

Numerical Optimization, 2023 Fall

Homework 3

Name: Zhou Shouchen

Student ID: 2021533042

Due 23:59 (CST), Nov. 16, 2023

Problem 1. Prove the dual of the dual of a linear programming (standard form) is itself. [25pts]

Problem 2. Prove the dual objective increases after a pivot of the dual simplex method. [25pts]

Problem 3. Let $L(\mathbf{x}, \boldsymbol{\lambda})$ be the Lagrangian of a linear programming problem, and $(\mathbf{x}^*, \boldsymbol{\lambda}^*)$ be the optimal primal-dual solution. Prove that

$$L(\mathbf{x}, \boldsymbol{\lambda}^*) \geq L(\mathbf{x}^*, \boldsymbol{\lambda}^*) \geq L(\mathbf{x}^*, \boldsymbol{\lambda}),$$

for any primal feasible \mathbf{x} and dual feasible $\boldsymbol{\lambda}$. [25pts]

Problem 4. Construct a linear programming problem for which both the primal and the dual problem has no feasible solution. [25pts]