

Unconstrained Local Optimization

$$\vec{x} \in \mathbb{R}^n$$

$f(x)$ is "smooth"

differentiable to some degree

Strategy

choose \vec{x}_0

for $k \in 1 \dots n$

$\vec{x}_k \leftarrow$ update based on local information near \vec{x}_{k-1}

return \vec{x}_n \leftarrow what direction?



$$-\nabla f(\vec{x})$$

Gradient Descent

for $k \in 1 \dots n$

$$\vec{x}_k \leftarrow \vec{x}_{k-1} - \alpha \nabla f(\vec{x}_{k-1})$$

Two General Strategies

1. Line Search

Choose direction \hat{d}

Choose a step size

$$\alpha^* = \underset{\alpha}{\operatorname{argmin}} f(\vec{x} + \alpha \hat{d})$$

$$\vec{x}_k \leftarrow \vec{x}_{k-1} + \alpha^* \hat{d}$$

2. Trust Region

Choose \hat{f} + trust region for \hat{f}

$$\vec{x}_k \leftarrow \underset{\vec{x}}{\operatorname{argmin}} \hat{f}(\vec{x})$$

subject to $d(\vec{x}, \vec{x}_{k-1}) \leq \delta$

