

### Part 1

Define a function in a very similar manner to Dr. Feser's example provided in lecture making relevant definitions, but making `dyvect_dt` a three-column vector.

Use `ode45()` to evaluate the ODE, using the given `n` span and initial conditions. Isolate each column as  $f$ ,  $f'$ ,  $f''$ . Evaluate where  $y_1=0$ ,  $y_2=0$ ,  $y_3=0.5$  as prompted. Plot solutions  $y_1$ ,  $y_2$ ,  $y_3$  vs.  $n$  for given initial conditions.

Evaluate  $y_2$  at 100, where it is horizontal, equivalent to the value at infinity. Run the script again after making a small alteration the third column entry in the  $y_0$  definition. Note the change in  $y_2(100)$ . If it got closer to 1, continue changing the initial condition in the same direction; if it got further from 1, begin changing the initial condition in the opposite direction as the original change. Record a range of values that will output  $y_2(100) = 1.0000$ .

Use an initial guess of .5 as used before. Make necessary definitions such as  $n$ ,  $y_0$ , and  $y_2$  (via `ode45`) to begin setting up a while loop. Find the difference between the  $y_2(\text{infinity})$  obtained using your initial guess and 1. If that difference is greater than zero, enter the appropriate while loop. Originally, the adjustments made to approximate which  $\alpha$  will give  $y_2(\text{infinity})=1$  were done in very tiny increments to provide precise results, but iterating  $\sim 1.68$  million times proved to be fairly time-consuming at around 5-10 min. This needed to be optimized. Instead of making all adjustments from your initial guess at the same step size, much courser adjustments were made while possible – and incrementally so. So as the step size was gradually being refined, the difference between the current  $\alpha$  value being looped and 1 was also decreasing as it honed in on a precise  $\alpha$  result. This provided a run time of a mater of seconds to achieve a resulting  $\alpha$ . If the difference between the  $y_2(\text{infinity})$  obtained using your initial guess and 1 is less than zero, then copy & paste the above-zero code and make the relevant necessary  $+$ ,  $-$ ,  $<$ ,  $>$  adjustments.

### Part 2

Make relevant if statements to reflect the piecewise functions defining  $f'$  as provided for  $u/U$ . Overlay that function with the  $y_2=f'$  found as the ODE solution on a plot vs.  $n$ .

### Part 3

As there are no fluid properties provided, the value of  $\nu$  cannot be determined, and the displacement thickness cannot be determined as instructed by using the given expression involving  $A$ . Use `trapz()` to evaluate the  $A$  integral using the  $y_2$  profile calculated.

### Part 4

Since  $\nu$  cannot be determined, the momentum thickness cannot be determined as instructed by using the given expression involving  $B$ . Use `trapz()` to evaluate the  $B$  integral using the  $y_2$  profile calculated.