

#### ĐẠI HỌC ĐÀ NẪNG

# TRƯỜNG ĐẠI HỌC CÔNG NGHỆ THÔNG TIN VÀ TRUYỀN THÔNG VIỆT - HÀN

**VIETNAM - KOREA UNIVERSITY OF INFORMATION AND COMMUNICATION TECHNOLOGY** 

한-베정보통신기술대학교

Nhân bản – Phụng sự – Khai phóng

# Stacks and Queues



# **CONTENT**

Stacks

Queues



#### CONTENT

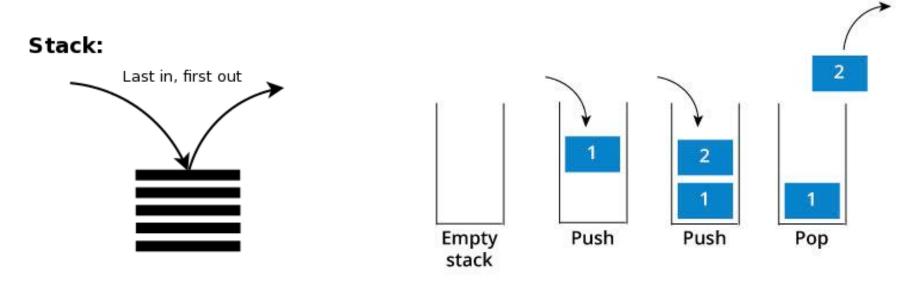
#### Stacks

- Introduction to Stacks
- Array representation of Stacks
- Linked representation of Stacks
- Applications of Stacks



#### Introduction to Stacks

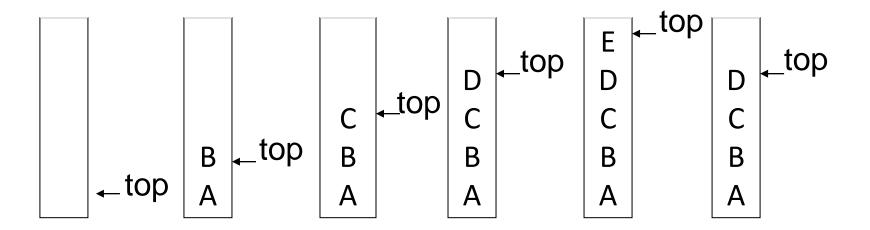
- Stack is a linear data structure
- Elements in a stack are added/deleted only from one end (called top)
- Stack is called a LIFO (Last-In-First-Out) data structure
- Operations on a stack: push(), pop()



Stacks can be implemented using either arrays or linked lists



- Introduction to Stacks
  - Last-In-First-Out (LIFO)





#### Introduction to Stacks

Example of function call

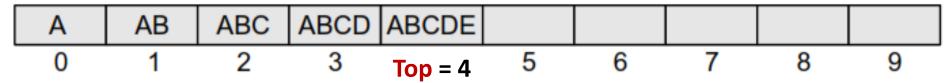
```
#include <stdio.h>
main(){
        int x;
       x = fact(5);
int fact(int n){
        if (n>1)
                return n*fact(n-1);
        else
                return 1;
```

```
X = ?
invoke fact(5)
invoke fact(4)
invoke fact(3)
invoke fact(2)
invoke fact(1)
return from fact(1) = 1
return from fact(2) = 2
return from fact(3) = 6
return from fact(4) = 24
return from fact(5) = 120
```



#### Array representation of stacks

- Variable top stores the address of the topmost element of the stack,
   the element will be added to or deleted from top
- Variable MAX is used to store the maximum number of elements that the stack can hold.
  - ⇒ top = -1, stack is empty; top = MAX-1, the stack is full
- Example,



- top = 4, so insertions/deletions will be done at this position.
- five more elements can still be stored.

