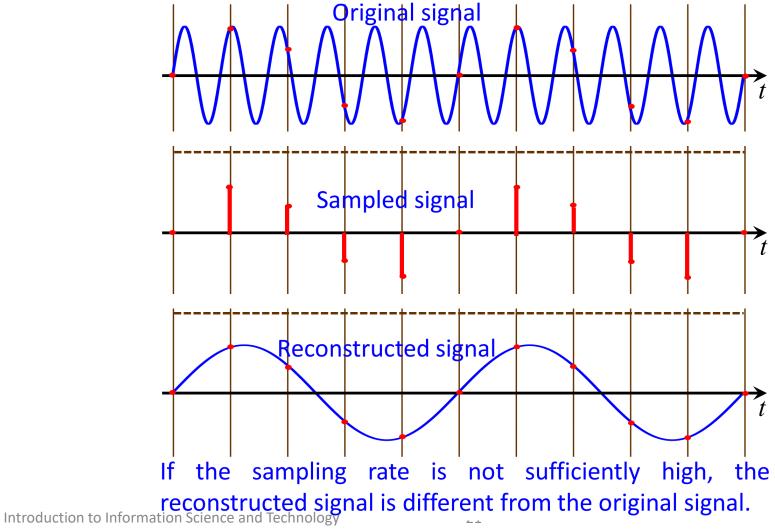
□ Q1: can we recover the original continuous signal?



□ Q1: can we recover the original continuous signal?



□ Q1: can we recover the original continuous signal?



#### The Famous Nyquist Theorem



**Birthdate** 

1889/02/07

**Birthplace** 

Nilsby, Sweden

Death date

1976/04/04

**Associated organizations** 

**Bell Labs** 

Fields of study

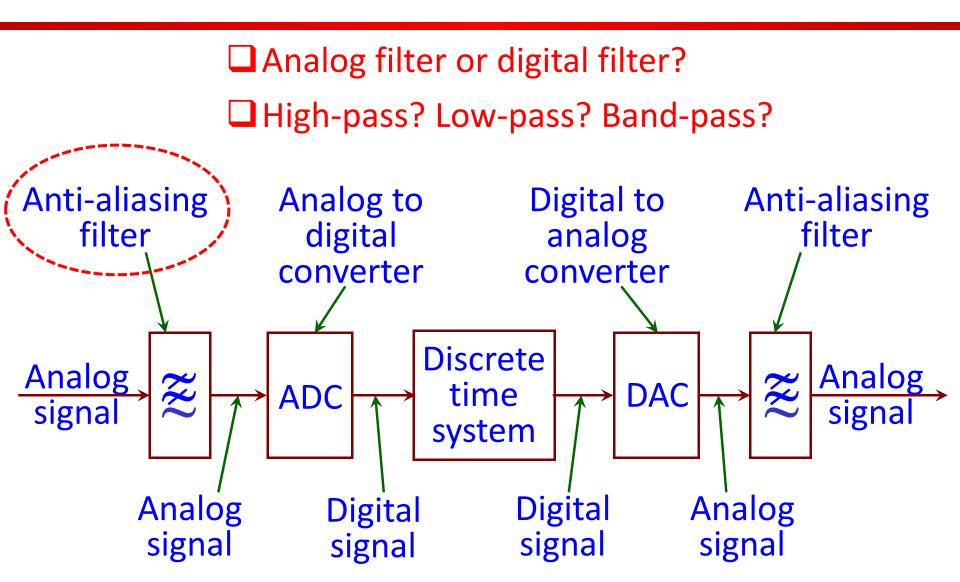
Signal processing

**Awards** 

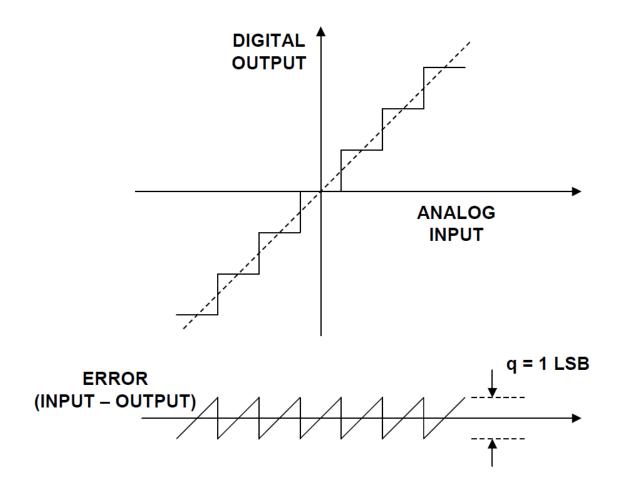
IRE Medal of Honor, Stuart Ballantine Medal of the Franklin Institute, Mervin J. Kelly award

☐ The Nyquist Theorem states that in order to adequately reproduce the original signal it should be periodically sampled at a rate that is 2X the highest frequency you wish to record

# **Typical DSP Systems**



□ Q2: how many bits we need to represent a sample?





