Homework 1 @ Prove that for all positive natural numbers 1-2+2-3+ ... + h(h+a) + h(h+a)(h+2) base case h=0 0.1 = 0.1.2 0=0 Inductive hypothesis 1.2+2-3+...+KKH) = K(K+1)(K+2) N=KHA 1-2+2-3+...+ K(K+1)+(K+1)(K+2)= (x+1)(K+2)(K+2) K(K+1)(K+2) + (K+1)(K+2) = (K+1)(K+2)(K+3) K(K+1)(K+2) + 3(K+2)(K+2)(K+2)(K+3) (K+1)(K+2) (K+3) [K+1)(K+2)(K+3) By proof of Mathematical Induction we conclude that Propher therefore the statement 1-2+2.3+ ... n(n+1)=h(n+2) isT.

B) for any natural number n, let Pu be the statement n+n+1 which is ever. i) Show that for every natural number now, we have that Pu-Py+s ii Show that Ph is always talse. We assume that

i) In= h3+ n+1 = 2k ii) Pu is always false n3+n+1=2k > n=2n (N+1) + (N+1) +1= base ase 20n+2+1= (2n+4)3+(24+1)+1+ T h3+3n+3n+1+n+2= 10n+1 >odd = 8n3 + 12n°+6n+1+2n+2= $(n^3+n+4)+3n(n+1)+2$ $=8n^3+12u^2+8n+3$ 13+1+1=3 first stakment always odd (because) 3 is an odd number C) Using the ordered pairs definition of the integers L, varity the distributive property for Therefore we have Property of M $(m_1, n_4) + (m_2, n_2) / \circ (m_3, n_3) =$ lym, n & M l(m+n) = lm+ln-= (M1, N1) = (M3, N3) + (M2, N2) (M3, N3) = $X_1 \cdot X_3 + X_2 \cdot X_3 =$ X₁, X₂, X₃ & Z $= (X_1 + X_2) \cdot X_3 -$ X WINT Distributive property X1 (2) m1, n2) = m2 n1, m1 EW X2 (2) m2/112) - m2-112 h2, m2 E/M X3(2) m3, h3) = m3-n3 h3, m3 EM Sidenote B Mothematical induction consists of his steps base ase and induction hypothesis Here if we go by the hypothesis with the assumption that the first statement is true we prove the hypothesis to be true. But the base Case is that which shows us that the first Statement is indeed talse.

