

Raghav - Regression Model with CPI Data

March 17, 2024

```
[1]: import pandas as pd
import numpy as np
import os
import yfinance as yf
from datetime import timedelta
import matplotlib.pyplot as plt
from sklearn.linear_model import LinearRegression
from sklearn.metrics import r2_score
```

```
[ ]:
```

```
[2]: SPX_Prices = yf.download('SPY', start='2002-01-01', end='2024-01-01', interval_
    ↳ "1d")
SPX_Prices
```

[*****100%*****] 1 of 1 completed

```
[2]:
```

	Open	High	Low	Close	Adj Close	\
Date						
2002-01-02	115.110001	115.750000	113.809998	115.529999	76.087906	
2002-01-03	115.650002	116.949997	115.540001	116.839996	76.950645	
2002-01-04	117.169998	117.980003	116.550003	117.620003	77.464355	
2002-01-07	117.699997	117.989998	116.559998	116.790001	76.917725	
2002-01-08	116.790001	117.059998	115.970001	116.519997	76.739883	
...	
2023-12-22	473.859985	475.380005	471.700012	473.649994	472.182892	
2023-12-26	474.070007	476.579987	473.989990	475.649994	474.176697	
2023-12-27	475.440002	476.660004	474.890015	476.510010	475.034058	
2023-12-28	476.880005	477.549988	476.260010	476.690002	475.213501	
2023-12-29	476.489990	477.029999	473.299988	475.309998	473.837769	

	Volume
Date	
2002-01-02	18651900
2002-01-03	15743000
2002-01-04	20140700
2002-01-07	13106500
2002-01-08	12683700

```
...
2023-12-22    67126600
2023-12-26    55387000
2023-12-27    68000300
2023-12-28    77158100
2023-12-29   122234100
```

[5537 rows x 6 columns]

```
[3]: VIX = yf.download('^VIX', start='2002-01-01', end='2024-01-01', interval = "1d")
VIX
```

[*****100%%*****] 1 of 1 completed

```
[3]:
```

	Open	High	Low	Close	Adj Close	Volume
Date						
2002-01-02	23.780001	24.200001	22.709999	22.709999	22.709999	0
2002-01-03	22.219999	22.430000	21.330000	21.340000	21.340000	0
2002-01-04	20.969999	21.530001	20.400000	20.450001	20.450001	0
2002-01-07	21.410000	22.150000	21.350000	21.940001	21.940001	0
2002-01-08	21.629999	22.290001	21.280001	21.830000	21.830000	0
...
2023-12-22	13.720000	13.960000	13.000000	13.030000	13.030000	0
2023-12-26	13.770000	13.800000	12.960000	12.990000	12.990000	0
2023-12-27	13.020000	13.040000	12.370000	12.430000	12.430000	0
2023-12-28	12.440000	12.650000	12.380000	12.470000	12.470000	0
2023-12-29	12.550000	13.190000	12.360000	12.450000	12.450000	0

[5537 rows x 6 columns]

```
[4]: def garman_klass_daily_variance(data):
      """
      Calculate daily Garman-Klass variance for given price data.
      """
      log_hl = np.log(data['High'] / data['Low'])
      log_co = np.log(data['Close'] / data['Open'])
      daily_variance = 0.5 * log_hl**2 - (2 * np.log(2) - 1) * log_co**2
      return daily_variance
```

```
[5]: def rolling_volatility(data, rolling_window):
      """
      Calculate annualized Garman-Klass volatility over a given period
      """
      Daily_Volatility = garman_klass_daily_variance(data)
      Rolling_Vol = np.sqrt((Daily_Volatility.rolling(rolling_window).mean())*252)
      return Rolling_Vol
```

```
[6]: daily_vol = rolling_volatility(SPX_Prices, 1)
next_day = daily_vol.shift(-1)
weekly_vol = rolling_volatility(SPX_Prices, 5)
monthly_vol = rolling_volatility(SPX_Prices, 21)
quartely_vol = rolling_volatility(SPX_Prices, 63)
volatilities = pd.DataFrame(
    data = {"daily_vol" : daily_vol,
            "weekly_vol" : weekly_vol,
            "monthly_vol" : monthly_vol,
            "quartely_vol" : quartely_vol,
            "next_day" : next_day
    },
    index = (SPX_Prices.index))
# Here we remove the NaN values from the volatility metrics
volatilities.dropna(inplace=True)
far_back = len(volatilities)

[7]: ### This is our regression model with only historical volatility as our
     ↳ independent variables ###

# Data with three independent variables (X1, X2, X3) and one dependent variable
     ↳ (Y)
All_Vols = {'X1': volatilities['daily_vol'],
            'X2': volatilities['weekly_vol'],
            'X3': volatilities['monthly_vol'],
            'Y': volatilities['next_day']}

df = pd.DataFrame(All_Vols)

# Separate independent variables (features) and dependent variable
X = df[['X1', 'X2', 'X3']]
y = df['Y']

# Create and fit the multiple regression model
all_preds = LinearRegression()
all_preds.fit(X, y)

# Predictions
y_pred = all_preds.predict(X)

# Plotting the actual vs predicted values
plt.scatter(y, y_pred)
plt.plot([min(y), max(y)], [min(y), max(y)], linestyle='--', color='red',
     ↳ label='Perfect Prediction Line')
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual Volatility vs Predicted Values (only historical volatility)')
```