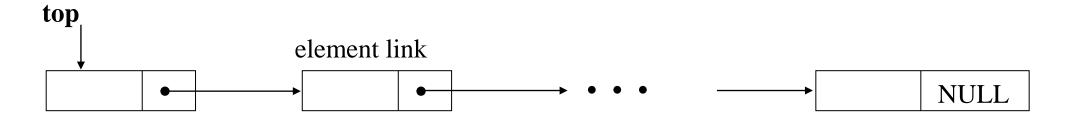


## Array representation of stacks

```
#define MAX 100
typedef struct {
         int key;
         /* other fields */
} element;
```

```
void push(element item){
    if (top == MAX-1)
       cout<<"stack full";</pre>
     stack[++top] = item;
element pop(){
   if (top == -1)
         return stack empty();
    return stack[top--];
```





- Every node has two parts: data & the address of the next node
- The START pointer of the linked list is used as top.
- Additions/deletions are done at the node pointed by top.
- top = NULL, stack is empty



Declarations

```
typedef struct stack *stack_pointer;
typedef struct stack {
    element item;
    stack_pointer link;
};
```

- Boundary conditions
  - top = NULL iff the ith stack is empty and
  - IS\_FULL(temp) iff the memory is full

```
typedef struct {
    int key;
    /* other fields */
} element;
```



```
void push(stack_pointer *top, element item){
       /* add an element to the top of the stack */
       stack_pointer temp = (stack_pointer) malloc (sizeof (stack));
       if (IS FULL(temp)) { //temp==NULL
              fprintf(stderr, "The memory is full\n");
              exit(1);
       temp->item = item;
       temp->link = *top;
       *top= temp;
```



```
element pop(stack_pointer *top) {
       /* delete an element from the stack */
       stack pointer temp = *top;
        element item;
       if (IS_EMPTY(temp)) {
              fprintf(stderr, "The stack is empty\n");
              exit(1);
       item = temp->item;
       *top = temp->link;
       free(temp);
       return item;
```





#### Comparing representations

- Array representation of Stacks
  - Fixed size (cannot grow and shrink dynamically)
- Linked representation of Stacks
  - May need to perform realloc calls when the currently allocated size is exceeded
  - But push and pop operations can be very fast
- Using the previously defined linked-list
  - Reuses existing implementation
  - Reduces the coding effort but may be a bit less efficient





#### Applications of Stacks

- Reversing a list
- Parentheses checker
- Matching Parentheses and HTML Tags
- Conversion of an infix expression into a postfix expression
- Evaluation of a postfix expression
- Conversion of an infix expression into a prefix expression
- Evaluation of a prefix expression
- Recursion
- Tower of Hanoi

• • • •



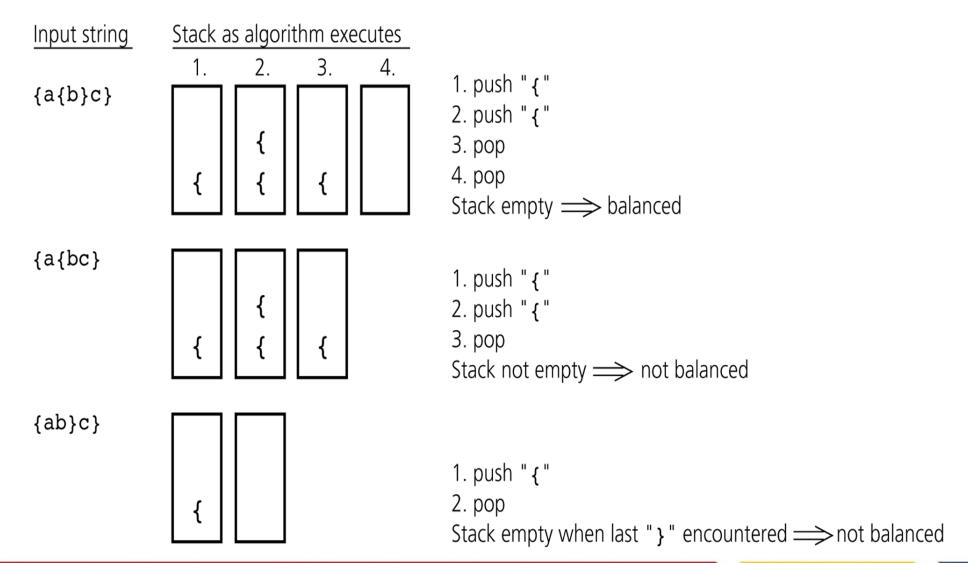


- Applications of Stacks Checking for Balanced Braces
  - A stack can be used to verify whether a program contains balanced braces
  - An example of balanced braces
    - abc{defg{ijk}{l{mn}}op}qr
  - An example of unbalanced braces
    - abc{def}}{ghij{kl}m
  - Requirements for balanced braces
    - Each time we encounter a "}", it matches an already encountered "{"
    - When we reach the end of the string, we have matched each "{"





