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"import torch"

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"x0: tensor(0.0121, requires\_grad=True) y0: tensor(0.0001, grad\_fn=<PowBackward0>) x0.grad: tensor(0.0242)\n"

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"#例题\n",

"import numpy as np\n",

"import matplotlib.pyplot as plt\n",

"\n",

"x0 = torch.tensor(5.0, requires\_grad=True)\n",

"y0 = x0\*\*2\n",

"\n",

"alpha = 0.1\n",

"epsilon = 0.0001\n",

"\n",

"x\_values = []\n",

"y\_values = []\n",

"\n",

"# 循环直到y的变化小于epsilon\n",

"while True:\n",

" # 计算梯度\n",

" y0.backward()\n",

" y = y0.item() # 保存y0在当前迭代的取值，用于判断迭代的停止条件\n",

" # 更新x0\n",

" with torch.no\_grad():\n",

" x0 -= alpha \* x0.grad # x0 = x0-alpha \* x0.grad 创建一个新的张量并赋值给x\n",

" x0.grad.zero\_()\n",

" # 计算新的y0\n",

" y0 = x0\*\*2\n",

" # 检查是否满足结束条件\n",

" if abs(y0.item() - y) < epsilon:\n",

" break\n",

"\n",

"y0.backward()\n",

"print(\"x0: \", x0, \"y0: \", y0, \"x0.grad: \", x0.grad)"

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"#设计两个波谷的一元函数，使用梯度下降算法找到全局最小值(作业)"

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"第一个波谷处最小值近似解：\n",

"x0: tensor(0., requires\_grad=True) y0: tensor(1., grad\_fn=<PowBackward0>)\n",

"第二个波谷处最小值近似解：\n",

"x0: tensor(-1.0035, requires\_grad=True) y0: tensor(4.9036e-05, grad\_fn=<PowBackward0>)\n"

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"# 定义目标函数\n",

"def objective\_function(x):\n",

" return (x\*\*2 - 1)\*\*2\n",

"\n",

"# 用于判断是否陷入局部最小值的计数器及阈值（通用设置）\n",

"stuck\_count\_general = 0\n",

"stuck\_threshold\_general = 100\n",

"\n",

"# 第一个波谷附近求最小值近似解\n",

"x0\_first = torch.tensor(0.0, requires\_grad=True)\n",

"y0\_first = objective\_function(x0\_first)\n",

"\n",

"alpha = 0.01\n",

"epsilon = 0.00001\n",

"\n",

"x\_values\_first = []\n",

"y\_values\_first = []\n",

"\n",

"while True:\n",

" # 计算梯度\n",

" y0\_first.backward()\n",

" y\_first = y0\_first.item() # 保存y0在当前迭代的取值，用于判断迭代的停止条件\n",

" # 更新x0\n",

" with torch.no\_grad():\n",

" x0\_first -= alpha \* x0\_first.grad # x0 = x0-alpha \* x0.grad 创建一个新的张量并赋值给x\n",

" x0\_first.grad.zero\_()\n",

" # 计算新的y0\n",

" y0\_first = objective\_function(x0\_first)\n",

"\n",

" # 检查是否满足结束条件\n",

" if abs(y0\_first.item() - y\_first) < epsilon:\n",

" break\n",

"\n",

" # 判断是否陷入局部最小值\n",

" if abs(y0\_first.item() - y\_first) < 0.0001: # 如果目标函数值变化很小\n",

" stuck\_count\_general += 1\n",

" else:\n",

" stuck\_count\_general = 0\n",

"\n",

" if stuck\_count\_general >= stuck\_threshold\_general: # 如果连续多次目标函数值变化很小，视为陷入局部最小值\n",

" # 重新初始化x0到第一个波谷附近区域\n",

" x0\_first = torch.tensor(0.0, requires\_grad=True)\n",

" y0\_first = objective\_function(x0\_first)\n",

" stuck\_count\_general = 0\n",

"\n",

"# 输出第一个波谷处最小值近似解\n",

"print(\"第一个波谷处最小值近似解：\")\n",

"print(\"x0: \", x0\_first, \"y0: \", y0\_first)\n",

"\n",

"# 第二个波谷附近求最小值近似解\n",

"x0\_second = torch.tensor(-2.0, requires\_grad=True)\n",

"y0\_second = objective\_function(x0\_second)\n",

"\n",

"x\_values\_second = []\n",

"y\_values\_second = []\n",

"\n",

"while True:\n",

" # 计算梯度\n",

" y0\_second.backward()\n",

" y\_second = y0\_second.item() # 保存y0在当前迭代的取值，用于判断迭代的停止条件\n",

" # 更新x0\n",

" with torch.no\_grad():\n",

" x0\_second -= alpha \* x0\_second.grad # x0 = x0-alpha \* x0.grad 创建一个新的张量并赋值给x\n",

" x0\_second.grad.zero\_()\n",

" # 计算新的y0\n",

" y0\_second = objective\_function(x0\_second)\n",

"\n",

" # 检查是否满足结束条件\n",

" if abs(y0\_second.item() - y\_second) < epsilon:\n",

" break\n",

"\n",

" # 判断是否陷入局部最小值\n",

" if abs(y0\_second.item() - y\_second) < 0.0001: # 如果目标函数值变化很小\n",

" stuck\_count\_general += 1\n",

" else:\n",

" stuck\_count\_general = 0\n",

"\n",

" if stuck\_count\_general >= stuck\_threshold\_general: # 如果连续多次目标函数值变化很小，视为陷入局部最小值\n",

" # 重新初始化x0到第二个波谷附近区域\n",

" x0\_second = torch.tensor(-2.0, requires\_grad=True)\n",

" y0\_second = objective\_function(x0\_second)\n",

" stuck\_count\_general = 0\n",

"\n",

"# 输出第二个波谷处最小值近似解\n",

"print(\"第二个波谷处最小值近似解：\")\n",

"print(\"x0: \", x0\_second, \"y0: \", y0\_second)"

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