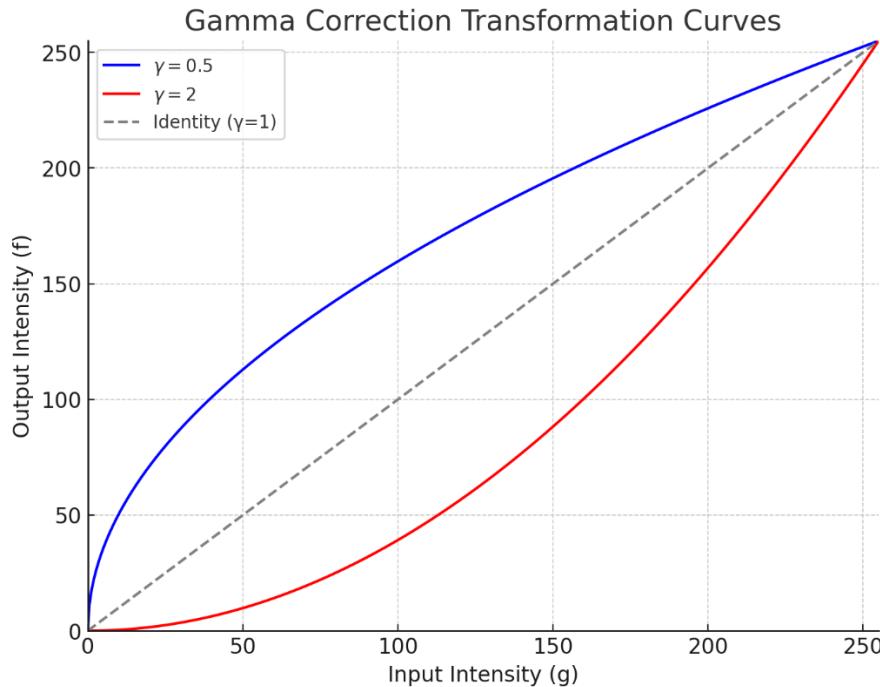


TASK 2

1. Sketch the transformation curve T_G for $\gamma_1 = 0.5$ and $\gamma_2 = 2$.



2. How is the coefficient c typically determined?

The constant c is a scaling constant that ensures our outputs remain in the [0,255] range. Therefore, it is determined as: If $g,f \in [0,255]$, then $c=255^{(1-\gamma)}$

3. In which respect and for which type of input images G do the two gamma values γ_1, γ_2 lead to an image enhancement respectively?

For $\gamma_1 < 1$, T_G increases the brightness of the image. Specifically, the transformation maps lower input values to higher output values, enhancing shadow details.

For $\gamma_2 > 1$, T_G decreases the brightness of the image. For $\gamma > 1$, the transformation maps higher input values to lower output values, enhancing contrast in bright regions.

4. What should be the minimum slope of the transform function? 1. for a grey value spread 2. for a grey value compression

In general:

For $\gamma > 1$ (compression): The slope decreases as $g \rightarrow 0$. Minimum slope occurs near $g = 0$.

For $\gamma < 1$ (spread): The slope increases as $g \rightarrow 0$. Minimum slope occurs near $g = 255$.

Minimum Slope for Grey Value Spread ($\gamma < 1$):

$$df/dg = 255 \cdot 0.5 \cdot (g/255)^{-0.5}$$

The slope decreases as $g \rightarrow 255$ and the **minimum slope occurs at $g=255$** :

$$(df/dg)|_{g=255} = 255 \cdot 0.5 \cdot (1)^{-0.5} = 127.5$$

Minimum Slope for Grey Value Compression ($\gamma > 1$):

For grey value compression ($\gamma = 2$):

$$df/dg = 255 \cdot 2 \cdot (g/255)^1$$

The slope decreases as $g \rightarrow 0$, and the **minimum slope occurs at $g=0$** . However, near $g=0$, the slope asymptotically approaches zero.

To avoid extreme compression in practical applications, a small positive threshold g (e.g., $g=1$) is typically used. At $g=1$:

$$(df/dg)|_{g=1} = 255 \cdot 2 \cdot (1/255) \approx 2$$