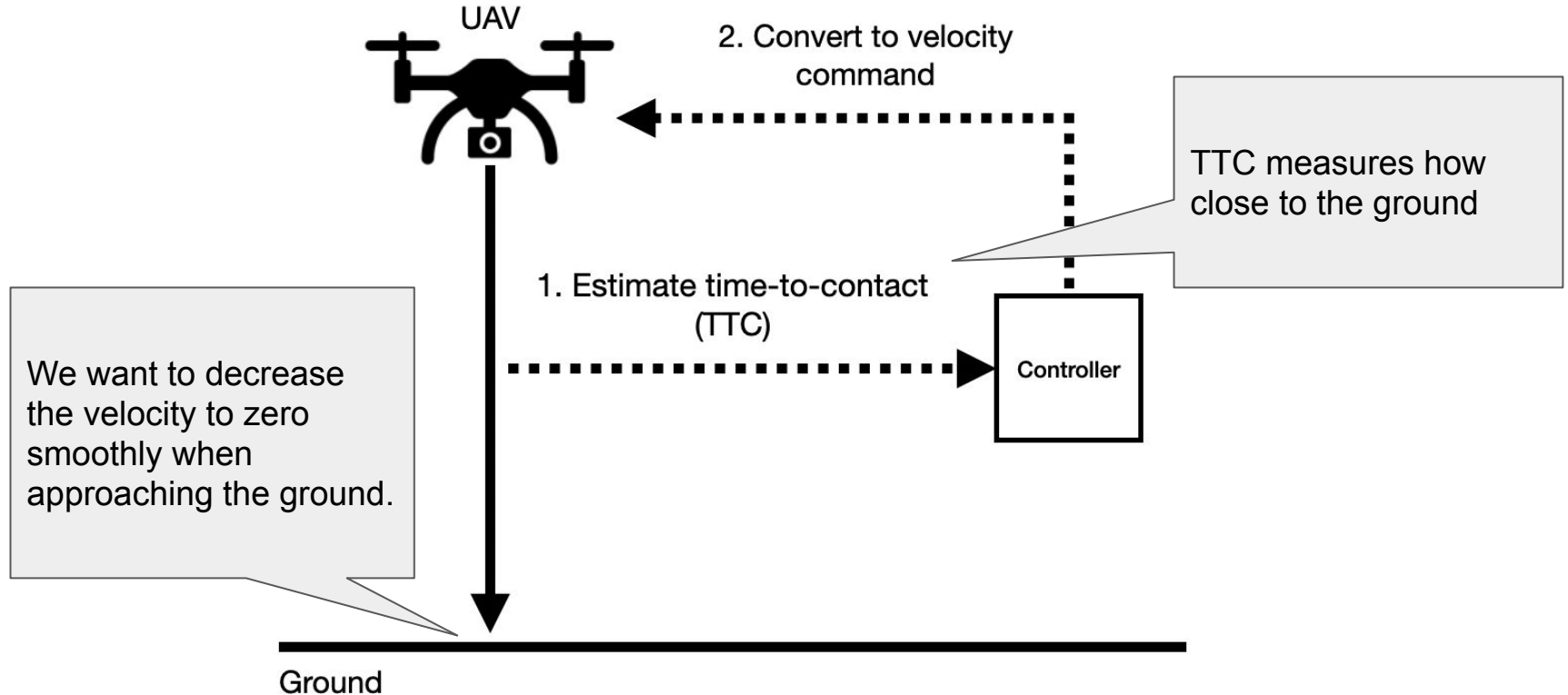


# Direct Time-to-Contact Estimation for Unmanned Aerial Vehicle Landing

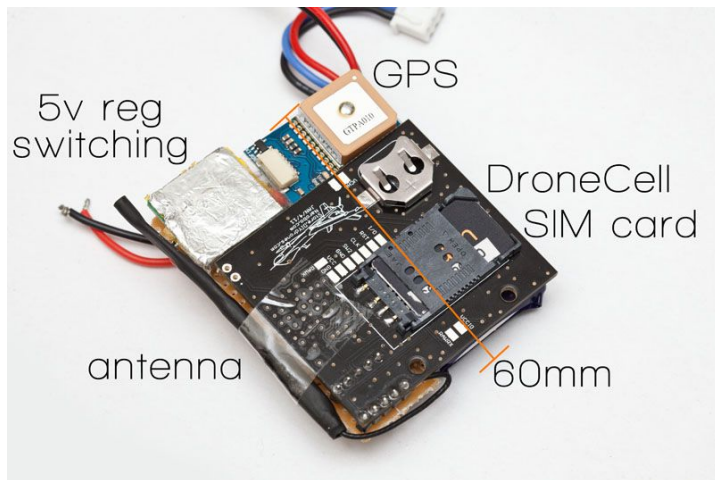
Zhang-Wei Hong & Tsun-Hsuan Wang

