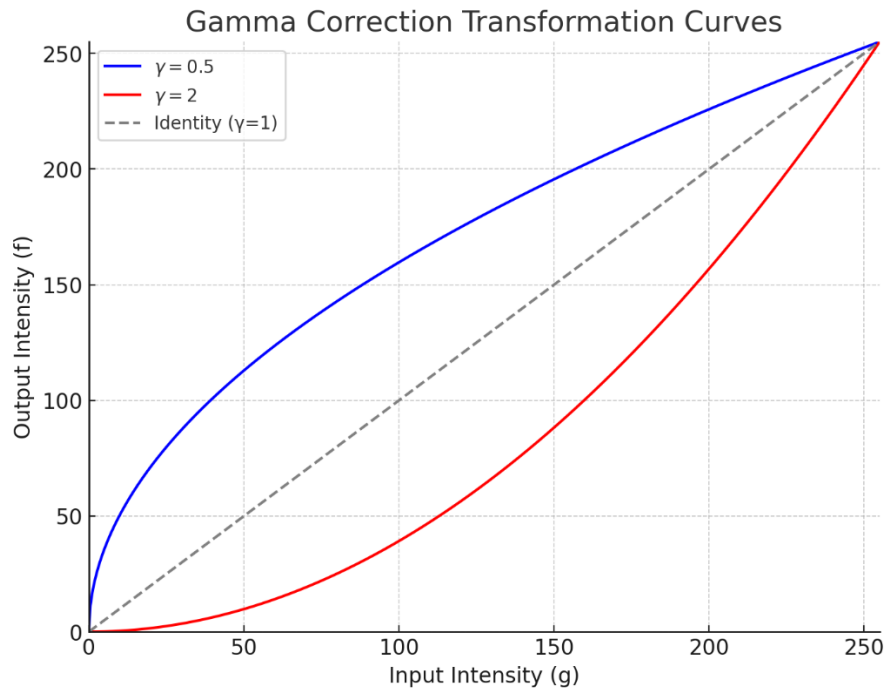


## TASK 2

1. Sketch the transformation curve TG for  $\gamma_1 = 0.5$  and  $\gamma_2 = 2$ .



2. How is the coefficient c typically determined?

The constant c is a scaling constant that ensures our outputs remain in the  $[0, 255]$  range. Therefore, it is determined as: If  $g, f \in [0, 255]$ , then  $c = 255^{(1-\gamma)}$

3. In which respect and for which type of input images G do the two gamma values  $\gamma_1$ ,  $\gamma_2$  lead to an image enhancement respectively?

For  $\gamma_1$ ,  $T_G$  increases the brightness of the image. Specifically, the transformation maps lower input values to higher output values, enhancing shadow details.

For  $\gamma_2$ ,  $T_G$  decreases the brightness of the image. For  $\gamma > 1$ , the transformation maps higher input values to lower output values, enhancing contrast in bright regions.

4. What should be the minimum slope of the transform function? 1. for a grey value spread 2. for a grey value compression

In general:

For  $\gamma > 1$  (compression): The slope decreases as  $g \rightarrow 0$ . Minimum slope occurs near  $g = 0$ .

For  $\gamma < 1$  (spread): The slope increases as  $g \rightarrow 0$ . Minimum slope occurs near  $g = 255$ .

**Minimum Slope for Grey Value Spread ( $\gamma < 1$ ):**

$$df/dg = 255 \cdot 0.5 \cdot (g/255)^{-0.5}$$

The slope decreases as  $g \rightarrow 255$  and the **minimum slope occurs at  $g=255$** :

$$(df/dg)|_{g=255} = 255 \cdot 0.5 \cdot (1)^{-0.5} = 127.5$$

**Minimum Slope for Grey Value Compression ( $\gamma > 1$ ):**

For grey value compression ( $\gamma=2$ ):

$$df/dg = 255 \cdot 2 \cdot (g/255)^1$$

The slope decreases as  $g \rightarrow 0$ , and the **minimum slope occurs at  $g=0$** . However, near  $g=0$ , the slope asymptotically approaches zero.

To avoid extreme compression in practical applications, a small positive threshold  $g$  (e.g.,  $g=1$ ) is typically used. At  $g=1$ :

$$(df/dg)|_{g=1} = 255 \cdot 2 \cdot (1/255) \approx 2$$