

Lagrangian Mechanics/Dynamics

In Chronological Order,

- Newtonian
- Lagrangian
- Hamiltonian

We define a new function, called the *Lagrangian*:

$$L(q, \dot{q}, t), \text{ WHERE}$$

- q is the generalized coordinates
- \dot{q} is the generalized velocity.
- $\dot{q} = \frac{dq}{dt}$. The dependence on time is implicit, not explicit.

The energy represented in a Lagrangian is:

$$L = K(q) - U(\dot{q})$$

Of many paths that can be taken in between 2 states (q_1, \dot{q}_1) and (q_2, \dot{q}_2) the path taken is the *Path of least action*

Deriving Lagrange's Equations of Motion:

Consider 2 paths: POLA and a neighbouring. Let δq be difference in the two's qs . We get

$$\frac{\partial L}{\partial q} - \frac{d}{dt} \left(\frac{\partial L}{\partial \dot{q}} \right)$$

Now, next step:

Relation between Lagrangian and Hamiltonian:

$$H = \sum_i (\dot{q}_i \frac{\partial L}{\partial \dot{q}_i} - L)$$