# Time-to-contact (TTC) based control for UAV landing



# Typical TTC-based control is unscalable

1. Expensive
2. Imprecise in indoor cases



GPS

1. Need visual features
2. Costly computation



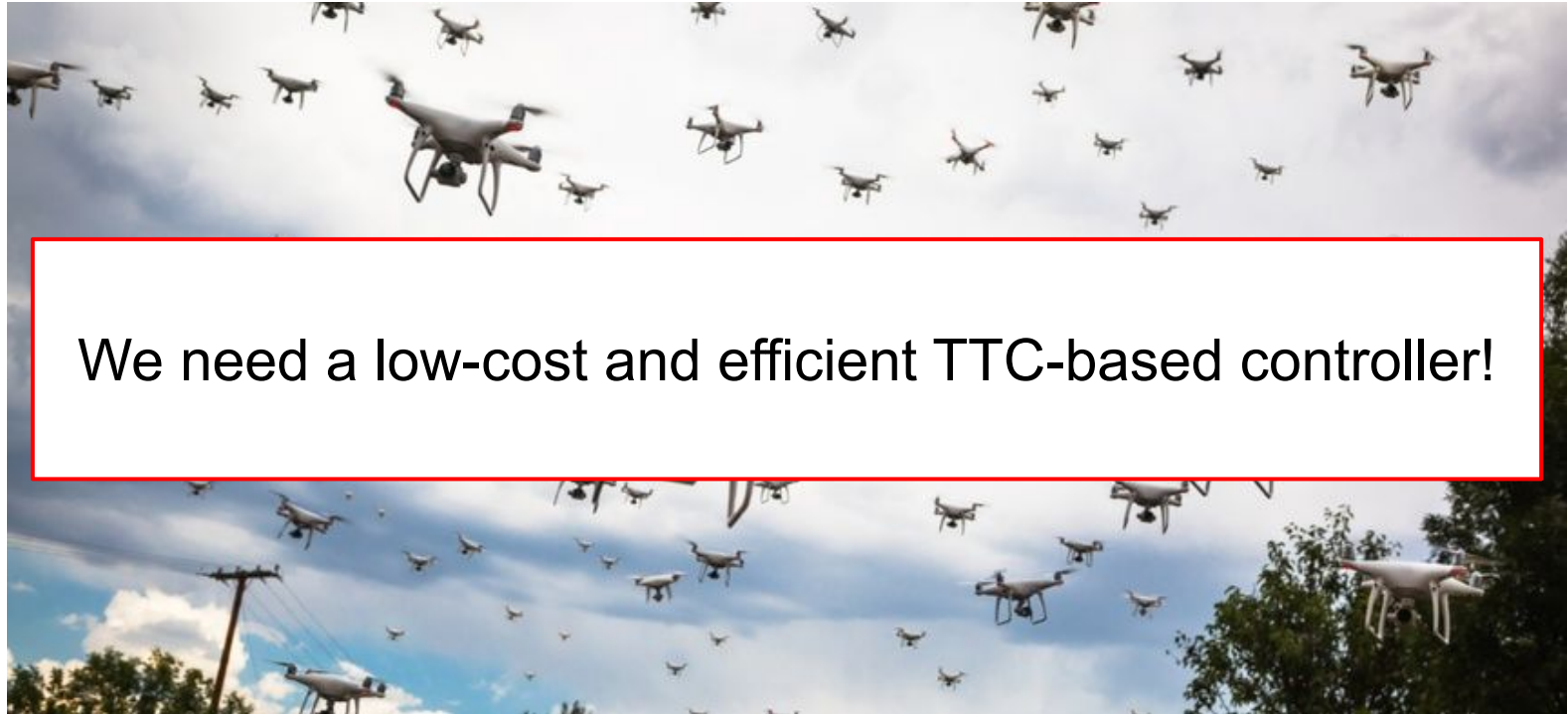
Optical flow

Typical methods cannot deploy in a scale



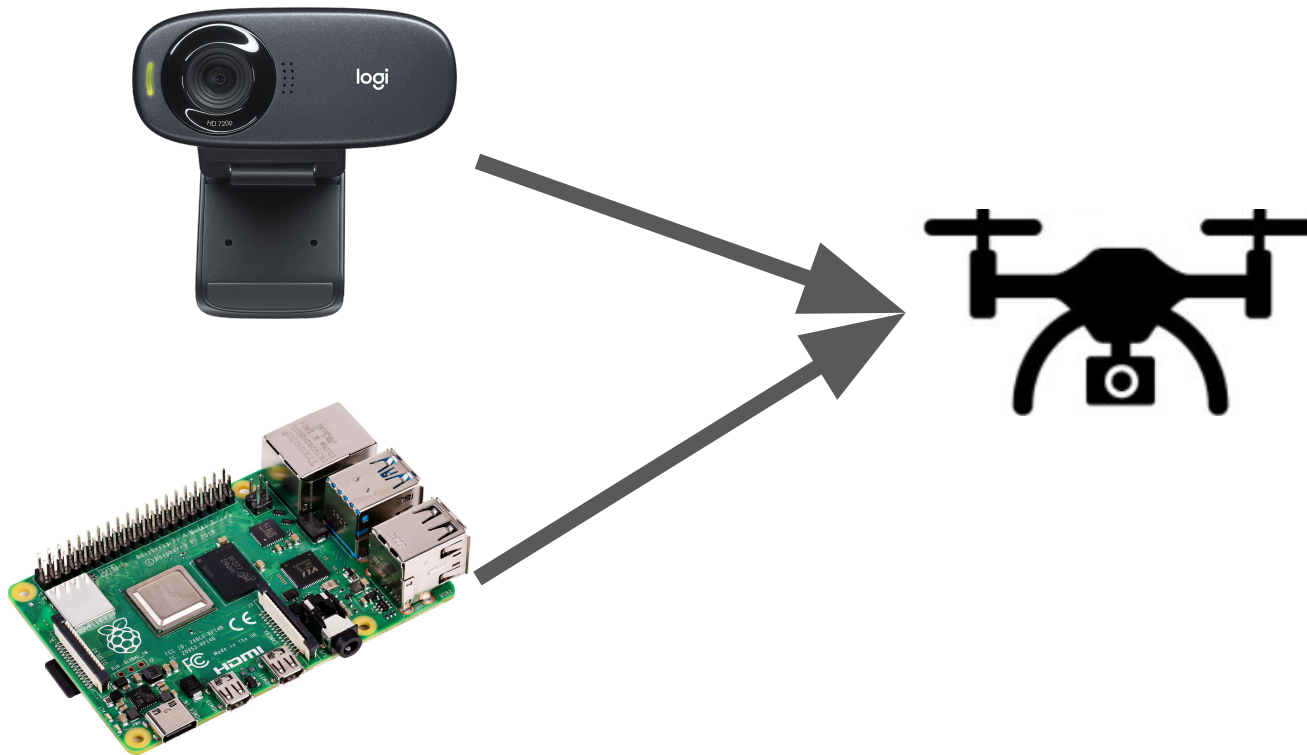
<https://roboticsandautomationnews.com/>