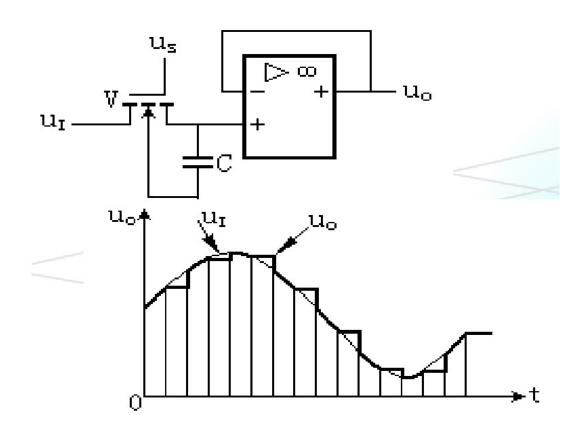
#### ☐ Commonly used ADC

➤8-bit, 10-bit, 12-bit, 14-bit, 16-bit, 24-bit

模拟电压Ui	量化结构	二进制码
0~1/8V	0V	0 0 0
1/8~2/8V	1/8V= △	0 0 1
2/8~3/8V	2/8V=2 ∆	0 1 0
3/8~4/8V	3/8V=3 ∆	0 1 1
4/8~5/8V	4/8V=4 ∆	1 0 0
5/8~6/8V	5/8V=5 ∆	1 0 1
6/8~7/8V	6/8V=6 ∆	1 1 0
7/8~8/8V	7/8V=7 △	微言 <b>4 al</b> n- <b>1</b> rina

#### **How Does an ADC Work?**

#### □ Sample & hold



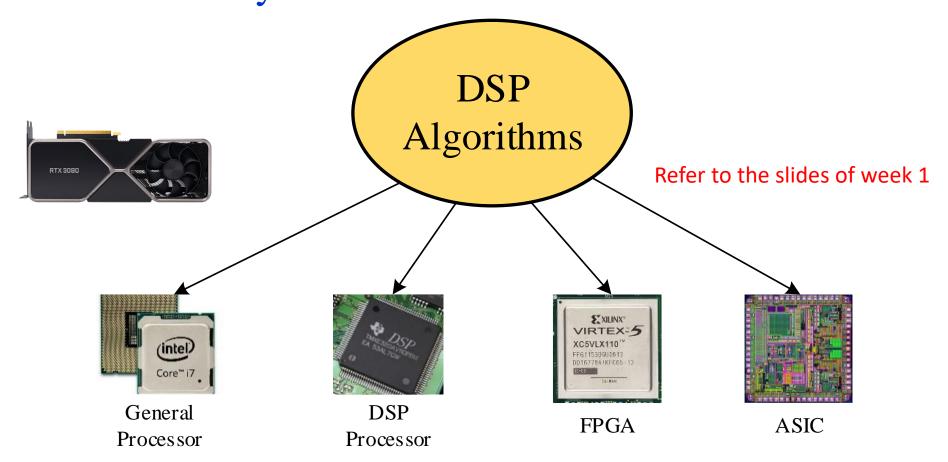
#### **How Does an ADC Work?**

#### ☐ Quantize & coding

模拟电压Ui	量化结构	二进制码
0~1/8V	0V	0 0 0
1/8~2/8V	1/8V= △	0 0 1
2/8~3/8V	2/8V=2 ∆	0 1 0
3/8~4/8V	3/8V=3 ∆	0 1 1
4/8~5/8V	4/8V=4 ∆	1 0 0
5/8~6/8V	5/8V=5 ∆	1 0 1
6/8~7/8V	6/8V=6 ∆	1 1 0
7/8~8/8V	7/8V=7 △	微言 <b>4: e1</b> in- <b>1</b> ning

