

Additional exercises

Sead Jahić

Teaching Assistant, Information Technologies

University of Primorska

Faculty of Mathematics, Natural Sciences and Information Technologies

(UP FAMNIT)

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Exercise

Implement program that will count binomial coefficient.

$$\binom{n}{k} = \frac{n!}{k! \cdot (n-k)!}, \quad \binom{n}{0} = \binom{n}{n} = 1$$

Binomial coefficients appears in Newton-binom equation:

$$(x + y)^n = \sum_{k=0}^n \binom{n}{k} x^{n-k} y^k$$

- create scanner, give opportunity to insert n, k .
- create functions:
 - factorial(input n)
 - binomial_coef(input n, k)
- use if statement to avoid input of negative number or zero

Exercise

Fibonacci sequence!

The Fibonacci Sequence is the series of numbers:

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, ...

The next number is sum of the two numbers before it.

The sequence F_n of Fibonacci numbers is defined by the recurrence relation:

$$F_n = F_{n-1} + F_{n-2},$$

$$F_0 = 0, F_1 = 1.$$

for more information about Fibonacci sequence see

https://en.wikipedia.org/wiki/Fibonacci_number.

Exercise

Another great thing to implement in JAVA as program is Horner's method!

Horner's method is used to calculate remainder of polynomial division (remainder of $f(x)$ on division by $x - \alpha$, α is integer).

	a_n	a_{n-1}	a_{n-2}	\dots	a_0
α	b_n	b_{n-1}	b_{n-2}	\dots	b_0
	=	=	=	\dots	=
	a_n	$\alpha \cdot b_n + a_{n-1}$	$\alpha \cdot b_{n-1} + a_{n-2}$	\dots	$\underbrace{\alpha \cdot b_1 + a_0}_{R\text{-remainder}}$

For example: Find remainder of division polynomial $P(x) = 4x^4 + 3x^3 - 2x^2 + x + 2$ with $Q(x) = x - 2$.

$$A[0] = B[0]$$

	4	3	-2	1	2	=A
2	4	11	20	41	84	=B
=						
α						

$B[1] = \alpha * B[0] + A[1]$
 $11 = 2 * 5 + 3$

Remainder can be also found using Bézout's theorem. It states that the remainder of the division of a polynomial $f(x)$ by a linear polynomial $x - r$ is equal to $f(r)$.

In our example it means:

$$P(2) = 4 \cdot 2^4 + 3 \cdot 2^3 - 2 \cdot 2^2 + 1 \cdot 2^1 + 2 \cdot 2^0 = 84.$$

Here is solution:

```
public static int Bezuot(int n, int alpha, int[] coeff){  
    int sum=0;  
    for (int i=0; i<=n; i++){  
        sum = (int) (sum+coeff[i]*Math.pow(alpha,n-i));  
    }  
    return sum;  
}
```