#### Applications of Stacks - Checking for Balanced Braces







## Applications of Stacks - Algebraic Expressions

- To evaluate an infix expression //infix: operator in b/w operands
- 1. Convert the infix expression to postfix form
- 2. Evaluate the postfix expression //postfix: operator after operands; similarly we have prefix: operator before operands

#### **Infix Expression**

$$5 + 2 * 3$$

$$5*2+3$$

$$5*(2+3)-4$$

## **Postfix Expression**

#### **Prefix Expression**





• Applications of Stacks - Algebraic Expressions

- Infix notation is easy to read for humans
- Pre-/postfix notation is easier to parse for a machine
- The big advantage in pre-/postfix notation is that there never arise any questions like operator precedence





- Applications of Stacks Algebraic Expressions
  - Evaluating Postfix Expressions
    - When an operand is entered, the calculator
      - Pushes it onto a stack
    - When an operator is entered, the calculator
      - Applies it to the top two operands of the stack
      - Pops the operands from the stack
      - Pushes the result of the operation on the stack



After stack eneration:



# • Applications of Stacks - Algebraic Expressions

Evaluating Postfix Expressions: 2 3 4 + \*

Key entered	Calculator action				Stack (bottom to top)		
2	push 2		2				
3	push 3		2	3			
4	push 4		2	3	4		
+	operand2 = pop stack operand1 = pop stack	(4) (3)	2	3			
	<pre>result = operand1 + operand2 push result</pre>	(7)	2	7			
*	operand2 = pop stack operand1 = pop stack	(7) (2)	2				
	<pre>result = operand1 * operand2 push result</pre>	(14)	14				





- Applications of Stacks Algebraic Expressions
  - Converting Infix Expressions to Postfix Expressions
    - Read the infix expression
      - When an operand is entered, append it to the end of postfix expression
      - When an '(' is entered, push it into the stack
      - When an ')' is entered, move operators from the stack to the end of postfix expression until '('
      - When an operator is entered, push it into the stack

Move the operators in the stack to the end of postfix expression





- Applications of Stacks Algebraic Expressions
  - Converting Infix Expressions to Postfix Expressions

<u>ch</u>	Stack (bottom to top)	<u>postfixExp</u>	
а		a	
_	_	а	/1 . 4 1\/
(	<b>–</b> (	а	a - (b + c * d)/ e
b	<b>–</b> (	ab	⇒ a b c d * + e / -
+	- ( +	ab	
C	- ( +	abc	
*	-(+*	abc	
d	- ( + *	abcd	
)	- ( <b>+</b>	abcd*	Move operators
	<b>–</b> (	abcd*+	from stack to
	_	abcd*+	postfixExp until " ( "
/	-/	abcd*+	
е	-/	abcd*+e	Copy operators from
		abcd*+e/-	stack to postfixExp



- Applications of Stacks Algebraic Expressions
  - Converting Infix Expressions to Postfix Expressions

```
for (each character ch in the infix expression) {
  switch (ch) {
    case operand: // append operand to end of postfixExpr
        postfixExpr=postfixExpr+ch; break;
    case '(': // save '(' on stack
        aStack.push(ch); break;
    case ')': // pop stack until matching '(', and remove '('
        while (top of stack is not '(') {
            postfixExpr=postfixExpr+(top of stack);
            aStack.pop();
        aStack.pop(); break;
```



- Applications of Stacks Algebraic Expressions
  - Converting Infix Expressions to Postfix Expressions

```
case operator:
    aStack.push(); break; // save new operator
} // end of switch and for

// append the operators in the stack to postfixExpr
while (!isStack.isEmpty()) {
    postfixExpr=postfixExpr+(top of stack);
    aStack(pop);
}
```





- Applications of Stacks Algebraic Expressions
  - Benefits about converting from infix to postfix
    - Operands always stay in the same order with respect to one another
    - An operator will move only "to the right" with respect to the operands
    - All parentheses are removed