### The Discrete-time System

☐ A given DSP algorithm can be implemented in various ways



# The Discrete-time System

☐ Fixed point VS Floating point



#### **Fixed Point Number**

- ☐ Fixed-point arithmetic
  - >high speed
  - **►**Low complexity
- □ Represented by an integer with a scaling factor

$$X = x_{W-1}x_{W-2}...x_M \cdot x_{M-1}...x_0 = x_{W-1}x_{W-2}...x_0 \times r^{-M}$$

### **Decimal Number System**

□ Decimal number system uses the 10 symbols (0, 1, 2, 3, 4, 5, 6, 7, 8, 9) to represent a number

#### □ Example:

$$(456)_{10} = 4 \times 10^2 + 5 \times 10^1 + 6 \times 10^0$$

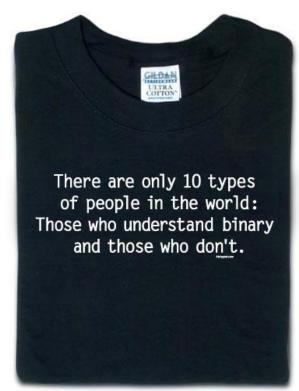
$$(3705.86)_{10} = 3 \times 10^{3} + 7 \times 10^{2} + 0 \times 10^{1} + 5 \times 10^{0} + 8 \times 10^{-1} + 6 \times 10^{-2}$$

#### **Binary Number System**

☐ In binary number system, 2 symbols (0 and 1) are used to represent a number

#### ☐ Example:

$$(101.01)_2 = (2^2)_{10} + (2^0)_{10} + (2^{-2})_{10}$$
  
=  $(4)_{10} + (1)_{10} + (0.25)_{10}$   
=  $(5.25)_{10}$ 



# Binary Number System (cont'd)

☐ Unsigned binary

$$X = x_{W-1} x_{W-2} \dots x_0 = \sum_{k=0}^{W-1} x_k \cdot 2^k, \ x_k \in \{0, 1\}$$

- □ The range of an *N*-bit unsigned binary number is  $[0, 2^N-1]$ 
  - The largest 4-bit number is  $(1111)_2 = 16$
- Negative number is not represented. To represent negative numbers, an extra bit, called sign bit is needed

#### **Negative Numbers**

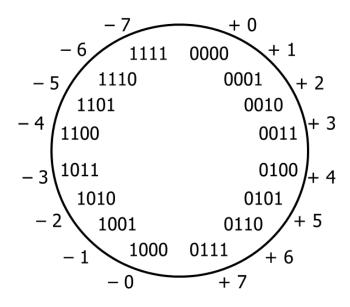
- ☐ Three approaches to represent negative numbers
  - ➤ Sign and magnitude
  - ➤ Two's-complement

☐ The two approaches represent positive numbers in the same way

### Signed-Magnitude

- ☐ The most significant bit (MSB) is the sign bit
- □ Remaining bits are the number's magnitude

$$X = x_{W-1} x_{W-2} \dots x_0 = (-1)^{x_{W-1}} \sum_{k=0}^{W-2} x_k \cdot 2^k, \ x_k \in \{0, 1\}.$$



# Sign and Magnitude (cont'd)

☐ Problem 1: Two representations of for zero

$$\rightarrow$$
 +0 = 0000 and -0 = 1000

☐ Problem 2: Arithmetic is cumbersome

$$>4-3 \neq 4+(-3)$$

	dd	
$\Delta$	a	
4	uu	

#### Subtract

#### Compare and subtract

4	0100	4	0100	0100	- 4	1100	1100
+ 3	+ 0011	- 3	+ 1011	- 0011	+ 3	+ 0011	- 0011
= 7	= 0111	= 1	≠ 1111	= 0001	- 1	≠ 1111	= 1001

### Two's complement

□ Negative number

>0111 
$$\equiv 7_{10}$$
  
>1001  $\equiv -7_{10}$ 

☐ The value of a two's complement number is

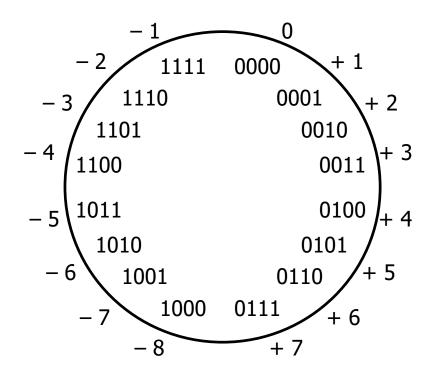
$$X = x_{W-1}x_{W-2}...x_0 = -x_{W-1} \cdot 2^{W-1} + \sum_{k=0}^{W-2} x_k \cdot 2^k, \ x_k \in \{0, 1\}.$$

