# **Monads**

CIS 194 Week 12 8 April 2013

Suggested reading:

- The Typeclassopedia
- LYAH Chapter 12: A Fistful of Monads
- LYAH Chapter 9: Input and Output
- RWH Chapter 7: I/O
- RWH Chapter 14: Monads
- RWH Chapter 15: Programming with monads

#### **Motivation**

Over the last couple of weeks, we have seen how the Applicative class allows us to idiomatically handle computations which take place in some sort of "special context"—for example, taking into account possible failure with Maybe, multiple possible outputs with [], consulting some sort of environment using ((->) e), or construct parsers using a "combinator" approach, as in the homework.

However, so far we have only seen computations with a fixed structure, such as applying a data constructor to a fixed set of arguments. What if we don't know the structure of the computation in advance – that is, we want to be able to decide what to do based on some intermediate results?

As an example, recall the Parser type from the homework, and assume that we have implemented Functor and Applicative instances for it:

```
newtype Parser a = Parser { runParser :: String -> Maybe (a, String) }
instance Functor Parser where
instance Applicative Parser where
```

Recall that a value of type Parser a represents a parser which can take a String as input and possibly integers, given as input the string

```
produce a value of type a, along with the remaining unparsed portion of the String. For example, a parser for
"143xkkj"
might produce as output
Just (143, "xkkj")
As you saw in the homework, we can now write things like
data Foo = Bar Int Int Char
parseFoo :: Parser Foo
parseFoo = Bar <$> parseInt <*> parseInt <*> parseInt <*>
assuming we have functions parseInt :: Parser Int and parseChar :: Parser Char. The
```

Applicative instance automatically handles the possible failure (if parsing any of the components fail, parsing the entire Foo will fail) and threading through the unconsumed portion of the String input to each component in turn

However, suppose we are trying to parse a file containing a sequence of numbers, like this:

```
4 78 19 3 44 3 1 7 5 2 3 2
```

The catch is that the first number in the file tells us the length of a following "group" of numbers; the next number after the group is the length of the next group, and so on. So the example above could be broken up into groups like this:

```
78 19 3 44 -- first group
1 7 5 -- second group
3 2 -- third group
```

This is a somewhat contrived example, but in fact there are many "real-world" file formats that follow a similar principle—you read some sort of header which then tells you the lengths of some following blocks, or where to find things in the file, and so on.

We would like to write a parser for this file format of type

```
parseFile :: Parser [[Int]]
```

Unfortunately, this is not possible using only the Applicative interface. The problem is that Applicative gives us no way to decide what to do next based on previous results: we must decide in advance what parsing operations we are going to run, before we see the results.

It turns out, however, that the Parser type can support this sort of pattern, which is abstracted into the Monad type class.

#### Monad

The Monad type class is defined as follows:

```
class Monad m where
  return :: a -> m a

(>>=) :: m a -> (a -> m b) -> m b

(>>) :: m a -> m b -> m b
  m1 >> m2 = m1 >>= \_ -> m2
```

This should look familiar! We have seen these methods before in the context of IO, but in fact they are not specific to IO at all. It's just that a monadic interface to IO has proved useful.

return also looks familiar because it has the same type as pure. In fact, every Monad should also be an Applicative, with pure = return. The reason we have both is that Applicative was invented after Monad had already been around for a while.

(>>) is just a specialized version of (>>=) (it is included in the Monad class in case some instance wants to provide a more efficient implementation, but usually the default implementation is just fine). So to understand it we first need to understand (>>=).

There is actually a fourth method called fail, but putting it in the Monad class was a mistake, and you should never use it, so I won't tell you about it (you can **read about it in the Typeclassopedia** if you are interested).

(>>=) (pronounced "bind") is where all the action is! Let's think carefully about its type:

```
(>>=) :: m a -> (a -> m b) -> m b
```

(>>=) takes two arguments. The first one is a value of type m a. (Incidentally, such values are sometimes called monadic values, or computations. It has also been proposed to call them mobits. The one thing you must not call them is "monads", since that is a kind error: the type constructor m is a monad.) In any case, the idea is that a mobit of type m a represents a computation which results in a value (or several values, or no values) of type a,

and may also have some sort of "effect":

- c1 :: Maybe a is a computation which might fail but results in an a if it succeeds.
- c2 :: [a] is a computation which results in (multiple) as.
- c3 :: Parser a is a computation which implicitly consumes part of a String and (possibly) produces an a.
- c4 :: IO a is a computation which potentially has some I/O effects and then produces an a.

And so on. Now, what about the second argument to (>>=)? It is a function of type (a -> m b). That is, it is a function which will *choose* the next computation to run based on the result(s) of the first computation. This is precisely what embodies the promised power of Monad to encapsulate computations which can choose what to do next based on the results of previous computations.

So all (>>=) really does is put together two mobits to produce a larger one, which first runs one and then the other, returning the result of the second one. The all-important twist is that we get to decide which mobit to run second based on the output from the first.

The default implementation of (>>) should make sense now:

```
(>>) :: m a -> m b -> m b
m1 >> m2 = m1 >>= \_ -> m2
```

m1 >> m2 simply does m1 and then m2, ignoring the result of m1.

## **Examples**

Let's start by writing a Monad instance for Maybe:

```
instance Monad Maybe where
  return = Just
  Nothing >>= _ = Nothing
  Just x >>= k = k x
```

return, of course, is Just. If the first argument of (>>=) is Nothing, then the whole computation fails; otherwise, if it is Just x, we apply the second argument to x to decide what to do next.

Incidentally, it is common to use the letter k for the second argument of (>>=) because k stands for "continuation". I wish I was joking.

Some examples:

addOneOrTwo x = [x+1, x+2]

### **Monad combinators**

One nice thing about the Monad class is that using only return and (>>=) we can build up a lot of nice general combinators for programming with monads. Let's look at a couple.

First, sequence takes a list of monadic values and produces a single monadic value which collects the results. What this means depends on the particular monad. For example, in the case of Maybe it means that the entire computation succeeds only if all the individual ones do; in the case of IO it means to run all the computations in sequence; in the case of Parser it means to run all the parsers on sequential parts of the input (and succeed only if they all do).

```
sequence :: Monad m => [m a] -> m [a]
sequence [] = return []
sequence (ma:mas) =
  ma >>= \a ->
  sequence mas >>= \as ->
  return (a:as)
```

Using sequence we can also write other combinators, such as

```
replicateM :: Monad m => Int -> m a -> m [a]
replicateM n m = sequence (replicate n m)
```

And now we are finally in a position to write the parser we wanted to write: it is simply

```
parseFile :: Parser [[Int]]
parseFile = many parseLine

parseLine :: Parser [Int]
parseLine = parseInt >>= \i -> replicateM i parseInt
```

(many was also known as zeroOrMore on the homework).

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