The envision of UAV is large scale deployment in smart cities



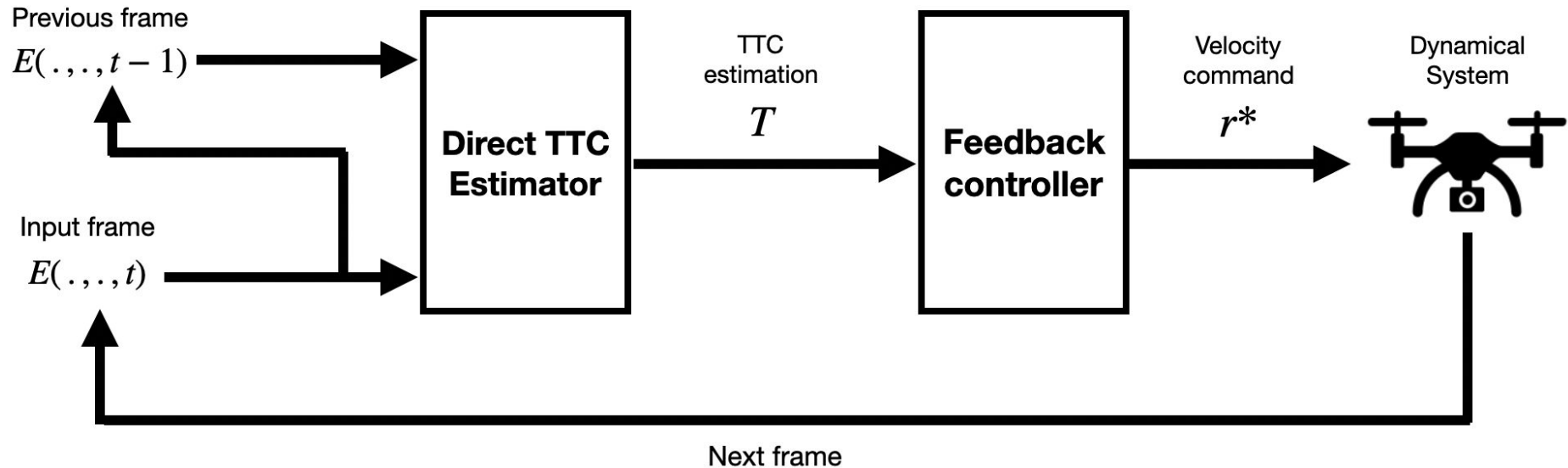
We need a low-cost and efficient TTC-based controller!

Our method only needs a monocular camera and a cheap computer



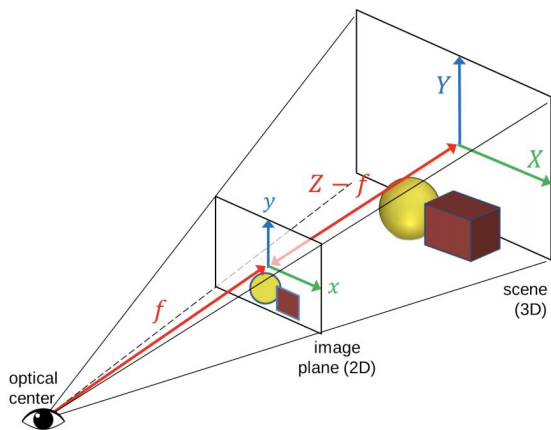
# Method - overview

Control UAVs via direct TTC estimation [1] from **image brightness**



# Method - TTC estimation

TTC can be connected to image brightness by **image motion**



TTC

$$T = -\frac{Z}{W}$$

Image motion

$$\frac{1}{f} \frac{dx}{dt} = \frac{1}{f} u = \frac{U}{Z} - \frac{x}{f} \frac{W}{Z}$$

$$\frac{1}{f} \frac{dy}{dt} = \frac{1}{f} v = \frac{V}{Z} - \frac{y}{f} \frac{W}{Z}$$

$$(U, V, W) = \left( \frac{dX}{dt}, \frac{dY}{dt}, \frac{dZ}{dt} \right) \quad (u, v) = \left( \frac{dx}{dt}, \frac{dy}{dt} \right)$$