☐ The MSB carries a negative weight

$$(1101)_{2's} = -2^3 + 2^2 + 2^0 = -8 + 4 + 1 = -3$$
  
 $(1001)_{2's} = -2^3 + 2^0 = -8 + 1 = -7$   
 $(0110)_{2's} = 2^2 + 2^1 = 4 + 2 = 6$   
 $(110)_{2's} = -2^2 + 2^1 = -4 + 2 = -2$ 

## Two's complement (cont'd)

- □ The range of an *N*-bit two's complement number is  $[-2^{N-1}, 2^{N-1}-1]$
- ☐ For a 4-bit two's complement number



## Two's complement (cont'd)

□ Benefits:

**EE115** Analog and Digital Circuits

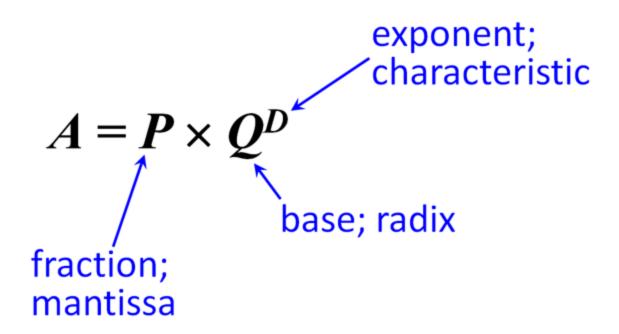
- >Simplified arithmetic
- ➤Only one zero!

	Add	Invert a	and add	Invert	and add
4	0100	4	0100	- 4	1100
+ 3	+ 0011	<b>–</b> 3	+ 1101	+ 3	+ 0011
= 7	= 0111	= 1	1 0001	- 1	1111
		drop carry	= 0001		

☐ As long as the results can be represented (no overflow)!

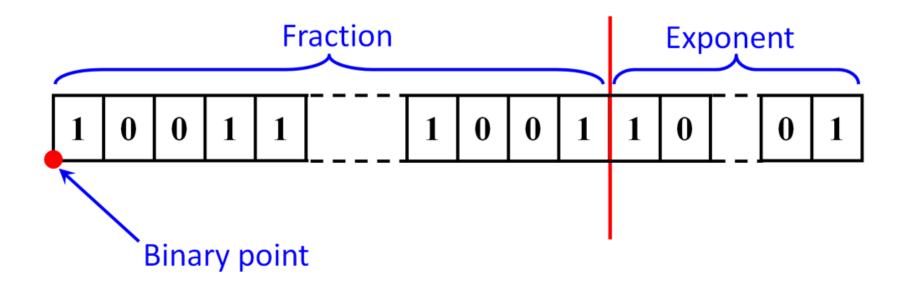


### Floating Point Number



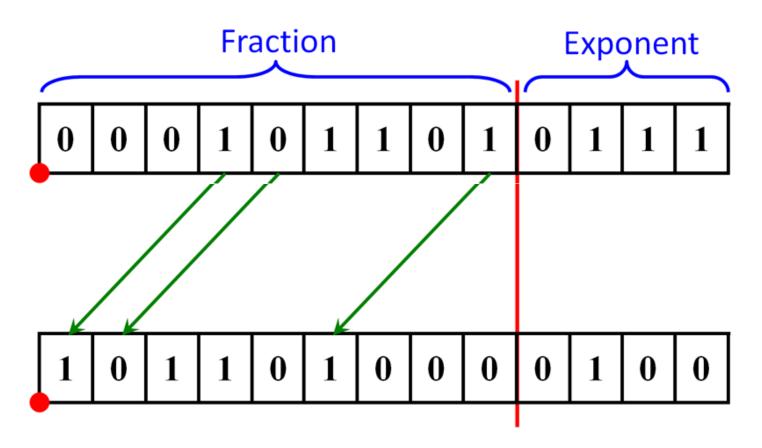
Example: 8934 can be written as  $0.8934 \times 10^4$ 