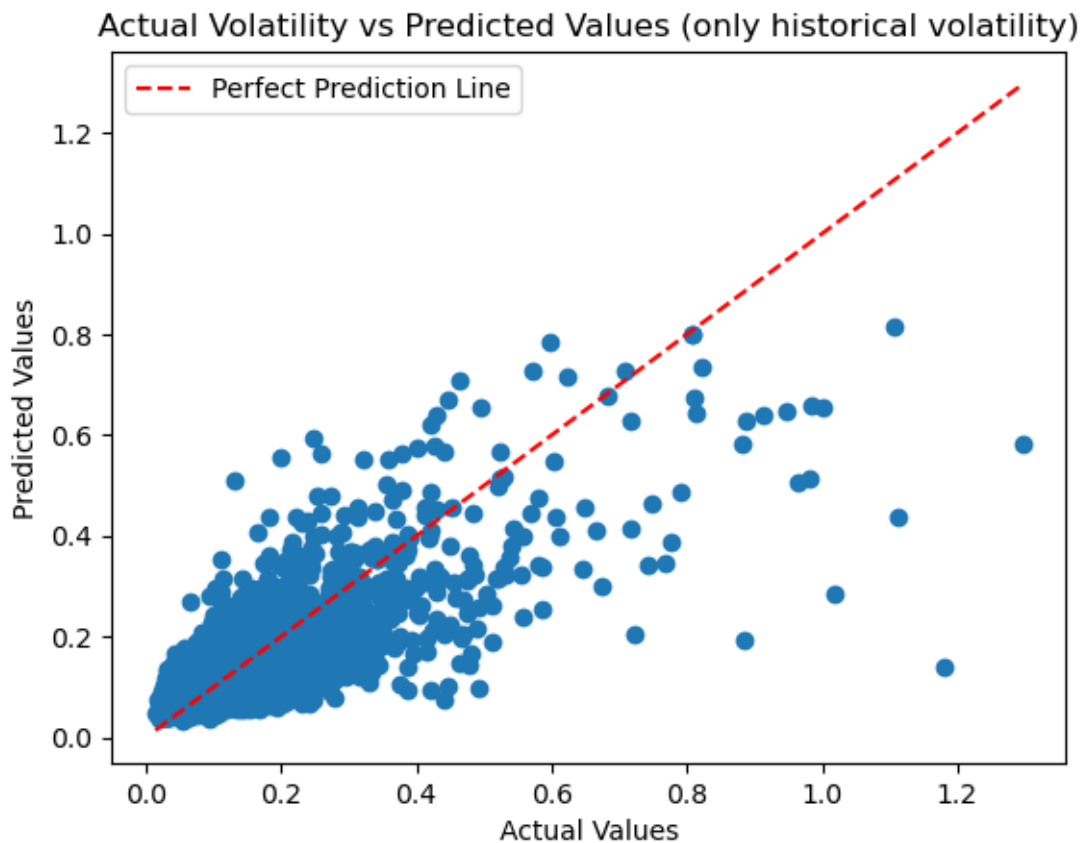
```

plt.legend()
plt.show()

# Finding the values of R-squared and Adjusted R-squared
r_squared = r2_score(y , y_pred)
observations = len(y) # number of observations
predictors = len(All_Vols) - 1 #number of predictors
adj_r_squared = 1 - ((1-r_squared)*((observations-1)/
    ↪(observations-predictors-1)))

# Print the coefficients (slope) and intercept
print('Coefficients (Slope):', all_preds.coef_)
print('Intercept:', all_preds.intercept_)
print('R-squared:' , r_squared)
print('Adjusted R-squared:' , adj_r_squared)

```



```

Coefficients (Slope): [0.2996955  0.34984096 0.2351574 ]
Intercept: 0.009734076213321813
R-squared: 0.6019867619238796
Adjusted R-squared: 0.6017684731278597