# Method - TTC estimator

Image motion is constrained by the **constant brightness equation (BCCE)**

$$uE_x + vE_y + E_t = 0$$

$E$  Image brightness

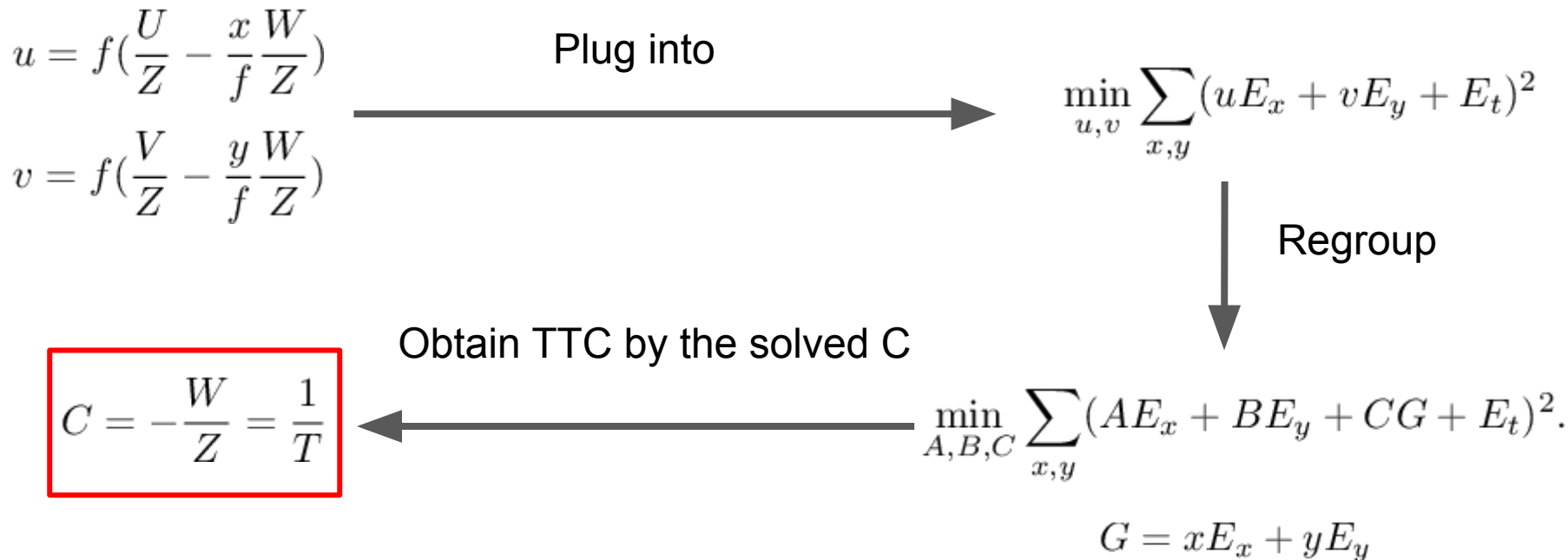
$E_x$  Partial derivative w.r.t.  $x$

$E_y$  Partial derivative w.r.t.  $y$

$E_t$  Partial derivative w.r.t.  $t$

# Method - TTC estimation

Then, TTC can be obtained by the least-square solution of BCCE



# Method - feedback controller

Landing control can be related to TTC by **the desired landing trajectory in vertical descending**

Distance to the ground at time  $t$ :  $d(t) = \frac{1}{2}at^2$  ( $a$  is the desired acceleration downward)

Relation to TTC: 
$$T = -\frac{Z}{W} = -\frac{d(t)}{\frac{dd(t)}{dt}} = -\frac{1}{2} \frac{at^2}{at} = -\frac{1}{2}t$$

Conversion to  
velocity command:

$$r^* = \frac{dd(t)}{dt} = -at = -2aT$$

# Method - feedback controller

Landing control can be related to TTC by **the desired landing trajectory in vertical descending**

Distance to the ground at time  $t$ :

$$d(t) = \frac{1}{2}at^2 \quad (a \text{ is the desired acceleration downward})$$

Rel

The velocity decreases to zero along with TTC

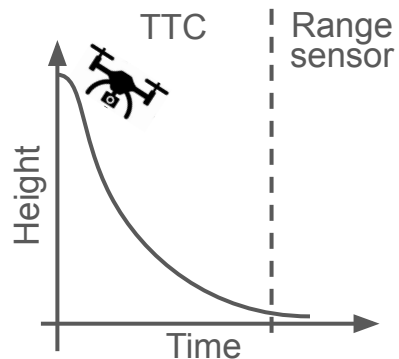
$$T = -\frac{Z}{W} = -\frac{d(t)}{\frac{dd(t)}{dt}} = -\frac{1}{2} \frac{at^2}{at} = -\frac{1}{2}t$$

Conversion to velocity command:

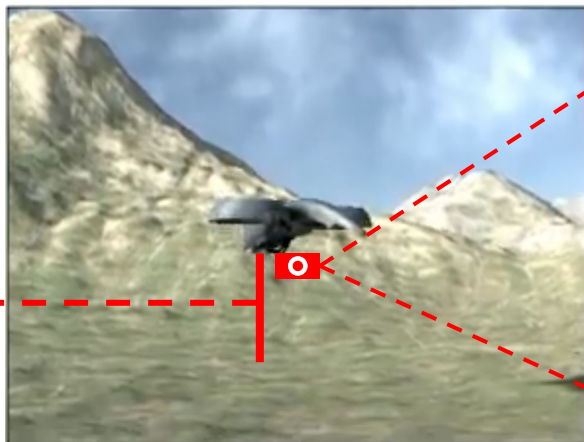
$$r^* = \frac{dd(t)}{dt} = -at = -2aT$$

# Experiments setup

## Sensors



Third-Person View



UAV's Camera View

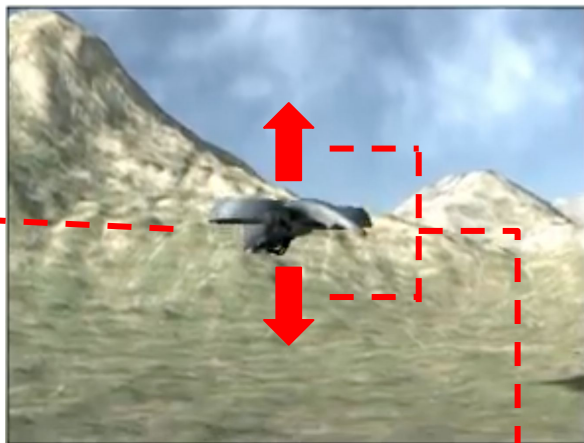


Range sensor with operational domain  $< 0.4\text{m}$

# Experiments setup

## Vehicle Dynamics

Third-Person View



Simple Rigid Body

Velocity control along  
vertical axis

UAV's View



# Experiments setup

## Weather Conditions

Dust Storm



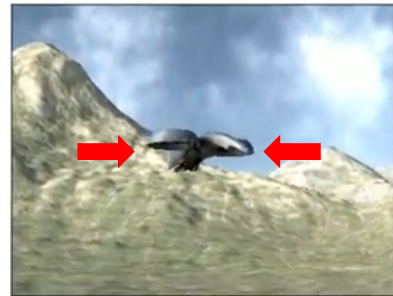
Cloudy



Rotational Light

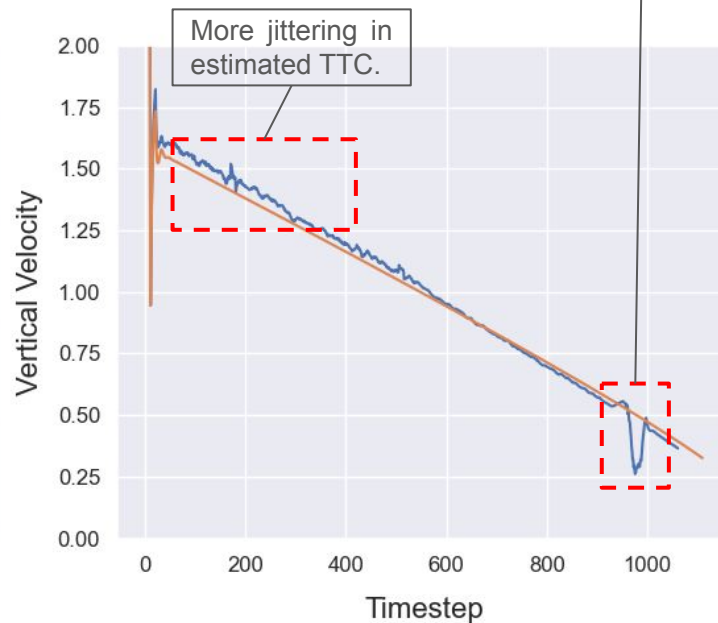
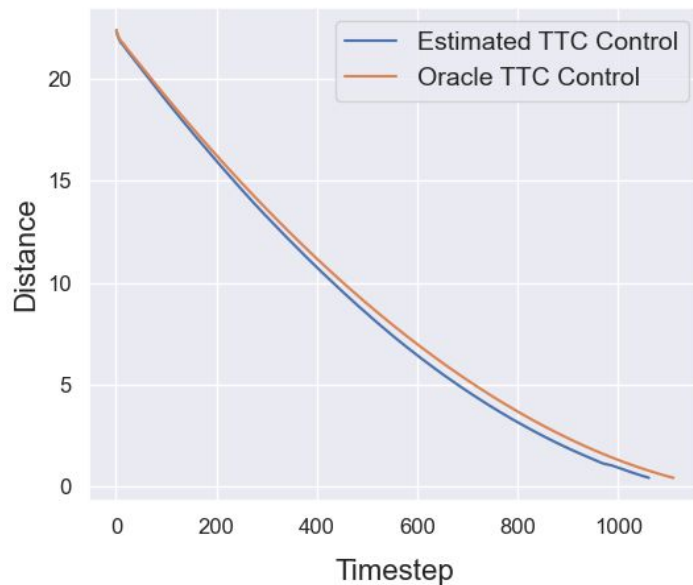