## • The Relationship Between Stacks and Recursion

- A strong relationship exists between recursion and stacks
- Typically, stacks are used by compilers to implement recursive methods
  - During execution, each recursive call generates an activation record that is pushed onto a stack
  - We can get stack overflow error if a function makes makes too many recursive calls
- Stacks can be used to implement a non recursive version of a recursive algorithm



#### **CONTENT**

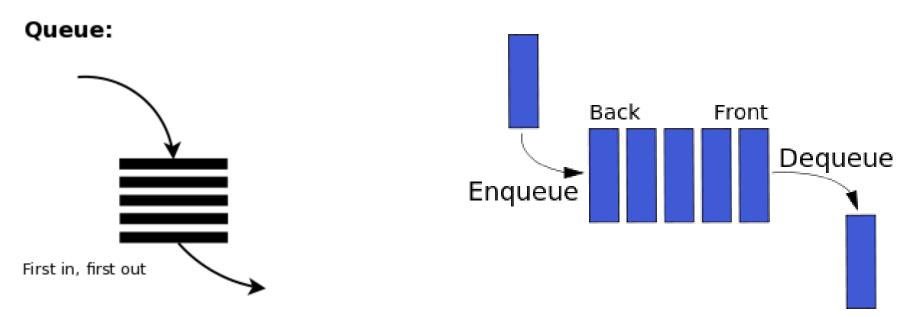
#### Queue

- Introduction to Queues
- Array representation of Queues
- Linked representation of Queues
- Applications of Queues



#### Introduction to Queues

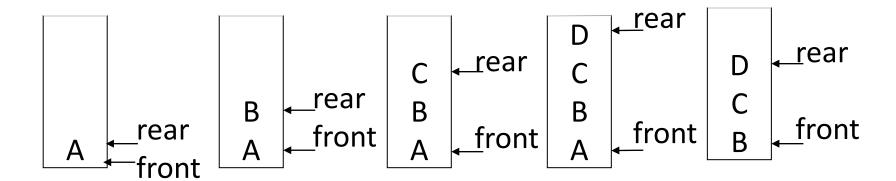
- The elements are added at one end (called rear) and deleted from the other end (called front).
- Queue is a FIFO (First-In, First-Out) data structure
- Operations on a queue: add(), delete()



Queues can be implemented by using arrays or linked lists.



- Introduction to Queues
  - First-In-First-Out (FIFO) list







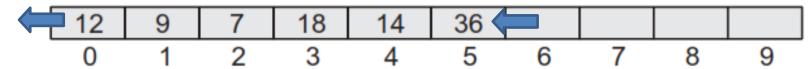
- Introduction to Queues
  - Example of Job scheduling

front	rear	Q[0]	Q[1] (	Q[2] Q[3]	Comments
-1	-1				queue is empty
-1	0	J1			Job 1 is added
-1	1	J1	J2		Job 2 is added
-1	2	J1	J2	J3	Job 3 is added
0	2		J2	J3	Job 1 is deleted
1	2			J3	Job 2 is deleted

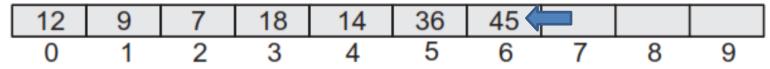


- Array representation of Queues
  - Every queue has front and rear variables that point to the position from where additions/deletions can be done
  - Operations on Queues:

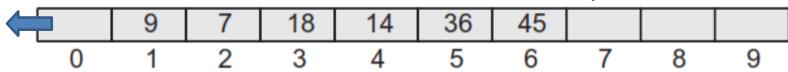
Queue (front = 0, rear = 5):



Queue after addition of a new element with value 45 (front = 0, rear = 6)



Queue after deletion of an element with value 12 (front = 1, rear = 6):





#### Array representation of Queues

- Initially, front = rear = -1
- Queues is empty, front = = rear
- Queues is full, rear == MAX-1

```
• void add(int *rear, element item){
   if (*rear == MAX_QUEUE_SIZE - 1){
      queue_full();
      return;
   }
   queue [++*rear] = item;
}
```

element delete(int \*front, int rear){
 if ( \*front == rear)
 return queue\_empty( );
 return queue [++ \*front];
}