# Binary Representation of Floating Point Number



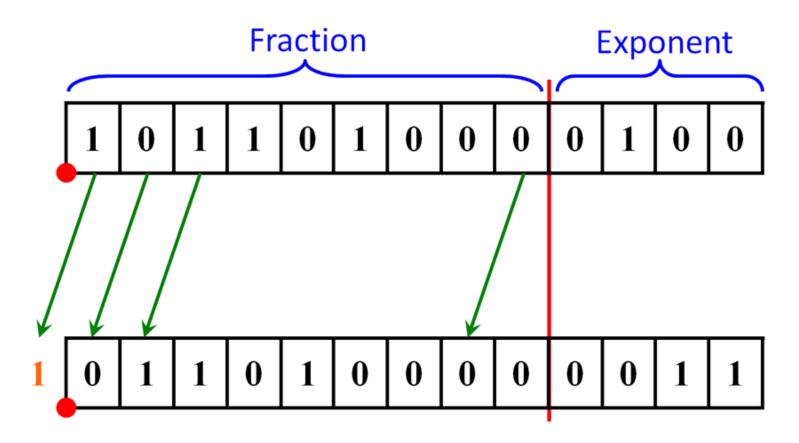
# Binary Representation of Floating Point Number (cont'd)

□ For maximum precision, the number can be normalized until the first digit is "1"



# Binary Representation of Floating Point Number (cont'd)

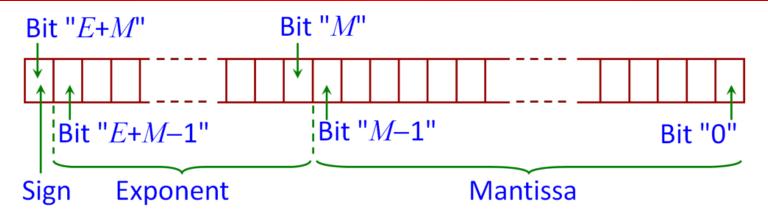
☐ Since the first digit is a "1", it is not necessary to record it



#### **IEEE 754**

- □ IEEE standard for binary floating-point arithmetic
- □ IEEE 754 specifies 4 formats
  - Single-precision (32-bit)
  - Double-precision (64-bit)
  - ➤ Signal-extended precision (≥43-bit, seldom used)
  - ➤ Double-extended precision (≥79-bit, usually 80-bit)

#### **IEEE 754 Number Format**

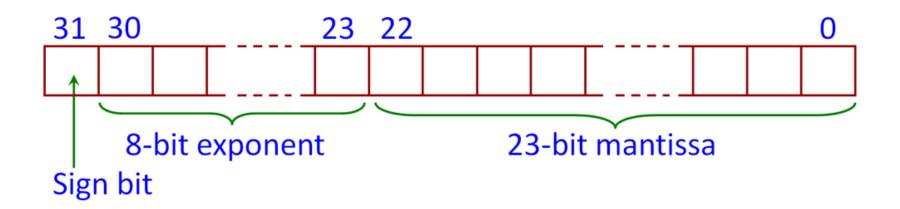


	Exponent	Mantissa
NaNs	$2^{E}$ – 1, i.e. all 1s	non zero
Infinities	$2^{E}$ – 1, i.e. all 1s	0
Zeroes	0, i.e. all 0s	0
Denormalized numbers	0, i.e. all 0s	non zero
Normalized numbers	1 to $2^E - 2$ . Biased binary	Any number

#### **IEEE 754 Number Format (cont'd)**

- □ Sign bit
  - Number is positive if sign bit is "0"
  - Number is negative if sign bit is "1"
- ☐ Biased exponent
  - The exponent is a signed value
    - for large and small magnitudes
  - ➤ Two's complement is not used
  - $\triangleright$  A constant  $2^{E-1}-1$  is added to the exponent
    - E.g., for E=8, the exponent bias is  $2^7$ -1=127, if the exponent is -3, it will be recorded as -3+127=124, i.e.,  $(011111100)_2$

### **32-bit Single Precision Format**



Value = 
$$(-1)^S \times 2^{Exp-127} \times M$$

Where

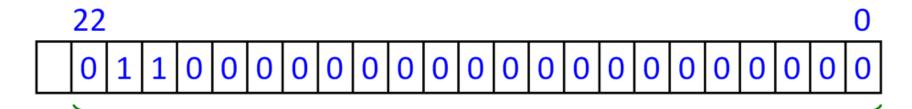
Exp = Recorded exponent.

M = 1.(value represented by fractional bit).

#### The Mantissa Value

Mantissa value = 1.(value represented by fractional bit).