Windy



# Experimental results

## Control with estimated and oracle TTC.

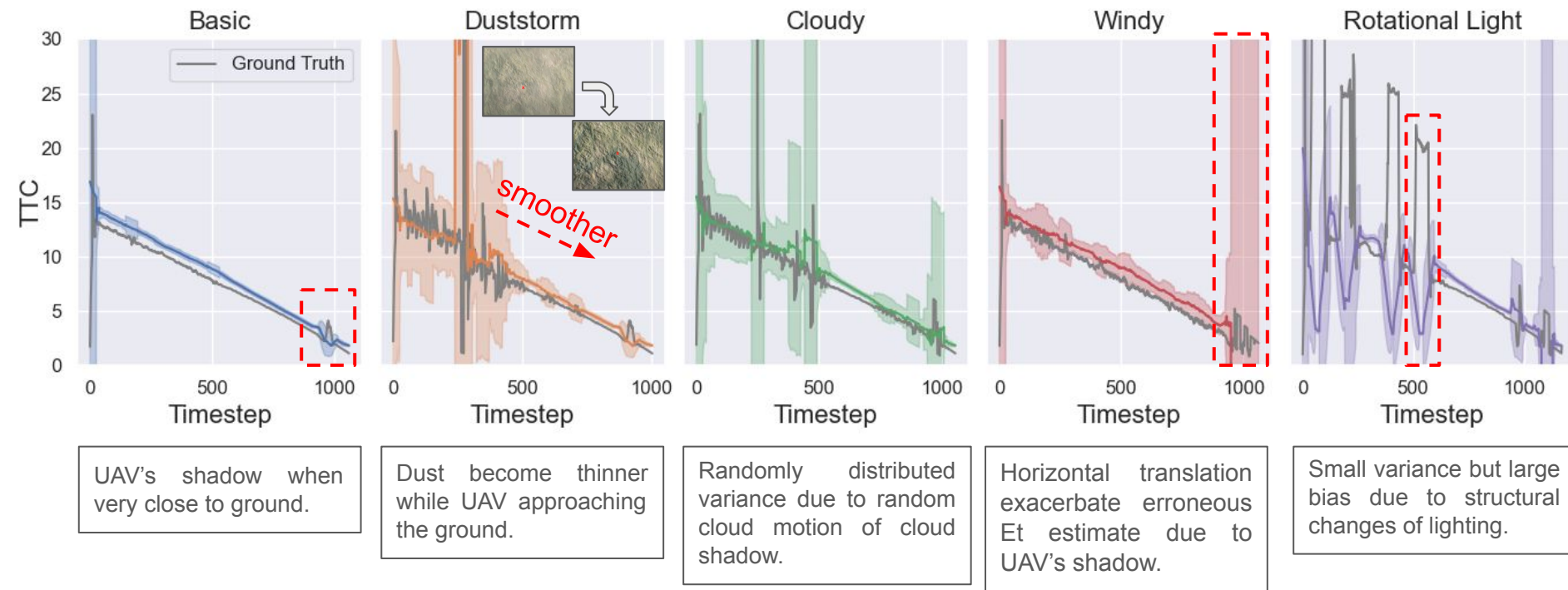




\* Running mean and standard deviation is shown with window size = 50 steps.