```

```

[12]: # Import the CPI data from FRED
CPI_Data = pd.read_csv('/Users/ganeshthondikulam/Downloads/Median CPI Data_
↳(Daily).csv')
# Make the data frame the same size as the other data
CPI_Data_df = pd.DataFrame(CPI_Data[-far_back:])
# make the data frame a series so it can be added to the other data
CPI_Data_series = pd.Series(CPI_Data_df['CPIRATE'])
# Change the indicies to the same as the other data
CPI_Data_series.index = df.index

[15]: ### This is our regression model with historical volatility and CPI Data as our
↳independent variables ###

# Data with four independent variables (X1, X2, X3, X4) and one dependent
↳variable (Y)
All_Vols = {'X1': volatilities['daily_vol'],
            'X2': volatilities['weekly_vol'],
            'X3': volatilities['monthly_vol'],
            'X4': CPI_Data_series,
            'Y': volatilities['next_day']}

df = pd.DataFrame(All_Vols)

# Separate independent variables (features) and dependent variable
X = df[['X1', 'X2', 'X3', 'X4']]
y = df['Y']

# Create and fit the multiple regression model
all_preds = LinearRegression()
all_preds.fit(X, y)

# Predictions
y_pred = all_preds.predict(X)

# Plotting the actual vs predicted values
plt.scatter(y, y_pred)
plt.plot([min(y), max(y)], [min(y), max(y)], linestyle='--', color='red',
↳label='Perfect Prediction Line')
plt.xlabel('Actual Values')
plt.ylabel('Predicted Values')
plt.title('Actual Volatility vs Predicted Values (with CPI Data)')
plt.legend()
plt.show()

# Finding the values of R-squared and Adjusted R-squared
r_squared = r2_score(y, y_pred)
observations = len(y) # number of observations

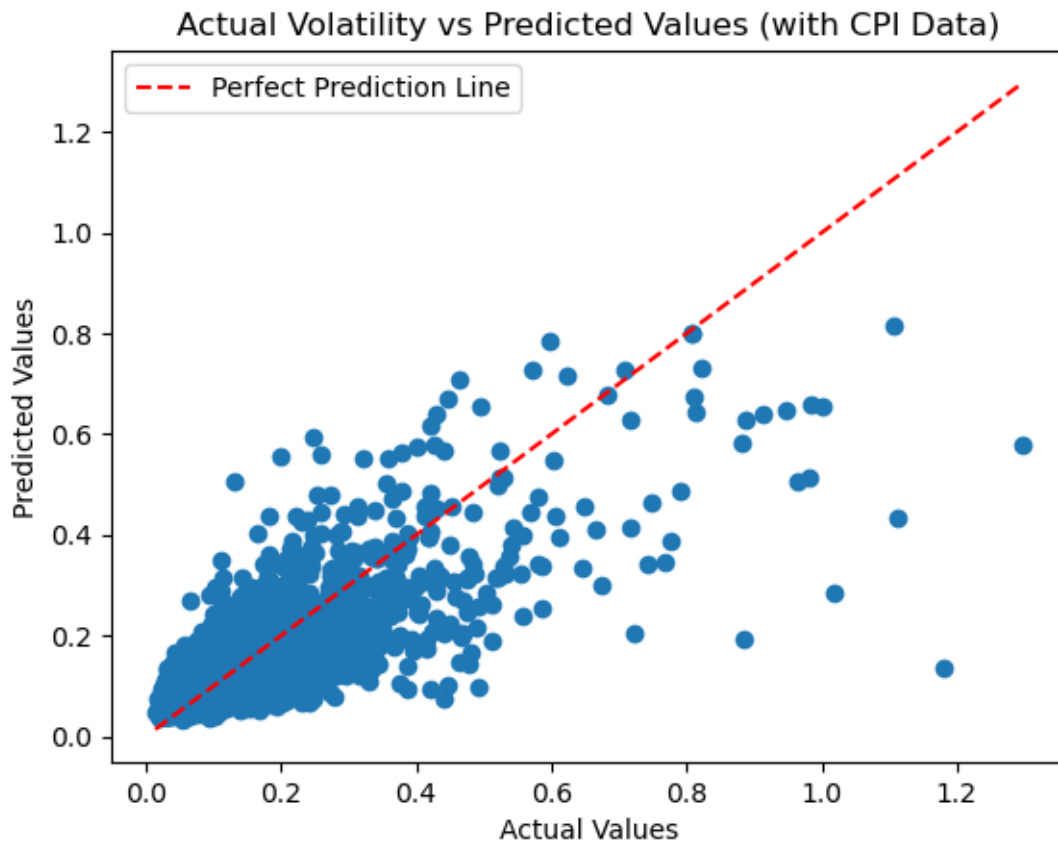
```

```

predictors = len(All_Vols) - 1 #number of predictors
adj_r_squared = 1 - ((1-r_squared)*((observations-1)/
↪(observations-predictors-1)))

# Print the coefficients (slope) and intercept
print('Coefficients (Slope):', all_preds.coef_)
print('Intercept:', all_preds.intercept_)
print('R-squared:', r_squared)
print('Adjusted R-squared:', adj_r_squared)

```



```

Coefficients (Slope): [0.29941964 0.34936615 0.2363022  0.0007142 ]
Intercept: 0.007729433442559552
R-squared: 0.6020899545233773
Adjusted R-squared: 0.6017989250514617

```

[]: