

fix

2018年3月19日 15:35

$$\begin{aligned} & \int_0^{15} 5(15-t) f(t) dt \\ & + \int_{15}^{\infty} 10(t-15) f(t) dt \\ & = 75 \int_0^{15} f(t) dt - 5 \int_0^{15} t f(t) dt \\ & + 10 \int_{15}^{\infty} t f(t) dt - 150 \int_{15}^{\infty} f(t) dt \end{aligned}$$

now

$$\int_0^{15} f(t) dt = [-\exp(-0.1t)]_0^{15}$$

$$= -\exp(-1.5)$$

$$\int_{15}^{\infty} t f(t) dt = [-\exp(-0.1t)]_{15}^{\infty}$$

$$= \exp(-1.5)$$

$$\begin{aligned} \int_0^{15} t f(t) dt &= \int_0^{15} t \cdot 0.1 \exp(-0.1t) dt \\ &= \left[ -t \exp(-0.1t) \right]_0^{15} + \int_0^{15} \exp(-0.1t) dt \\ &= -15 \exp(-1.5) + \left[ \frac{\exp(-0.1t)}{-0.1} \right]_0^{15} \end{aligned}$$

$$= -15 \exp(-1.5) - 10 \exp(-1.5) + 10$$

$$= \boxed{-25 \exp(-1.5) + 10}$$

$$\int_{15}^{\infty} + 0.1 \exp(-0.1t) dt$$

$$= \left[ -t \exp(-0.1t) \right]_{15}^{\infty} + \int_{15}^{\infty} \exp(-0.1t) dt$$

$$= 15 \exp(-1.5) + \left[ -\frac{\exp(-0.1t)}{0.1} \right]_{15}^{\infty}$$

$$= 15 \exp(-1.5) + \frac{\exp(-1.5)}{0.1}$$

$$= \boxed{25 \exp(-1.5)}$$

$$\begin{aligned} & 75 \left[ 1 - \exp(-1.5) \right] - 5 \left[ 10 - 25 \exp(-1.5) \right] \\ & + 10 \left[ 25 \exp(-1.5) \right] - 150 \left[ \exp(-1.5) \right] \\ & = 75 - 50 + \exp(-1.5) \left[ -75 + 125 \right] \end{aligned}$$

$$250 - 150]$$

$$= 25 + \exp(-1.5) \times 150 = 58.4695$$