

$$(4) (C) |+\rangle, \left\{ \frac{1}{2}|0\rangle + \frac{\sqrt{3}}{2}|1\rangle, \frac{\sqrt{3}}{2}|0\rangle - \frac{1}{2}|1\rangle \right\}$$

$$|+\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$

$$\therefore \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) = a \cdot \left( \frac{1}{2}|0\rangle + \frac{\sqrt{3}}{2}|1\rangle \right) + b \cdot \left( \frac{\sqrt{3}}{2}|0\rangle - \frac{1}{2}|1\rangle \right)$$

$$\text{Assumindo } a = \frac{\sqrt{3}+1}{2\sqrt{2}} \text{ e } b = \frac{\sqrt{3}-1}{2\sqrt{2}}$$

$$\frac{\sqrt{3}+1}{2\sqrt{2}} \left( \frac{1}{2}|0\rangle + \frac{\sqrt{3}}{2}|1\rangle \right) + \frac{\sqrt{3}-1}{2\sqrt{2}} \left( \frac{\sqrt{3}}{2}|0\rangle - \frac{1}{2}|1\rangle \right)$$

$$\frac{\sqrt{3}+1}{4\sqrt{2}} |0\rangle + \frac{3+\sqrt{3}}{4\sqrt{2}} |1\rangle + \frac{3-\sqrt{3}}{4\sqrt{2}} |0\rangle - \frac{\sqrt{3}-1}{4\sqrt{2}} |1\rangle$$

$$\therefore \frac{4}{4\sqrt{2}} |0\rangle + \frac{4}{4\sqrt{2}} |1\rangle = \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle)$$

Logo, as probabilidades:

$$\cdot \frac{1}{2}|0\rangle + \frac{\sqrt{3}}{2}|1\rangle \Rightarrow \left| \frac{\sqrt{3}+1}{2\sqrt{2}} \right|^2 = \boxed{\frac{4+2\sqrt{3}}{8}}$$

$$\cdot \frac{\sqrt{3}}{2}|0\rangle - \frac{1}{2}|1\rangle \Rightarrow \left| \frac{\sqrt{3}-1}{2\sqrt{2}} \right|^2 = \boxed{\frac{4-2\sqrt{3}}{8}}$$