

8) Usando o estado $\cos(\theta/2)|0\rangle + e^{i\varphi}\sin(\theta/2)|1\rangle$, que pode ser representado na esfera de Bloch:

$$|+\rangle = \frac{1}{\sqrt{2}}(|0\rangle + |1\rangle), \text{ logo } \cos\left(\frac{\theta}{2}\right) = \frac{1}{\sqrt{2}} \therefore \boxed{\theta = \frac{\pi}{2}}$$

É temos que $e^{i\varphi} = 1$, logo usando a propriedade $e^{ia\pi} = (-1)^a$

$$\therefore e^{ia\pi} = (-1)^a, \text{ com } \boxed{a=0}, \text{ temos } \boxed{\varphi=0}$$

$$\text{Logo: } \boxed{|+\rangle \rightarrow \theta = \frac{\pi}{2} \text{ e } \varphi = 0}$$

$$|-\rangle = \frac{1}{\sqrt{2}}(|0\rangle - |1\rangle), \text{ logo } \cos\left(\frac{\theta}{2}\right) = \frac{1}{\sqrt{2}} \therefore \boxed{\theta = \frac{\pi}{2}}$$

É temos que $e^{i\varphi} = -1$, logo usando a propriedade $e^{ia\pi} = (-1)^a$

$$\therefore e^{ia\pi} = (-1)^a, \text{ com } \boxed{a=1}, \text{ temos } \boxed{\varphi = \pi}$$

$$\boxed{e^{i\pi} = -1}$$

$$\text{Logo } \boxed{|-\rangle \rightarrow \theta = \frac{\pi}{2} \text{ e } \varphi = \pi}$$

$$|i\rangle = \frac{1}{\sqrt{2}}(|0\rangle + i|1\rangle), \text{ logo } \cos\left(\frac{\theta}{2}\right) = \frac{1}{\sqrt{2}} \therefore \boxed{\theta = \frac{\pi}{2}}$$

É temos que $e^{i\varphi} = i$, logo usando a propriedade $e^{ia\pi} = (-1)^a$

$$\therefore e^{ia\pi} = (-1)^a, \text{ com } \boxed{a = \frac{1}{2}}, \text{ temos } \boxed{\varphi = \frac{\pi}{2}}$$

$$e^{i\frac{\pi}{2}} = (-1)^{\frac{1}{2}} = \sqrt{-1} = \boxed{i}$$

$$\text{Logo } \boxed{|i\rangle \rightarrow \theta = \frac{\pi}{2} \text{ e } \varphi = \frac{\pi}{2}}$$

$$|-i\rangle = \frac{1}{\sqrt{2}}(|0\rangle - i|1\rangle), \text{ logo } \cos\left(\frac{\theta}{2}\right) = \frac{1}{\sqrt{2}} \therefore \boxed{\theta = \frac{\pi}{2}}$$

$$\therefore e^{ia\pi} = (-1)^a, \text{ com } \boxed{a = \frac{3}{2}}, \text{ temos } \boxed{\varphi = \frac{3\pi}{2}}$$

$$e^{i\frac{3\pi}{2}} = (-1), (-1)^{\frac{1}{2}} = \boxed{-i}$$

$$\text{Logo } \boxed{|-i\rangle \rightarrow \theta = \frac{\pi}{2} \text{ e } \varphi = \frac{3\pi}{2}}$$