2017

(Old Syllabus)

## COMPUTER SCIENCE AND ENGINEERING

Paper - CSEB - 506

(Cryptography)

Full Marks - 70

The figures in the margin indicate full marks

Candidates are required to give their answers in their own words as far as practicable

## Answer Question No. 1, 2 and any four from the rest

1. Answer any five questions:

2×5

- (a) Find all multiplicative pairs in Z<sub>11</sub>.
- (b) Distinguish between  $Z_n$  and  $Z_n^*$ .
- (c) For the following equation, find an integer that satisfies the equation.  $7x \equiv 4 \pmod{5}$ 
  - (d) Define Galois Field.
  - (e) Find the value of  $\phi(32)$ , Where  $\phi$  denotes Euler's totient function.
  - (f) Verify that the number 17 is a prime through square root test.
  - (g) Find the order of all elements in  $G = \langle Z_{10}^*, X \rangle$ .
  - (h) What do you mean by "Avalanche effect"?
  - 2. Answer any five questions:

4×5

- (a) Write an algorithm for testing primality of a number using Miller-Rabin test.
- (b) State extended Euclidean algorithm and use it to find the GCD of (84,320).
  - (c) What is Key wrapping? How is it useful?
- (d) State the second criterion for a cryptographic hash function and associate the concerned birthday problem.

[Turn Over]

- (e) Find the results of 21<sup>24</sup> mod 8 using Fast exponentiation method.
- (f) Discuss the advantage(s) of using counter algorithmic mode compared to CBC.
- (g) Discuss the Lamport's Hash algorithm for authentication and state the uniqueness of the said algorithm.
- (h) Why do you think the mixing transformation (Mix Columns) is not needed in DES; but is needed in AES?
- 3. (a) Use the extended Euclidean algorithm to find the inverse of  $(x^4 + x^3 + 1)$  in GF (2<sup>5</sup>) using the modulus  $(x^5 + x^2 + 1)$ .
- (b) Prove that the difficulty of an alternative collision attack is proportional to  $2^{n/2}$ .
- 4. State the properties of a standard public-key cryptography algorithm.

  Describe RSA and show that these properties hold in context of RSA.

  3+7
- 5. Comment on the Key management issue for secret key cryptography.

  Describe the role of Key Distribution Centre for Key management. Is it helps for authentication? Justify your answer.

  2+4+4
- 6. Discuss the principle behind proposing a product cipher by Shannon. Show how these principles are implemented in DES.

  3+7
  - 7. (a) Discuss "Chosen cipher text attack" with an example.
    - (b) Write an algorithm for decryption in Knapsack cryptosystem.
    - (c) What do you mean by "Digital signature"? 4+4+2
- 8. (a) Write a short note on "Analysis of Diffie-Hellman" key exchange algorithm.
  - (b) Describe the sub-key generation algorithm in AES. 5+5