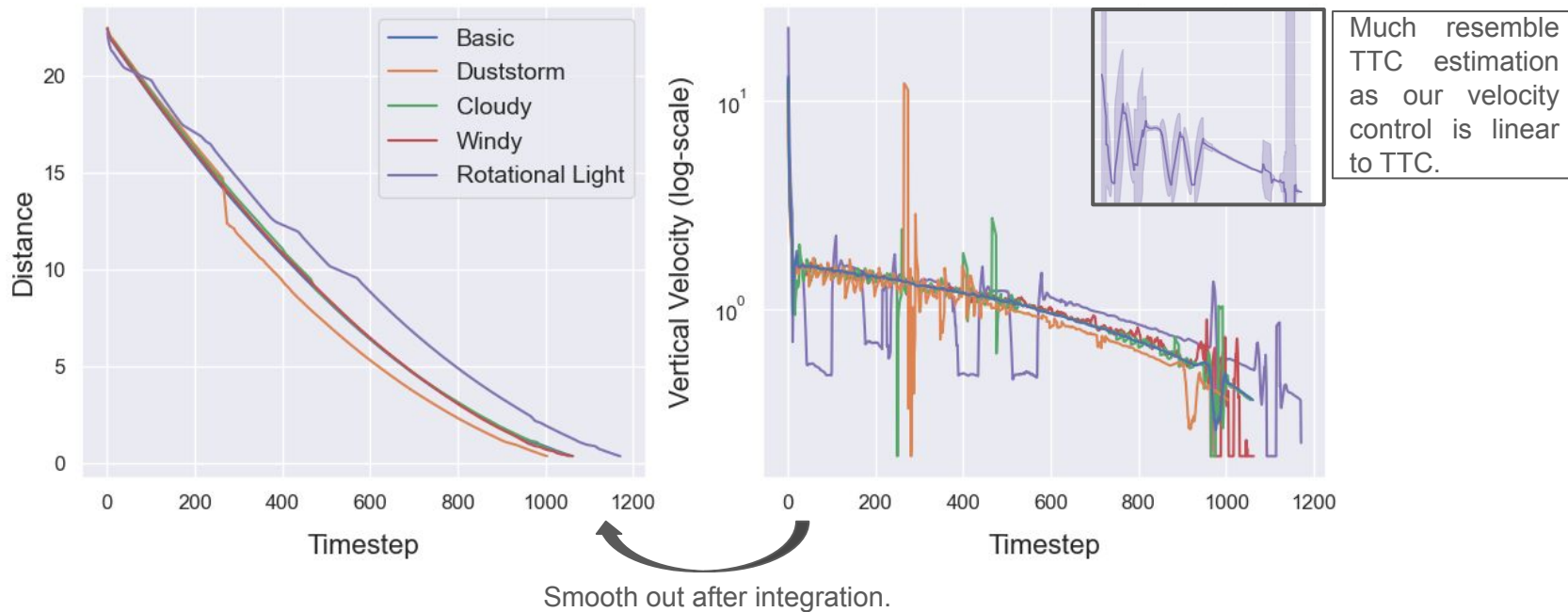
# Experimental results

## TTC estimates in various weather conditions.



# Experimental results

Distance to ground and vertical velocity in various weather conditions.



Slide link:  
<https://docs.google.com/presentation/d/1ORkHkvDeMTCSJEANafhsImeJVZhqEMRU9VSqOTVInxw/edit?usp=sharing>

**BASIC**

Velocity = (0.00, -1.15, 0.00)  
Distance to Ground: 9.60532663  
TTC = 472.468

UAV's View



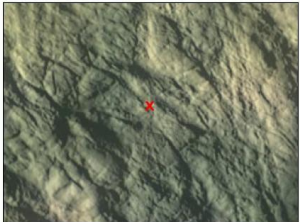
Third-Person View



**DUST STORM**

Velocity = (0.00, -0.54, 0.00)  
Distance to Ground: 1.51558272  
TTC = 169.755

UAV's View



Third-Person View



**WINDY**

Velocity = (0.26, -1.14, -0.70)  
Distance to Ground: 9.73055412  
TTC = 468.371

UAV's View



Third-Person View



**FREE FALL**

Velocity = (0.00, -14.72, 0.00)  
Distance to Ground: 11.48951047  
TTC = 52.856

UAV's View



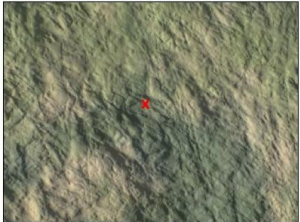
Third-Person View



**CLOUDY**

Velocity = (0.00, -0.82, 0.00)  
Distance to Ground: 4.60415001  
TTC = 309.813

UAV's View



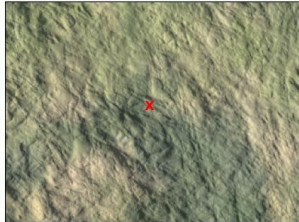
Third-Person View



**ROTATIONAL LIGHT**

Velocity = (0.00, -0.82, 0.00)  
Distance to Ground: 4.65465098  
TTC = 300.919

UAV's View



Third-Person View



Q & A