Example



23-bit mantissa

# Fixed point VS Floating point

- ☐ Example: 32bit
- ☐ For fixed point

The smallest  $1 \times 2^{-N}$ 

The largest  $(2^{32}-1)\times 2^{-N}$ 

8-bit exponent 23-bit mantissa Sign bit 
$$Value = (-1)^{S} \times 2^{Exp-127} \times M$$
 Where 
$$Exp = \text{Recorded exponent.}$$
 
$$M = 1. \text{(value represented by fractional bit).}$$

23 22

Dynamic range 
$$20\log(\frac{(2^{32}-1)\times 2^{-N}}{1\times 2^{-N}}) \approx 192dB$$

☐ For floating point

Dynamic range 
$$20\log(\frac{3.402823\times10^{38}}{1.175494\times10^{-38}}) \approx 1667.6\text{dB}$$

# Fixed point VS Floating point

- ☐ Fixed point
  - Limited dynamic range, fast, low-power
- ☐ Floating point
  - High dynamic range, complex, slow

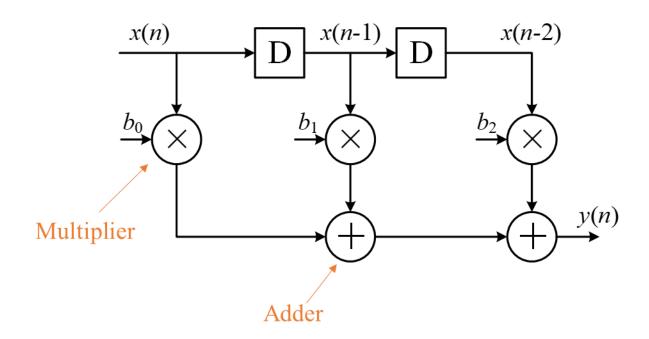
- Example
  - Filter coefficient quantization

#### Question

☐ The word-length of commonly used ADCs are around 16 bit, why need such a large dynamic range?

- □ Answer
  - > Multiplications

# **Typical DSP Operations**



□ Adders and multipliers are important components in DSP circuits

## Other Number Systems

- ☐ Signed digit number system (SD)
- □ Residual number system (RNS)
- □ Logarithmic number system (LNS)

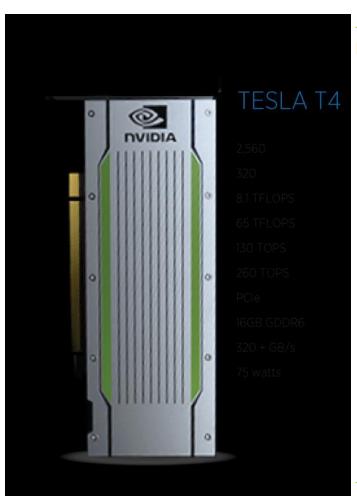
## It Is Always a Tradeoff

☐ A number system with high dynamic range, high precision, low-complexity...

Does not exist!



#### **NVIDIA T4 SPECIFICATIONS**



Performance

**TURING TENSOR CORES** 

320

NVIDIA CUDA® CORES

2,560

SINGLE PRECISION PERFORMANCE (FP32)

8.1 TFLOPS

MIXED PRECISION (FP16/FP32)

65 FP16 TFLOPS

INT8 PRECISION

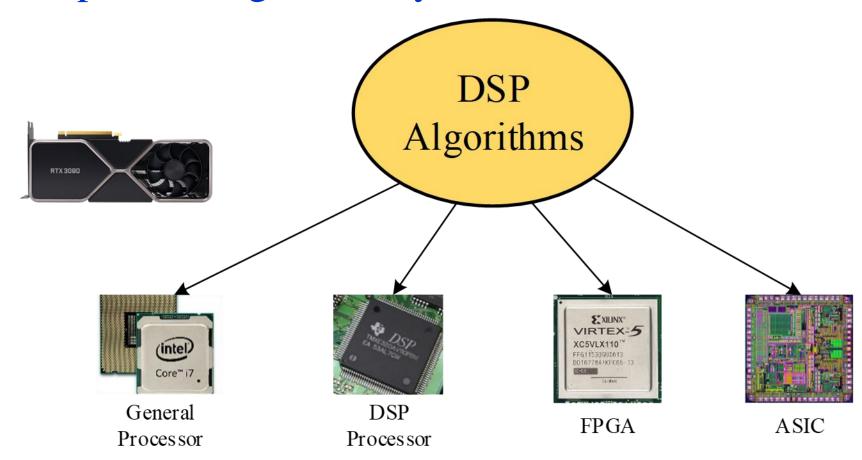
130 INT8 TOPS

INT4 PRECISION

260 INT4 TOPS

### **Other Things**

□ Other things you need to think about when implementing a DSP system





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