

Zachary Tabrick

I pledge my honor that I have abided by the Stevens Honor System.

Problem Set 4

① a. ~~Prove~~ If A and B are countably infinite individually then $A \cup B$ is countably infinite since $A \cup B$ combines all the numbers in both sets which are countable.

b. If every number in a set is countable then a subset of that set has to be countable and if the subset is infinite it will be countably infinite.

c. If A and B are countable infinite would be infinite for ~~any~~ pairs of numbers in A and B (x, y) where x and y are both countable then $A \times B$ has to be countable infinite.

d. If you map \mathbb{Q} to $\mathbb{Z} \times (\mathbb{N} - \{0\})$ then it is injective and since $\mathbb{Z} \times \mathbb{N}$ is countably infinite so is \mathbb{Q} since it's injective.

② a. ~~$\{(1,1), (1,2), (2,2), (3,3), (4,4), (1,4), (4,1), (4,2)\}$~~ $\{(1,1), (1,2), (2,2), (3,3), (4,4), (1,4), (4,1), (4,2)\}$

b. ~~$\{(1,1), (1,2), (2,1), (1,4), (4,1), (3,3), (2,4), (4,2)\}$~~ $\{(1,2), (2,1), (1,4), (4,1), (3,3), (2,4), (4,2)\}$

c. $\{(1,1), (1,2), (2,2), (3,3), (4,4), (1,4), (4,1), (2,4), (4,2)\}$