Array representation of Queues - Circular array

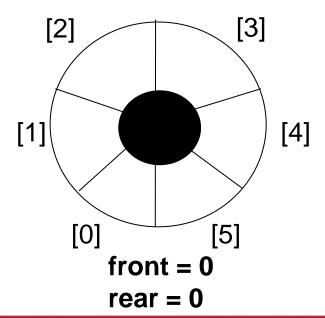
#### Problem:

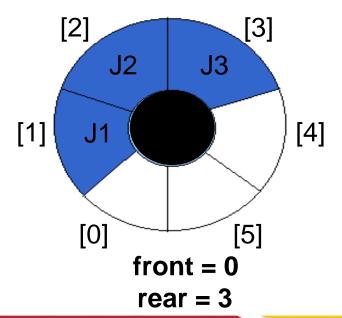
- The two pointers only increments, never decrements.
- We eventually fall off the right end of the array.

⇒This problem can be solved by periodically moving the elements to the left, to make room on the right end.



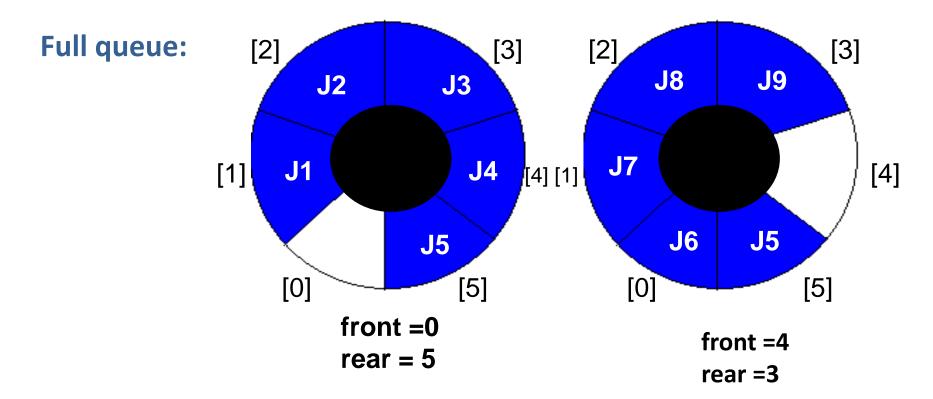
- Array representation of Queues Circular array
  - Use a circular array plus 2 pointers to implement a queue.
  - The **front** index always points one position counterclockwise from the first element in the queue.
  - The rear index points to the current end of the queue.







- Array representation of Queues Circular array
  - Though there are MAX slots in the circular array, we can store at most MAX 1 elements in the circular array at any instant.





Array representation of Queues - Circular array

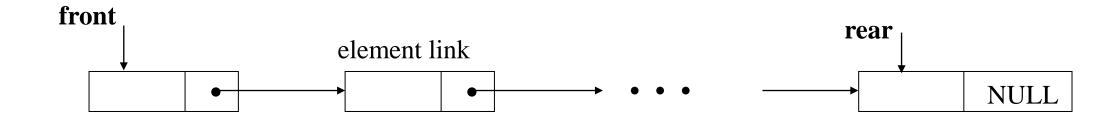
```
• void addQ(int front, int *rear, element item){
    *rear = (*rear +1) % MAX;
    if (front == *rear) {
            queue_full(rear);
            return;
    }
    queue[*rear] = item;
}
```



Array representation of Queues - Circular array



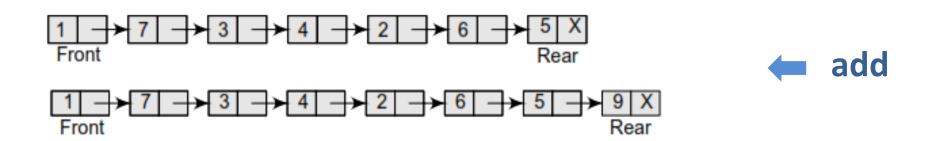
#### Linked representation of Queues

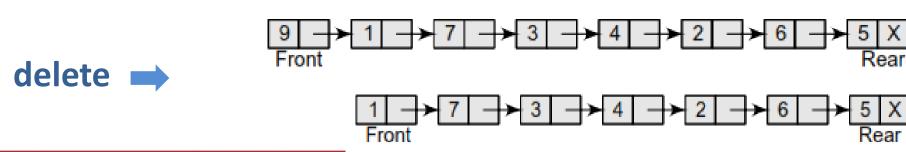


- Every element has two parts: data & the address of the next element
- The START pointer of the linked list is used as **front**. The **rear** pointer store the address of the last element in the queue.
- Additions will be done at the rear, deletions will be done at the front.
- front = rear = NULL, the queue is empty.



- Linked representation of Queues
  - 2 basic operations:
  - add: inserts an element to the end of the queue
  - delete: removes an element from the front or the start of the queue







#### Linked representation of Queues

Declarations

```
typedef struct queue *queue_pointer;
typedef struct queue {
     element item;
     queue_pointer link;
};
```

- Boundary conditions
  - front = NULL iff the ith queue is empty and
  - IS\_FULL(temp) iff the memory is full





- Linked representation of Queues
  - Add to the rear of a linked queue

```
void addQ(queue_pointer *front, queue_pointer *rear, element item){
        /* add an element to the rear of the queue */
        queue pointer temp = (queue pointer) malloc(sizeof (queue));
        if (IS_FULL(temp)) {
               fprintf(stderr, "The memory is full\n");
               exit(1);
        temp->item = item;
        temp->link = NULL;
       if (*front) (*rear) -> link = temp;
        else *front = temp; /* the queue is empty */
        *rear = temp;
```



- Linked representation of Queues
  - Delete from the **front** of a linked queue

```
element deleteQ(queue pointer *front) {
         /* delete an element from the queue */
         queue pointer temp = *front;
         element item;
         if (IS EMPTY(*front)) {
                fprintf(stderr, "The queue is empty\n");
                exit(1);
         item = temp->item;
         *front = temp->link;
         free(temp);
         return item;
```



#### Comparing representations

- Array representation of Queues
  - A statically allocated array
    - Prevents the enqueue operation from adding an item to the queue if the array is full
  - A resizable array or a reference-based implementation
    - Does not impose this restriction on the enqueue operation
- Linked representation of Queues
  - A linked list implementation
    - More efficient; no size limit



#### Applications of Queues

- Job scheduling
- Waiting lists for a single shared resource like printer, disk, CPU.
- Transfer data asynchronously (data not necessarily received at same rate as sent) between two processes (IO buffers), e.g., fileIO, sockets.
- Buffers on MP3 players and portable CD players, iPod playlist.
- Playlist to add songs to the end, play from the front of the list.
- Operating system for handling interrupts.

• ...





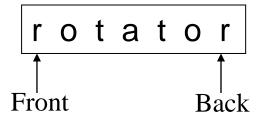
- Applications of Queues Recognizing Palindromes
  - A palindrome
    - A string of characters that reads the same from left to right as its does from right to left
  - To recognize a palindrome, a queue can be used in conjunction with a stack
    - A stack reverses the order of occurrences
    - A queue preserves the order of occurrences
  - A nonrecursive recognition algorithm for palindromes
    - As you traverse the character string from left to right, insert each character into both a queue and a stack
    - Compare the characters at the front of the queue and the top of the stack



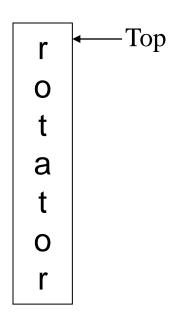


- Applications of Queues Recognizing Palindromes
  - String: rotator

• Queue:



• Stack:



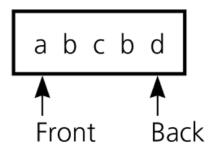
The results of inserting a string into both a queue and a stack



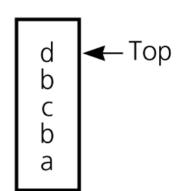
#### Applications of Queues - Recognizing Palindromes

String: abcbd

Queue:



Stack:



The results of inserting a string into both a queue and a stack

### **SUMMARY**



Stacks

Queues





## ĐẠI HỌC ĐÀ NẰNG

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